

```
In [59]: from sympy.abc import x
from sympy import sqrt,diff,plot,solve,evalf
```

```
In [60]: eq = x**2-x-1
eq
```

Out[60]:  $x^2 - x - 1$

```
In [61]: solve(eq)
```

Out[61]:  $[1/2 - \sqrt{5}/2, 1/2 + \sqrt{5}/2]$

```
In [62]: r1 = 1/2 - sqrt(5)/2
r1
```

Out[62]:  $0.5 - \frac{\sqrt{5}}{2}$

```
In [63]: r2 = 1/2 + sqrt(5)/2
r2
```

Out[63]:  $0.5 + \frac{\sqrt{5}}{2}$

```
In [6]: r1.evalf(10)
```

Out[6]:  $-0.6180339888$

```
In [28]: r2.evalf(60)
```

Out[28]:  $1.61803398874989484820458683436563811772030917980576286213545$

```
In [1]: for i in range(2,1_000_000,100_000):
import time
from sympy import sqrt
r2 = 1/2 + sqrt(5)/2
startTime = time.time()

digits = i
result = r2.evalf(digits)

executionTime = (time.time() - startTime)
print('Execution time to calculate',digits,'Digits of Phi (in seconds): ' + str(executionTime))
print("Last digit is:", str(result)[-1])
print("
")
```

Execution time to calculate 2 Digits of Phi (in seconds): 0.0001571178436279297  
Last digit is: 6

Execution time to calculate 100002 Digits of Phi (in seconds): 0.06370139122009277  
Last digit is: 8

Execution time to calculate 200002 Digits of Phi (in seconds): 0.18637681007385254  
Last digit is: 0

Execution time to calculate 300002 Digits of Phi (in seconds): 0.3826889991760254  
Last digit is: 8

Execution time to calculate 400002 Digits of Phi (in seconds): 0.4409317970275879  
Last digit is: 2

Execution time to calculate 500002 Digits of Phi (in seconds): 0.77689528465271  
Last digit is: 3

Execution time to calculate 600002 Digits of Phi (in seconds): 1.0968341827392578  
Last digit is: 6

Execution time to calculate 700002 Digits of Phi (in seconds): 1.3132565021514893  
Last digit is: 5

Execution time to calculate 800002 Digits of Phi (in seconds): 1.5213916301727295  
Last digit is: 3

Execution time to calculate 900002 Digits of Phi (in seconds): 1.693979263305664  
Last digit is: 2

```
In [2]: # Execution Times
t0 = 0.0001571178436279297
t1 = 0.06370139122009277
t2 = 0.18637681007385254
t3 = 0.3826889991760254
t4 = 0.4409317970275879
t5 = 0.77689528465271
t6 = 1.0968341827392578
t7 = 1.3132565021514893
t8 = 1.5213916301727295
t9 = 1.693979263305664
```

```
In [42]: # Digits calculated per second
d1 = (10_002-2)/(t1-t0)
d2 = (20_002-10_002)/(t2-t1)
d3 = (30_002-20_002)/(t3-t2)
d4 = (40_002-30_002)/(t4-t3)
d5 = (50_002-40_002)/(t5-t4)
d6 = (60_002-50_002)/(t6-t5)
d7 = (70_002-60_002)/(t7-t6)
d8 = (80_002-70_002)/(t8-t7)
d9 = (90_002-80_002)/(t9-t8)
```

```
In [58]: # Average Digits calculated per second
(d1+d2+d3+d4+d5+d6+d7+d8+d9)/9
```

```
Out[58]: 74970.5764998911
```

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In [64]: # 75,000 digits of Phi calculated per second.
```

```
In [47]: # A Record divided by my rate
(10**13)/75_000 # 10^13 is the amount of accurate digits Phi has been calculated to
                # - Yee, Alexander J. (13 March 2021). "Records Set by y-cruncher". numberword.org.
                # Two independent computations done by Clifford Spielman.
```

```
Out[47]: 133333333.33333333
```

```
In [65]: # 133_333_333 seconds
```

```
In [55]: 133_333_333 / 60
```

```
Out[55]: 2222222.216666667
```

```
In [52]: # 2_222_222 minutes
```

```
In [56]: 2_222_222 / 60
```

```
Out[56]: 37037.03333333333
```

```
In [54]: #37_037 hours
```

```
In [57]: 37_037 / 8_766 # (8_766 hours in a year)
```

```
Out[57]: 4.225074150125485
```

```
In [ ]: # 4.225 years to compute 10^13 digits of Phi with my computer.
```