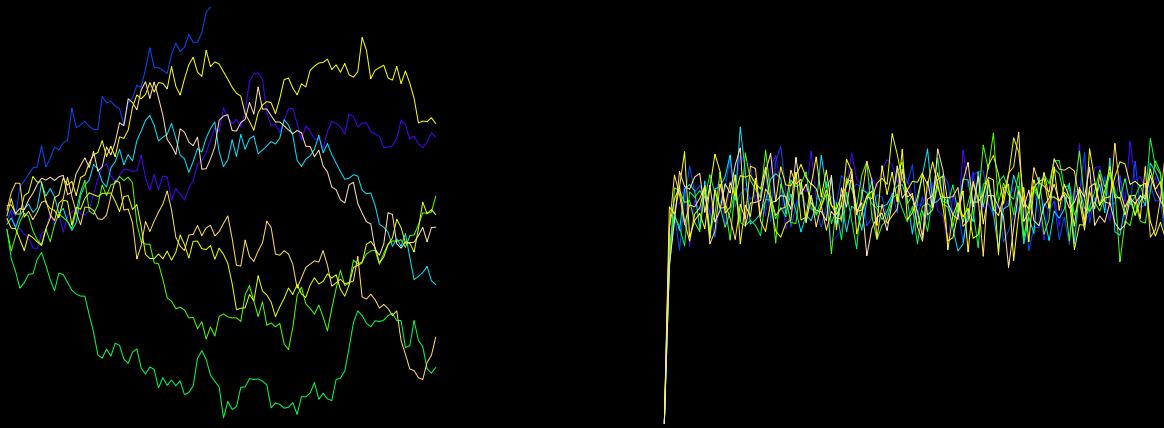


Trait Evolution



SSB Workshop 26th June 2015
Samantha Price



National Science Foundation
WHERE DISCOVERIES BEGIN



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Outline

- **Section 1:** Discrete traits
- **Section 2:** Basic models of continuous trait evolution (Brownian motion & OU)
- **Section 3:** Combining discrete and continuous traits

1: Modeling discrete traits with continuous time Markov models

- Q matrix

$$\begin{matrix} & 0 & 1 \\ 0 & -0.5 & 0.5 \\ 1 & 0.5 & -0.5 \end{matrix}$$

Equal Rates

$$\begin{matrix} & 0 & 1 \\ 0 & -1 & 1 \\ 1 & 0.5 & -0.5 \end{matrix}$$

All Rates Different

1: Modeling discrete traits with continuous time Markov models

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Equal Rates

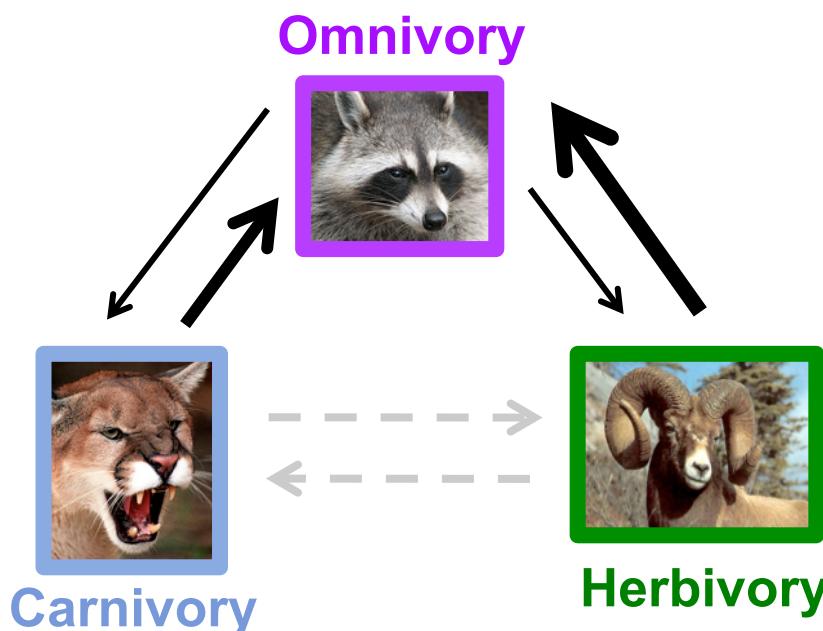
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All Rates Different

Over time: $P_{(t)} = e^{-Qt}$

1: Examples

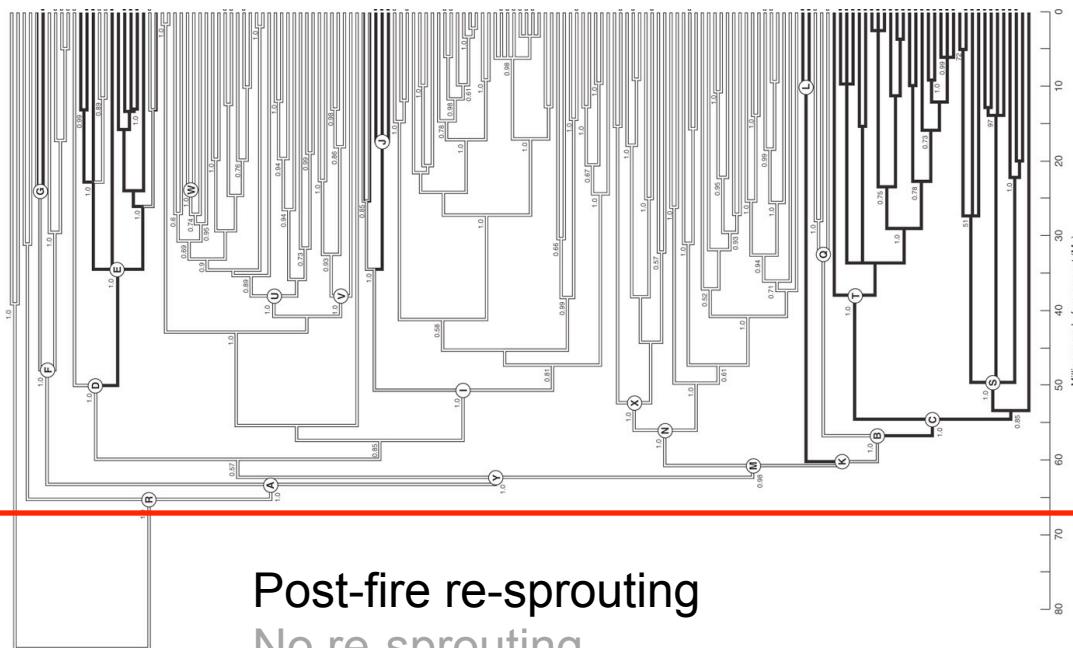
- Are the transition rates between states equal or is it easier to change between some states than others?



- Mammalian omnivory as a transitional state and evolutionary sink.

1: Examples

- Are the transition rates between states equal or is it easier to change between some states than others?
- What is the history of the character on the phylogeny?
 - Timing of post-fire re-sprouting in eucalypts suggests much earlier evolution of fire-dependent communities

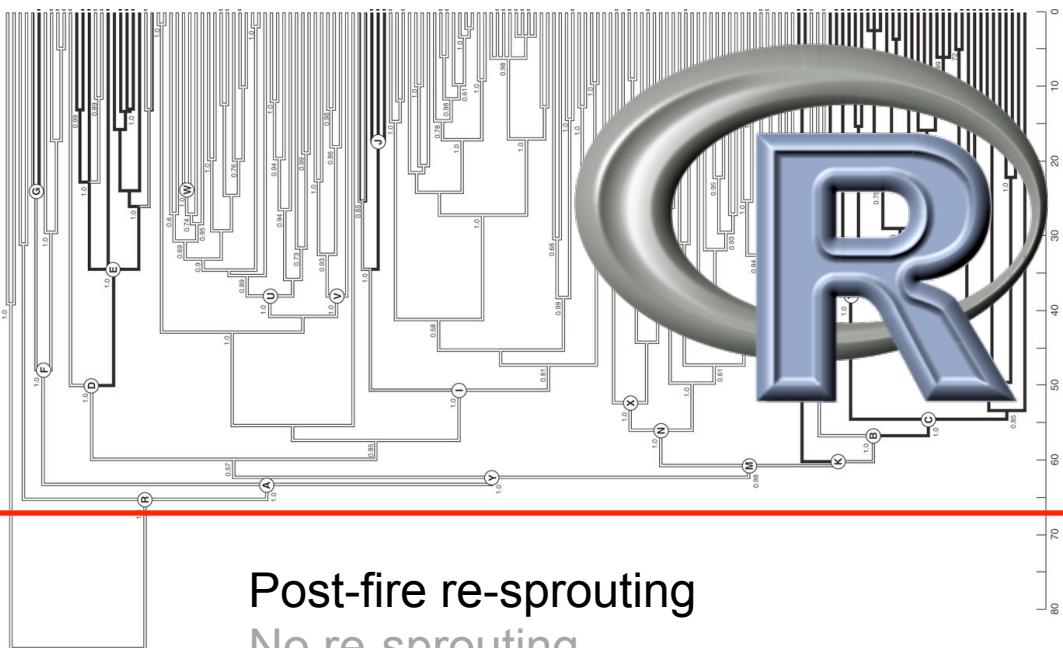


Post-fire re-sprouting
No re-sprouting

Crisp et al. 2011 Nature Comm.

1: Examples

- Are the transition rates between states equal or is it easier to change between some states than others?
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K-Pg

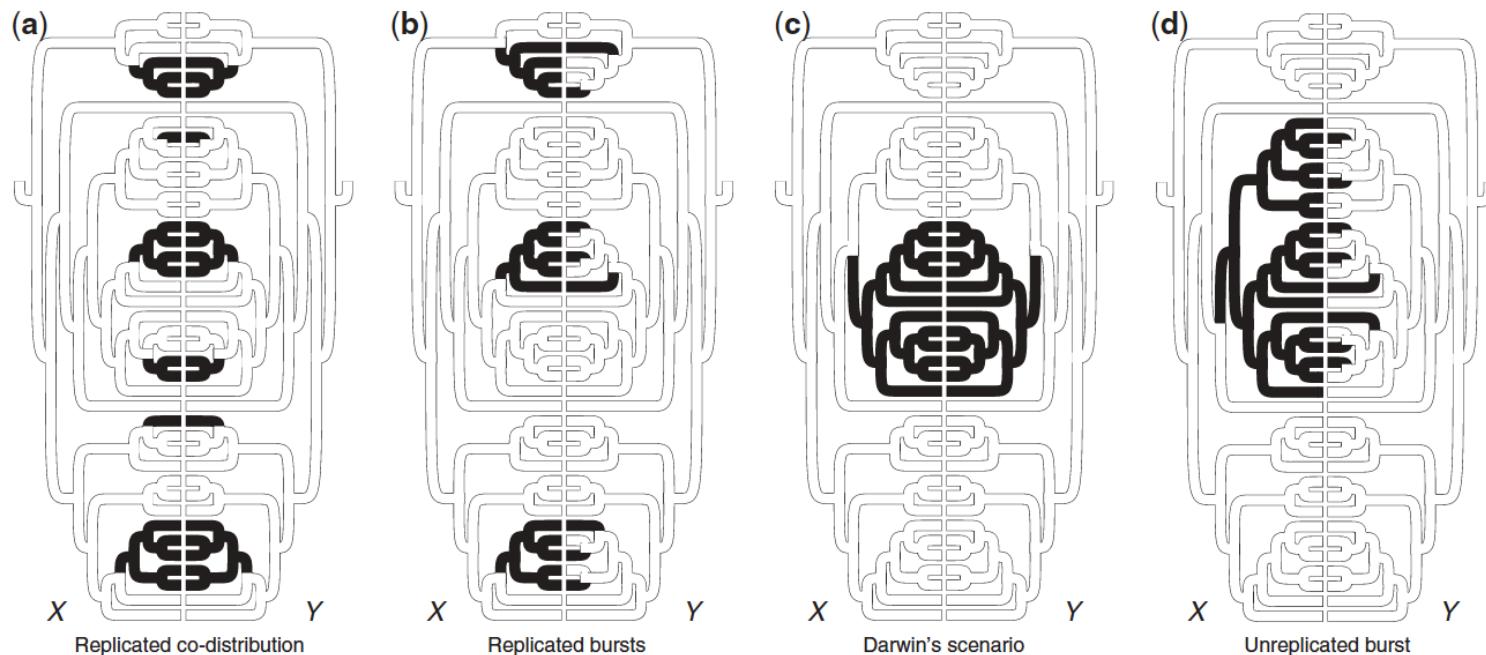
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1: Caution & Caveats

- Potential importance of the root state and not being at equilibrium state frequencies.

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- Potential importance of the root state and not being at equilibrium state frequencies.
- **Difficult to correlate discrete traits** (Maddison & Fitzjohn 2015; Rabosky & Goldberg 2015).



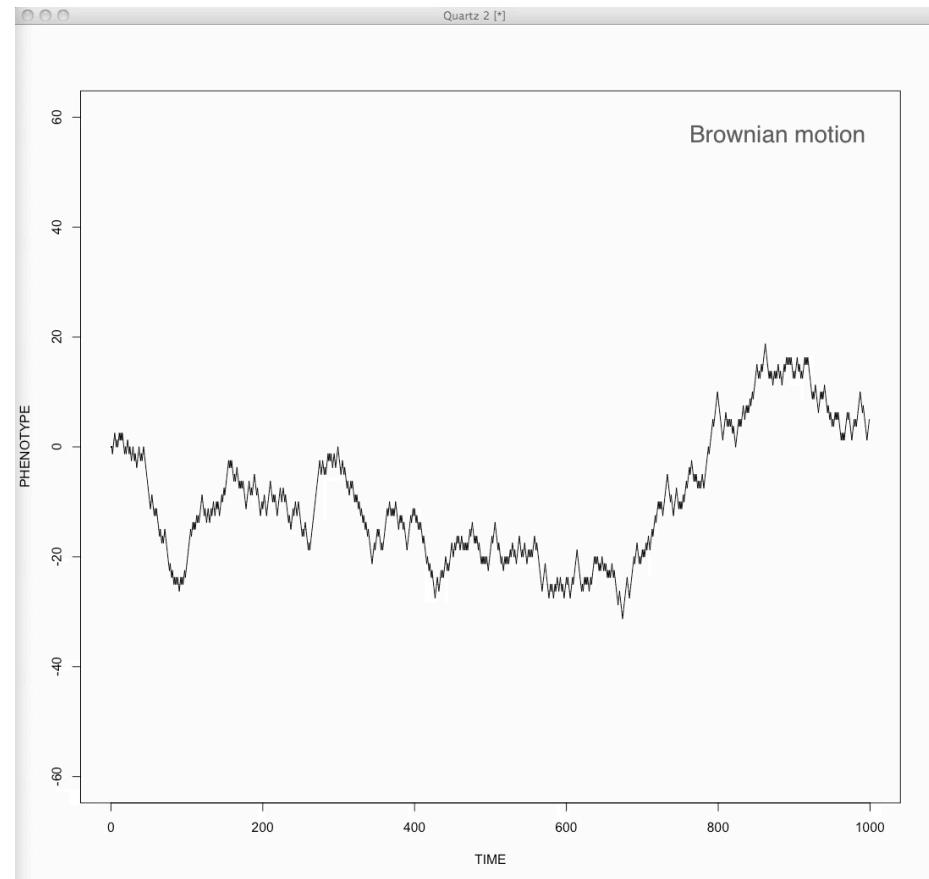
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2: Brownian motion

At a point in time:

- A character can increase, decrease or stay the same
- Direction and magnitude of change is independent of current or past character states
 - Probability of change is drawn from a normal distribution with a mean of 0
- Constant rate

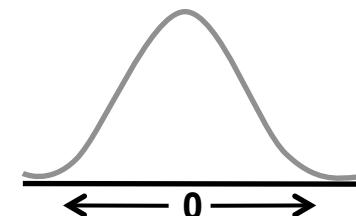


2: Brownian motion

$$dX_{(t)} = \sigma dB_{(t)}$$

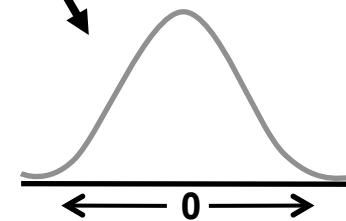
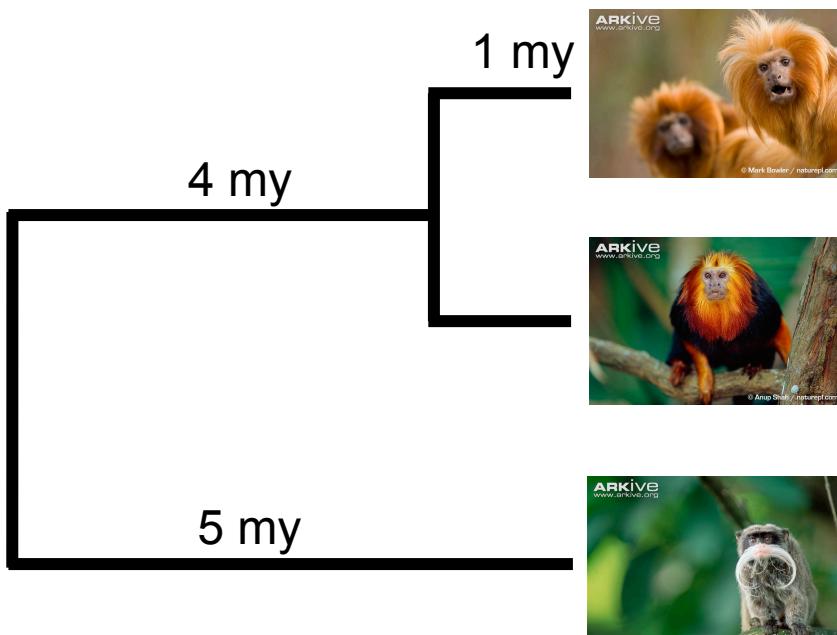
Rate

Trait change as
described by
normal distribution
mean = 0



2: Brownian motion on a phylogeny

$$dX_{(t)} = \sigma dB_{(t)}$$



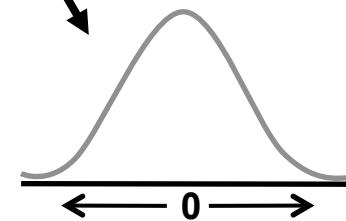
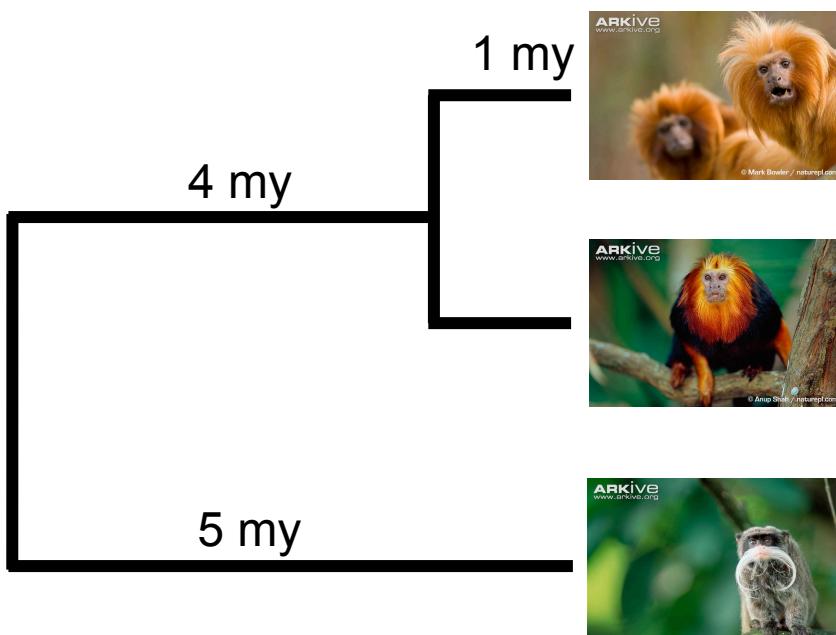
$$SD = \sqrt{\sigma^2 * time}$$

* Disclaimer these ages are entirely made up and do not reflect reality

2: Brownian motion on a phylogeny

Variance proportional to time and rate

$$dX_{(t)} = \sigma dB_{(t)}$$



$$SD = \sqrt{\sigma^2 * \text{time}}$$

* Disclaimer these ages are entirely made up and do not reflect reality

2: Ornstein-Uhlenbeck

Strength of selection
is proportional to distance of
current trait value from optimum

$$dX_{(t)} = \alpha[\theta - X_{(t)}]dt + \sigma dB_{(t)}$$

Pull towards optimum
(Strength of selection)

Primary optimum

Brownian motion
(Brownian motion rate σ^2)

2: Ornstein-Uhlenbeck = Brownian motion when α is 0

$$dX_{(t)} = \color{purple}{0}[\theta - X_{(t)}]dt + \sigma dB_{(t)}$$


Brownian motion

2: Ornstein-Uhlenbeck = Brownian motion when α is 0

Variance determined by time, σ and α

$$dX_{(t)} = \alpha[\theta - X_{(t)}]dt + \sigma dB_{(t)}$$



Brownian motion

$$dX_{(t)} = \alpha[\theta - X_{(t)}]dt + \sigma dB_{(t)}$$

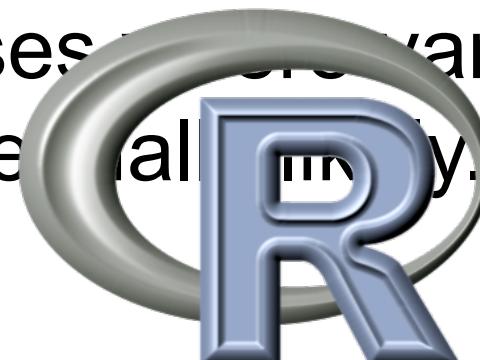
Are σ and α identifiable? As a decrease in rate (σ^2) and an increase in α both reduce variance of the trait at the tips of the tree.

- Yes (theoretically) an increase in α will erode the phylogenetic pattern of the trait but a decrease in σ^2 will not.
- However there will be cases where various estimates σ of and α are equally likely.

$$dX_{(t)} = \alpha[\theta - X_{(t)}]dt + \sigma dB_{(t)}$$

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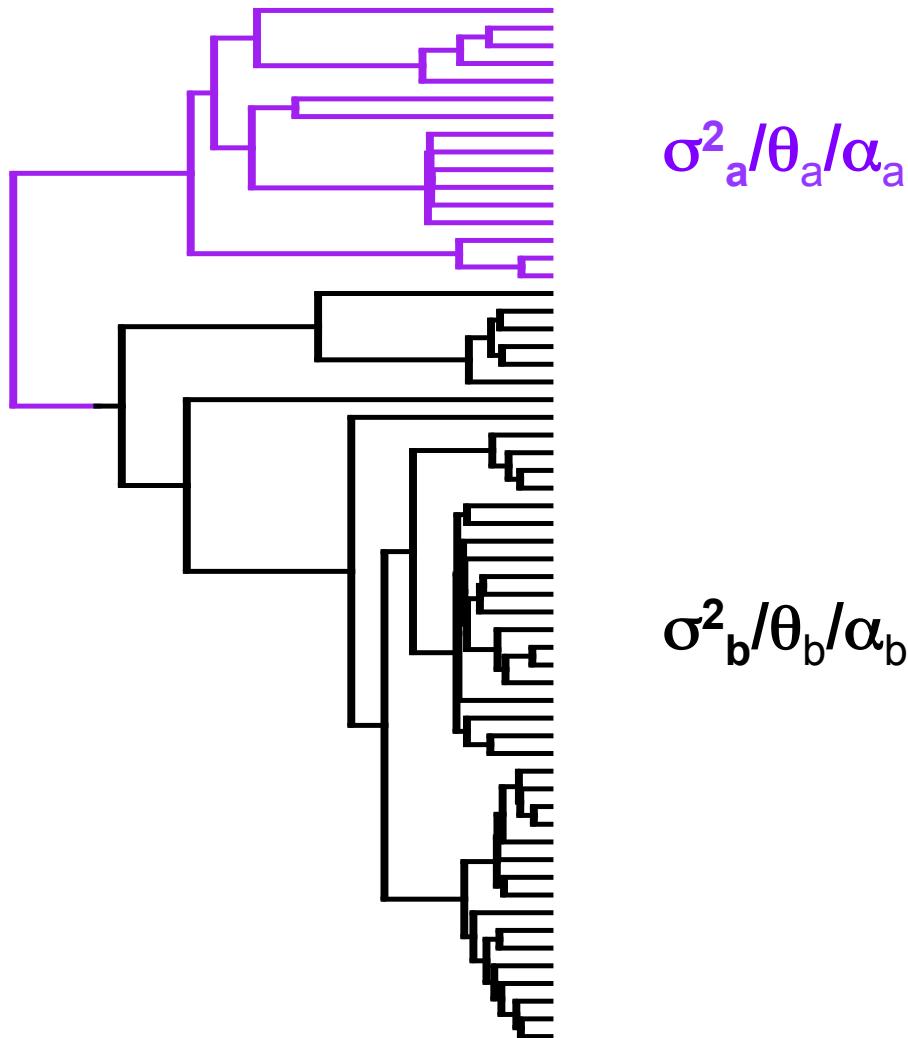
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3: Different θ , α and/or σ on different branches

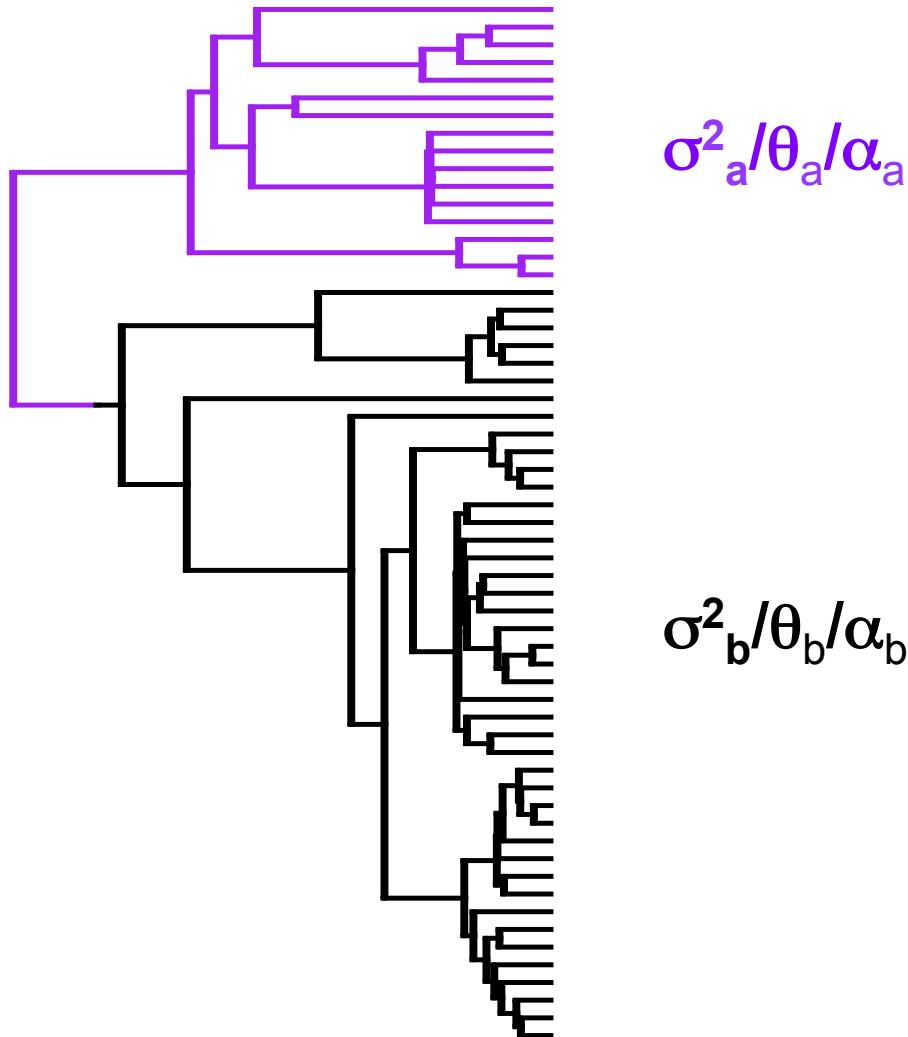


Hypothesis testing

OUCH
OUWIE
Geomorph
MotMot
Phytools
mvMORPH
SLOUCH
mvSLOUCH



3: Different θ , α and/or σ on different branches



Hypothesis testing

OUCH
OUWIE
Geomorph
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Identification of shifts

with no *a priori* hypothesis
MotMot
bayOU
phytools
SURFACE (convergence)
BAMM (not in R)

3: Examples

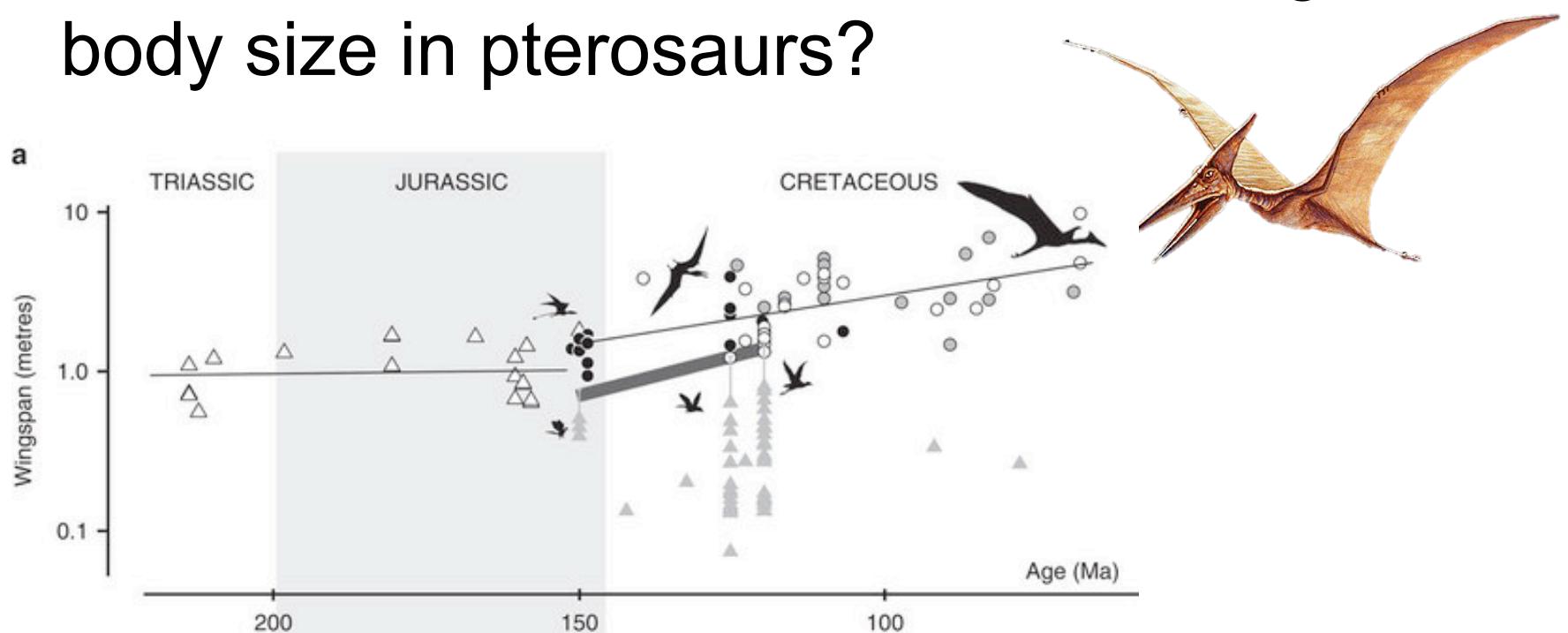
- Does the loss of heterostyly constrain floral morphology in primroses?



de Vos et al. 2014 Evolution 68 (4)

3: Examples

- Do did the evolution of birds drive larger body size in pterosaurs?



Benson et al. 2014 Nature

3: Different θ , α and/or σ on different branches

Model	θ	σ	α
BM1	-	Universal	-
OU1	Universal	Universal	Universal
BMS	-	Variable	-
OUM	Variable	Universal	Universal
OUMA	Variable	Universal	Variable
OUMV	Variable	Variable	Universal
OUMVA	Variable	Variable	Variable



**MODELING STABILIZING SELECTION:
EXPANDING THE ORNSTEIN-UHLENBECK
MODEL OF ADAPTIVE EVOLUTION**

doi:10.1111/j.1558-5646.2012.01619.x



OUwie

Jeremy M. Beaulieu,^{1,2} Dwueng-Chwuan Jhwueng,^{3,4} Carl Boettiger,⁵ and Brian C. O'Meara⁶

3: Caution/Caveat

- BM/OU models influenced by
 - Tree shape
 - Measurement error
 - Number of regimes/parameters estimated vs number taxa
 - Evenness of species number in each regime.

Remember: simulation!

MACROEVOLUTIONARY EXPERIMENTAL DESIGN

Either pick your questions appropriate to your clade (i.e. that you have the power to answer) or pick your clade to answer your question of interest.

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Either pick your questions appropriate to your clade (i.e. that you have the power to answer) or pick your clade to answer your question of interest.

- **Simulation is your friend**, with small datasets you can demonstrate what you have the power to detect.