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Let's make  
these two  
look more  
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**More generally,**

$$P(k \text{ heads on } n \text{ flips}) = \binom{n}{k} \cdot P(H)^k \cdot (1 - P(H))^{n-k}$$