10920EECS101001 Logic Design

Homework 2

1. (20%) Simplify the following Boolean function, together with the don't-care conditions d. Express the simplified function in sum-of-products form. Also express the canonical form of each simplified function.

$$F(A, B, C, D) = \Sigma m(1,3,5,7,9,15) + \Sigma d(4,11,12)$$

- 2. (20%) Simplify the following Boolean function by first finding the essential prime implicants. Please also indicate the essential prime implicants and the other (nonessential) prime implicants.
 - (a) (10%) F(w, x, y, z) = wz' + xy + y'z + wx'z
 - (b) (10%) $F(w, x, y, z) = \Sigma(0,2,3,5,7,8,10,11,14,15)$
- **3.** (20%) Simplify the following function and show its logic circuit. Is there a potential hazard in the circuit? How do you eliminate it if there is one?

$$F(x, y, z) = \Sigma(3,4,6,7)$$

- **4.** (20%) For the Boolean functions f and g, as given in the truth table.
 - (a) (10%) Express f and g in sum-of-minterms algebraic form, and then simplify them to reduced sop form.
 - (b) (10%) Draw the logic diagrams for f and g from its reduced sop form, using only the NOT, AND, and OR gates.

а	b	С	f	8
0 0 0 0 1 1 1	0 0 1 1 0 0	0 1 0 1 0 1	0 0 0 1 0 1	0 1 1 0 1 0 0
1 1	1 1	0 1	$\begin{vmatrix} 1 \\ 1 \end{vmatrix}$	0 1

5. (20%) Simplify the following Boolean function F using

$$F(A, B, C, D) = AB + BCD + AD + A'CD' + A'B'CD$$

- (a) (15%) NAND-AND two-level form, and draw its logic diagram
- (b) (5%) NOR-AND two-level form, and draw its logic diagram