1.
$$xy^2y' = y+1$$
; $y(3e^2) = 2$
 $\left\{ \frac{1}{2}y^2 - y + \ln(y+1) = \ln(x) - 2 \right\}$

2.
$$y + e^{x} + xy' = 0$$

{ $xy + e^{x} = c$ }

3.
$$1+(3x-e^{-2y})y'=0$$

{ $xe^{3y}-e^y=c$ }

4.
$$y' - \frac{3}{x}y = 2x^2$$

{ $y = cx^3 + 2x^3 \ln|x|$ }

5.
$$yy' = 2x \sec(3y)$$
; $y(2/3) = \pi/3$
 $\{3y \sin(3y) + \cos(3y) = 9x^2 - 5\}$

6.
$$y' + \frac{1}{x-2}y = 3x$$
; $y(3) = 4$
{ $y = x^2 - x - 2$ }

7.
$$y' = \frac{3x - y - 9}{x + y + 1}$$

{3(x-2)² - 2(x-2)(y+3) - (y+3)² = c}

8.
$$\frac{dy}{dx} = \frac{x - e^{-x}}{y + e^{y}}$$
$$\{ y^{2} - x^{2} + 2(e^{y} - e^{-x}) = c \}$$

9.
$$y' + \frac{2}{x+1}y = 3$$
; $y(0) = 5$
{ $y = x+1+4(x+1)^{-2}$ }

10.
$$yx^{y-1} + x^y \ln(x)y' = 0$$

{ $x^y = c$ }

11.
$$y' = \frac{x - y + 8}{y - 3x + 2}$$

$$(\sqrt{2}-1)\ln(\sqrt{2}+1-\frac{y-13}{x-5})-(\sqrt{2}+1)\ln(\sqrt{2}-1+\frac{y-13}{x-5})-2\ln(x-5)=c$$

12.
$$4xy + 6y^2 + (2x^2 + 6xy)y' = 0$$

 $\{x^4y^2 + 2x^3y^3 = c\}$

13.
$$xy' + y = x \sin x$$

 $\{ y = \frac{1}{x} (c + \sin x) - \cos x \}$

14.
$$y'-4y = x-x^2$$

 $\{y = ce^{4x} + \frac{x^2}{4} - \frac{x}{8} - \frac{1}{32}\}$

15.
$$y' = (\cos^2 x)(\cos^2 2y)$$

{ $2\tan 2y - 2x - \sin 2x = c$ }

16.
$$y' = \frac{x^2 + 2xy - 4y^2}{x^2 - 8xy - 4y^2}$$

{ $x + y = c(x^2 + 4y^2)$ }

17.
$$y' = -e^{-x}y^2 + y + e^x$$

 $\{ y = e^x + \frac{2e^x}{ce^{2x} - 1} \}$

18.
$$y' = \frac{x^2 - y^2}{xy}$$

{ $x^2(x^2 - 2y^2) = c$ }

19.
$$y' = \frac{2x - 5y - 9}{-4x + y + 9}$$

{ $(2x + y - 3)^2 = c(y - x + 3)$ }

20.
$$(6x + y^2)dx + y(2x - 3y)dy = 0$$

 $\{3x^2 + y^2x - y^3 = c\}$

21.
$$xy'+(x-2)y = 3x^3e^{-x}$$

{ $y = x^2(c+3x)e^{-x}$ }