

Your name: \_\_\_\_\_ ID: \_\_\_\_\_ Oct. 26<sup>th</sup>, 2020

EE214000 Electromagnetics, Fall, 2020

Quiz #7-2, Open books, notes (15 points), due in class, Monday, Oct. 26<sup>st</sup>, 2020

1. What are the electrostatic boundary conditions between a dielectric/ideal conductor interface. Denote the dielectric and the ideal conductor as materials 1 and 2, respectively. (5 points)

$$\hat{a}_{n12} \cdot (\vec{D}_1 - \vec{D}_2) = \rho_s$$

$$\therefore \hat{a}_{n12} \cdot \vec{D}_1 = \rho_s$$

2. Given  $S$  and  $d$  in the following expression for a parallel plate capacitor,

$$C = \frac{\epsilon S}{d},$$

create a physical picture to explain the larger  $\epsilon$ , the larger  $C$ . (5 points)

$\epsilon = \epsilon_r \epsilon_0$ , 當  $\epsilon_r \uparrow \Rightarrow \epsilon \uparrow \Rightarrow \chi_e \uparrow$   
(其中  $\epsilon_r = 1 + \chi_e$ )

$\chi_e$  越大表示介電質的極化程度越大  
 $\Rightarrow$  產生更多 electric dipole moment

$\Rightarrow E_{in} \uparrow$

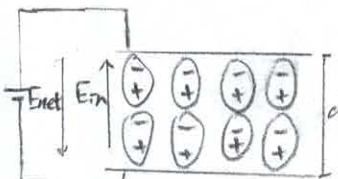
$\Rightarrow E_{net} \downarrow$

但為達到相同  $V$

故會有更多電荷跑

至導體板上 (此時  $E_{net}$  又會重新  $\uparrow$ )

$\therefore C \uparrow$



3. An infinite long line charge along the  $z$  axis has a line charge density of  $\rho_l$ . Calculate the voltage difference  $V_2(r_2, \phi_2, z_2) - V_1(r_1, \phi_1, z_1)$ . (5 points)

無限長線電荷  $\vec{E} = \frac{\rho_l}{2\pi\epsilon_0 r} \hat{a}_r$

$$V_2(r_2, \phi_2, z_2) - V_1(r_1, \phi_1, z_1) = \int_{r_1}^{r_2} dV = - \int_{r_1}^{r_2} \vec{E} \cdot d\vec{r} = - \int_{r_1}^{r_2} \frac{\rho_l}{2\pi\epsilon_0 r} dr$$

$$= \frac{\rho_l}{2\pi\epsilon_0} \ln\left(\frac{r_1}{r_2}\right)$$