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p的倍较

 $(1a)^{1}$ n=1, F₁ = F₀ +2 = 3 + 2 = 5 = True.

2° Assume n = k-1 is True.

s.t. Fk-1 = Fox F, x ... x Fk-2 +2 = 22 +1

then Fk = 22k+1

 $=(2^{2^{k-1}}+1)(2^{2^{k-1}}-1)+2$

= Fk-1 × (Fk-1-2) + 2

= FK-1 (FoxF1x ... x FK-2) +2

= Fox Fix x Fk-2 x Fk-1 + 2 #

3° By 1° 2°, We proved.

(16) Choose 2 num from F

Fn = Fox ... × Fn-1 +2 (Fn+k = Fo x ... x Fn+k-1 + 2

Assume p is Fn's 因數, then: Fn+k=Fox...xFn+k-1+2

(s: Fn = Fox ... Fxn-1 +2 = p = 1 = p = 1 非2的倍较)

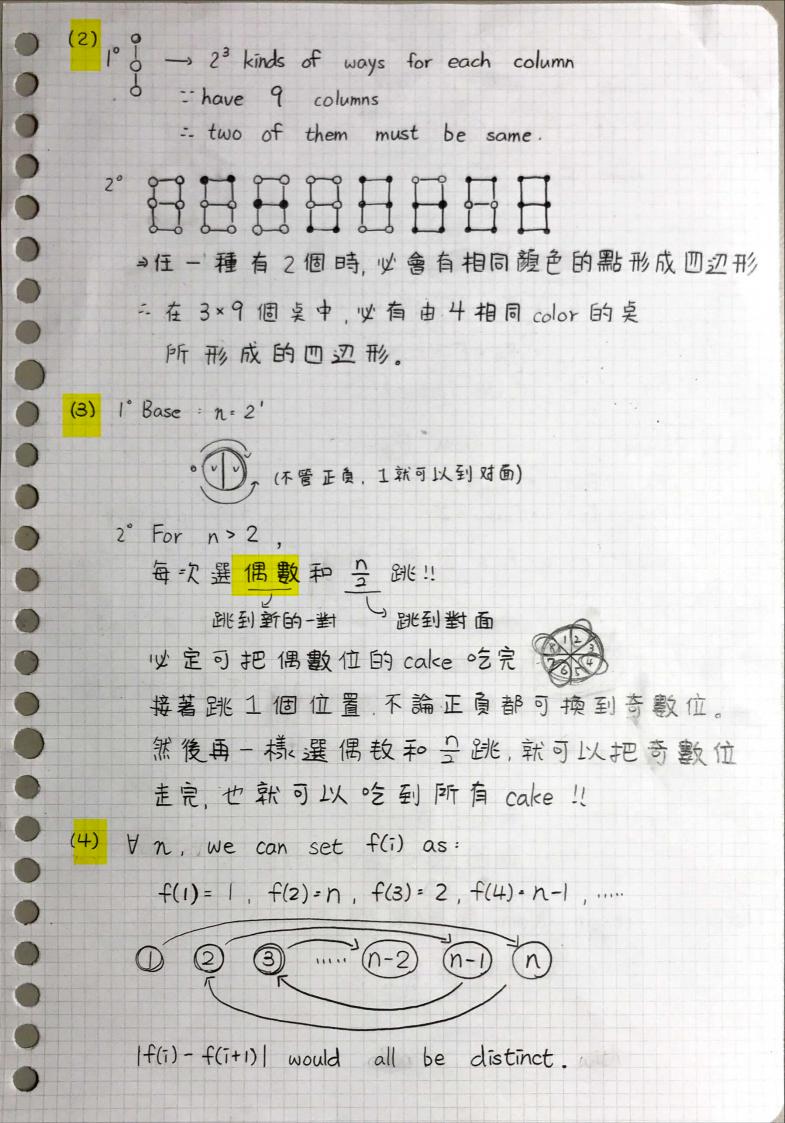
⇒ Fn+k = p×(——) + 2 ○ 不是 p 的 倍 较

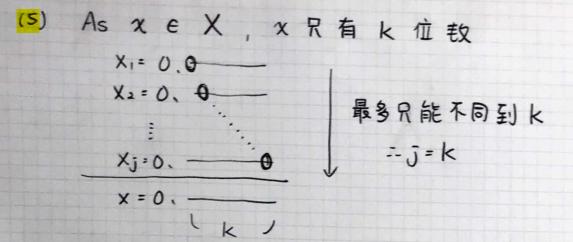
-- Fermat Num 必定互質

(Ic) By (Ib), 二兩兩互質 二質因 牧业 定不 同!!

Fermat Num 有無限個且 (Ic) (Id)

-- prime 有無限多個!!





但Xk+1 立後的項有可能與 X 一樣,所以 證明不成立。