## 10720EECS203002

Ordinary Differential Equation 1st Midterm Exam – Home Test

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## First order ODE

1: 
$$y' + 2y = x \sin x$$
 (10%)  
2:  $y' + 2y = e^{-2x} \tan x$  (10%)

## **Second order ODE**

(Non-homogeneous)

$$3: y'' + 2y' + y = e^{-4x}$$
 (10%)

$$4: y'' + 3y' + 2y = e^{-x}$$
 (10%)

$$5: y'' + 2y' + y = e^{-x}$$
 (10%)

(Cauchy equation)

6: 
$$x^2y'' + xy' + y = 4\sin(\ln x)$$
 (10%)

(Taylor)

7: 
$$(1-x^2)y'' - 2xy' + 12y = 0$$
,  $-1 \le x \le 1$  (10%)  
8:  $y'' + xy = 0$  (10%)

(Frobenius)

9: 
$$x^2y'' - (x^2 + x)y' + y = 0$$
 (10%)

$$10: x^2y'' + xy' + (x^2 - u^2)y = 0 \ , \ 0 \le x \le R \ , \ u = 0,1,2,3 \dots \ \ (10\%)$$