

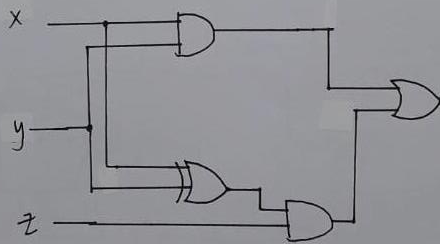
1.

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$$(a) x'y'z + xy'z + xyz + xyz'$$

$$= z(x'y' + xy') + xy(z + z')$$

$$= z(x+y)(x'+y') + xy$$



$$\begin{aligned}
 (b) \quad & [x(y' + z) + y'z(x + w)]' \\
 &= [x(y' + z)]' \cdot [y'z(x + w)]' \\
 &= [x' + (y' + z)'] \cdot [(y' + z)' + (x + w)'] \\
 &= (x' + y'z') \cdot (y + z' + x'w')
 \end{aligned}$$

$$\begin{aligned}
 (c) \quad & [x(y + y'(z + w))]' \\
 &= x' + (y + y'(z + w))' \\
 &= x' + y' \cdot [y'(z + w)]' \\
 &= x' + y' \cdot (y + (z + w)') \\
 &= x' + y' \cdot (y + z'w')
 \end{aligned}$$

$$\begin{aligned}
 (d) \quad & (xy' + y(x + z))' \\
 &= (xy')' \cdot (y(x + z))' \\
 &= (x' + y) \cdot (y' + (x + z)') \\
 &= (x' + y) \cdot (y' + x'z')
 \end{aligned}$$

3. $A = 11010101$

$B = 01110001$

(a) $A \cdot B = 01010001$

(b)

$$A \odot B = A \cdot B + (A + B)'$$

$$A \cdot B = 01010001$$

$$A' \cdot B' = 00001010$$

$$A \odot B = 01011011$$

(c) $\text{NOT } A \Rightarrow A' = 00101010$

4. $F = x'yz' + w'y + wyz'$

| w | x | y | z | F | |
|---|---|---|---|---|----------|
| 0 | 0 | 0 | 0 | 0 | m_0 |
| 0 | 0 | 0 | 1 | 0 | m_1 |
| 0 | 0 | 1 | 0 | 1 | m_2 |
| 0 | 0 | 1 | 1 | 0 | m_3 |
| 0 | 1 | 0 | 0 | 0 | m_4 |
| 0 | 1 | 0 | 1 | 0 | m_5 |
| 0 | 1 | 1 | 0 | 1 | m_6 |
| 0 | 1 | 1 | 1 | 0 | m_7 |
| 1 | 0 | 0 | 0 | 0 | m_8 |
| 1 | 0 | 0 | 1 | 0 | m_9 |
| 1 | 0 | 1 | 0 | 1 | m_{10} |
| 1 | 0 | 1 | 1 | 0 | m_{11} |
| 1 | 1 | 0 | 0 | 0 | m_{12} |
| 1 | 1 | 0 | 1 | 0 | m_{13} |
| 1 | 1 | 1 | 0 | 1 | m_{14} |
| 1 | 1 | 1 | 1 | 0 | m_{15} |

$$F = \Sigma(2, 6, 10, 14).$$

$$= w'x'y'z' + w'x'yz' + w'xy'z + wxyz'$$

$$\begin{aligned} F' &= w'x'y'z' + w'x'y'z + w'x'yz' + w'xy'z' \\ &\quad + w'xyz + w'x'yz' + w'xy'z + w'xyz \\ &\quad + w'x'yz' + w'xyz' + w'xyz + w'xyz. \end{aligned}$$

$$F = (F')'$$

$$= (w+x+y+z)(w+x+y+z')(w+x+y'+z')(w+x'+y+z)$$

$$(w+x'+y+z')(w+x'+y'+z')(w'+x+y+z)(w'+x+y+z')$$

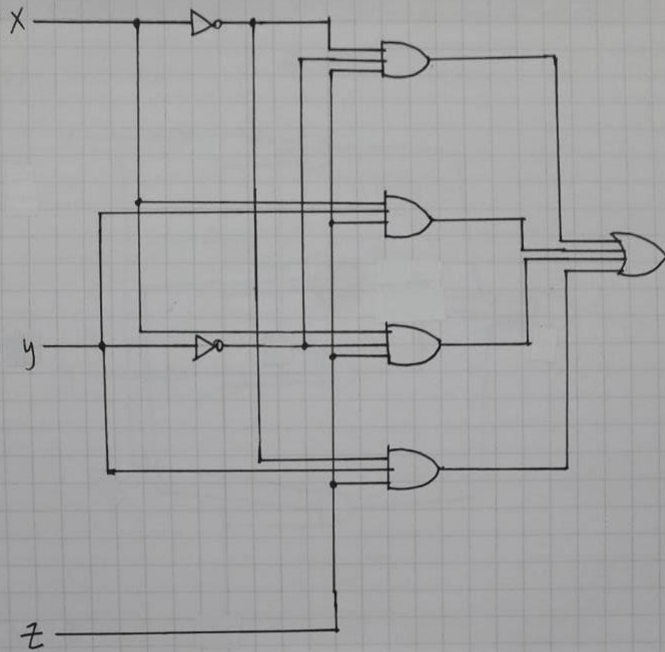
$$(w'+x+y'+z')(w'+x'+y+z)(w'+x'+y+z')$$

$$(w'+x'+y'+z')$$

5. $F = x'y'z + x'y'z + xy'z + x'y'z$

| x | y | z | F |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 1 | 1 |
| 0 | 1 | 0 | 0 |
| 0 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 |
| 1 | 0 | 1 | 1 |
| 1 | 1 | 0 | 0 |
| 1 | 1 | 1 | 1 |

(b)



$$(c) \quad x'y'z + \underline{x'y'z} + \underline{xy'z} + x'yz$$

$$= xz(y' + y) + x'z(y' + y)$$

$$= xz + x'z$$

$$= z(x + x')$$

$$= z$$

(d)

| z | G |
|---|---|
| 0 | 0 |
| 1 | 1 |

(e) $F = x'y'z + xy'z + xyz + x'yz$

3 AND, 1 OR, 4 gates

$G = z$

1 AND, 1 gate

