

Your name: _____ ID: _____

Sep. 21, 2020

EE214000 Electromagnetics, Fall, 2020

Quiz #3-1, Open books, notes (32 points), due 11 pm, Wednesday, Sep. 23, 2020
(email solutions to 劉峰麒 alex851225@gmail.com)

Late submission won't be accepted!

1. Given a vector, \vec{A} , how do you calculate its unit vector? (1 point) Suppose $\vec{B} = 2\hat{a}_x + 4\hat{a}_y + 4\hat{a}_z$, what is its unit vector? (1 point)
2. In the x - y plane, assume $\vec{A} = \hat{a}_x + 3\hat{a}_y$ and $\vec{B} = 2\hat{a}_x + \hat{a}_y$. Explain that the calculation $\vec{C} = \vec{A} + \vec{B} = (1+2)\hat{a}_x + (3+1)\hat{a}_y = 3\hat{a}_x + 4\hat{a}_y$ is consistent with the head-to-tail construction for \vec{C} in the x - y plane. (5 points)
3. What is the physical meaning of the scalar product of a vector \vec{A} and an unit vector \hat{a}_u or $\vec{A} \cdot \hat{a}_u$? Use graph illustration to explain it. (3 points)
4. What is the area of the parallelogram expanded by the two vectors, $\vec{l}_A = \hat{a}_x + 3\hat{a}_y$ (m) and $\vec{l}_B = 2\hat{a}_x + \hat{a}_y$ (m)? (3 points)

5. What is the physical meaning of $(\vec{A} \times \vec{B}) \cdot \vec{C}$ in space. Use graphic illustration to explain it. (5 points).
6. In an orthogonal coordinate system with a differential length of $d\vec{l} = d\vec{l}_{u_1} + d\vec{l}_{u_2} + d\vec{l}_{u_3}$, what are the expressions for a differential surface (3 points) and a differential volume in this coordinate system? (1 point)
7. What are the 3 differential length vectors in the cylindrical coordinate system? (3 points)
8. What are the 3 differential area vectors in the spherical coordinate system? (3 points)
9. Use vector calculus to calculate the surface area of a sphere with radius of a . (2 points)
10. Use vector calculus to calculate the volume of a sphere with radius a . (2 points)