

Комбинаторная задача
Вариант №3

2)

A	B	C	$(A \& B) \vee (B \& \bar{C})$
0	0	0	1
1	0	0	1
0	1	0	1
0	0	1	1
1	1	0	1
1	0	1	1
0	1	1	1
1	1	1	0

3)

x	y	z	$\phi(x, y, z)$	
0	0	0	1	$\bar{x} \bar{y} \bar{z}$
1	0	0	0	
2	0	1	0	
3	0	1	1	$\bar{x} \bar{y} z$
4	1	0	0	
5	1	0	1	

6	1	1	0	1	$x \bar{y} y \bar{z}$
7	1	1	1	1	$x \bar{y} y \bar{z}$

$$f(x, y, z) = (\bar{x} \wedge \bar{y} \wedge \bar{z}) \vee (\bar{x} \wedge y \wedge \bar{z}) \vee (x \wedge y \wedge \bar{z}) \vee (x \wedge y \wedge z)$$

$$4) W = (011001101010001001) = 8$$

$$W = (11100010) = 5$$

$$5) A = (1010101010101010)$$

$$B = (0000111110111111)$$

$$d(A, B) = 7$$

$$6) t = 1$$

$$V_{000} \quad d(V_1, V_0) = 1 \quad d(V_5, V_3) = 2 \quad d(V_7, V_1) = 2$$

$$001 \quad d(V_2, V_0) = 1 \quad d(V_5, V_6) = 2$$

$$010 \quad d(V_3, V_0) = 2 \quad d(V_5, V_6) = 1$$

$$V_{011} \quad d(V_4, V_0) = 1$$

$$100 \quad d(V_5, V_0) = 2$$

$$V_{101} \quad d(V_6, V_0) = 2$$

$$V_{110} \quad d(V_3, V_0) = 3$$

$$111$$

$$G = \{V_0\}$$

$$G = \{V_0, V_1\}$$

$$G = \{V_0, V_1, V_2\}$$

$$G = \{V_0, V_1, V_2, V_3\}$$

$$5) 0000$$

$$0001$$

$$0010$$

$$0011$$

$$0100$$

$$0101$$

$$0110$$

$$0111$$

$$1000$$

$$1001$$

$$1010$$

$$1011$$

$$1100$$

$$1101$$

$$1110$$

$$1111$$

$$G = \{V_0\}$$

$t=2$

$$d(V_1, V_0) = 1$$

$$d(V_2, V_0) = 1$$

$$d(V_3, V_0) = 2$$

$$d(V_4, V_0) = 1$$

$$d(V_5, V_0) = 2$$

$$d(V_6, V_0) = 2$$

$$d(V_7, V_0) = 3$$

$$d(V_8, V_0) = 1$$

$$d(V_9, V_0) = 2$$

$$d(V_{10}, V_0) = 2$$

$$d(V_{11}, V_0) = 3$$

$$d(V_{12}, V_0) = 2$$

$$d(V_{13}, V_0) = 3$$

$$d(V_{14}, V_0) = 3$$

$$d(V_{15}, V_0) = 4$$

$$G = \{V_0, V_1, V_2\}$$

$$d(V_{11}, V_4) = 2$$

$$d(V_{11}, V_{13}) = 2$$

$$d(V_{11}, V_{14}) = 2$$

$$d(V_{11}, V_{15}) = 1$$

$$G = \{V_0, V_{15}\}$$

$$8) P = \lceil \log_2(1+1) \rceil = 1$$

$$P_2 \lceil \log_2 4 \rceil = 2$$

$$P_{16} \lceil \log_2 16 \rceil = 4$$

$$P_{22} \lceil \log_2 23 \rceil = 5$$

$$9) M = 10111 \quad P_5 = \lceil \log_2 6 \rceil = 3$$

$$M_4 = 10111000$$

1	2	3	4	5	6	7	8	9
0	1	0	1	1	0	1	0	0

0	0	1	1
0	1	0	1
<hr/>			
0	1	1	0

$$10) \begin{array}{cccccccccccc} 1 & 1 & 1 & 1 & 1 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 0 & 1 \end{array}$$

$$1100 \quad 111$$

$$J_1 = 1 + 1 + \cancel{1} + 1 + \cancel{1} + 1 + 1 + 0 + 0 + 0 + 1 + 0 + 1 +$$

$$+ 1 = 1$$

$$J_2 = 1 + 1 + 0 + 1 + 0 + 1 + 1 + \cancel{0} + \cancel{0} + \cancel{1} + \cancel{0} + \cancel{1} + 0 + 1 + 1 =$$

$$21$$

$$J_3 = 1 + 1 + 0 + 1 + 0 + 1 + 1 + 0 + 1 + 1 + 1 + 0 =$$

$$= 0$$

$$j_4 = 0 + 0 + 1 + 0 + 1 + 1 + 0 + 0 + 1 + 1 + 1 + 2 = 10$$

$$j_5 = 0 + 0 + 1 + 0 + 1 + 1 + 1 + 0 + 0 + 1 + 1 + 1 = 9$$

$$J = 11001_2 = 25$$

Ошибка в 25 разряде, нечетная 0.

1111 1011 0010 1100 0101 1100 0111

11)

$$G = \begin{pmatrix} 100 & 110 \\ 010 & 011 \\ 001 & 101 \end{pmatrix}$$

$$H = \begin{pmatrix} 101100 \\ 110010 \\ 011001 \end{pmatrix}$$

$$H^T = \begin{pmatrix} 110 \\ 011 \\ 101 \\ 100 \\ 010 \\ 001 \end{pmatrix}$$

$$\oplus \begin{array}{r} 100110 \\ 010011 \\ \hline 110101 \end{array}$$

$$a = 110101$$

$$\hat{a} = 010101$$

$$\hat{a} H^T = (0 \cdot 1 \oplus 1 \cdot 0 \oplus 0 \cdot 1 \oplus 1 \cdot 1 \oplus 0 \cdot 0 \oplus 1 \cdot 0 = 1$$

$$0 \cdot 1 \oplus 1 \cdot 1 \oplus 0 \cdot 0 \oplus 1 \cdot 0 \oplus 0 \cdot 1 \oplus 1 \cdot 0 = 1$$

$$0 \cdot 0 \oplus 1 \cdot 1 \oplus 0 \cdot 0 \oplus 1 \cdot 0 \oplus 0 \cdot 0 \oplus 1 \cdot 1 = 0 = 110$$

110 соответствует 100, гармонично.

$$1) A \vee \bar{A} \wedge (B \wedge \vee A) = 1 \wedge (B \wedge 1) = \\ = 1 \wedge 1 = 1$$

$$((x \vee y) \& \bar{x}) \vee ((\bar{x} \vee y) \& \bar{x}) = (x \vee y) \vee (\bar{x} \vee y) = \\ = 1$$

$$(A \vee \bar{B}) \& (\bar{A} \vee B) \vee \overline{A \& B} = (A \vee \bar{B}) \& (\bar{A} \vee B) \vee \bar{A} \vee \bar{B} = \\ = \overline{(\bar{A} \vee \bar{B})} \& (\bar{A} \vee \bar{B}) \& (\bar{A} \vee \bar{B})$$

$$= (A \vee \bar{B}) \& (\bar{A} \vee B) \vee \bar{A} \vee \bar{B} = (A \vee B) \& 1 \vee A = \\ = A \vee B \& 1 = \overline{A \vee B} \& 1 = 1 \& B = B$$

$$a \wedge (\bar{a} \vee b \vee c) \vee b \wedge (\bar{a} \vee \bar{b}) = (a \wedge (\bar{a} \vee a \vee c) \vee \bar{a} \wedge \\ \wedge (\bar{b} \vee \bar{b})) = b \wedge (1 \vee c) \vee \bar{a} \wedge 1 = b \wedge 1 \vee \bar{a} = \\ = 1 \vee \bar{a} = 1$$

$$a \wedge 1(x \rightarrow c) \vee c = a \wedge (x \vee c) \vee c = a \wedge (c \vee c) \vee \bar{x} = \\ = a \wedge c \vee \bar{x} = a \wedge (c \vee \bar{x})$$