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第一章 Combinatorial optimization

1.1 Sparse max-flow

```
// Adjacency list implementation of Dinic's blocking flow algorithm.
   // This is very fast in practice, and only loses to push—relabel flow.
   // Running time:
5
          O(|V|^2 |E|)
   //
   // INPUT:
   //
          - graph, constructed using AddEdge()
9
           source and sink
10
   //
11
   // OUTPUT:
12
   //
          - maximum flow value
13
           - To obtain actual flow values, look at edges with capacity > 0
14
   //
             (zero capacity edges are residual edges).
15
   #include<cstdio>
16
17
   #include<vector>
18
   #include<queue>
19
   using namespace std;
   typedef long long LL;
20
21
22
   struct Edge {
23
      int u, v;
     LL cap, flow;
24
25
     Edge() {}
     Edge(int u, int v, LL cap): u(u), v(v), cap(cap), flow(0) {}
26
27
   };
28
29
   struct Dinic {
30
     int N;
     vector<Edge> E;
31
32
     vector<vector<int>> g;
     vector<int> d, pt;
33
34
     Dinic(int N): N(N), E(0), g(N), d(N), pt(N) {}
35
36
     void AddEdge(int u, int v, LL cap) {
37
        if (u != v) {
38
          E.emplace_back(Edge(u, v, cap));
39
40
          g[u].emplace_back(E.size() - 1);
          E.emplace_back(Edge(v, u, 0));
41
42
          g[v].emplace_back(E.size() - 1);
```

```
43
       }
      }
44
45
46
      bool BFS(int S, int T) {
47
        queue<int> q({S});
        fill(d.begin(), d.end(), N + 1);
48
        d[S] = 0;
49
50
        while(!q.empty()) {
          int u = q.front(); q.pop();
51
          if (u == T) break;
52
          for (int k: g[u]) {
53
            Edge &e = E[k];
54
            if (e.flow < e.cap && d[e.v] > d[e.u] + 1) {
55
56
              d[e.v] = d[e.u] + 1;
57
              q.emplace(e.v);
58
            }
59
          }
60
61
        return d[T] != N + 1;
     }
62
63
      LL DFS(int u, int T, LL flow = -1) {
64
65
        if (u == T || flow == 0) return flow;
        for (int &i = pt[u]; i < g[u].size(); ++i) {</pre>
66
67
          Edge &e = E[g[u][i]];
68
          Edge &oe = E[g[u][i]^1];
69
          if (d[e.v] == d[e.u] + 1) {
70
            LL amt = e.cap - e.flow;
71
            if (flow !=-1 && amt > flow) amt = flow;
72
            if (LL pushed = DFS(e.v, T, amt)) {
73
              e.flow += pushed;
74
              oe.flow -= pushed;
75
              return pushed;
76
77
          }
78
        }
79
        return 0;
80
81
82
     LL MaxFlow(int S, int T) {
83
        LL total = 0;
84
        while (BFS(S, T)) {
85
          fill(pt.begin(), pt.end(), 0);
86
          while (LL flow = DFS(S, T))
87
            total += flow;
88
        }
89
        return total;
90
     }
91
   };
92
93
   // BEGIN CUT
94
    // The following code solves SPOJ problem #4110: Fast Maximum Flow (FASTFLOW)
95
96
   int main()
```

```
97
98
      int N, E;
      scanf("%d%d", &N, &E);
99
      Dinic dinic(N);
100
      for(int i = 0; i < E; i++)
101
102
103
        int u, v;
104
        LL cap;
        scanf("%d%d%lld", &u, &v, &cap);
105
        dinic.AddEdge(u - 1, v - 1, cap);
106
107
        dinic.AddEdge(v - 1, u - 1, cap);
108
      }
      printf("%lld\n", dinic.MaxFlow(0, N - 1));
109
110
      return 0;
111
    }
112
113 // END CUT
```

1.2 测试

- 1. 模板分三类,公式模板,函数模板,类模板。
- 2. 需使用宏定义,库函数,直接在开头定义,尽量少使用全局变量。
- 3. 函数名, 类名使用驼峰命名法, 开头字母大写。
- 4. 除数论模板尽量使用 long long 类型,其他无特殊情况尽量使用 int 类型。
- 5. 类开头注释标注公有接口函数,除接口函数外,其他变量函数,尽量私有。
- 6. 使用 C++14 标准,尽量少包含 C 风格代码。
- 7. 若函数或类返回值有特殊含义,需标注。
- 8. 注意事项代码开头用注释形式标注,注释格式使用如下。

```
/*
*代码格式
*代码格式
*代码格式
*(代码格式
*/
//代码格式
```

- 9. 图论邻接表、邻接矩阵等数组存储结构,都是从1开始存储。
- 10. 模板前标明作者

1.3 最小费用最大流

```
1 // Implementation of min cost max flow algorithm using adjacency
   // matrix (Edmonds and Karp 1972). This implementation keeps track of
   // forward and reverse edges separately (so you can set cap[i][j] !=
4
   // cap[j][i]). For a regular max flow, set all edge costs to 0.
5
   //
   // Running time, O(|V|^2) cost per augmentation
6
          max flow:
                              O(|V|^3) augmentations
7
   //
8
          min cost max flow: O(|V|^4 * MAX\_EDGE\_COST) augmentations
9
   //
   // INPUT:
10
11
   //
          graph, constructed using AddEdge()
12
          source
          sink
13
   //
   //
14
15
16
   直接中文
17
18
   //
19
20
   测试在代码中加入中文
21
   //
22
23
24
   english中文
25
26
27
   // OUTPUT:
28
29
   //
          - (maximum flow value, minimum cost value)
          - To obtain the actual flow, look at positive values only.
30
31
32
   #include <cmath>
33
   #include <vector>
34
   #include <iostream>
35
36
   using namespace std;
37
38
   typedef vector<int> VI;
39
   typedef vector<VI> VVI;
   typedef long long L;
40
   typedef vector<L> VL;
41
42
   typedef vector<VL> VVL;
   typedef pair<int, int> PII;
43
   typedef vector<PII> VPII;
44
45
46
   const L INF = numeric_limits<L>::max() / 4;
47
48
   struct MinCostMaxFlow {
49
     int N;
50
     VVL cap, flow, cost;
51
     VI found;
52
     VL dist, pi, width;
53
     VPII dad;
54
```

```
55
      MinCostMaxFlow(int N) :
         N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N, VL(N)),
56
57
        found(N), dist(N), pi(N), width(N), dad(N) {}
58
59
      void AddEdge(int from, int to, L cap, L cost) {
60
        this->cap[from][to] = cap;
61
        this->cost[from][to] = cost;
62
      }
63
      void Relax(int s, int k, L cap, L cost, int dir) {
64
65
        L val = dist[s] + pi[s] - pi[k] + cost;
66
        if (cap && val < dist[k]) {</pre>
67
          dist[k] = val;
68
          dad[k] = make_pair(s, dir);
69
          width[k] = min(cap, width[s]);
70
        }
      }
71
72
73
      L Dijkstra(int s, int t) {
        fill(found.begin(), found.end(), false);
74
75
        fill(dist.begin(), dist.end(), INF);
         fill(width.begin(), width.end(), 0);
76
77
        dist[s] = 0;
78
         width[s] = INF;
79
80
        while (s != -1) {
81
           int best = -1;
82
          found[s] = true;
83
          for (int k = 0; k < N; k++) {
84
             if (found[k]) continue;
85
             Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
86
             Relax(s, k, flow[k][s], -\cos t[k][s], -1);
87
             if (best == -1 \mid \mid dist[k] < dist[best]) best = k;
88
          }
89
          s = best;
90
91
92
         for (int k = 0; k < N; k++)
93
           pi[k] = min(pi[k] + dist[k], INF);
94
        return width[t];
95
      }
96
97
      pair<L, L> GetMaxFlow(int s, int t) {
98
         L totflow = 0, totcost = 0;
99
         while (L amt = Dijkstra(s, t)) {
100
          totflow += amt;
101
          for (int x = t; x != s; x = dad[x].first) {
102
             if (dad[x].second == 1) {
103
               flow[dad[x].first][x] += amt;
104
               totcost += amt * cost[dad[x].first][x];
105
             } else {
               flow[x][dad[x].first] -= amt;
106
107
               totcost -= amt * cost[x][dad[x].first];
108
```

```
109
110
111
        return make_pair(totflow, totcost);
112
      }
113
    };
114
115
    // BEGIN CUT
116
    // The following code solves UVA problem #10594: Data Flow
117
118
    int main() {
119
      int N, M;
120
121
      while (scanf("%d%d", &N, &M) == 2) {
122
        VVL \ v(M, \ VL(3));
123
        for (int i = 0; i < M; i++)
           scanf("%Ld%Ld%Ld", &v[i][0], &v[i][1], &v[i][2]);
124
125
126
         scanf("%Ld%Ld", &D, &K);
127
128
        MinCostMaxFlow mcmf(N+1);
129
        for (int i = 0; i < M; i++) {
130
           mcmf.AddEdge(int(v[i][0]), int(v[i][1]), K, v[i][2]);
131
           mcmf.AddEdge(int(v[i][1]), int(v[i][0]), K, v[i][2]);
132
133
        mcmf.AddEdge(0, 1, D, 0);
134
135
        pair<L, L> res = mcmf.GetMaxFlow(0, N);
136
137
        if (res.first == D) {
           printf("%Ld\n", res.second);
138
139
        } else {
           printf("Impossible.\n");
140
141
        }
142
      }
143
144
      return 0;
145
    }
146
147 // END CUT
```

1.4 Push-relabel max-flow

```
// Adjacency list implementation of FIFO push relabel maximum flow
// with the gap relabeling heuristic. This implementation is
// significantly faster than straight Ford—Fulkerson. It solves
// random problems with 10000 vertices and 1000000 edges in a few
// seconds, though it is possible to construct test cases that
// achieve the worst—case.
// //
// Running time:
// O(|V|^3)
// O(|V|^3)
```

```
// INPUT:
11
           graph, constructed using AddEdge()
12
   //
13
   //
           source
14
           – sink
15
   //
   // OUTPUT:
16
17
   //

    maximum flow value

18
           - To obtain the actual flow values, look at all edges with
             capacity > 0 (zero capacity edges are residual edges).
19
   //
20
21
   #include <cmath>
   #include <vector>
22
23
   #include <iostream>
   #include <queue>
24
25
26
   using namespace std;
27
28
   typedef long long LL;
29
30
   struct Edge {
31
     int from, to, cap, flow, index;
      Edge(int from, int to, int cap, int flow, int index) :
32
33
        from(from), to(to), cap(cap), flow(flow), index(index) {}
34
   };
35
36
   struct PushRelabel {
37
      int N;
38
      vector<vector<Edge> > G;
39
     vector<LL> excess;
40
      vector<int> dist, active, count;
41
      queue<int> Q;
42
      PushRelabel(int N) : N(N), G(N), excess(N), dist(N), active(N), count(2*N) {}
43
44
45
     void AddEdge(int from, int to, int cap) {
46
        G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
47
        if (from == to) G[from].back().index++;
48
        G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
49
     }
50
51
     void Enqueue(int v) {
52
        if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
53
     }
54
     void Push(Edge &e) {
55
56
        int amt = int(min(excess[e.from], LL(e.cap - e.flow)));
57
        if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
        e.flow += amt;
58
        G[e.to][e.index].flow -= amt;
59
60
        excess[e.to] += amt;
61
        excess[e.from] -= amt;
        Enqueue(e.to);
62
63
     }
64
```

```
65
      void Gap(int k) {
         for (int v = 0; v < N; v++) {
66
           if (dist[v] < k) continue;</pre>
67
68
           count[dist[v]]--;
69
           dist[v] = max(dist[v], N+1);
           count[dist[v]]++;
70
           Enqueue(v);
71
72
        }
      }
73
74
      void Relabel(int v) {
75
76
         count[dist[v]]--;
77
         dist[v] = 2*N;
         for (int i = 0; i < G[v].size(); i++)</pre>
78
           if (G[v][i].cap - G[v][i].flow > 0)
79
80
         dist[v] = min(dist[v], dist[G[v][i].to] + 1);
81
         count[dist[v]]++;
82
         Enqueue(v);
83
      }
84
85
      void Discharge(int v) {
         for (int i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]);
86
87
         if (excess[v] > 0) {
           if (count[dist[v]] == 1)
88
89
         Gap(dist[v]);
90
           else
91
         Relabel(v);
92
         }
93
      }
94
95
      LL GetMaxFlow(int s, int t) {
96
         count[0] = N-1;
97
         count[N] = 1;
98
         dist[s] = N;
99
         active[s] = active[t] = true;
100
         for (int i = 0; i < G[s].size(); i++) {</pre>
101
           excess[s] += G[s][i].cap;
102
           Push(G[s][i]);
103
         }
104
105
         while (!Q.empty()) {
106
           int v = Q.front();
107
           Q.pop();
108
           active[v] = false;
109
           Discharge(v);
110
         }
111
112
         LL totflow = 0;
113
         for (int i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;</pre>
114
         return totflow;
115
      }
116
    };
117
118 // BEGIN CUT
```

```
// The following code solves SPOJ problem #4110: Fast Maximum Flow (FASTFLOW)
119
120
121
    int main() {
122
      int n, m;
      scanf("%d%d", &n, &m);
123
124
      PushRelabel pr(n);
125
126
      for (int i = 0; i < m; i++) {
127
       int a, b, c;
         scanf("%d%d%d", &a, &b, &c);
128
129
        if (a == b) continue;
130
        pr.AddEdge(a-1, b-1, c);
131
        pr.AddEdge(b-1, a-1, c);
132
      }
133
      printf("%Ld\n", pr.GetMaxFlow(0, n-1));
134
      return 0;
135
    }
136
137 // END CUT
```

1.5 最小费用匹配

```
2
  // Min cost bipartite matching via shortest augmenting paths
3
  //
4
  // This is an O(n^3) implementation of a shortest augmenting path
  // algorithm for finding min cost perfect matchings in dense
5
  // graphs. In practice, it solves 1000x1000 problems in around 1
6
7
  // second.
8
  //
       cost[i][j] = cost for pairing left node i with right node j
9
       Lmate[i] = index of right node that left node i pairs with
10
   //
   //
       Rmate[j] = index of left node that right node j pairs with
11
12
  //
   // The values in cost[i][j] may be positive or negative. To perform
13
   // maximization, simply negate the cost[][] matrix.
14
   15
16
  #include <algorithm>
17
   #include <cstdio>
18
   #include <cmath>
19
20
   #include <vector>
21
   using namespace std;
22
23
   typedef vector<double> VD;
24
   typedef vector<VD> VVD;
25
   typedef vector<int> VI;
26
27
   double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
28
     int n = int(cost.size());
29
30
```

```
31
     // construct dual feasible solution
     VD u(n);
32
33
     VD v(n);
34
     for (int i = 0; i < n; i++) {
35
        u[i] = cost[i][0];
        for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);
36
37
     }
38
     for (int j = 0; j < n; j++) {
        v[j] = cost[0][j] - u[0];
39
        for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);
40
41
     }
42
     // construct primal solution satisfying complementary slackness
43
44
      Lmate = VI(n, -1);
      Rmate = VI(n, -1);
45
46
      int mated = 0;
     for (int i = 0; i < n; i++) {
47
48
        for (int j = 0; j < n; j++) {
49
          if (Rmate[j] != -1) continue;
50
          if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {</pre>
51
        Lmate[i] = j;
52
        Rmate[j] = i;
53
        mated++;
54
        break;
55
          }
56
57
     }
58
59
     VD dist(n);
60
     VI dad(n);
61
     VI seen(n);
62
     // repeat until primal solution is feasible
63
64
      while (mated < n) {</pre>
65
66
        // find an unmatched left node
67
        int s = 0;
68
        while (Lmate[s] != -1) s++;
69
70
        // initialize Dijkstra
71
        fill(dad.begin(), dad.end(), -1);
72
        fill(seen.begin(), seen.end(), 0);
73
        for (int k = 0; k < n; k++)
74
          dist[k] = cost[s][k] - u[s] - v[k];
75
76
        int j = 0;
77
        while (true) {
78
79
          // find closest
80
          j = -1;
81
          for (int k = 0; k < n; k++) {
82
        if (seen[k]) continue;
        if (j == -1 \mid | dist[k] < dist[j]) j = k;
83
84
```

```
85
           seen[j] = 1;
86
           // termination condition
87
88
           if (Rmate[j] == -1) break;
89
           // relax neighbors
90
           const int i = Rmate[j];
91
92
           for (int k = 0; k < n; k++) {
        if (seen[k]) continue;
93
         const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
94
        if (dist[k] > new_dist) {
95
96
           dist[k] = new_dist;
97
           dad[k] = j;
98
99
           }
100
        }
101
102
        // update dual variables
103
        for (int k = 0; k < n; k++) {
           if (k == j || !seen[k]) continue;
104
           const int i = Rmate[k];
105
           v[k] += dist[k] - dist[j];
106
107
           u[i] -= dist[k] - dist[j];
108
109
        u[s] += dist[j];
110
111
        // augment along path
112
        while (dad[j] >= 0) {
113
           const int d = dad[j];
114
           Rmate[j] = Rmate[d];
115
           Lmate[Rmate[j]] = j;
116
           j = d;
117
118
        Rmate[j] = s;
119
        Lmate[s] = j;
120
121
        mated++;
122
123
124
      double value = 0;
125
      for (int i = 0; i < n; i++)
126
        value += cost[i][Lmate[i]];
127
128
      return value;
129
    }
```

1.6 Max bipartite matchine

```
1 // This code performs maximum bipartite matching.
2 //
3 // Running time: O(|E| |V|) — often much faster in practice
4 //
```

```
INPUT: w[i][j] = edge between row node i and column node j
         OUTPUT: mr[i] = assignment for row node i, -1 if unassigned
   //
6
                 mc[j] = assignment for column node j, -1 if unassigned
7
   //
8
                 function returns number of matches made
9
   #include <vector>
10
11
12
    using namespace std;
13
14
    typedef vector<int> VI;
    typedef vector<VI> VVI;
15
16
    bool FindMatch(int i, const VVI &w, VI &mr, VI &mc, VI &seen) {
17
     for (int j = 0; j < w[i].size(); j++) {</pre>
18
19
        if (w[i][j] && !seen[j]) {
20
          seen[j] = true;
21
          if (mc[j] < 0 || FindMatch(mc[j], w, mr, mc, seen)) {</pre>
22
            mr[i] = j;
23
            mc[j] = i;
            return true;
24
25
          }
26
        }
27
28
      return false;
29
   }
30
31
    int BipartiteMatching(const VVI &w, VI &mr, VI &mc) {
32
     mr = VI(w.size(), -1);
33
     mc = VI(w[0].size(), -1);
34
35
     int ct = 0;
     for (int i = 0; i < w.size(); i++) {</pre>
36
37
       VI seen(w[0].size());
        if (FindMatch(i, w, mr, mc, seen)) ct++;
38
39
     }
40
      return ct;
41
   }
```

1.7 Global min-cut

```
// Adjacency matrix implementation of Stoer-Wagner min cut algorithm.
2 //
  // Running time:
3
  //
        0(|V|^3)
4
   11
5
   // INPUT:
6
7
         - graph, constructed using AddEdge()
8
   //
   // OUTPUT:
9
          - (min cut value, nodes in half of min cut)
10
11
12 #include <cmath>
```

```
13
    #include <vector>
    #include <iostream>
14
15
16
    using namespace std;
17
    typedef vector<int> VI;
18
    typedef vector<VI> VVI;
19
20
    const int INF = 1000000000;
21
22
    pair<int, VI> GetMinCut(VVI &weights) {
23
24
      int N = weights.size();
25
      VI used(N), cut, best_cut;
26
      int best_weight = -1;
27
28
      for (int phase = N-1; phase >= 0; phase--) {
29
        VI w = weights[0];
30
        VI added = used;
31
        int prev, last = 0;
        for (int i = 0; i < phase; i++) {</pre>
32
33
          prev = last;
34
          last = -1;
35
          for (int j = 1; j < N; j++)
        if (!added[j] \&\& (last == -1 || w[j] > w[last])) last = j;
36
37
          if (i == phase-1) {
38
        for (int j = 0; j < N; j++) weights[prev][j] += weights[last][j];</pre>
39
        for (int j = 0; j < N; j++) weights[j][prev] = weights[prev][j];</pre>
40
        used[last] = true;
41
        cut.push_back(last);
        if (best_weight == -1 || w[last] < best_weight) {</pre>
42
43
          best_cut = cut;
44
          best_weight = w[last];
45
46
          } else {
47
        for (int j = 0; j < N; j++)
48
          w[j] += weights[last][j];
49
        added[last] = true;
50
          }
51
        }
52
      return make pair(best weight, best cut);
53
54
55
   // BEGIN CUT
56
   // The following code solves UVA problem #10989: Bomb, Divide and Conquer
57
   int main() {
58
59
      int N;
60
      cin >> N;
61
      for (int i = 0; i < N; i++) {
62
        int n, m;
63
        cin >> n >> m;
64
        VVI weights(n, VI(n));
65
        for (int j = 0; j < m; j++) {
66
          int a, b, c;
```

1.8 Graph cut inference

```
1 // Special-purpose {0,1} combinatorial optimization solver for
   // problems of the following by a reduction to graph cuts:
3
   //
4
              minimize
                               sum_i psi_i(x[i])
   // x[1]...x[n] in \{0,1\}
                                 + sum_{i < j} phi_{ij}(x[i], x[j])
5
   //
6
7
   // where
           psi_i : {0, 1} --> R
8
        phi_{ij} : \{0, 1\} \times \{0, 1\} \longrightarrow R
9
   //
10
11
   // such that
        phi_{ij}(0,0) + phi_{ij}(1,1) \le phi_{ij}(0,1) + phi_{ij}(1,0) (*)
12
13
   // This can also be used to solve maximization problems where the
14
15
   // direction of the inequality in (*) is reversed.
16
   // INPUT: phi — a matrix such that <math>phi[i][j][u][v] = phi_{ij}(u, v)
17
             psi — a matrix such that psi[i][u] = psi_i(u)
18
19
   //
              x — a vector where the optimal solution will be stored
20
   // OUTPUT: value of the optimal solution
21
22
   // To use this code, create a GraphCutInference object, and call the
23
   // DoInference() method. To perform maximization instead of minimization,
24
   // ensure that #define MAXIMIZATION is enabled.
25
26
   #include <vector>
27
   #include <iostream>
28
29
30
   using namespace std;
31
   typedef vector<int> VI;
32
   typedef vector<VI> VVI;
33
   typedef vector<VVI> VVVI;
34
   typedef vector<VVVI> VVVVI;
35
36
   const int INF = 1000000000;
37
38
   // comment out following line for minimization
39
   #define MAXIMIZATION
40
41
```

```
42
   struct GraphCutInference {
43
      int N;
44
     VVI cap, flow;
45
     VI reached;
46
      int Augment(int s, int t, int a) {
47
48
        reached[s] = 1;
49
        if (s == t) return a;
        for (int k = 0; k < N; k++) {
50
51
          if (reached[k]) continue;
52
          if (int aa = min(a, cap[s][k] - flow[s][k])) {
53
        if (int b = Augment(k, t, aa)) {
54
          flow[s][k] += b;
55
          flow[k][s] -= b;
56
          return b;
57
        }
58
          }
59
60
        return 0;
61
      }
62
63
      int GetMaxFlow(int s, int t) {
64
        N = cap.size();
65
        flow = VVI(N, VI(N));
66
        reached = VI(N);
67
68
        int totflow = 0;
69
        while (int amt = Augment(s, t, INF)) {
70
          totflow += amt;
71
          fill(reached.begin(), reached.end(), 0);
72
        }
73
        return totflow;
74
     }
75
76
     int DoInference(const VVVVI &phi, const VVI &psi, VI &x) {
77
        int M = phi.size();
78
        cap = VVI(M+2, VI(M+2));
79
        VI b(M);
80
        int c = 0;
81
82
        for (int i = 0; i < M; i++) {
83
          b[i] += psi[i][1] - psi[i][0];
84
          c += psi[i][0];
85
          for (int j = 0; j < i; j++)
86
        b[i] += phi[i][j][1][1] - phi[i][j][0][1];
87
          for (int j = i+1; j < M; j++) {
88
        cap[i][j] = phi[i][j][0][1] + phi[i][j][1][0] - phi[i][j][0][0] - phi[i][j][1][1];
        b[i] += phi[i][j][1][0] - phi[i][j][0][0];
89
90
        c += phi[i][j][0][0];
91
          }
92
        }
93
94
   #ifdef MAXIMIZATION
95
        for (int i = 0; i < M; i++) {
```

```
96
           for (int j = i+1; j < M; j++)
         cap[i][j] *= -1;
97
           b[i] *= −1;
98
99
         }
         c *= −1;
100
101
    #endif
102
103
         for (int i = 0; i < M; i++) {
104
           if (b[i] >= 0) {
105
         cap[M][i] = b[i];
106
           } else {
107
         cap[i][M+1] = -b[i];
108
         c += b[i];
109
           }
110
         }
111
112
         int score = GetMaxFlow(M, M+1);
113
         fill(reached.begin(), reached.end(), 0);
114
         Augment(M, M+1, INF);
115
         x = VI(M);
         for (int i = 0; i < M; i++) x[i] = reached[i] ? 0 : 1;
116
117
         score += c;
118
    #ifdef MAXIMIZATION
119
         score *=-1;
120
    #endif
121
122
         return score;
      }
123
124
125
    };
126
127
    int main() {
128
      // solver for "Cat vs. Dog" from NWERC 2008
129
130
131
      int numcases;
132
      cin >> numcases;
133
      for (int caseno = 0; caseno < numcases; caseno++) {</pre>
134
         int c, d, v;
135
         cin >> c >> d >> v;
136
         VVVVI phi(c+d, VVVI(c+d, VVI(2, VI(2))));
137
         VVI psi(c+d, VI(2));
138
         for (int i = 0; i < v; i++) {
139
140
           char p, q;
141
           int u, v;
142
           cin >> p >> u >> q >> v;
143
           u--; v--;
144
           if (p == 'C') {
145
         phi[u][c+v][0][0]++;
146
         phi[c+v][u][0][0]++;
147
           } else {
148
         phi[v][c+u][1][1]++;
149
         phi[c+u][v][1][1]++;
```

第二章 Geometry

2.1 Convex hull

```
// Compute the 2D convex hull of a set of points using the monotone chain
   // algorithm. Eliminate redundant points from the hull if REMOVE REDUNDANT is
3
   // #defined.
4
   //
5
   // Running time: O(n log n)
6
   //
         INPUT:
                  a vector of input points, unordered.
8
   //
         OUTPUT: a vector of points in the convex hull, counterclockwise, starting
9
                  with bottommost/leftmost point
10
11
   #include <cstdio>
   #include <cassert>
12
13
   #include <vector>
   #include <algorithm>
   #include <cmath>
15
   // BEGIN CUT
16
17
   #include <map>
18
   // END CUT
19
   using namespace std;
20
21
22
   #define REMOVE_REDUNDANT
23
   typedef double T;
24
25
   const T EPS = 1e-7;
   struct PT {
26
27
     T x, y;
     PT() {}
28
     PT(T x, T y) : x(x), y(y) {}
29
     bool operator<(const PT &rhs) const { return make_pair(y,x) < make_pair(rhs.y,rhs.x); }</pre>
30
     bool operator==(const PT &rhs) const { return make_pair(y,x) == make_pair(rhs.y,rhs.x); }
31
32
   };
33
   T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
34
   T area2(PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a); }
35
36
   #ifdef REMOVE REDUNDANT
37
   bool between(const PT &a, const PT &b, const PT &c) {
38
39
     return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) <= 0 && (a.y-b.y)*(c.y-b.y) <= 0);
40
   }
   #endif
41
42
```

```
43
    void ConvexHull(vector<PT> &pts) {
44
      sort(pts.begin(), pts.end());
45
      pts.erase(unique(pts.begin(), pts.end()), pts.end());
46
      vector<PT> up, dn;
47
      for (int i = 0; i < pts.size(); i++) {</pre>
48
        while (up.size() > 1 \& area2(up[up.size()-2], up.back(), pts[i]) >= 0) up.pop_back();
49
        while (dn.size() > 1 \& area2(dn[dn.size()-2], dn.back(), pts[i]) <= 0) dn.pop_back();
50
        up.push_back(pts[i]);
51
        dn.push_back(pts[i]);
52
      }
53
      pts = dn;
54
      for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(up[i]);
55
56
    #ifdef REMOVE_REDUNDANT
57
      if (pts.size() <= 2) return;</pre>
58
      dn.clear();
59
      dn.push_back(pts[0]);
60
      dn.push_back(pts[1]);
61
      for (int i = 2; i < pts.size(); i++) {</pre>
62
        if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop_back();
63
        dn.push_back(pts[i]);
64
65
      if (dn.size() >= 3 && between(dn.back(), dn[0], dn[1])) {
66
        dn[0] = dn.back();
67
        dn.pop_back();
68
      }
69
      pts = dn;
70
   #endif
71
   }
72
73
   // BEGIN CUT
74
   // The following code solves SPOJ problem #26: Build the Fence (BSHEEP)
75
   int main() {
76
77
      int t;
78
      scanf("%d", &t);
79
      for (int caseno = 0; caseno < t; caseno++) {</pre>
        int n;
80
81
        scanf("%d", &n);
        vector<PT> v(n);
82
83
        for (int i = 0; i < n; i++) scanf("%lf%lf", &v[i].x, &v[i].y);</pre>
        vector<PT> h(v);
84
        map<PT,int> index;
85
        for (int i = n-1; i >= 0; i--) index[v[i]] = i+1;
86
        ConvexHull(h);
87
88
89
        double len = 0;
        for (int i = 0; i < h.size(); i++) {</pre>
90
          double dx = h[i].x - h[(i+1)\%h.size()].x;
91
92
          double dy = h[i].y - h[(i+1)\%h.size()].y;
93
          len += sqrt(dx*dx+dy*dy);
94
        }
95
96
        if (caseno > 0) printf("\n");
```

```
97
         printf("%.2f\n", len);
         for (int i = 0; i < h.size(); i++) {</pre>
98
99
           if (i > 0) printf("□");
100
           printf("%d", index[h[i]]);
101
102
         printf("\n");
103
      }
104
    }
105
106 // END CUT
```

2.2 Miscellaneous geometry

```
// C++ routines for computational geometry.
2
   #include <iostream>
3
   #include <vector>
4
5
   #include <cmath>
   #include <cassert>
6
7
8
   using namespace std;
9
   double INF = 1e100;
10
   double EPS = 1e-12;
11
12
13
   struct PT {
     double x, y;
14
15
     PT() {}
     PT(double x, double y) : x(x), y(y) {}
16
17
     PT(const PT \&p) : x(p.x), y(p.y)
     PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
18
     PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
19
     PT operator * (double c)
                                   const { return PT(x*c,
20
                                                           y*c ); }
     PT operator / (double c)
21
                                   const { return PT(x/c,
                                                           y/c ); }
22
   };
23
   double dot(PT p, PT q)
24
                              { return p.x*q.x+p.y*q.y; }
25
   double dist2(PT p, PT q) { return dot(p-q,p-q); }
   double cross(PT p, PT q)
26
                             { return p.x*q.y-p.y*q.x; }
   ostream &operator<<(ostream &os, const PT &p) {</pre>
27
      return os << "(" << p.x << "," << p.y << ")";
28
29
   }
30
   // rotate a point CCW or CW around the origin
31
   PT RotateCCW90(PT p)
                           { return PT(-p.y,p.x); }
32
   PT RotateCW90(PT p)
                           { return PT(p.y,-p.x); }
33
   PT RotateCCW(PT p, double t) {
34
     return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
35
   }
36
37
38
   // project point c onto line through a and b
   // assuming a != b
```

```
PT ProjectPointLine(PT a, PT b, PT c) {
40
      return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);
41
42
   }
43
44
   // project point c onto line segment through a and b
45
   PT ProjectPointSegment(PT a, PT b, PT c) {
46
      double r = dot(b-a,b-a);
47
      if (fabs(r) < EPS) return a;</pre>
      r = dot(c-a, b-a)/r;
48
      if (r < 0) return a;
49
50
     if (r > 1) return b;
51
      return a + (b-a)*r;
52
   }
53
54
   // compute distance from c to segment between a and b
55
   double DistancePointSegment(PT a, PT b, PT c) {
      return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
56
57
   }
58
59
   // compute distance between point (x,y,z) and plane ax+by+cz=d
   double DistancePointPlane(double x, double y, double z,
60
                               double a, double b, double c, double d)
61
62
   {
63
      return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
   }
64
65
   // determine if lines from a to b and c to d are parallel or collinear
66
   bool LinesParallel(PT a, PT b, PT c, PT d) {
67
68
      return fabs(cross(b-a, c-d)) < EPS;</pre>
69
   }
70
71
   bool LinesCollinear(PT a, PT b, PT c, PT d) {
72
      return LinesParallel(a, b, c, d)
          && fabs(cross(a-b, a-c)) < EPS
73
74
          && fabs(cross(c-d, c-a)) < EPS;
75
   }
76
   // determine if line segment from a to b intersects with
77
   // line segment from c to d
78
   bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
79
      if (LinesCollinear(a, b, c, d)) {
80
        if (dist2(a, c) < EPS || dist2(a, d) < EPS ||</pre>
81
          dist2(b, c) < EPS || dist2(b, d) < EPS) return true;</pre>
82
        if (dot(c-a, c-b) > 0 \&\& dot(d-a, d-b) > 0 \&\& dot(c-b, d-b) > 0)
83
          return false;
84
        return true;
85
86
      }
      if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
87
      if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
88
      return true;
89
90
   }
91
   // compute intersection of line passing through a and b
   // with line passing through c and d, assuming that unique
```

```
// intersection exists; for segment intersection, check if
95
    // segments intersect first
96
    PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
97
      b=b-a; d=c-d; c=c-a;
      assert(dot(b, b) > EPS && dot(d, d) > EPS);
98
      return a + b*cross(c, d)/cross(b, d);
99
100
   }
101
    // compute center of circle given three points
102
103
   PT ComputeCircleCenter(PT a, PT b, PT c) {
104
      b=(a+b)/2;
105
      c = (a+c)/2;
      return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
106
107
108
109
   // determine if point is in a possibly non-convex polygon (by William
110 // Randolph Franklin); returns 1 for strictly interior points, 0 for
    // strictly exterior points, and 0 or 1 for the remaining points.
111
112 // Note that it is possible to convert this into an *exact* test using
    // integer arithmetic by taking care of the division appropriately
113
    // (making sure to deal with signs properly) and then by writing exact
114
    // tests for checking point on polygon boundary
115
116
   bool PointInPolygon(const vector<PT> &p, PT q) {
117
      bool c = 0;
118
      for (int i = 0; i < p.size(); i++){
119
        int j = (i+1)%p.size();
120
        if ((p[i].y \le q.y \&\& q.y < p[j].y ||
121
          p[j].y <= q.y && q.y < p[i].y) &&
122
          q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
123
          c = !c;
124
      }
125
      return c;
126
    }
127
128
    // determine if point is on the boundary of a polygon
129
    bool PointOnPolygon(const vector<PT> &p, PT q) {
130
      for (int i = 0; i < p.size(); i++)</pre>
131
        if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)</pre>
132
          return true;
133
        return false;
134
    }
135
136
    // compute intersection of line through points a and b with
137
    // circle centered at c with radius r > 0
    vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
138
139
      vector<PT> ret;
140
      b = b-a;
141
      a = a-c;
      double A = dot(b, b);
142
143
      double B = dot(a, b);
144
      double C = dot(a, a) - r*r;
145
      double D = B*B - A*C;
146
      if (D < -EPS) return ret;
147
      ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
```

```
148
      if (D > EPS)
149
        ret.push_back(c+a+b*(-B-sqrt(D))/A);
150
      return ret;
151
   }
152
153
    // compute intersection of circle centered at a with radius r
154
    // with circle centered at b with radius R
155
    vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
156
      vector<PT> ret;
      double d = sqrt(dist2(a, b));
157
      if (d > r+R \mid | d+min(r, R) < max(r, R)) return ret;
158
      double x = (d*d-R*R+r*r)/(2*d);
159
160
      double y = sqrt(r*r-x*x);
      PT v = (b-a)/d;
161
162
      ret.push_back(a+v*x + RotateCCW90(v)*y);
163
      if (y > 0)
        ret.push_back(a+v*x - RotateCCW90(v)*y);
164
165
      return ret;
166
    }
167
168
   // This code computes the area or centroid of a (possibly nonconvex)
169
    // polygon, assuming that the coordinates are listed in a clockwise or
170
   // counterclockwise fashion. Note that the centroid is often known as
    // the "center of gravity" or "center of mass".
171
    double ComputeSignedArea(const vector<PT> &p) {
172
173
      double area = 0;
174
      for(int i = 0; i < p.size(); i++) {
        int j = (i+1) % p.size();
175
176
        area += p[i].x*p[j].y - p[j].x*p[i].y;
177
178
      return area / 2.0;
179
    }
180
181
    double ComputeArea(const vector<PT> &p) {
182
      return fabs(ComputeSignedArea(p));
183
184
185
    PT ComputeCentroid(const vector<PT> &p) {
186
      PT c(0,0);
187
      double scale = 6.0 * ComputeSignedArea(p);
188
      for (int i = 0; i < p.size(); i++){</pre>
        int j = (i+1) % p.size();
189
190
        c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
191
      }
192
      return c / scale;
193
    }
194
195
    // tests whether or not a given polygon (in CW or CCW order) is simple
    bool IsSimple(const vector<PT> &p) {
196
      for (int i = 0; i < p.size(); i++) {</pre>
197
198
        for (int k = i+1; k < p.size(); k++) {
199
          int j = (i+1) % p.size();
200
          int 1 = (k+1) % p.size();
201
          if (i == 1 \mid | j == k) continue;
```

```
202
           if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
203
             return false;
204
         }
205
       }
206
       return true;
207
    }
208
209
    int main() {
210
211
      // expected: (-5,2)
212
      cerr << RotateCCW90(PT(2,5)) << endl;</pre>
213
214
      // expected: (5,-2)
215
       cerr << RotateCW90(PT(2,5)) << endl;</pre>
216
217
      // expected: (-5,2)
218
      cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
219
220
      // expected: (5,2)
221
      cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
222
223
      // expected: (5,2) (7.5,3) (2.5,1)
224
       cerr << ProjectPointSegment(PT(-5,-2), PT(10,4), PT(3,7)) << ""
225
            << ProjectPointSegment(PT(7.5,3), PT(10,4), PT(3,7)) << ""</pre>
226
            << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;</pre>
227
228
      // expected: 6.78903
229
       cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;</pre>
230
231
      // expected: 1 0 1
232
       cerr << LinesParallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << ""
233
            << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << ""
            << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
234
235
236
      // expected: 0 0 1
       cerr << LinesCollinear(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << """
237
            << LinesCollinear(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << "" "
238
239
            << LinesCollinear(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;</pre>
240
241
       // expected: 1 1 1 0
242
       cerr << SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << "\Box"
243
            << SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << "" "
244
            << SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << "_{\perp}"
245
            << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;
246
247
      // expected: (1,2)
248
       cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;
249
250
      // expected: (1,1)
251
       cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;</pre>
252
253
       vector<PT> v;
254
      v.push_back(PT(0,0));
255
      v.push_back(PT(5,0));
```

```
256
      v.push_back(PT(5,5));
257
      v.push_back(PT(0,5));
258
259
      // expected: 1 1 1 0 0
260
      cerr << PointInPolygon(v, PT(2,2)) << ""
            << PointInPolygon(v, PT(2,0)) << ""
261
262
           << PointInPolygon(v, PT(0,2)) << ""
263
            << PointInPolygon(v, PT(5,2)) << ""
           << PointInPolygon(v, PT(2,5)) << endl;
264
265
266
      // expected: 0 1 1 1 1
      cerr << PointOnPolygon(v, PT(2,2)) << ""
267
           << PointOnPolygon(v, PT(2,0)) << ""
268
            << PointOnPolygon(v, PT(0,2)) << "u"
269
270
           << PointOnPolygon(v, PT(5,2)) << ""
           << PointOnPolygon(v, PT(2,5)) << endl;
271
272
273
      // expected: (1,6)
274
      //
                    (5,4)(4,5)
275
      //
                    blank line
276
      //
                    (4,5) (5,4)
277
      //
                    blank line
278
      //
                    (4,5) (5,4)
      vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
279
280
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;
281
      u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);
282
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;
      u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
283
284
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;
285
      u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
286
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;</pre>
287
      u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
288
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;
      u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 5, sqrt(2.0)/2.0);
289
290
      for (int i = 0; i < u.size(); i++) cerr << u[i] << ""; cerr << endl;</pre>
291
292
      // area should be 5.0
293
      // centroid should be (1.1666666, 1.166666)
294
      PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
295
      vector<PT> p(pa, pa+4);
296
      PT c = ComputeCentroid(p);
      cerr << "Area: □" << ComputeArea(p) << endl;</pre>
297
298
      cerr << "Centroid:" << c << endl;</pre>
299
300
      return 0;
301
```

2.3 Java geometry

```
1 // In this example, we read an input file containing three lines, each
2 // containing an even number of doubles, separated by commas. The first two
3 // lines represent the coordinates of two polygons, given in counterclockwise
```

```
// (or clockwise) order, which we will call "A" and "B". The last line
   // contains a list of points, p[1], p[2], ...
6
   //
7
   // Our goal is to determine:
   //
         (1) whether B - A is a single closed shape (as opposed to multiple shapes)
         (2) the area of B-A
         (3) whether each p[i] is in the interior of B-A
10
11
   // INPUT:
12
13
        0 0 10 0 0 10
14
   //
        0 0 10 10 10 0
15
        8 6
16
   //
         5 1
17
   // OUTPUT:
18
19
         The area is singular.
20
   //
        The area is 25.0
        Point belongs to the area.
21
   //
22
        Point does not belong to the area.
   //
23
24
   import java.util.*;
25
   import java.awt.geom.*;
   import java.io.*;
26
27
28
   public class JavaGeometry {
29
30
        // make an array of doubles from a string
31
        static double[] readPoints(String s) {
32
            String[] arr = s.trim().split("\\s++");
33
            double[] ret = new double[arr.length];
34
            for (int i = 0; i < arr.length; i++) ret[i] = Double.parseDouble(arr[i]);</pre>
35
            return ret;
36
        }
37
38
        // make an Area object from the coordinates of a polygon
39
        static Area makeArea(double[] pts) {
40
            Path2D.Double p = new Path2D.Double();
            p.moveTo(pts[0], pts[1]);
41
42
            for (int i = 2; i < pts.length; i += 2) p.lineTo(pts[i], pts[i+1]);</pre>
            p.closePath();
43
            return new Area(p);
44
45
        }
46
47
        // compute area of polygon
        static double computePolygonArea(ArrayList<Point2D.Double> points) {
48
49
            Point2D.Double[] pts = points.toArray(new Point2D.Double[points.size()]);
50
            double area = 0;
            for (int i = 0; i < pts.length; i++){
51
                int j = (i+1) % pts.length;
52
                area += pts[i].x * pts[j].y - pts[j].x * pts[i].y;
53
54
            return Math.abs(area)/2;
55
56
        }
57
```

```
58
        // compute the area of an Area object containing several disjoint polygons
        static double computeArea(Area area) {
59
60
             double totArea = 0;
             PathIterator iter = area.getPathIterator(null);
61
62
             ArrayList<Point2D.Double> points = new ArrayList<Point2D.Double>();
63
64
             while (!iter.isDone()) {
65
                 double[] buffer = new double[6];
                 switch (iter.currentSegment(buffer)) {
66
67
                 case PathIterator.SEG_MOVETO:
68
                 case PathIterator.SEG_LINETO:
69
                     points.add(new Point2D.Double(buffer[0], buffer[1]));
70
                     break;
71
                 case PathIterator.SEG_CLOSE:
72
                     totArea += computePolygonArea(points);
73
                     points.clear();
74
                     break;
                 }
75
76
                 iter.next();
77
78
             return totArea;
79
        }
80
81
        // notice that the main() throws an Exception — necessary to
82
        // avoid wrapping the Scanner object for file reading in a
83
        // try { ... } catch block.
        public static void main(String args[]) throws Exception {
84
85
86
             Scanner scanner = new Scanner(new File("input.txt"));
87
             // also.
88
                  Scanner scanner = new Scanner (System.in);
89
90
             double[] pointsA = readPoints(scanner.nextLine());
91
             double[] pointsB = readPoints(scanner.nextLine());
92
             Area areaA = makeArea(pointsA);
93
             Area areaB = makeArea(pointsB);
94
             areaB.subtract(areaA);
95
             // also,
                  areaB.exclusiveOr (areaA);
96
                  areaB.add (areaA);
97
98
                  areaB.intersect (areaA);
99
100
             // (1) determine whether B - A is a single closed shape (as
101
                    opposed to multiple shapes)
102
             boolean isSingle = areaB.isSingular();
103
             // also.
104
                  areaB.isEmpty();
105
106
             if (isSingle)
107
                 System.out.println("The_area_is_singular.");
108
             else
109
                 System.out.println("The_area_is_not_singular.");
110
111
             // (2) compute the area of B - A
```

```
112
             System.out.println("The_area_is_" + computeArea(areaB) + ".");
113
114
            // (3) determine whether each p[i] is in the interior of B-A
115
             while (scanner.hasNextDouble()) {
116
                 double x = scanner.nextDouble();
                 assert(scanner.hasNextDouble());
117
                 double y = scanner.nextDouble();
118
119
                 if (areaB.contains(x,y)) {
120
                     System.out.println ("Pointubelongsutoutheuarea.");
121
122
123
                     System.out.println ("Point_does_not_belong_to_the_area.");
124
                 }
125
             }
126
127
             // Finally, some useful things we didn't use in this example:
128
129
                  Ellipse2D.Double\ ellipse = new\ Ellipse2D.Double\ (double\ x,\ double\ y,
130
             //
                                                                      double w, double h);
131
132
             //
                    creates an ellipse inscribed in box with bottom—left corner (x,y)
133
                    and upper-right corner (x+y,w+h)
134
135
                  Rectangle 2D. Double rect = new Rectangle 2D. Double (double x, double y,
136
                                                                       double w, double h);
             //
137
138
                    creates a box with bottom-left corner (x,y) and upper-right
139
                    corner (x+y,w+h)
140
             //
141
            // Each of these can be embedded in an Area object (e.g., new Area (rect)).
142
143
        }
144
    }
```

2.4 3D geometry

```
public class Geom3D {
     // distance from point (x, y, z) to plane aX + bY + cZ + d = 0
2
     public static double ptPlaneDist(double x, double y, double z,
3
         double a, double b, double c, double d) {
4
       return Math.abs(a*x + b*y + c*z + d) / Math.sqrt(a*a + b*b + c*c);
5
6
     }
7
     // distance between parallel planes aX + bY + cZ + d1 = 0 and
8
9
     // aX + bY + cZ + d2 = 0
     public static double planePlaneDist(double a, double b, double c,
10
         double d1, double d2) {
11
       return Math.abs(d1 - d2) / Math.sqrt(a*a + b*b + c*c);
12
     }
13
14
15
     // distance from point (px, py, pz) to line (x1, y1, z1)–(x2, y2, z2)
16
     // (or ray, or segment; in the case of the ray, the endpoint is the
```

```
// first point)
17
      public static final int LINE = 0;
18
19
      public static final int SEGMENT = 1;
20
      public static final int RAY = 2;
21
      public static double ptLineDistSq(double x1, double y1, double z1,
22
          double x2, double y2, double z2, double px, double py, double pz,
23
          int type) {
24
        double pd2 = (x1-x2)*(x1-x2) + (y1-y2)*(y1-y2) + (z1-z2)*(z1-z2);
25
26
        double x, y, z;
        if (pd2 == 0) {
27
28
          x = x1;
29
          y = y1;
30
          z = z1;
31
        } else {
32
          double u = ((px-x1)*(x2-x1) + (py-y1)*(y2-y1) + (pz-z1)*(z2-z1)) / pd2;
33
          x = x1 + u * (x2 - x1);
34
          y = y1 + u * (y2 - y1);
35
          z = z1 + u * (z2 - z1);
          if (type != LINE && u < 0) {</pre>
36
37
            x = x1;
38
            y = y1;
39
            z = z1;
40
41
          if (type == SEGMENT && u > 1.0) {
42
            x = x2;
43
            y = y2;
44
            z = z2;
45
          }
46
47
48
        return (x-px)*(x-px) + (y-py)*(y-py) + (z-pz)*(z-pz);
49
     }
50
51
      public static double ptLineDist(double x1, double y1, double z1,
52
          double x2, double y2, double z2, double px, double py, double pz,
53
          int type) {
        return Math.sqrt(ptLineDistSq(x1, y1, z1, x2, y2, z2, px, py, pz, type));
54
55
      }
56 }
```

2.5 Slow Delaunay triangulation

```
// Slow but simple Delaunay triangulation. Does not handle
// degenerate cases (from O'Rourke, Computational Geometry in C)
//
// Running time: O(n^4)
// Running time: x[] = x-coordinates
// INPUT: x[] = y-coordinates
// y[] = y-coordinates
// OUTPUT: triples = a vector containing m triples of indices
```

```
10
   //
                             corresponding to triangle vertices
11
12
   #include<vector>
13
   using namespace std;
14
    typedef double T;
15
16
17
    struct triple {
18
        int i, j, k;
19
        triple() {}
20
        triple(int i, int j, int k) : i(i), j(j), k(k) {}
21
   };
22
23
    vector<triple> delaunayTriangulation(vector<T>& x, vector<T>& y) {
24
        int n = x.size();
25
        vector<T> z(n);
26
        vector<triple> ret;
27
28
        for (int i = 0; i < n; i++)
29
            z[i] = x[i] * x[i] + y[i] * y[i];
30
        for (int i = 0; i < n-2; i++) {
31
32
            for (int j = i+1; j < n; j++) {
            for (int k = i+1; k < n; k++) {
33
34
                 if (j == k) continue;
35
                 double xn = (y[j]-y[i])*(z[k]-z[i]) - (y[k]-y[i])*(z[j]-z[i]);
36
                 double yn = (x[k]-x[i])*(z[j]-z[i]) - (x[j]-x[i])*(z[k]-z[i]);
37
                 double zn = (x[j]-x[i])*(y[k]-y[i]) - (x[k]-x[i])*(y[j]-y[i]);
38
                 bool flag = zn < 0;</pre>
39
                for (int m = 0; flag && m < n; m++)
40
                flag = flag && ((x[m]-x[i])*xn +
41
                         (y[m]-y[i])*yn +
42
                         (z[m]-z[i])*zn <= 0);
43
                 if (flag) ret.push_back(triple(i, j, k));
44
            }
45
            }
46
        }
47
        return ret;
48
   }
49
   int main()
50
51
    {
52
        T xs[]={0, 0, 1, 0.9};
53
        T ys[]={0, 1, 0, 0.9};
54
        vector<T> x(&xs[0], &xs[4]), y(&ys[0], &ys[4]);
55
        vector<triple> tri = delaunayTriangulation(x, y);
56
57
        //expected: 0 1 3
                     0 3 2
58
        //
59
60
        int i;
61
        for(i = 0; i < tri.size(); i++)</pre>
62
            printf("%d<sub>\\\\\</sub>%d\\\n", tri[i].i, tri[i].j, tri[i].k);
63
        return 0;
```

64 }

第三章 Numerical algorithms

3.1 Number theory (modular, Chinese remainder, linear Diophantine)

```
// This is a collection of useful code for solving problems that
   // involve modular linear equations. Note that all of the
   // algorithms described here work on nonnegative integers.
4
5
   #include <iostream>
   #include <vector>
    #include <algorithm>
8
9
    using namespace std;
10
11
    typedef vector<int> VI;
12
    typedef pair<int, int> PII;
13
14
   // return a % b (positive value)
    int mod(int a, int b) {
15
16
        return ((a\%b) + b) \% b;
17
18
19
   // computes gcd(a,b)
20
   int gcd(int a, int b) {
        while (b) { int t = a%b; a = b; b = t; }
21
22
        return a;
23
   }
24
25
   // computes lcm(a,b)
   int lcm(int a, int b) {
26
27
        return a / gcd(a, b)*b;
28
   }
29
30
   // (a^b) mod m via successive squaring
    int powermod(int a, int b, int m)
31
32
   {
        int ret = 1;
33
        while (b)
34
35
            if (b & 1) ret = mod(ret*a, m);
36
            a = mod(a*a, m);
37
            b >>= 1;
38
39
40
        return ret;
41
   }
42
```

```
43
   // returns g = gcd(a, b); finds x, y such that d = ax + by
   int extended_euclid(int a, int b, int &x, int &y) {
44
45
        int xx = y = 0;
46
        int yy = x = 1;
47
        while (b) {
48
            int q = a / b;
49
            int t = b; b = a%b; a = t;
50
            t = xx; xx = x - q*xx; x = t;
51
            t = yy; yy = y - q*yy; y = t;
52
53
        return a;
54
   }
55
   // finds all solutions to ax = b (mod n)
56
57
   VI modular_linear_equation_solver(int a, int b, int n) {
58
        int x, y;
59
        VI ret;
        int g = extended_euclid(a, n, x, y);
60
61
        if (!(b%g)) {
62
            x = mod(x*(b / g), n);
63
            for (int i = 0; i < g; i++)
64
                ret.push_back(mod(x + i*(n / g), n));
65
        }
66
        return ret;
67
   }
68
   // computes b such that ab = 1 (mod n), returns -1 on failure
69
70
   int mod_inverse(int a, int n) {
71
        int x, y;
        int g = extended_euclid(a, n, x, y);
72
73
        if (g > 1) return -1;
74
        return mod(x, n);
75
   }
76
   // Chinese remainder theorem (special case): find z such that
77
   // z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1, m2).
78
   // Return (z, M). On failure, M = -1.
79
   PII chinese remainder theorem(int m1, int r1, int m2, int r2) {
80
81
        int s, t;
        int g = extended_euclid(m1, m2, s, t);
82
        if (r1\%g != r2\%g) return make pair(0, -1);
83
        return make_pair(mod(s*r2*m1 + t*r1*m2, m1*m2) / g, m1*m2 / g);
84
85
   }
86
   // Chinese remainder theorem: find z such that
87
   // z % m[i] = r[i] for all i. Note that the solution is
88
89
   // unique modulo M = lcm_i (m[i]). Return (z, M). On
   // failure, M = -1. Note that we do not require the a[i]'s
90
   // to be relatively prime.
91
   PII chinese_remainder_theorem(const VI &m, const VI &r) {
92
93
        PII ret = make_pair(r[0], m[0]);
        for (int i = 1; i < m.size(); i++) {</pre>
94
95
            ret = chinese_remainder_theorem(ret.second, ret.first, m[i], r[i]);
96
            if (ret.second == -1) break;
```

```
97
98
         return ret;
99
    }
100
101
    // computes x and y such that ax + by = c
102
    // returns whether the solution exists
103
    bool linear_diophantine(int a, int b, int c, int &x, int &y) {
104
         if (!a && !b)
105
106
             if (c) return false;
107
             x = 0; y = 0;
108
             return true;
109
         }
         if (!a)
110
111
         {
112
             if (c % b) return false;
113
             x = 0; y = c / b;
114
             return true;
115
         }
         if (!b)
116
117
         {
118
             if (c % a) return false;
119
             x = c / a; y = 0;
120
             return true;
121
         }
122
         int g = gcd(a, b);
123
         if (c % g) return false;
124
         x = c / g * mod_inverse(a / g, b / g);
125
         y = (c - a*x) / b;
126
         return true;
127
    }
128
129
    int main() {
130
         // expected: 2
131
         cout << gcd(14, 30) << endl;</pre>
132
133
         // expected: 2 −2 1
134
         int x, y;
135
         int g = extended_euclid(14, 30, x, y);
136
         cout << g << "\sqcup" << x << "\sqcup" << y << endl;
137
138
         // expected: 95 451
139
         VI sols = modular_linear_equation_solver(14, 30, 100);
         for (int i = 0; i < sols.size(); i++) cout << sols[i] << "□";</pre>
140
141
         cout << endl;</pre>
142
143
         // expected: 8
144
         cout << mod inverse(8, 9) << endl;</pre>
145
146
         // expected: 23 105
147
148
         PII ret = chinese_remainder_theorem(VI({ 3, 5, 7 }), VI({ 2, 3, 2 }));
         cout << ret.first << "" << ret.second << endl;</pre>
149
150
         ret = chinese_remainder_theorem(VI({ 4, 6 }), VI({ 3, 5 }));
```

3.2 Systems of linear equations, matrix inverse, determinant

```
// Gauss-Jordan elimination with full pivoting.
2
   //
   // Uses:
3
        (1) solving systems of linear equations (AX=B)
         (2) inverting matrices (AX=I)
5
        (3) computing determinants of square matrices
   //
6
7
8
   // Running time: O(n^3)
9
   // INPUT: a[][] = an nxn matrix
10
11
   //
                 b[][] = an nxm matrix
12
   //
   // OUTPUT: X
                      = an nxm matrix (stored in b[][])
13
                A^{-1} = an nxn matrix (stored in a[][])
14
   //
   //
                 returns determinant of a[][]
15
16
   #include <iostream>
17
   #include <vector>
18
   #include <cmath>
19
20
   using namespace std;
21
22
   const double EPS = 1e-10;
23
24
   typedef vector<int> VI;
25
   typedef double T;
26
    typedef vector<T> VT;
27
   typedef vector<VT> VVT;
28
29
   T GaussJordan(VVT &a, VVT &b) {
30
     const int n = a.size();
31
32
     const int m = b[0].size();
     VI irow(n), icol(n), ipiv(n);
33
     T det = 1;
34
35
     for (int i = 0; i < n; i++) {
36
       int pj = -1, pk = -1;
37
       for (int j = 0; j < n; j++) if (!ipiv[j])
38
          for (int k = 0; k < n; k++) if (!ipiv[k])
39
        if (pj == -1 \mid | fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
40
        if (fabs(a[pj][pk]) < EPS) { cerr << "Matrixuisusingular." << endl; exit(0); }</pre>
41
42
       ipiv[pk]++;
```

```
43
        swap(a[pj], a[pk]);
        swap(b[pj], b[pk]);
44
45
        if (pj != pk) det *= -1;
46
        irow[i] = pj;
47
        icol[i] = pk;
48
        T c = 1.0 / a[pk][pk];
49
50
        det *= a[pk][pk];
        a[pk][pk] = 1.0;
51
52
        for (int p = 0; p < n; p++) a[pk][p] *= c;
53
        for (int p = 0; p < m; p++) b[pk][p] *= c;
54
        for (int p = 0; p < n; p++) if (p != pk) {
55
          c = a[p][pk];
56
          a[p][pk] = 0;
57
          for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
58
          for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
59
        }
      }
60
61
      for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
62
63
        for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);</pre>
64
      }
65
66
      return det;
67
   }
68
69
    int main() {
70
      const int n = 4;
71
      const int m = 2;
72
      double A[n][n] = \{ \{1,2,3,4\}, \{1,0,1,0\}, \{5,3,2,4\}, \{6,1,4,6\} \};
73
      double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
74
      VVT a(n), b(n);
75
      for (int i = 0; i < n; i++) {
76
        a[i] = VT(A[i], A[i] + n);
77
        b[i] = VT(B[i], B[i] + m);
78
79
80
      double det = GaussJordan(a, b);
81
82
      // expected: 60
83
      cout << "Determinant:" << det << endl;</pre>
84
85
      // expected: -0.233333 0.166667 0.133333 0.0666667
                    0.166667 0.166667 0.333333 -0.333333
86
87
      //
                    0.233333 0.833333 -0.133333 -0.0666667
88
                    0.05 - 0.75 - 0.1 0.2
89
      cout << "Inverse:" << endl;</pre>
90
      for (int i = 0; i < n; i++) {
        for (int j = 0; j < n; j++)
91
92
          cout << a[i][j] << 'u';
93
        cout << endl;</pre>
94
      }
95
96
      // expected: 1.63333 1.3
```

```
97
       //
                     -0.166667 0.5
       //
                     2.36667 1.7
98
99
       //
                     -1.85 -1.35
100
       cout << "Solution:" << endl;</pre>
       for (int i = 0; i < n; i++) {
101
         for (int j = 0; j < m; j++)
102
103
           cout << b[i][j] << 'u';
104
         cout << endl;</pre>
105
       }
106 }
```

3.3 Reduced row echelon form, matrix rank

```
1 // Reduced row echelon form via Gauss—Jordan elimination
   // with partial pivoting. This can be used for computing
   // the rank of a matrix.
3
   //
4
5
   // Running time: O(n^3)
6
   // INPUT:
                 a[][] = an nxm matrix
7
8
9
   // OUTPUT: rref[][] = an nxm matrix (stored in a[][])
10
                 returns rank of a[][]
11
   #include <iostream>
12
13
   #include <vector>
   #include <cmath>
14
15
   using namespace std;
16
17
   const double EPSILON = 1e-10;
18
19
   typedef double T;
20
21
   typedef vector<T> VT;
   typedef vector<VT> VVT;
22
23
   int rref(VVT &a) {
24
25
     int n = a.size();
     int m = a[0].size();
26
     int r = 0;
27
     for (int c = 0; c < m && r < n; c++) {
28
29
        int j = r;
        for (int i = r + 1; i < n; i++)
30
          if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
31
        if (fabs(a[j][c]) < EPSILON) continue;</pre>
32
        swap(a[j], a[r]);
33
34
        T s = 1.0 / a[r][c];
35
        for (int j = 0; j < m; j++) a[r][j] *= s;
36
        for (int i = 0; i < n; i++) if (i != r) {
37
38
          T t = a[i][c];
39
          for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];
```

```
40
41
        r++;
42
      }
43
      return r;
44
   }
45
   int main() {
46
47
      const int n = 5, m = 4;
      double A[n][m] = {
48
        {16, 2, 3, 13},
49
        { 5, 11, 10, 8},
50
        { 9, 7, 6, 12},
51
        { 4, 14, 15, 1},
52
        {13, 21, 21, 13}};
53
      VVT a(n);
54
      for (int i = 0; i < n; i++)
55
        a[i] = VT(A[i], A[i] + m);
56
57
58
      int rank = rref(a);
59
      // expected: 3
60
      cout << "Rank:" << rank << endl;</pre>
61
62
      // expected: 1 0 0 1
63
64
      //
                    0 1 0 3
      //
                    0 0 1 -3
65
66
      //
                    0 0 0 3.10862e-15
                    0 0 0 2.22045e-15
67
      cout << "rref:" << endl;</pre>
68
      for (int i = 0; i < 5; i++) {
69
70
        for (int j = 0; j < 4; j++)
71
          cout << a[i][j] << 'u';
        cout << endl;</pre>
72
73
      }
74 }
```

3.4 Fast Fourier transform

```
#include <cassert>
2
   #include <cstdio>
3
   #include <cmath>
4
   struct cpx
5
6
   {
7
     cpx(){}
     cpx(double aa):a(aa),b(0){}
8
      cpx(double aa, double bb):a(aa),b(bb){}
9
     double a;
10
11
     double b;
     double modsq(void) const
12
13
14
        return a * a + b * b;
```

```
15
16
     cpx bar(void) const
17
18
        return cpx(a, -b);
19
     }
20
   };
21
22
   cpx operator +(cpx a, cpx b)
23
24
     return cpx(a.a + b.a, a.b + b.b);
25
   }
26
27
   cpx operator *(cpx a, cpx b)
28
   {
     return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
29
30
   }
31
32
   cpx operator /(cpx a, cpx b)
33
   {
     cpx r = a * b.bar();
34
35
     return cpx(r.a / b.modsq(), r.b / b.modsq());
36
   }
37
38
   cpx EXP(double theta)
39
40
     return cpx(cos(theta),sin(theta));
41
   }
42
43
   const double two_pi = 4 * acos(0);
44
45
   // in:
               input array
46
   // out:
               output array
47
   // step:
               {SET TO 1} (used internally)
   // size:
               length of the input/output {MUST BE A POWER OF 2}
48
49
   // dir:
               either plus or minus one (direction of the FFT)
   // RESULT: out[k] = \sum_{j=0}^{size - 1} in[j] * exp(dir * 2pi * i * j * k / size)
50
   void FFT(cpx *in, cpx *out, int step, int size, int dir)
51
52
53
     if(size < 1) return;</pre>
     if(size == 1)
54
55
56
        out[0] = in[0];
57
       return;
58
     FFT(in, out, step * 2, size / 2, dir);
59
60
      FFT(in + step, out + size / 2, step * 2, size / 2, dir);
61
     for(int i = 0; i < size / 2; i++)
62
     {
63
        cpx even = out[i];
64
        cpx odd = out[i + size / 2];
65
        out[i] = even + EXP(dir * two_pi * i / size) * odd;
        out[i + size / 2] = even + EXP(dir * two_pi * (i + size / 2) / size) * odd;
66
67
     }
68
   }
```

```
69
    // Usage:
70
71
   // f[0...N-1] and g[0..N-1] are numbers
    // Want to compute the convolution h, defined by
72
   // h[n] = sum \ of \ f[k]g[n-k] \ (k = 0, ..., N-1).
73
    // Here, the index is cyclic; f[-1] = f[N-1], f[-2] = f[N-2], etc.
74
   // Let F[0...N-1] be FFT(f), and similarly, define G and H.
75
76
    // The convolution theorem says H[n] = F[n]G[n] (element—wise product).
    // To compute h[] in O(N log N) time, do the following:
77
        1. Compute F and G (pass dir = 1 as the argument).
78
79
    //
         2. Get H by element—wise multiplying F and G.
80
        3. Get h by taking the inverse FFT (use dir = -1 as the argument)
             and *dividing by N*. DO NOT FORGET THIS SCALING FACTOR.
81
    //
82
83
    int main(void)
84
    {
85
      printf("Ifurowsucomeuinuidenticalupairs,uthenueverythinguworks.\n");
86
87
      cpx a[8] = \{0, 1, cpx(1,3), cpx(0,5), 1, 0, 2, 0\};
88
      cpx b[8] = \{1, cpx(0,-2), cpx(0,1), 3, -1, -3, 1, -2\};
89
      cpx A[8];
90
      cpx B[8];
91
      FFT(a, A, 1, 8, 1);
      FFT(b, B, 1, 8, 1);
92
93
94
      for(int i = 0; i < 8; i++)
95
        printf("%7.21f%7.21f", A[i].a, A[i].b);
96
97
      }
      printf("\n");
98
99
      for(int i = 0; i < 8; i++)
100
      {
101
        cpx Ai(0,0);
102
        for(int j = 0; j < 8; j++)
103
104
          Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
105
106
        printf("%7.21f%7.21f", Ai.a, Ai.b);
107
108
      printf("\n");
109
110
      cpx AB[8];
111
      for(int i = 0; i < 8; i++)
112
        AB[i] = A[i] * B[i];
113
      cpx aconvb[8];
114
      FFT(AB, aconvb, 1, 8, -1);
115
      for(int i = 0; i < 8; i++)
116
        aconvb[i] = aconvb[i] / 8;
      for(int i = 0; i < 8; i++)
117
118
      {
119
        printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
120
      }
121
      printf("\n");
122
      for(int i = 0; i < 8; i++)
```

```
123
124
        cpx aconvbi(0,0);
        for(int j = 0; j < 8; j++)
125
126
           aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
127
128
        printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
129
130
131
      printf("\n");
132
133
       return 0;
134
```

3.5 Simplex algorithm

```
// Two-phase simplex algorithm for solving linear programs of the form
   //
2
   //
3
           maximize
                        c^T X
           subject to
                        Ax <= b
4
5
   //
                        x >= 0
6
7
   // INPUT: A — an m x n matrix
              b — an m-dimensional vector
8
              c — an n-dimensional vector
   //
9
10
   //
              x — a vector where the optimal solution will be stored
11
   // OUTPUT: value of the optimal solution (infinity if unbounded
12
               above, nan if infeasible)
   //
13
14
   // To use this code, create an LPSolver object with A, b, and c as
15
   // arguments. Then, call Solve(x).
16
17
   #include <iostream>
18
19
   #include <iomanip>
   #include <vector>
20
   #include <cmath>
21
   #include <limits>
22
23
   using namespace std;
24
25
   typedef long double DOUBLE;
26
27
   typedef vector<DOUBLE> VD;
   typedef vector<VD> VVD;
28
   typedef vector<int> VI;
29
30
   const DOUBLE EPS = 1e-9;
31
32
   struct LPSolver {
33
     int m, n;
34
35
     VI B, N;
     VVD D;
36
37
```

```
38
      LPSolver(const VVD &A, const VD &b, const VD &c) :
        m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
39
        for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];
40
41
        for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + 1] = b[i]; }
42
        for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
        N[n] = -1; D[m + 1][n] = 1;
43
44
     }
45
     void Pivot(int r, int s) {
46
        double inv = 1.0 / D[r][s];
47
48
        for (int i = 0; i < m + 2; i++) if (i != r)
49
          for (int j = 0; j < n + 2; j++) if (j != s)
            D[i][j] -= D[r][j] * D[i][s] * inv;
50
        for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
51
        for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
52
53
        D[r][s] = inv;
54
        swap(B[r], N[s]);
55
      }
56
57
      bool Simplex(int phase) {
58
        int x = phase == 1 ? m + 1 : m;
59
        while (true) {
60
          int s = -1;
61
          for (int j = 0; j <= n; j++) {
            if (phase == 2 \& N[j] == -1) continue;
62
            if (s == -1 \mid D[x][j] < D[x][s] \mid D[x][j] == D[x][s] && N[j] < N[s]) s = j;
63
          }
64
65
          if (D[x][s] > -EPS) return true;
66
          int r = -1;
67
          for (int i = 0; i < m; i++) {
            if (D[i][s] < EPS) continue;</pre>
68
            if (r == -1 \mid | D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] \mid |
69
70
              (D[i][n + 1] / D[i][s]) == (D[r][n + 1] / D[r][s]) && B[i] < B[r]) r = i;
71
          }
72
          if (r == -1) return false;
73
          Pivot(r, s);
74
       }
75
      }
76
      DOUBLE Solve(VD &x) {
77
78
        int r = 0;
        for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
79
        if (D[r][n + 1] < -EPS) {
80
          Pivot(r, n);
81
          if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return -numeric limits<DOUBLE>::infinity();
82
          for (int i = 0; i < m; i++) if (B[i] == -1) {
83
84
            int s = -1;
            for (int j = 0; j \leftarrow n; j++)
85
              if (s == -1 \mid D[i][j] < D[i][s] \mid D[i][j] == D[i][s] && N[j] < N[s]) s = j;
86
            Pivot(i, s);
87
88
          }
89
90
        if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
91
        x = VD(n);
```

```
for (int i = 0; i < m; i++) if (B[i] < n) \times [B[i]] = D[i][n + 1];
92
         return D[m][n + 1];
93
94
      }
95
    };
96
97
    int main() {
98
99
      const int m = 4;
      const int n = 3;
100
      DOUBLE A[m][n] = {
101
102
        \{ 6, -1, 0 \},
103
        \{ -1, -5, 0 \},
104
        { 1, 5, 1 },
105
        \{ -1, -5, -1 \}
106
      };
107
      DOUBLE _{b[m]} = \{ 10, -4, 5, -5 \};
108
      DOUBLE _{c[n]} = \{ 1, -1, 0 \};
109
110
      VVD A(m);
111
      VD b(b, b + m);
112
      VD c(_c, _c + n);
113
      for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);
114
115
      LPSolver solver(A, b, c);
116
      VD x;
117
      DOUBLE value = solver.Solve(x);
118
      cerr << "VALUE: " << value << endl; // VALUE: 1.29032
119
120
      cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1</pre>
121
      for (size_t i = 0; i < x.size(); i++) cerr << "" << x[i];</pre>
122
      cerr << endl;</pre>
123
       return 0;
124 }
```

第四章 Graph algorithms

4.1 Fast Dijkstra's algorithm

```
// Implementation of Dijkstra's algorithm using adjacency lists
   // and priority queue for efficiency.
3
   // Running time: O(|E| log |V|)
5
6
   #include <queue>
   #include <cstdio>
8
9
   using namespace std;
10
   const int INF = 2000000000;
   typedef pair<int, int> PII;
11
12
13
   int main() {
14
15
        int N, s, t;
16
        scanf("%d%d%d", &N, &s, &t);
17
        vector<vector<PII> > edges(N);
18
        for (int i = 0; i < N; i++) {
19
            int M;
            scanf("%d", &M);
20
21
            for (int j = 0; j < M; j++) {
22
                int vertex, dist;
                scanf("%d%d", &vertex, &dist);
23
                edges[i].push_back(make_pair(dist, vertex)); // note order of arguments here
24
25
            }
        }
26
27
        // use priority queue in which top element has the "smallest" priority
28
29
        priority_queue<PII, vector<PII>, greater<PII> > Q;
30
        vector<int> dist(N, INF), dad(N, −1);
        Q.push(make_pair(0, s));
31
32
        dist[s] = 0;
        while (!Q.empty()) {
33
            PII p = Q.top();
34
35
            Q.pop();
36
            int here = p.second;
            if (here == t) break;
37
            if (dist[here] != p.first) continue;
38
39
40
            for (vector<PII>::iterator it = edges[here].begin(); it != edges[here].end(); it++) {
                if (dist[here] + it->first < dist[it->second]) {
41
42
                    dist[it->second] = dist[here] + it->first;
```

```
43
                     dad[it->second] = here;
                     Q.push(make_pair(dist[it->second], it->second));
44
                 }
45
            }
46
47
        }
48
        printf("%d\n", dist[t]);
49
50
        if (dist[t] < INF)</pre>
            for (int i = t; i != -1; i = dad[i])
51
                 printf("%d%c", i, (i == s ? '\n' : '\_'));
52
53
        return 0;
54
   }
55
56
57
   Sample input:
58
   5 0 4
   2 1 2 3 1
59
   2 2 4 4 5
60
61
   3 1 4 3 3 4 1
   2 0 1 2 3
62
   2 1 5 2 1
63
64
65
   Expected:
66
67
   4 2 3 0
68
```

4.2 Strongly connected components

```
1
   #include<memory.h>
2
   struct edge{int e, nxt;};
   int V, E;
   edge e[MAXE], er[MAXE];
   int sp[MAXV], spr[MAXV];
5
   int group_cnt, group_num[MAXV];
6
   bool v[MAXV];
7
   int stk[MAXV];
8
   void fill_forward(int x)
9
   {
10
     int i;
11
12
     v[x]=true;
     for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i].e);
13
14
      stk[++stk[0]]=x;
15
   }
   void fill_backward(int x)
16
17
   {
      int i;
18
19
     v[x]=false;
20
      group_num[x]=group_cnt;
      for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(er[i].e);
21
22
23
   void add_edge(int v1, int v2) //add edge v1->v2
```

```
24
   {
      e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
25
26
     er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
27
   void SCC()
28
29
   {
     int i;
30
31
      stk[0]=0;
32
      memset(v, false, sizeof(v));
     for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
33
34
35
      for(i=stk[0];i>=1;i--) if(v[stk[i]]){group_cnt++; fill_backward(stk[i]);}
36
   }
```

4.3 Eulerian path

```
struct Edge;
    typedef list<Edge>::iterator iter;
2
3
   struct Edge
4
5
   {
6
        int next_vertex;
7
        iter reverse_edge;
8
9
        Edge(int next_vertex)
10
            :next_vertex(next_vertex)
            { }
11
12
   };
13
14
    const int max_vertices = ;
   int num_vertices;
15
   list<Edge> adj[max_vertices];
                                         // adjacency list
16
17
18
    vector<int> path;
19
   void find_path(int v)
20
    {
21
22
        while(adj[v].size() > 0)
23
        {
            int vn = adj[v].front().next_vertex;
24
            adj[vn].erase(adj[v].front().reverse_edge);
25
26
            adj[v].pop_front();
            find_path(vn);
27
28
        path.push_back(v);
29
30
31
   void add_edge(int a, int b)
32
   {
33
        adj[a].push_front(Edge(b));
34
        iter ita = adj[a].begin();
35
        adj[b].push_front(Edge(a));
36
```

```
iter itb = adj[b].begin();
ita->reverse_edge = itb;
itb->reverse_edge = ita;
40 }
```

第五章 Data structures

5.1 Suffix array

```
1 // Suffix array construction in O(L log^2 L) time. Routine for
   // computing the length of the longest common prefix of any two
   // suffixes in O(log L) time.
4
   //
5
   // INPUT:
               string s
6
   //
   // OUTPUT: array suffix[] such that suffix[i] = index (from 0 to L-1)
   //
                of substring s[i...L-1] in the list of sorted suffixes.
9
                That is, if we take the inverse of the permutation suffix[],
10
                we get the actual suffix array.
11
   #include <vector>
12
13
   #include <iostream>
   #include <string>
14
15
   using namespace std;
16
17
18
   struct SuffixArray {
19
     const int L;
     string s;
20
21
     vector<vector<int> > P;
22
     vector<pair<int,int>,int> > M;
23
24
     SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)), M(L) {
25
        for (int i = 0; i < L; i++) P[0][i] = int(s[i]);
        for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {</pre>
26
27
         P.push back(vector<int>(L, 0));
         for (int i = 0; i < L; i++)
28
29
       M[i] = make_pair(make_pair(P[level-1][i], i + skip < L ? P[level-1][i + skip] : -1000), i)
          sort(M.begin(), M.end());
30
31
         for (int i = 0; i < L; i++)
        P[level][M[i].second] = (i > 0 && M[i].first == M[i-1].first) ? P[level][M[i-1].second] :
32
           i;
33
       }
34
     }
35
     vector<int> GetSuffixArray() { return P.back(); }
36
37
38
     // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1]
     int LongestCommonPrefix(int i, int j) {
39
40
       int len = 0;
```

```
41
        if (i == j) return L - i;
42
        for (int k = P.size() - 1; k >= 0 && i < L && j < L; k--) {
43
          if (P[k][i] == P[k][j]) {
        i += 1 << k;
44
45
        j += 1 << k;
        len += 1 << k;</pre>
46
47
          }
48
49
        return len;
50
51
   };
52
53
   // BEGIN CUT
   // The following code solves UVA problem 11512: GATTACA.
54
55
   #define TESTING
   #ifdef TESTING
56
57
   int main() {
      int T;
58
59
      cin >> T;
      for (int caseno = 0; caseno < T; caseno++) {</pre>
60
61
        string s;
62
        cin >> s;
63
        SuffixArray array(s);
        vector<int> v = array.GetSuffixArray();
64
65
        int bestlen = -1, bestpos = -1, bestcount = 0;
        for (int i = 0; i < s.length(); i++) {</pre>
66
67
          int len = 0, count = 0;
          for (int j = i+1; j < s.length(); j++) {</pre>
68
69
        int 1 = array.LongestCommonPrefix(i, j);
70
        if (1 >= len) {
71
          if (1 > len) count = 2; else count++;
72
          len = 1;
73
        }
74
75
          if (len > bestlen || len == bestlen && s.substr(bestpos, bestlen) > s.substr(i, len)) {
76
        bestlen = len;
77
        bestcount = count;
        bestpos = i;
78
79
          }
80
81
        if (bestlen == 0) {
82
          cout << "Nourepetitionsufound!" << endl;</pre>
83
          cout << s.substr(bestpos, bestlen) << "" << bestcount << endl;</pre>
84
85
        }
86
87
   }
88
   #else
89
    // END CUT
90
91
   int main() {
92
93
      // bobocel is the 0'th suffix
94
     // obocel is the 5'th suffix
```

```
95
           bocel is the 1'st suffix
      //
            ocel is the 6'th suffix
96
            cel is the 2'nd suffix
97
      //
98
              el is the 3'rd suffix
              l is the 4'th suffix
99
      //
      SuffixArray suffix("bobocel");
100
101
      vector<int> v = suffix.GetSuffixArray();
102
103
      // Expected output: 0 5 1 6 2 3 4
104
      //
105
      for (int i = 0; i < v.size(); i++) cout << v[i] << "";
106
      cout << suffix.LongestCommonPrefix(0, 2) << endl;</pre>
107
108
109
    // BEGIN CUT
110
   #endif
111 // END CUT
```

5.2 Binary Indexed Tree

```
#include <iostream>
   using namespace std;
2
3
   #define LOGSZ 17
4
5
6
   int tree[(1<<LOGSZ)+1];</pre>
   int N = (1 << LOGSZ);
7
8
9
   // add v to value at x
   void set(int x, int v) {
10
      while(x <= N) {
11
       tree[x] += v;
12
        x += (x \& -x);
13
14
      }
   }
15
16
    // get cumulative sum up to and including x
17
   int get(int x) {
18
      int res = 0;
19
      while(x) {
20
        res += tree[x];
21
22
        x = (x \& -x);
23
      }
24
      return res;
   }
25
26
   // get largest value with cumulative sum less than or equal to x;
27
   // for smallest, pass x-1 and add 1 to result
28
   int getind(int x) {
29
      int idx = 0, mask = N;
30
      while(mask && idx < N) {</pre>
31
        int t = idx + mask;
32
```

```
if(x >= tree[t]) {
    idx = t;
    x -= tree[t];
    mask >>= 1;
    }
    return idx;
}
```

5.3 Union-find set

```
#include <iostream>
   #include <vector>
3
  using namespace std;
   int find(vector<int> &C, int x) { return (C[x] == x) ? x : C[x] = find(C, C[x]); }
   void merge(vector<int> &C, int x, int y) { C[find(C, x)] = find(C, y); }
   int main()
6
7
   {
8
       int n = 5;
9
       vector<int> C(n);
       for (int i = 0; i < n; i++) C[i] = i;
10
11
       merge(C, 0, 2);
12
       merge(C, 1, 0);
       merge(C, 3, 4);
13
       for (int i = 0; i < n; i++) cout << i << "_{\sqcup}" << find(C, i) << endl;
14
15
       return 0;
16
```

5.4 KD-tree

```
1 // -
   // A straightforward, but probably sub-optimal KD-tree implmentation
   // that's probably good enough for most things (current it's a
3
4 // 2D—tree)
5
   //
   // - constructs from n points in O(n lg^2 n) time
6
   // - handles nearest-neighbor query in O(lg n) if points are well
7
       distributed
8
   // - worst case for nearest-neighbor may be linear in pathological
9
   //
10
         case
11
   // Sonny Chan, Stanford University, April 2009
12
   // -
13
14
   #include <iostream>
15
16 #include <vector>
   #include <limits>
17
   #include <cstdlib>
18
19
```

```
20
   using namespace std;
21
22
   // number type for coordinates, and its maximum value
   typedef long long ntype;
23
24
   const ntype sentry = numeric_limits<ntype>::max();
25
   // point structure for 2D-tree, can be extended to 3D
26
27
   struct point {
28
        ntype x, y;
29
        point(ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
30
   };
31
32
   bool operator==(const point &a, const point &b)
33
   {
34
        return a.x == b.x && a.y == b.y;
35
   }
36
   // sorts points on x-coordinate
37
38
   bool on_x(const point &a, const point &b)
39
   {
40
        return a.x < b.x;
41
   }
42
43
   // sorts points on y-coordinate
   bool on_y(const point &a, const point &b)
44
45
   {
46
        return a.y < b.y;</pre>
47
   }
48
49
   // squared distance between points
50
   ntype pdist2(const point &a, const point &b)
51
   {
52
        ntype dx = a.x-b.x, dy = a.y-b.y;
        return dx*dx + dy*dy;
53
54
   }
55
   // bounding box for a set of points
56
   struct bbox
57
58
   {
        ntype x0, x1, y0, y1;
59
60
        bbox() : x0(sentry), x1(-sentry), y0(sentry), y1(-sentry) {}
61
62
63
        // computes bounding box from a bunch of points
64
        void compute(const vector<point> &v) {
            for (int i = 0; i < v.size(); ++i) {</pre>
65
66
                x0 = min(x0, v[i].x); x1 = max(x1, v[i].x);
67
                y0 = min(y0, v[i].y);
                                        y1 = max(y1, v[i].y);
68
            }
69
        }
70
        // squared distance between a point and this bbox, 0 if inside
71
72
        ntype distance(const point &p) {
73
            if (p.x < x0) {
```

```
74
                 if (p.y < y0)
                                      return pdist2(point(x0, y0), p);
75
                 else if (p.y > y1)
                                      return pdist2(point(x0, y1), p);
76
                 else
                                      return pdist2(point(x0, p.y), p);
77
             }
78
             else if (p.x > x1) {
79
                 if (p.y < y0)
                                      return pdist2(point(x1, y0), p);
80
                 else if (p.y > y1) return pdist2(point(x1, y1), p);
81
                 else
                                      return pdist2(point(x1, p.y), p);
82
             }
83
             else {
84
                 if (p.y < y0)
                                      return pdist2(point(p.x, y0), p);
85
                 else if (p.y > y1) return pdist2(point(p.x, y1), p);
86
                 else
                                      return 0;
87
             }
88
        }
89
    };
90
    // stores a single node of the kd-tree, either internal or leaf
91
    struct kdnode
92
93
    {
94
        bool leaf;
                         // true if this is a leaf node (has one point)
95
        point pt;
                         // the single point of this is a leaf
96
        bbox bound;
                         // bounding box for set of points in children
97
98
        kdnode *first, *second; // two children of this kd-node
99
100
        kdnode() : leaf(false), first(0), second(0) {}
101
        ~kdnode() { if (first) delete first; if (second) delete second; }
102
103
        // intersect a point with this node (returns squared distance)
104
        ntype intersect(const point &p) {
105
             return bound.distance(p);
106
        }
107
108
        // recursively builds a kd-tree from a given cloud of points
109
        void construct(vector<point> &vp)
110
        {
111
             // compute bounding box for points at this node
112
             bound.compute(vp);
113
114
             // if we're down to one point, then we're a leaf node
115
             if (vp.size() == 1) {
116
                 leaf = true;
117
                 pt = vp[0];
118
             }
119
             else {
120
                 // split on x if the bbox is wider than high (not best heuristic...)
121
                 if (bound.x1-bound.x0 >= bound.y1-bound.y0)
122
                     sort(vp.begin(), vp.end(), on_x);
123
                 // otherwise split on y-coordinate
124
                 else
125
                     sort(vp.begin(), vp.end(), on_y);
126
127
                 // divide by taking half the array for each child
```

```
128
                 // (not best performance if many duplicates in the middle)
129
                 int half = vp.size()/2;
                 vector<point> v1(vp.begin(), vp.begin()+half);
130
131
                 vector<point> vr(vp.begin()+half, vp.end());
132
                 first = new kdnode(); first->construct(v1);
133
                 second = new kdnode(); second->construct(vr);
134
             }
135
        }
136
    };
137
    // simple kd—tree class to hold the tree and handle queries
138
    struct kdtree
139
140
    {
141
        kdnode *root;
142
143
        // constructs a kd-tree from a points (copied here, as it sorts them)
144
        kdtree(const vector<point> &vp) {
145
             vector<point> v(vp.begin(), vp.end());
146
             root = new kdnode();
147
             root->construct(v);
148
149
        ~kdtree() { delete root; }
150
151
        // recursive search method returns squared distance to nearest point
        ntype search(kdnode *node, const point &p)
152
153
        {
154
             if (node->leaf) {
                 // commented special case tells a point not to find itself
155
156
    //
                   if (p == node->pt) return sentry;
157
    //
158
                     return pdist2(p, node->pt);
159
             }
160
161
             ntype bfirst = node->first->intersect(p);
162
             ntype bsecond = node->second->intersect(p);
163
164
             // choose the side with the closest bounding box to search first
165
             // (note that the other side is also searched if needed)
166
             if (bfirst < bsecond) {</pre>
167
                 ntype best = search(node->first, p);
168
                 if (bsecond < best)</pre>
                     best = min(best, search(node->second, p));
169
170
                 return best;
171
             }
172
             else {
173
                 ntype best = search(node->second, p);
174
                 if (bfirst < best)</pre>
                     best = min(best, search(node->first, p));
175
176
                 return best;
177
             }
178
         }
179
180
        // squared distance to the nearest
181
        ntype nearest(const point &p) {
```

```
182
             return search(root, p);
183
        }
184
    };
185
186
    // some basic test code here
187
188
189
    int main()
190
    {
191
        // generate some random points for a kd-tree
192
        vector<point> vp;
        for (int i = 0; i < 100000; ++i) {
193
             vp.push_back(point(rand()%100000, rand()%100000));
194
195
        kdtree tree(vp);
196
197
198
        // query some points
199
        for (int i = 0; i < 10; ++i) {
200
             point q(rand()%100000, rand()%100000);
201
             cout << "Closest⊔squared⊔distance⊔to⊔(" << q.x << ",⊔" << q.y << ")"
                  << "_is_" << tree.nearest(q) << endl;
202
203
204
205
        return 0;
206
    }
207
```

5.5 Splay tree

```
#include <cstdio>
2
    #include <algorithm>
    using namespace std;
3
4
   const int N_MAX = 130010;
5
    const int oo = 0x3f3f3f3f3f;
6
7
    struct Node
8
    {
9
      Node *ch[2], *pre;
10
      int val, size;
      bool isTurned;
11
12
    } nodePool[N_MAX], *null, *root;
13
    Node *allocNode(int val)
14
15
      static int freePos = 0;
16
      Node *x = &nodePool[freePos ++];
17
      x->val = val, x->isTurned = false;
18
19
      x\rightarrow ch[0] = x\rightarrow ch[1] = x\rightarrow pre = null;
      x\rightarrow size = 1;
20
21
      return x;
22
```

```
23
    inline void update(Node *x)
24
25
    {
26
       x\rightarrow size = x\rightarrow ch[0]\rightarrow size + x\rightarrow ch[1]\rightarrow size + 1;
27
    }
28
     inline void makeTurned(Node *x)
29
30
    {
       if(x == null)
31
32
          return;
33
       swap(x\rightarrow ch[0], x\rightarrow ch[1]);
34
       x->isTurned ^= 1;
35
    }
36
37
     inline void pushDown(Node *x)
38
     {
       if(x->isTurned)
39
40
41
          makeTurned(x->ch[0]);
42
          makeTurned(x->ch[1]);
          x->isTurned ^= 1;
43
44
       }
45
    }
46
47
     inline void rotate(Node *x, int c)
48
    {
49
       Node *y = x\rightarrow pre;
50
       x\rightarrow pre = y\rightarrow pre;
51
       if(y->pre != null)
52
          y\rightarrow pre\rightarrow ch[y == y\rightarrow pre\rightarrow ch[1]] = x;
53
       y\rightarrow ch[!c] = x\rightarrow ch[c];
       if(x->ch[c] != null)
54
55
          x\rightarrow ch[c]\rightarrow pre = y;
56
       x\rightarrow ch[c] = y, y\rightarrow pre = x;
57
       update(y);
58
       if(y == root)
59
          root = x;
60
    }
61
62
     void splay(Node *x, Node *p)
63
     {
64
       while(x->pre != p)
65
66
          if(x->pre->pre == p)
67
            rotate(x, x == x->pre->ch[0]);
68
          else
69
          {
70
            Node *y = x->pre, *z = y->pre;
71
            if(y == z \rightarrow ch[0])
72
73
               if(x == y \rightarrow ch[0])
74
                  rotate(y, 1), rotate(x, 1);
75
               else
76
                  rotate(x, 0), rotate(x, 1);
```

```
77
           }
           else
78
79
           {
80
              if(x == y \rightarrow ch[1])
81
                rotate(y, 0), rotate(x, 0);
82
                rotate(x, 1), rotate(x, 0);
83
84
           }
         }
85
86
87
       update(x);
88
89
     void select(int k, Node *fa)
90
91
     {
       Node *now = root;
92
       while(1)
93
94
       {
95
         pushDown(now);
         int tmp = now->ch[0]->size + 1;
96
         if(tmp == k)
97
           break;
98
99
         else if(tmp < k)</pre>
           now = now \rightarrow ch[1], k = tmp;
100
101
         else
102
           now = now \rightarrow ch[0];
103
104
       splay(now, fa);
105
     }
106
107
     Node *makeTree(Node *p, int 1, int r)
108
     {
       if(1 > r)
109
110
         return null;
111
       int mid = (1 + r) / 2;
       Node *x = allocNode(mid);
112
113
       x\rightarrow pre = p;
       x\rightarrow ch[0] = makeTree(x, 1, mid - 1);
114
115
       x->ch[1] = makeTree(x, mid + 1, r);
116
       update(x);
117
       return x;
118
     }
119
     int main()
120
121
     {
122
       int n, m;
123
       null = allocNode(0);
124
       null->size = 0;
125
       root = allocNode(0);
126
       root->ch[1] = allocNode(oo);
127
       root->ch[1]->pre = root;
128
       update(root);
129
130
       scanf("%d%d", &n, &m);
```

```
131
       root->ch[1]->ch[0] = makeTree(root->ch[1], 1, n);
       splay(root->ch[1]->ch[0], null);
132
133
134
       while(m --)
135
136
         int a, b;
         scanf("%d%d", &a, &b);
137
138
         a ++, b ++;
139
         select(a - 1, null);
         select(b + 1, root);
140
141
         makeTurned(root->ch[1]->ch[0]);
142
       }
143
144
       for(int i = 1; i <= n; i ++)
145
       {
146
         select(i + 1, null);
147
         printf("%d<sub>\(\pi\)</sub>, root->val);
148
       }
149
    }
```

5.6 Lazy segment tree

```
public class SegmentTreeRangeUpdate {
 1
2
        public long[] leaf;
3
        public long[] update;
4
        public int origSize;
        public SegmentTreeRangeUpdate(int[] list)
5
            origSize = list.length;
6
 7
            leaf = new long[4*list.length];
8
            update = new long[4*list.length];
9
            build(1,0,list.length-1,list);
10
        public void build(int curr, int begin, int end, int[] list) {
11
12
            if(begin == end)
                leaf[curr] = list[begin];
13
            else
14
                int mid = (begin+end)/2;
15
16
                build(2 * curr, begin, mid, list);
                build(2 * curr + 1, mid+1, end, list);
17
                leaf[curr] = leaf[2*curr] + leaf[2*curr+1];
18
            }
19
20
        public void update(int begin, int end, int val) {
21
            update(1,0,origSize-1,begin,end,val);
22
23
        public void update(int curr, int tBegin, int tEnd, int begin, int end, int val)
24
            if(tBegin >= begin && tEnd <= end)</pre>
25
                update[curr] += val;
26
                    {
27
            else
                leaf[curr] += (Math.min(end,tEnd)-Math.max(begin,tBegin)+1) * val;
28
                int mid = (tBegin+tEnd)/2;
29
30
                if(mid >= begin && tBegin <= end)</pre>
```

```
31
                     update(2*curr, tBegin, mid, begin, end, val);
32
                 if(tEnd >= begin && mid+1 <= end)</pre>
33
                     update(2*curr+1, mid+1, tEnd, begin, end, val);
34
            }
35
36
        public long query(int begin, int end)
37
            return query(1,0,origSize-1,begin,end);
38
        public long query(int curr, int tBegin, int tEnd, int begin, int end)
39
40
            if(tBegin >= begin && tEnd <= end) {</pre>
41
                 if(update[curr] != 0)
42
                     leaf[curr] += (tEnd-tBegin+1) * update[curr];
43
                     if(2*curr < update.length){</pre>
44
                          update[2*curr] += update[curr];
45
                         update[2*curr+1] += update[curr];
46
47
                     update[curr] = 0;
48
49
                 return leaf[curr];
50
            }
51
            else
52
                 leaf[curr] += (tEnd-tBegin+1) * update[curr];
                 if(2*curr < update.length){</pre>
53
54
                     update[2*curr] += update[curr];
                     update[2*curr+1] += update[curr];
55
56
                 update[curr] = 0;
57
58
                 int mid = (tBegin+tEnd)/2;
59
                 long ret = 0;
                 if(mid >= begin && tBegin <= end)</pre>
60
61
                     ret += query(2*curr, tBegin, mid, begin, end);
62
                 if(tEnd >= begin && mid+1 <= end)</pre>
63
                     ret += query(2*curr+1, mid+1, tEnd, begin, end);
                 return ret;
64
65
            }
66
        }
67
   }
```

5.7 Lowest common ancestor

```
const int max_nodes, log_max_nodes;
2
   int num_nodes, log_num_nodes, root;
3
                                      // children[i] contains the children of node i
4
   vector<int> children[max_nodes];
   int A[\max_nodes][\log_max_nodes+1]; // A[i][j] is the 2^j-th ancestor of node i, or -1 if that
5
        ancestor does not exist
   int L[max_nodes];
                                // L[i] is the distance between node i and the root
6
7
   // floor of the binary logarithm of n
8
   int lb(unsigned int n)
9
   {
10
11
       if(n==0)
```

```
12
        return -1;
        int p = 0;
13
        if (n >= 1<<16) { n >>= 16; p += 16; }
14
15
        if (n >= 1<< 8) { n >>= 8; p += 8; }
16
        if (n >= 1 << 4) \{ n >>= 4; p += 4; \}
        if (n >= 1 << 2) \{ n >>= 2; p +=
17
                                            2; }
        if (n >= 1<< 1) {
18
                                      p +=
                                            1; }
19
        return p;
20
   }
21
    void DFS(int i, int 1)
22
23
    {
24
        L[i] = 1;
25
        for(int j = 0; j < children[i].size(); j++)</pre>
26
        DFS(children[i][j], l+1);
27
   }
28
29
   int LCA(int p, int q)
30
   {
        // ensure node p is at least as deep as node q
31
32
        if(L[p] < L[q])
33
        swap(p, q);
34
        // "binary search" for the ancestor of node p situated on the same level as q
35
36
        for(int i = log_num_nodes; i >= 0; i--)
        if(L[p] - (1 << i) >= L[q])
37
38
            p = A[p][i];
39
40
        if(p == q)
41
        return p;
42
        // "binary search" for the LCA
43
44
        for(int i = log_num_nodes; i >= 0; i--)
45
        if(A[p][i] != -1 && A[p][i] != A[q][i])
46
        {
47
            p = A[p][i];
48
            q = A[q][i];
49
        }
50
        return A[p][0];
51
52
   }
53
54
    int main(int argc,char* argv[])
55
    {
56
        // read num nodes, the total number of nodes
57
        log_num_nodes=lb(num_nodes);
58
        for(int i = 0; i < num nodes; i++)</pre>
59
60
        {
61
        int p;
62
        // read p, the parent of node i or -1 if node i is the root
63
64
        A[i][0] = p;
65
        if(p != -1)
```

```
children[p].push_back(i);
66
67
        else
68
            root = i;
        }
69
70
        // precompute A using dynamic programming
71
        for(int j = 1; j <= log_num_nodes; j++)</pre>
72
        for(int i = 0; i < num_nodes; i++)</pre>
73
            if(A[i][j−1] != −1)
74
            A[i][j] = A[A[i][j-1]][j-1];
75
76
            else
77
            A[i][j] = -1;
78
        // precompute L
79
80
        DFS(root, 0);
81
82
83
        return 0;
84 }
```

第六章 Miscellaneous

6.1 Longest increasing subsequence

```
// Given a list of numbers of length n, this routine extracts a
   // longest increasing subsequence.
   //
3
   // Running time: O(n Log n)
5
6
   //
         INPUT: a vector of integers
         OUTPUT: a vector containing the longest increasing subsequence
8
9
   #include <iostream>
10
   #include <vector>
   #include <algorithm>
11
12
13
   using namespace std;
14
   typedef vector<int> VI;
15
   typedef pair<int,int> PII;
16
   typedef vector<PII> VPII;
17
18
19
   #define STRICTLY INCREASIG
20
   VI LongestIncreasingSubsequence(VI v) {
21
22
     VPII best;
23
     VI dad(v.size(), -1);
24
25
     for (int i = 0; i < v.size(); i++) {
   #ifdef STRICTLY INCREASIG
26
27
        PII item = make_pair(v[i], 0);
        VPII::iterator it = lower_bound(best.begin(), best.end(), item);
28
29
        item.second = i;
30
        PII item = make_pair(v[i], i);
31
32
        VPII::iterator it = upper_bound(best.begin(), best.end(), item);
   #endif
33
34
        if (it == best.end()) {
          dad[i] = (best.size() == 0 ? -1 : best.back().second);
35
36
          best.push_back(item);
        } else {
37
          dad[i] = it == best.begin() ? -1 : prev(it)->second;
38
39
          *it = item;
40
        }
      }
41
42
```

```
43  VI ret;
44  for (int i = best.back().second; i >= 0; i = dad[i])
45    ret.push_back(v[i]);
46    reverse(ret.begin(), ret.end());
47    return ret;
48 }
```

6.2 Dates

```
1 // Routines for performing computations on dates. In these routines,
   // months are expressed as integers from 1 to 12, days are expressed
2
   // as integers from 1 to 31, and years are expressed as 4-digit
3
   // integers.
4
5
6
   #include <iostream>
7
   #include <string>
8
9
   using namespace std;
10
   string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"};
11
12
13
   // converts Gregorian date to integer (Julian day number)
   int dateToInt (int m, int d, int y){
14
     return
15
16
       1461 * (y + 4800 + (m - 14) / 12) / 4 +
17
       367 * (m - 2 - (m - 14) / 12 * 12) / 12 -
       3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
18
       d - 32075;
19
20
   }
21
   // converts integer (Julian day number) to Gregorian date: month/day/year
22
   void intToDate (int jd, int &m, int &d, int &y){
23
     int x, n, i, j;
24
25
     x = jd + 68569;
26
     n = 4 * x / 146097;
27
     x = (146097 * n + 3) / 4;
28
29
     i = (4000 * (x + 1)) / 1461001;
     x = 1461 * i / 4 - 31;
30
     j = 80 * x / 2447;
31
     d = x - 2447 * j / 80;
32
33
     x = j / 11;
     m = j + 2 - 12 * x;
34
     y = 100 * (n - 49) + i + x;
35
   }
36
37
   // converts integer (Julian day number) to day of week
38
   string intToDay (int jd){
39
      return dayOfWeek[jd % 7];
40
41
   }
42
   int main (int argc, char **argv){
```

```
44
      int jd = dateToInt (3, 24, 2004);
45
      int m, d, y;
46
      intToDate (jd, m, d, y);
47
      string day = intToDay (jd);
48
49
      // expected output:
            2453089
50
      //
51
            3/24/2004
52
      //
            Wed
53
      cout << jd << endl
        << m << "/" << d << "/" << y << endl
54
55
        << day << endl;
56
   }
```

6.3 Regular expressions

```
// Code which demonstrates the use of Java's regular expression libraries.
   // This is a solution for
2
   //
3
   //
        Loglan: a logical language
4
5
   //
        http://acm.uva.es/p/v1/134.html
6
   //
7
   // In this problem, we are given a regular language, whose rules can be
   // inferred directly from the code. For each sentence in the input, we must
   // determine whether the sentence matches the regular expression or not.
9
   // code consists of (1) building the regular expression (which is fairly
10
   // complex) and (2) using the regex to match sentences.
11
12
   import java.util.*;
13
14
   import java.util.regex.*;
15
16
   public class LogLan {
17
        public static String BuildRegex (){
18
        String space = "⊔+";
19
20
        String A = "([aeiou])";
21
22
        String C = "([a-z&&[^aeiou]])";
        String MOD = "(g" + A + ")";
23
        String BA = "(b" + A + ")";
24
        String DA = (d' + A + ");
25
26
        String LA = "(1" + A + ")";
        String NAM = "([a-z]*" + C + ")";
27
        String PREDA = "(" + C + C + A + C + A + "|" + C + A + C + C + A + ")";
28
29
        String predstring = "(" + PREDA + "(" + space + PREDA + ")*)";
30
        String predname = "(" + LA + space + predstring + "|" + NAM + ")";
31
        String preds = "(" + predstring + "(" + space + A + space + predstring + ")*)";
32
        String predclaim = "(" + predname + space + BA + space + preds + "|" + DA + space +
33
34
                preds + ")";
        String verbpred = "(" + MOD + space + predstring + ")";
35
        String statement = "(" + predname + space + verbpred + space + predname + "|" +
36
```

```
37
                predname + space + verbpred + ")";
        String sentence = "(" + statement + "|" + predclaim + ")";
38
39
40
        return "^" + sentence + "$";
41
        }
42
43
        public static void main (String args[]){
44
45
        String regex = BuildRegex();
46
        Pattern pattern = Pattern.compile (regex);
47
48
        Scanner s = new Scanner(System.in);
49
        while (true) {
50
51
                // In this problem, each sentence consists of multiple lines, where the last
52
            // line is terminated by a period. The code below reads lines until
            // encountering a line whose final character is a '.'. Note the use of
53
                //
54
                //
                      s.length() to get length of string
55
                      s.charAt() to extract characters from a Java string
56
                //
                //
                      s.trim() to remove whitespace from the beginning and end of Java string
57
58
                //
                // Other useful String manipulation methods include
59
60
                //
                //
                      s.compareTo(t) < 0 if s < t, lexicographically</pre>
61
62
                //
                      s.indexOf("apple") returns index of first occurrence of "apple" in s
                //
                      s.lastIndexOf("apple") returns index of last occurrence of "apple" in s
63
64
                //
                      s.replace(c,d) replaces occurrences of character c with d
65
                //
                      s.startsWith("apple) returns (s.indexOf("apple") == 0)
66
                //
                      s.toLowerCase() / s.toUpperCase() returns a new lower/uppercased string
67
                //
68
                //
                      Integer.parseInt(s) converts s to an integer (32-bit)
69
                //
                      Long.parseLong(s) converts s to a long (64-bit)
                //
                      Double.parseDouble(s) converts s to a double
70
71
72
            String sentence = "";
            while (true){
73
            sentence = (sentence + "" + s.nextLine()).trim();
74
            if (sentence.equals("#")) return;
75
            if (sentence.charAt(sentence.length()-1) == '.') break;
76
77
78
                // now, we remove the period, and match the regular expression
79
80
                String removed period = sentence.substring(0, sentence.length()-1).trim();
81
            if (pattern.matcher (removed_period).find()){
82
83
            System.out.println ("Good");
            } else {
84
            System.out.println ("Bad!");
85
86
87
        }
88
        }
89
   }
```

6.4 Prime numbers

```
// O(sqrt(x)) Exhaustive Primality Test
2
   #include <cmath>
3
   #define EPS 1e-7
   typedef long long LL;
4
   bool IsPrimeSlow (LL x)
5
6
   {
7
      if(x<=1) return false;</pre>
      if(x<=3) return true;</pre>
8
      if (!(x%2) || !(x%3)) return false;
9
      LL s=(LL)(sqrt((double)(x))+EPS);
10
11
     for(LL i=5;i<=s;i+=6)</pre>
12
        if (!(x%i) || !(x%(i+2))) return false;
13
      }
14
15
      return true;
16
   }
   // Primes less than 1000:
17
                        5
                               7
                                                                                37
   //
            2
                  3
                                    11
                                          13
                                                 17
                                                       19
                                                             23
                                                                    29
                                                                          31
18
   //
           41
                 43
                        47
                              53
                                    59
                                           61
                                                 67
                                                       71
                                                             73
                                                                    79
                                                                          83
                                                                                89
19
   //
           97
                101
                      103
                             107
                                   109
                                         113
                                                127
                                                      131
                                                            137
                                                                   139
                                                                         149
                                                                               151
20
   //
          157
                163
                      167
                             173
                                   179
                                         181
                                                191
                                                      193
                                                            197
                                                                   199
                                                                         211
                                                                               223
21
22
   //
                229
                      233
                             239
                                   241
                                         251
                                                257
                                                                               281
          227
                                                      263
                                                            269
                                                                   271
                                                                         277
   //
          283
                293
                      307
                             311
                                   313
                                         317
                                                331
                                                      337
                                                            347
                                                                   349
                                                                         353
                                                                               359
23
   //
                      379
                             383
                                   389
                                         397
                                                401
                                                      409
                                                            419
                                                                               433
24
          367
                373
                                                                   421
                                                                         431
   //
          439
                443
                      449
                             457
                                   461
                                         463
                                                467
                                                      479
                                                            487
                                                                   491
                                                                         499
                                                                               503
25
                             541
                                   547
                                                                               593
   //
          509
                521
                      523
                                         557
                                                563
                                                      569
                                                            571
                                                                   577
                                                                         587
26
   //
          599
                601
                      607
                             613
                                   617
                                         619
                                                631
                                                      641
                                                            643
                                                                   647
                                                                         653
                                                                               659
27
                                                709
                                                                               743
   //
          661
                673
                      677
                             683
                                   691
                                         701
                                                      719
                                                            727
                                                                   733
                                                                         739
28
   //
          751
                757
                      761
                             769
                                   773
                                         787
                                                797
                                                      809
                                                                               827
29
                                                            811
                                                                   821
                                                                         823
          829
                839
                                   859
                                         863
   //
                      853
                             857
                                                877
                                                      881
                                                            883
                                                                   887
                                                                         907
                                                                               911
30
   //
          919
                929
                      937
                             941
                                   947
                                         953
                                                      971
                                                            977
                                                                               997
31
                                                967
                                                                   983
                                                                         991
32
33
   // Other primes:
   //
          The largest prime smaller than 10 is 7.
34
   //
35
          The largest prime smaller than 100 is 97.
   //
          The largest prime smaller than 1000 is 997.
36
   //
          The largest prime smaller than 10000 is 9973.
37
   //
          The largest prime smaller than 100000 is 99991.
38
   //
39
          The largest prime smaller than 1000000 is 999983.
   //
          The largest prime smaller than 10000000 is 9999991.
40
   //
          The largest prime smaller than 100000000 is 99999989.
41
42
   //
          The largest prime smaller than 1000000000 is 999999937.
   //
43
          The largest prime smaller than 1000000000 is 9999999967.
          The largest prime smaller than 10000000000 is 99999999977.
   //
44
   //
          The largest prime smaller than 100000000000 is 999999999989.
45
          The largest prime smaller than 1000000000000 is 999999999971.
   //
46
47
   //
          The largest prime smaller than 1000000000000 is 9999999999973.
          The largest prime smaller than 10000000000000 is 99999999999999.
48
   //
   //
          The largest prime smaller than 100000000000000 is 99999999999937.
49
          The largest prime smaller than 100000000000000 is 999999999999997.
50
   //
   //
          51
```

6.5 C++ input/output

```
#include <iostream>
2
    #include <iomanip>
3
   using namespace std;
4
5
   int main()
6
7
   {
        // Ouput a specific number of digits past the decimal point,
8
9
        // in this case 5
        cout.setf(ios::fixed); cout << setprecision(5);</pre>
10
        cout << 100.0/7.0 << endl;</pre>
11
12
        cout.unsetf(ios::fixed);
13
        // Output the decimal point and trailing zeros
14
15
        cout.setf(ios::showpoint);
16
        cout << 100.0 << endl;</pre>
        cout.unsetf(ios::showpoint);
17
18
        // Output a '+' before positive values
19
20
        cout.setf(ios::showpos);
        cout << 100 << "" << -100 << endl;</pre>
21
22
        cout.unsetf(ios::showpos);
23
24
        // Output numerical values in hexadecimal
        cout << hex << 100 << "" << 1000 << "" << 10000 << dec << endl;
25
26
```

6.6 Knuth-Morris-Pratt

```
Finds all occurrences of the pattern string p within the
   text string t. Running time is O(n + m), where n and m
4
   are the lengths of p and t, respecitvely.
   */
5
   #include <iostream>
7
   #include <string>
    #include <vector>
9
10
11
    using namespace std;
12
   typedef vector<int> VI;
13
14
15
    void buildPi(string& p, VI& pi)
16
   {
     pi = VI(p.length());
17
18
      int k = -2;
     for(int i = 0; i < p.length(); i++) {</pre>
19
        while(k >= -1 \&\& p[k+1] != p[i])
20
          k = (k == -1) ? -2 : pi[k];
21
```

```
22
        pi[i] = ++k;
      }
23
24
    }
25
    int KMP(string& t, string& p)
26
27
      VI pi;
28
29
      buildPi(p, pi);
      int k = -1;
30
      for(int i = 0; i < t.length(); i++) {</pre>
31
        while(k >= -1 \&\& p[k+1] != t[i])
32
          k = (k == -1) ? -2 : pi[k];
33
        k++;
34
        if(k == p.length() - 1) {
35
          // p matches t[i-m+1, ..., i]
36
          cout << "matcheduatuindexu" << i-k << ":u";</pre>
37
          cout << t.substr(i-k, p.length()) << endl;</pre>
38
          k = (k == -1) ? -2 : pi[k];
39
40
        }
      }
41
42
      return 0;
43
    }
44
45
    int main()
46
      string a = "AABAACAADAABAABA", b = "AABA";
47
48
      KMP(a, b); // expected matches at: 0, 9, 12
      return 0;
49
50
    }
```

6.7 Latitude/longitude

```
Converts from rectangular coordinates to latitude/longitude and vice
2
   versa. Uses degrees (not radians).
3
4
5
   #include <iostream>
6
7
   #include <cmath>
8
   using namespace std;
9
10
   struct 11
11
12
      double r, lat, lon;
13
14
   };
15
   struct rect
16
17
18
      double x, y, z;
   };
19
20
```

```
21
    11 convert(rect& P)
22
   {
23
     11 Q;
24
     Q.r = sqrt(P.x*P.x+P.y*P.y+P.z*P.z);
25
     Q.lat = 180/M_PI*asin(P.z/Q.r);
     Q.lon = 180/M_PI*acos(P.x/sqrt(P.x*P.x+P.y*P.y));
26
27
28
      return Q;
29
   }
30
31
    rect convert(11& Q)
32
    {
33
     rect P;
34
     P.x = Q.r*cos(Q.lon*M_PI/180)*cos(Q.lat*M_PI/180);
35
     P.y = Q.r*sin(Q.lon*M_PI/180)*cos(Q.lat*M_PI/180);
36
     P.z = Q.r*sin(Q.lat*M PI/180);
37
38
      return P;
39
   }
40
41
   int main()
42
    {
43
      rect A;
44
     11 B;
45
46
     A.x = -1.0; A.y = 2.0; A.z = -3.0;
47
48
     B = convert(A);
      cout << B.r << "□" << B.lat << "□" << B.lon << endl;
49
50
51
     A = convert(B);
      cout << A.x << "" << A.y << "" << A.z << endl;
52
53
```

6.8 Emacs settings

```
;; Jack's .emacs file
 1
2
   (global—set—key "\C—z"
                                 'scroll-down)
3
   (global—set—key "\C—x\C—p"
                                 '(lambda() (interactive) (other-window -1)) )
4
   (global-set-key "\C-x\C-o"
                                 'other-window)
5
6
   (global—set—key "\C—x\C—n"
                                 'other-window)
   (global-set-key "\M-."
                                 'end-of-buffer)
   (global-set-key "\M-,"
                                 'beginning-of-buffer)
8
    (global—set—key "\M—g"
                                 'goto-line)
9
   (global—set—key "\C—c\C—w"
                                 'compare-windows)
10
11
12
   (tool-bar-mode 0)
   (scroll-bar-mode -1)
13
14
   (global-font-lock-mode 1)
15
16
   (show-paren-mode 1)
```

```
17
18 (setq-default c-default-style "linux")
19
20 (custom-set-variables
21 '(compare-ignore-whitespace t)
22 )
```