

*Exercise 3:*

$P_1$ : Let  $x(n)$  be an AR(2) process, i.e.,

$$x(n) + a_1^0(n-1) + a_2^0x(n-2) = w(n).$$

- Derive the one-step forward linear predictor of order  $p$  and the corresponding mean-square prediction error in terms of the auto-correlation function  $\gamma_x(m)$  for  $p = 1, 2$ , respectively.
- With  $a_1^0 = -1$ ,  $a_2^0 = 0.6$  and  $\sigma_w^2 = 1$ , compute  $\gamma_x(m)$  for  $m = 0, 1, 2, 3, 4, 5$ . Then specify the predictors obtained above.

$P_2$ : Look at the noise canceller depicted in Figure 1, where the measurable signal  $d(n)$  has the desired signal  $s(n)$  and an additive noise  $v(n)$ , which is uncorrelated with  $s(n)$ . The second measurable signal  $x(n)$  is assumed uncorrelated with the zero-mean  $s(n)$  but correlated with  $v(n)$ .

The Wiener filter is designed to minimize  $E[e^2(n)]$ . Show that the Wiener filter can be obtained by minimizing  $E[|\hat{v}(n) - v(n)|^2]$ . Find out the optimum FIR Wiener filter of order  $N$ .

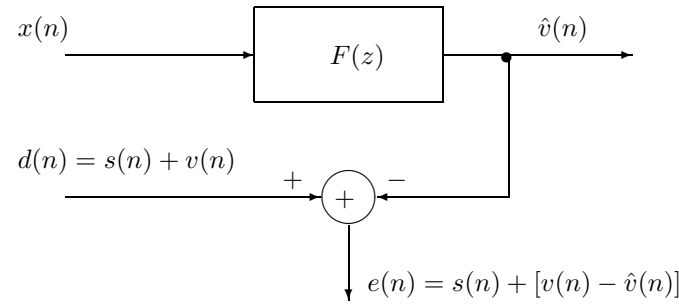


Figure 1: Block diagram of a noise canceller.

$P_3$ : If the noise canceller depicted in Figure 1 above is an adaptive FIR filter. Derive the corresponding LMS algorithm and analyze its convergence behavior.