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# A SHORT INTRODUCTION TO MATLAB







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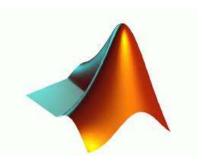
#### **CHAPTER I**

#### Introduction





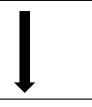
- **(**
- MatLab is an acronym for matrix laboratory and is owned by MathWorks.
- It was conceptualized in University of New Mexico and Stanford University before being commercialized via MathWorks in 1984.
- The latest version is MatLab R2012b.
- MatLab is a programming software to
  - aid visualization of mathematical functions
  - aid algorithmic development
  - compute complex functions
  - and many more



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A typical algorithm development cycle involves the following

#### **Setting the goal (aim)**



**Problem formulation** 



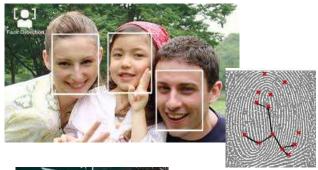
Real-time implementation

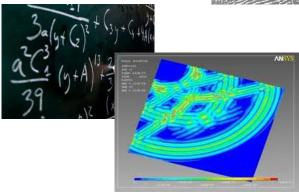


- Acoustic source localization
- Face detection
- Fingerprint authentication
- Footstep detection



- Mathematical formulation
- Wave propagation
- Contrast detection
- PC-based (C/C++)
- DSP implementation (TI, Analog Devices)
- Android based (Arduino)
- Field programmable gate array (FPGA)





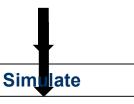


#### A typical algorithm development cycle involves the following

Setting the goal (aim)



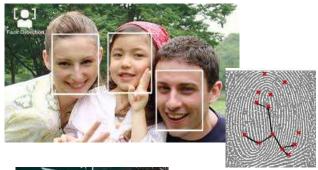
**Problem formulation** 

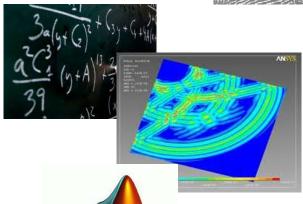


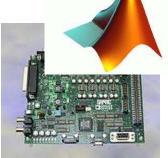
**Real-time** implementation



- Acoustic source localization
- **Face detection**
- Fingerprint authentication
- Footstep detection
- Signal processing tools
- Mathematical formulation
- Wave propagation
- Contrast detection
- MatLab
- PC-based (C/C++)
- **DSP** implementation (TI, Analog Devices)
- Android based (Arduino)
- Field programmable gate array (FPGA)

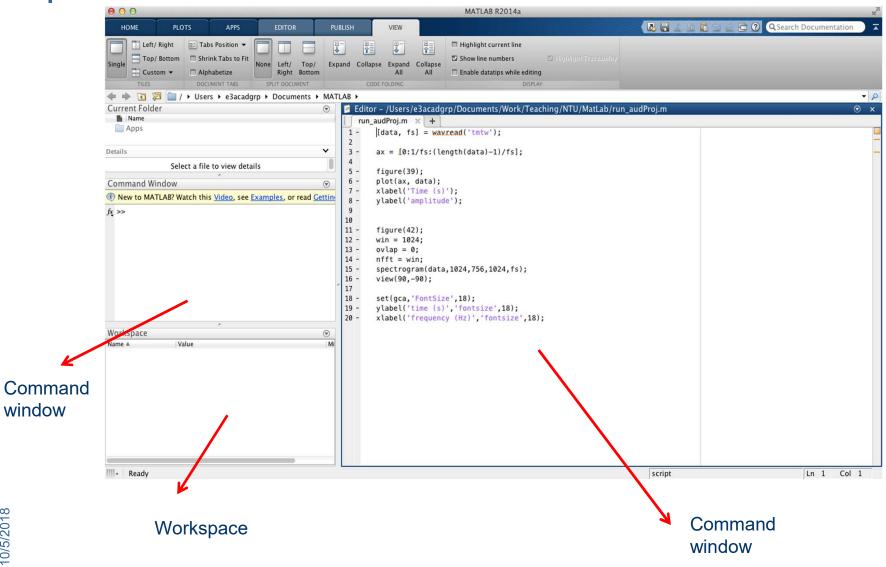






## 1.2 Interface 🕒









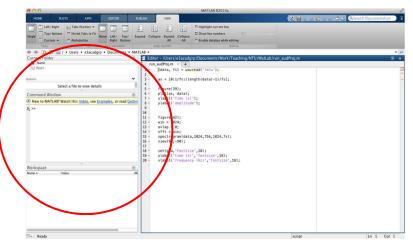


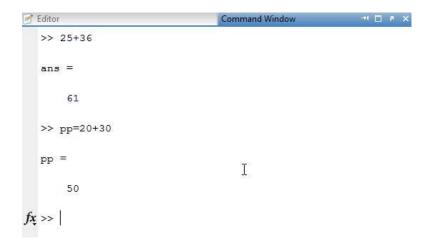
- The command window is where a lot of researchers will do their programming.
- It offers a fast and easy way to compute equations just like an ordinary calculator.





Try also the following: >> pp = 20+30





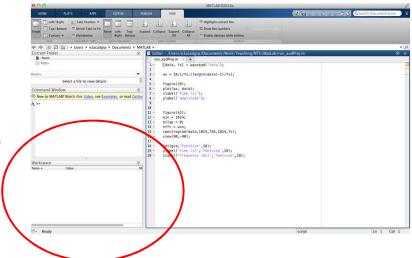
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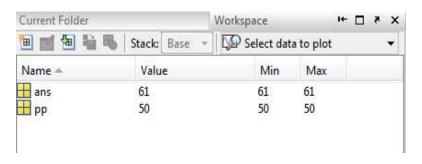


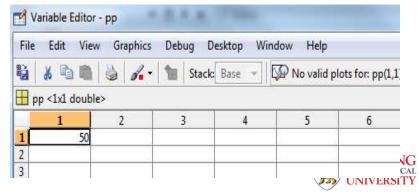
- -ф
- Very often, in a research project, we define a lot of variables (> 30).
- The workspace is where we would like to keep track of variables and their values.



- what has been defined
- the maximum and minimum values
- Double-clicking the variables will allow you to see the variables in a form similar to excel spreadsheet.







#### 1.5 Command history



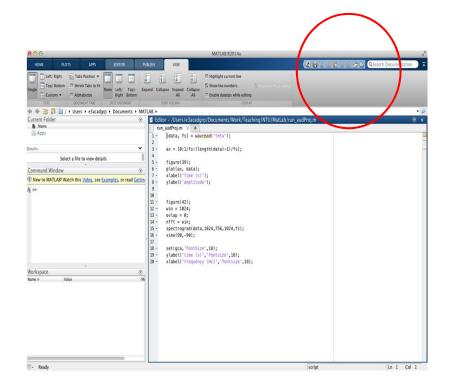
- Very often, we enter a lot of commands and it is sometimes useful to keep track of them.
- To repeat some computations without re-typing them, simply hit the "up" arrow key in the command window
- Another way to repeat any previous commands is
  - to place the cursor in the command window
  - hit the "up" or "down" arrow keys to cycle through previous commands





- MatLab has documented a comprehensive set of help files.
- These files can be accessed from the "Help" menu.
- Try accessing it via
   Help → Product Help
- You may search different functions by typing keywords into the search box.





### 1.7 Clearing memory and command window



- For large projects, one often have to declare lots of variables.
- Some variables may hold many numbers and if the program is not using them, it may be wise to free up the memory by deleting these variables.
- To delete a particular variable, say the variable "pp", use
   >> clear pp
   You will notice the variable "pp" disappearing from the workspace.
- To delete all variables, i.e., to clear all memory simply type>> clear
- To clear the command window, use>> clc

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#### **CHAPTER 2**

#### **Vectors and Matrices**



#### 2.1 Defining vectors and matrices (

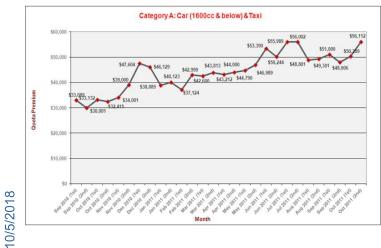


- Vectors are arrays that store a series of numbers
- Vectors can be classified into row and column vectors

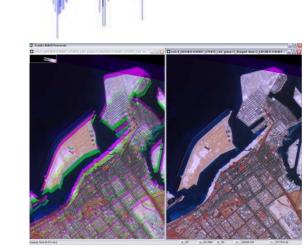
$$\begin{bmatrix} 1 & 40 & 2 & 200 & 12 \end{bmatrix} \qquad \begin{bmatrix} 2.4 \\ 3.2 \\ 3 \end{bmatrix}$$

Many real-world signals can be expressed in the form of vectors/









## 2.1 Defining vectors and matrices





- To define a row vector use
  - >> rowVecA = [1 4 2]

$$rowVecA = \begin{bmatrix} 1 & 4 & 2 \end{bmatrix}$$

The semi-colon ";" is used to concatenate numbers to the next row. Useful to form a column vector:

$$colVecB = \begin{bmatrix} 2\\1\\3 \end{bmatrix}$$

- The above can be extended to form a matrix.
  - First define the row
  - To define the next row, use the semi-colon
  - Remember to make sure each row has the same number of elements

$$matC = \begin{bmatrix} 1 & 3 & 5 \\ 3 & 2 & 6 \\ 1 & 1 & 3 \end{bmatrix}$$

## 2.1 Defining vectors and matrices



- Sometimes its clumsy to list down all elements manually if the numbers exhibits certain characteristics.
- We can use the colon ":" operator which is the same as counting from a number "to" another number (in steps of 1).
- Example: To generate a vector called "num" containing numbers 30 to 50, we use

$$>> num = [30:50]$$

$$num = \begin{bmatrix} 30 & 31 & \dots & 50 \end{bmatrix}$$

- We can use two colons if we want to count in steps other than 1.
- Example: To generate a vector of even numbers from 30 to 50

$$>> eveNum = [30:2:50]$$

eveNum = 
$$\begin{bmatrix} 30 & 32 & 34 & \dots & 50 \end{bmatrix}$$

## 2.2 Referencing elements





- Therefore, to reference an element, we use the format
  - >> variableName(rowIndex,columnIndex)
- To reference the 2<sup>nd</sup> element of the vector "rowVecA", defined in Section 2.1, we use
   >> rowVecA(2)

$$rowVecA = \begin{bmatrix} 1 & 4 \\ 2 \end{bmatrix}$$

 To reference the 2nd row, 3rd column of the matrix "matC", defined in Section 2.1, we use
 >> matC(2,3)

$$matC = \begin{bmatrix} 1 & 3 & 5 \\ 3 & 2 & 6 \\ 1 & 1 & 3 \end{bmatrix}$$





- We can also use the colon operator ":" to reference a range of elements.
- Therefore, to reference the 2<sup>nd</sup> to 3<sup>rd</sup> element of "rowVecA", we use
  - >> rowVecA(2:3)

$$rowVecA = \begin{bmatrix} 1 & 4 & 2 \end{bmatrix}$$

- To reference the last element of the vector, we can use the keyword "end"
  - >> rowVecA(end)

$$rowVecA = \begin{bmatrix} 1 & 4 & 2 \end{bmatrix}$$

- To determine the length of the vector, we can use the keyword "length"
  - >> lenVecA = length(rowVecA)

### 2.3 Matrix/vector transpose



- To transpose a matrix, use the "prime" key, located on the immediate left of the "Enter" key.
- Transpose of the column vector "colVecB" will form a row vector:

$$colVecB = \begin{bmatrix} 2\\1\\3 \end{bmatrix}$$
$$transpVecB = \begin{bmatrix} 2 & 1 & 3 \end{bmatrix}$$

 To transpose a matrix, we use the same prime notation

$$matC = \begin{bmatrix} 1 & 3 & 5 \\ 3 & 2 & 6 \\ 1 & 1 & 3 \end{bmatrix}$$

transpmatC = 
$$\begin{bmatrix} 1 & 3 & 1 \\ 3 & 2 & 1 \\ 5 & 6 & 3 \end{bmatrix}$$

### 2.3 Matrix/vector multiplication





- Unlike scalar multiplication, matrix/vector multiplication can only be performed when we take the dimension into account.
- In general,

$$\mathbf{A}_{M\times N} \times \mathbf{B}_{N\times P} = \mathbf{C}_{M\times P}$$

Example

Would the following work?

$$\mathbf{A}_{2\times 3} = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 4 & 7 \end{bmatrix} \qquad \mathbf{B}_{3\times 1} = \begin{bmatrix} 5 \\ 6 \\ 1 \end{bmatrix}$$

$$\mathbf{C}_{2\times 1} = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 4 & 7 \end{bmatrix} \begin{bmatrix} 5 \\ 6 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} (1\times 5) + (3\times 6) + (4\times 1) \\ (2\times 5) + (4\times 6) + (7\times 1) \end{bmatrix}$$

$$= \begin{bmatrix} 27 \\ 41 \end{bmatrix}$$

### 2.4 Element-by-element multiplication





- It is possible to perform element-by-element multiplication using the dot-multiplication notation, i.e., " \* "
- For element-by-element operation, make sure they are of the same dimensions.
- Example

$$\mathbf{A}_{2\times 3} = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 4 & 7 \end{bmatrix} \qquad \mathbf{D}_{2\times 3} = \begin{bmatrix} 2 & 8 & 1 \\ 1 & 1 & 5 \end{bmatrix}$$

$$\mathbf{E}_{2\times3} = \begin{bmatrix} (1\times2) & (3\times8) & (4\times1) \\ (2\times1) & (4\times1) & (7\times5) \end{bmatrix} \\ = \begin{bmatrix} 2 & 24 & 4 \\ 2 & 4 & 35 \end{bmatrix}$$

Are the following valid?

$$>> E = A*D$$

## 2.5 Solving simultaneous equations





- MatLab offers an excellent tool for solving simultaneous equations.
- Consider the following example:

$$3x + 4y - 2z = 6$$

$$4x - 6y + 2z = 1$$

$$2x + y + 0.2z = 2$$

• To find the unknown variables x, y and z, we re-write in matrix form

$$\begin{bmatrix} 3 & 4 & -2 \\ 4 & -6 & 2 \\ 2 & 1 & 0 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 1 \\ 2 \end{bmatrix}$$

$$Aq = p$$

• To find the unknown, i.e., elements in the vector  $\mathbf{q}$ , we only need to use the following

$$\mathbf{q} = \mathbf{A}^{-1}\mathbf{p}$$

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### 2.5 Solving simultaneous equations (

 $\mathbf{a} = \mathbf{A}^{-1}\mathbf{p}$ 





$$\begin{bmatrix} 3 & 4 & -2 \\ 4 & -6 & 2 \\ 2 & 1 & 0.2 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 6 \\ 1 \\ 2 \end{bmatrix}$$

$$\mathbf{Aq} = \mathbf{p}$$

Define all variables. Compute the unknown by calculating the inverse of a matrix using "inv()"

$$>> A = [3 \ 4 \ -2; 4 \ -6 \ 2; 2 \ 1 \ 0.2]$$

$$>> q = inv(A)*p$$

$$\mathbf{A} = \begin{bmatrix} 3 & 4 & -2 \\ 4 & -6 & 2 \\ 2 & 1 & 0.2 \end{bmatrix}$$

$$\mathbf{p} = \left[ egin{array}{c} 6 \ 1 \ 2 \end{array} 
ight]$$

$$\mathbf{A} = \begin{bmatrix} 3 & 4 & -2 \\ 4 & -6 & 2 \\ 2 & 1 & 0.2 \end{bmatrix} \qquad \mathbf{p} = \begin{bmatrix} 6 \\ 1 \\ 2 \end{bmatrix} \qquad \mathbf{q} = \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1.0417 \\ 0.1458 \\ -1.1458 \end{bmatrix}$$

### 2.6 Condition number and invertibility





$$3x + 4y = 6$$
$$6x + 8y = 12$$

• To find the unknown variables x, y and z, we re-write in matrix form

$$\begin{bmatrix} 3 & 4 \\ 6 & 8 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 6 \\ 12 \end{bmatrix}$$
$$\mathbf{Aq} = \mathbf{p}$$

• To find the unknown, i.e., elements in the vector **q**, we only need to use the following

$$\mathbf{q} = \mathbf{A}^{-1}\mathbf{p}$$

In MatLab

### 2.6 Condition number and invertibility



The above generates the result

$$\mathbf{q} = \left[ \begin{array}{c} x \\ y \end{array} \right] = \left[ \begin{array}{c} \inf \\ \inf \end{array} \right]$$

with the warning message

Warning: Matrix is singular to working precision.

- The above implies that there are no solutions for x, and y
- This can be verified by the high condition number of the matrix A
   >> cond(A)
- A high conditional number of A implies that it is non-invertible.
- An invertible A has a low condition number of 1.

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#### **CHAPTER 3**

## **Complex Numbers**



### 3.1 Defining complex numbers





 This is achieve via the variables "i" and "j" (if they haven't been defined). These variables have already been pre-defined as complex numbers in MatLab

$$i = 0 + 1i$$

$$j = 0 + 1j$$

We can define complex numbers using

$$>> val = 3+2j$$

$$val = 3 + 2j$$

An array of complex numbers can then be defined using

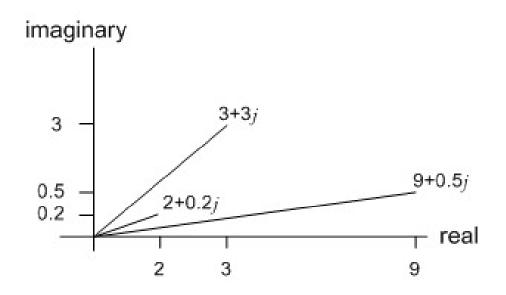
$$>> cplAry = [2+0.2j; 3+3j; 9+0.5j]$$

$$cplAry = \begin{bmatrix} 2\\3\\9 \end{bmatrix} + j \begin{bmatrix} 0.2\\3\\0.5 \end{bmatrix} = \begin{bmatrix} 2+0.2j\\3+3j\\9+0.5j \end{bmatrix}$$



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 Any complex numbers can be characterized by its magnitude and phase



$$cplAry = \begin{bmatrix} 2 + 0.2j \\ 3 + 3j \\ 9 + 0.5j \end{bmatrix}$$

### 3.2 Magnitude and phase





To compute the magnitude use "abs()"

$$cplAry = \begin{bmatrix} 2 + 0.2j \\ 3 + 3j \\ 9 + 0.5j \end{bmatrix}$$

absAry = 
$$\begin{bmatrix} \sqrt{2^2 + 0.2^2} \\ \sqrt{3^2 + 3^2} \\ \sqrt{9^2 + 0.5^2} \end{bmatrix} = \begin{bmatrix} 2.01 \\ 4.24 \\ 9.01 \end{bmatrix}$$

The phase can be computed via "phase()"

$$phAry = \begin{bmatrix} tan^{-1}(0.2/2) \\ tan^{-1}(3/3) \\ tan^{-1}(0.5/9) \end{bmatrix} = \begin{bmatrix} 0.0997 \\ 0.7854 \\ 0.0555 \end{bmatrix}$$

 Note that since, by default, MatLab computes angles in radians, angles in degrees can be computed easily using

phAry = 
$$\begin{bmatrix} \tan^{-1}(0.2/2) \\ \tan^{-1}(3/3) \\ \tan^{-1}(0.5/9) \end{bmatrix} \times 180/\pi$$
= 
$$\begin{bmatrix} 5.71 \\ 45.00 \\ 3.18 \end{bmatrix}$$

#### 3.3 Real and imaginary



- To extract the real parts within an array, simply use "real()"
  - >> rlAry = real(cplAry)

$$cplAry = \begin{bmatrix} 2 + 0.2j \\ 3 + 3j \\ 9 + 0.5j \end{bmatrix}$$

- To extract the real part of a particular element, you may apply Section 2.2. Therefore, to extract the real part of the 3<sup>rd</sup> element in the variable "cplAry", use
  - >> real(cplAry(3))

 $rlAry = \begin{bmatrix} 2\\3\\9 \end{bmatrix}$ 

 To extract the imaginary parts within an array, use "imag()"

$$imAry = \begin{bmatrix} 0.2\\3\\0.5 \end{bmatrix}$$



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#### **CHAPTER 4**

## **Plotting**





- Compared to C/C++, MatLab offers an excellent and simple way to visualize functions.
- Plotting is done via the "plot()" function and specifying the abscissa and ordinate values.
- The plot function has two arguments (inputs)
  - a vector containing abscissa values
  - a vector containing ordinate values
  - plot (abscissaValues, ordinateValues)
- Note that the number of elements in both vectors must be the same.

## 4.1 Plotting lines



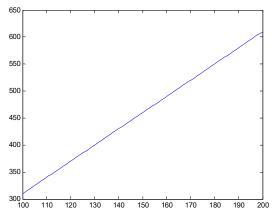
- Example: To plot the function of y = 3x + 10 within the range of x = 100...200
  - Create a new figure
    - >> figure(20)
  - Specify a vector containing the abscissa (counting from 100 to 200)

$$>> x = [100:200];$$

Compute the ordinate values

$$>> y = 3*x+10;$$

Plot the function



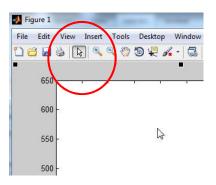
- The number "20" after the "figure" keyword is to identify which figure MatLab should plot the data. If there is no figure 20, it will create a new one.
- The semi-colon ";" at the end of the 2<sup>nd</sup> and 3<sup>rd</sup> command is there to prevent MatLab from listing down the elements of the vector.
- It is very useful particularly if you do not want to display long vectors.

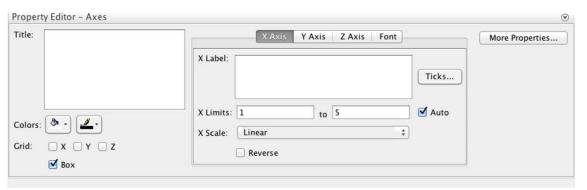
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#### 4.2 Axes labelling, titles, font size (+)



- As engineers its very important to label the axes of the plots.
- The programming way to label the axes is to employ
  - >> xlabel('x values')
  - >> ylabel('y values')
- One can also use the graphical approach.
  - Click on the arrow icon in the figure you have plotted
  - Double-click on the white space of your plot
  - Use the property-editor at the bottom of your plot to change/insert information.



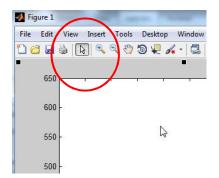




### 4.3 Color and markers 🕒



- It is also very useful to plot the lines in different colors and place markers on the lines
- The graphical approach offers a simple way to do that
  - Click on the arrow icon in the figure you have plotted
  - Double-click on the line you have plotted
  - Use the property-editor at the bottom of your plot to change/insert information.









- "Holding" allows researchers to plot multiple equations on the same graph.
- You may use the following command to "hold" a figure >> hold on;
- Example: Plot the following equations for x = 1 to 40

$$y_1 = 3x - 10$$
  
$$y_2 = x + 10$$

- Generate an array of x values
- Generate the output vectors for each equation
- Plot the figures



$$y_1 = 3x - 10$$
  
$$y_2 = x + 10$$

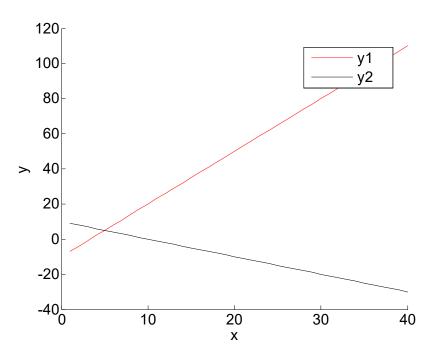
Generate an array of x values

$$>> x=[1:40];$$

Generate the output vectors for each equation

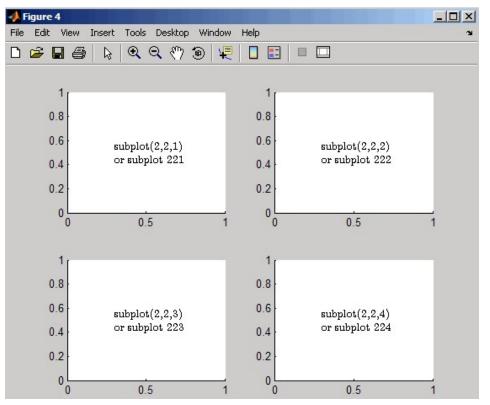
$$>> y1 = 3*x-10;$$
  
 $>> y2 = -x+10;$ 

Plot the figures

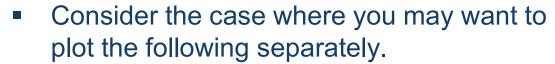




- Subplot allows one to plot two or more functions on separate axes.
- The function "subplot(m,n,p)"
  - breaks the figure into m-by-n matrix
  - the integer "p" defines the subplot index



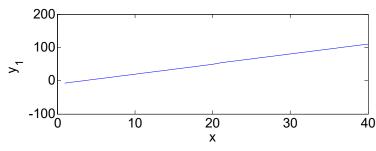


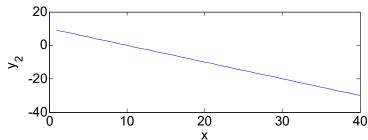


$$y_1 = 3x - 10$$
  
$$y_2 = x + 10$$

- Generate a new figure
  - >> figure(39);
- Define the 1<sup>st</sup> subplot position and plot 1<sup>st</sup> graph

Define the 2<sup>nd</sup> subplot position and plot 2<sup>nd</sup> graph





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### **CHAPTER 5**

## Scripts and Functions



# 10/5/2018

### 5.1 Saving your scripts



- Thus far, all commands have been entered into the "Command window"
- Advantages of using this command window include
  - simple interface for users to type in commands
  - providing a quick way to validate computations
- However, disadvantages of using the command window include
  - not being able to save the commands for future reference
  - the need to re-key commands all over again
    - if there is a typo error
    - on a separate occasion (after you close MatLab)
  - not being able to execute multiple commands in a single run (commands are currently executed after every line)
- The use of scripts allows one to save the commands in a file, and run multiple commands



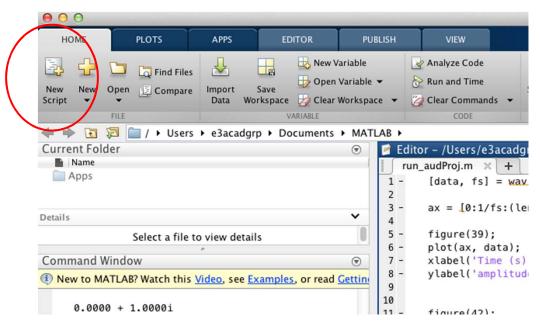
### 5.1 Saving your scripts (+)



Here, we will create a script which solves the following equations and verifies the answer graphically.

$$2x + 10y = 54$$
$$3x - 5y = -19$$

- First create a folder under desktop and name it "projects"
- Create a script by clicking the "New Script" button at the "Home" tab

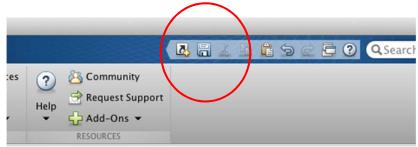




### 5.1 Saving your scripts 🕒



- You will be brought to the "Editor" page with a filename "Untitled"
- Save this file as "run\_solveSimEqns" in the desktop folder you created



Formulate the problem in Matrix notation according to Section 2.5

$$2x + 10y = 54$$

$$3x - 5y = -19$$

$$\left[\begin{array}{cc} 2 & 10 \\ 3 & -5 \end{array}\right] \left[\begin{array}{c} x \\ y \end{array}\right] = \left[\begin{array}{c} 54 \\ -19 \end{array}\right]$$

$$Aq = p$$

$$\mathbf{q} = \mathbf{A}^{-1}\mathbf{p}$$

### 5.1 Saving your scripts





### Key in the following commands

### To verify the result graphically, we use

$$2x + 10y = 54$$
$$3x - 5y = -19$$

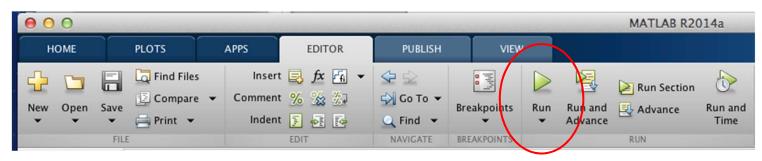
$$\left[\begin{array}{cc} 2 & 10 \\ 3 & -5 \end{array}\right] \left[\begin{array}{c} x \\ y \end{array}\right] = \left[\begin{array}{c} 54 \\ -19 \end{array}\right]$$

$$\mathbf{Aq} = \mathbf{p}$$
$$\mathbf{q} = \mathbf{A}^{-1}\mathbf{p}$$

### 5.1 Saving your scripts 🕒

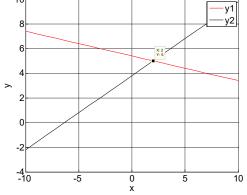


Click on the "run" icon after all commands have been entered



- Error messages, if any, will appear in the command window.
- The unknowns can be found by double clicking the q variable in the Workspace.

$$\mathbf{q} = \left[ \begin{array}{c} x \\ y \end{array} \right] = \left[ \begin{array}{c} 2 \\ 5 \end{array} \right]$$



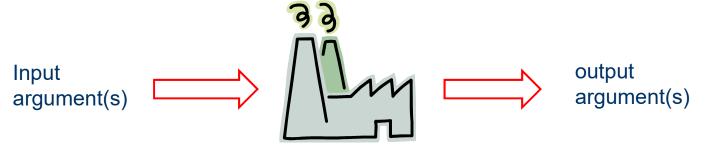
You may now solve any simultaneous equations by changing the values of variables **A** and **p** in the script without having to key in all the commands.



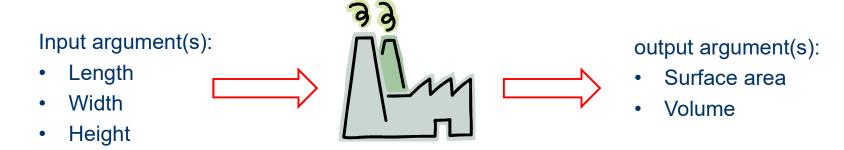
- Functions are a neat way to organize your codes, particularly if you are working on large projects.
- The relationship between "functions" and "scripts" can best be described using the following figure.

Script (running a set of commands)	Function
Function call	
Function call	

 Functions are analogous to an automation factory; it takes in raw materials (input argument(s)) and generates products (output argument(s)).



 For example, we can have a function which computes the volume and the surface area of a cuboid.





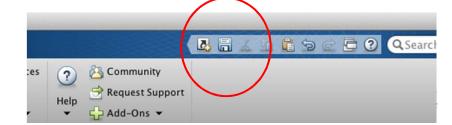
- Example: Write a script and a function to compute the surface area and volume of a cuboid.
  - We first create the script by clicking on "New Script" under the "Home" tab
  - Save this script as "run\_solveCuboid.m" in the desktop folder you created.
     Use "Save" under the "Editor" tab.
  - Key in the following commands
    - >> length = 4;
    - >> width = 3;
    - >> height = 2.5;
    - >> [volCubd, surfAreaCubd] = compCubd (length, width, height);



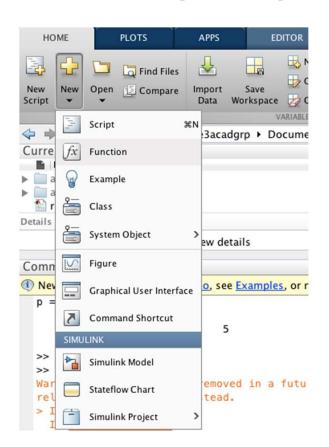
Function name



Save the file by clicking the save icon



- Create the function using
- Change the first line to function [vol, area] = compCubd (len, wid, hgt);



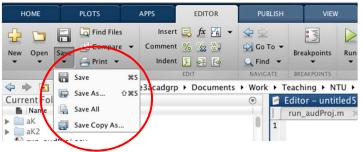
```
Untitled*
     function [ output args ] = Untitled( input args )
 2
     5 %UNTITLED Summary of this function goes here
           Detailed explanation goes here
 3
 4
 5
       end
```

```
Untitled*
     function [ vol, area ] = compCubd( len, wid, hgt )
 1
     5 %UNTITLED Summary of this function goes here
 2
 3
            Detailed explanation goes here
 4
 5
        end
 6
```

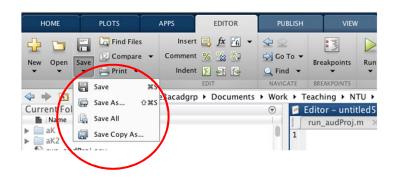
51



 Click the save icon, save the file under the default file name "compCubd.m" in the same folder as the script.



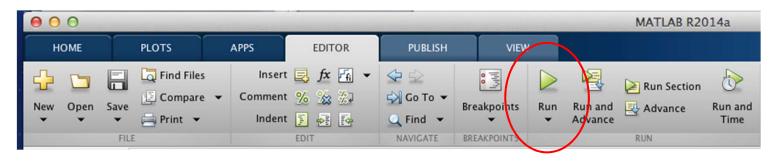
- Key in the following commands
  - >> vol = len\*wid\*hgt;
  - >> area = 2\*(len\*wid)+2\*(len\*hgt)+2\*(wid\*hgt);
- Click the save icon

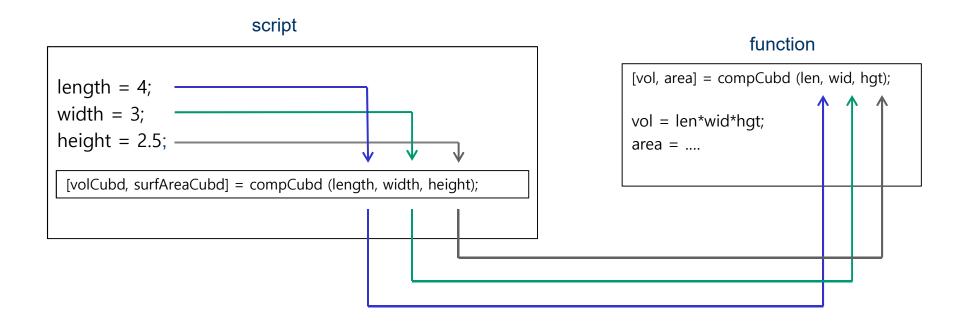




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Open the "run\_solveCuboid.m" script and run it







## CHAPTER 6

### Sine/Cosine Plots



### 6.1 Sampling- definition



An analog sinusoid is in the form of

$$x(t) = A\cos(2\pi f t)$$
$$= A\cos(\omega t)$$

Therefore, by definition,

f: analog frequency in cycles/sec (Hz)

 $\omega$ : angular (analog) frequency in rad/sec

A digital sinusoid is in the form of

$$x[n] = A\cos(2\pi f_0 n)$$
$$= A\cos(\omega_0 n)$$

Therefore, by definition,

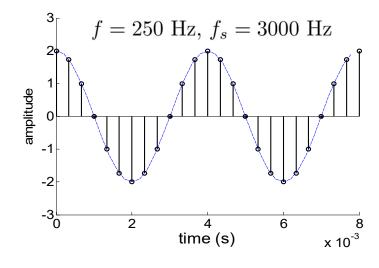
 $f_0$ : digital frequency in cycles/sample

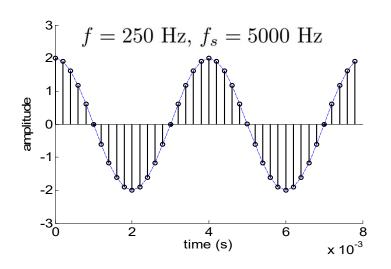
 $\omega_0$ : angular (digital) frequency in rad/sample

## <u>6.</u>2 Discrete-time signal from continuous-time signal 🨉



- Sampling a continuous-time signal results in a discrete-time signal.
- We often write  $x[n] = x_{\text{continuous}}(nT)$  $T = 1/f_s$  is the sampling period in sec sampling frequency in Hz
- A higher  $f_s$  implies that the analog signal is sampled more frequently.







### 



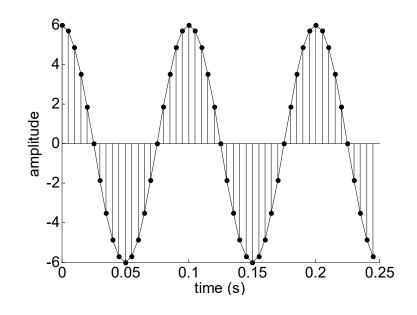
Consider an analog signal  $x(t) = 6\cos(20\pi t)$ . Given a sampling rate of  $f_s = 200 \text{ Hz}$ , find the discrete representation of the signal.

A sampling rate of  $f_s = 200 \text{ Hz}$  corresponds to a sampling period of T = 1/200 = 0.005 sec.

This implies that we have a digital signal at sample index n every 0.005 s.

Sampling x(t) at this period will result in

$$x[n] = 6\cos(20\pi \times nT)$$
$$= 6\cos(0.1\pi n)$$





# 10/5/2018

### 6.3 Plotting a discrete cosine wave



- Example: To plot the first 200 samples of the signal  $x(t) = \cos(200\pi t)$  at a sampling rate of  $f_s = 200~{\rm Hz}$ 
  - First create the script using



Save this script as "run\_sinegen.m" in the desktop folder you created

Key in the following commands

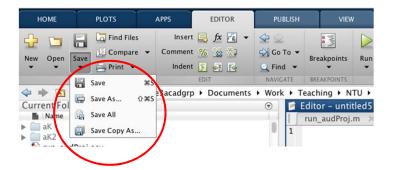
$$>> fs = 8000;$$

$$>> fsig = 100;$$

$$>> nsamp = 200;$$

$$>> t = [0:1/fs:(nsamp-1)/fs];$$

$$>>$$
 sig = sin(2\*pi\*fsig\*t);





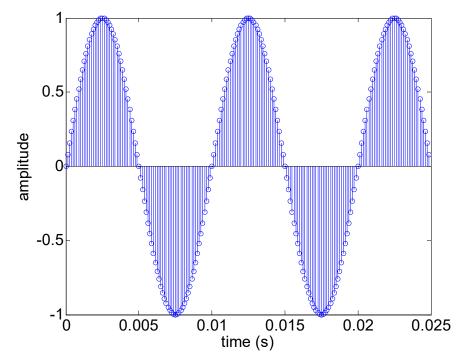
### 6.3 Plotting a discrete cosine wave



- >> figure(25);
- >> stem(t,sig);
- >> xlabel('time (s)');
- >> ylabel('amplitude');



### Save and run this script







## **Applications**

**CHAPTER 7** 



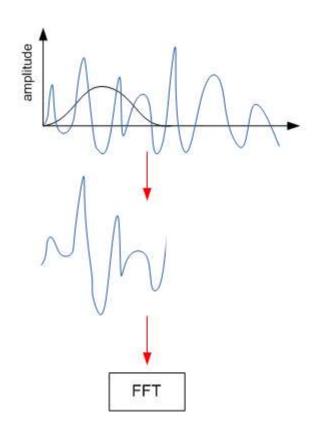


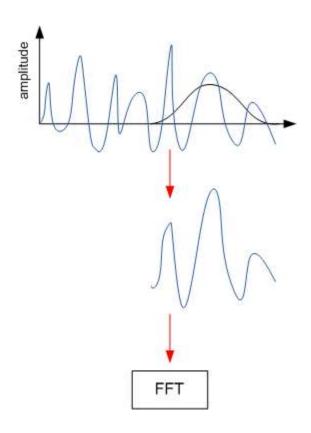
- It is very easy to read audio files into MatLab and process them using signal processing technique(s).
- For versions before MatLab 2012, you may read .wav files using the function "wavread()"
- For versions MatLab 2012 or later, you may read audio files using the function "audioread()". This supports the following file formats
  - AU, SND
  - FLAC
  - OGG
  - WAV
  - MP4 and any formats supported by Microsoft Media Foundation
- You may also write a processed signal using the following functions "wavwrite()" or "audiowrite()"





- One important tool when analyzing the audio signal is to determine how the frequency changes with time.
- This is known as the short-time Fourier transform.





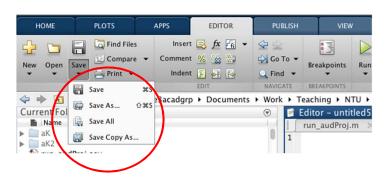




- ✓ generate a script,
- ✓ read in an audio file
- ✓ plot the signal
- ✓ view its frequency content of the signal
- Copy the wav file "tmtw.wav" into a desktop folder.
- Create a new script



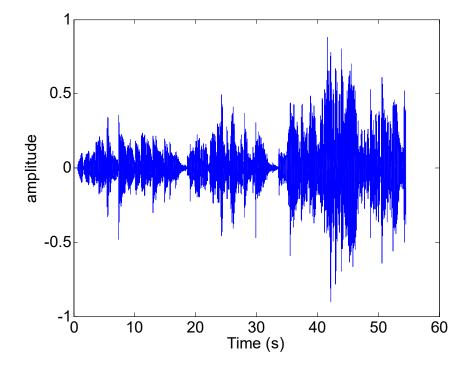
- Save this script as "run\_audProj.m" in the desktop folder you created
- Read the way file
  - >> [data, fs] = wavread('tmtw');



# 10/5/2018



- Generate a vector containing the time sequence starting from 0 to the length of data minus 1. Since the sampling rate is  $\,f_s$ , the time step will be  $1/f_s$ .
  - >> ax = [0:1/fs:(length(data)-1)/fs];
- We can now plot the figure
  - >> figure(39);
  - >> plot(ax, data);
  - >> xlabel('Time (s)');
  - >> ylabel('amplitude');





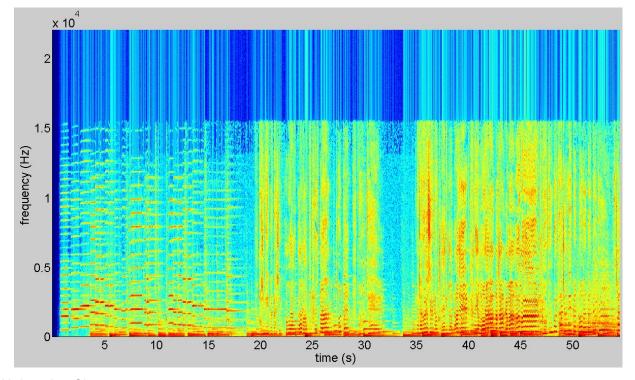
## 10/5/2018

### 7.1 Acoustic signal processing (



Generate the spectrogram using the following

```
>> figure(42);
>> win = 1024;
>> ovlap = 0;
>> nfft = win;
>> spectrogram(data,win,756,nfft,fs);
>> view(90,-90);
```



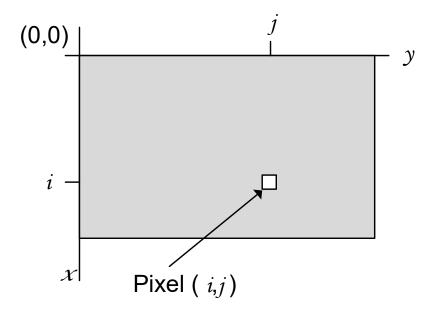


- It is very easy to read image files into MatLab and process them using signal processing technique(s).
- The function "imread()" supports the following file formats

BMP — Windows Bitmap	JPEG — Joint Photographic Experts Group	PNG — Portable Network Graphics	
CUR — Cursor File	JPEG 2000 — Joint Photographic Experts Group 2000	PPM — Portable Pixmap	
GIF — Graphics Interchange Format	PBM — Portable Bitmap	RAS — Sun Raster	
HDF4 — Hierarchical Data Format	PCX — Windows Paintbrush	TIFF — Tagged Image File Format	
ICO — Icon File	PGM — Portable Graymap	XWD — X Window Dump	

The function "imshow()" displays the image in MatLab.

An image in MatLab is treated as a matrix, i.e., every pixel is a matrix element.

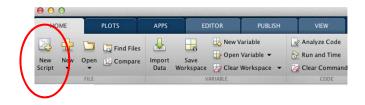


Note that the (0,0) position is located at the top-left corner of the image.



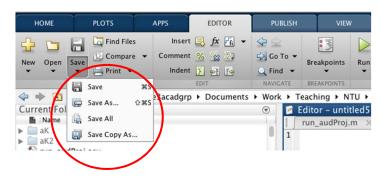


- Example: We can generate a 500×500 matrix corresponding to greyscale (black-white) values via the following.
  - Create the script



Save this script as "run\_genGreyScale.m" in the desktop folder you created

Define the size of the matrix>> size = 500;



• Generate a vector containing integers from 1 to 500<sup>2</sup>. The last element will hold the value 500<sup>2</sup> since, for a 500×500 matrix, there will be 500<sup>2</sup> pixels.

$$>> y = [1: size^2];$$





• We next reshape the  $1 \times 500^2$  vector into a  $50 \times 50$  matrix

>> Y = reshape(y,size,size);

1 Z 500 <sup>2</sup> L
------------------------

1	501	 249501
2		 249502
•••		 
500		 500 <sup>2</sup>

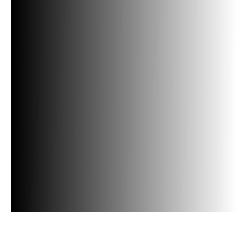
• Normalize each value by dividing all elements in the vector by the largest number, i.e., 5002. This is to ensure that the largest value in the matrix is 1.

$$>> Y = Y./Y(end);$$

We now show the image using

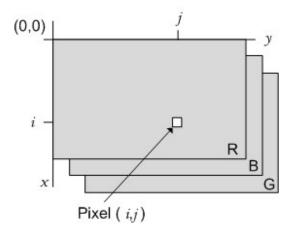
>> imshow(Y);

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- Images, in general, are not greyscale, i.e., its values do not vary between 0 and 1.
- True color images comprise of RGB values.

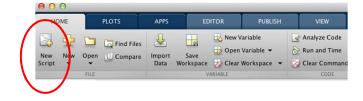


- The function "imread()" for true color image will therefore result in a 3D matrix with the 3<sup>rd</sup> dimension corresponding to the RBG values.
- http://web.njit.edu/~kevin/rgb.txt.html

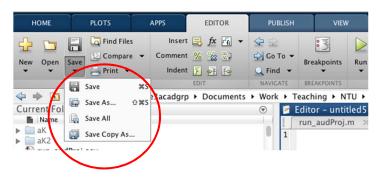




- In this example, we will
- ✓ generate a script,
- ✓ read in an image file
- ✓ show the image on MatLab
- ✓ adjust its RBG values
- Copy the jpg file "zoo.jpg" into a desktop folder.
- Create the script using



- Save this script as "run\_imgProj.m" in the desktop folder you created
- Read the image file
  - >> image = imread('zoo.jpg');





### ıg (

### 7.2 Image signal processing



- Plot the image file
  - >> figure(32);
  - >> imshow(image);
  - >> title('original image');
- To reduce the blue component, we first create a dummy variable and equate it to the original image
  - >> imageA = image;
- Next we change the blue component by changing the 2<sup>nd</sup> component of "imageA"
  - >> imageA(:,:,2)= 0.5\*imageA(:,:,2);
  - >> figure(34)
  - >> imshow(imageA);
  - >> title('Image A- reduced Blue component');

# 10/5/2018







Image A- reduced Blue component













# 谢谢













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