## HW2

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## **Environment**

Python == 3.11.0

opency-python == 4.12.0.88

numpy == 2.2.6

open3d == 0.19.0

pandas == 2.3.2

scipy == 1.16.2

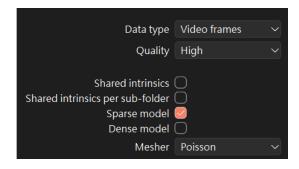
tqdm == 4.67.1

## Problem1

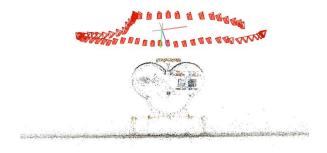
#### 1-1

使用 splitvideo.py 將影片每 1 秒擷取 5 frame,輸入到 colmap 用 automatic reconstruction

設定:



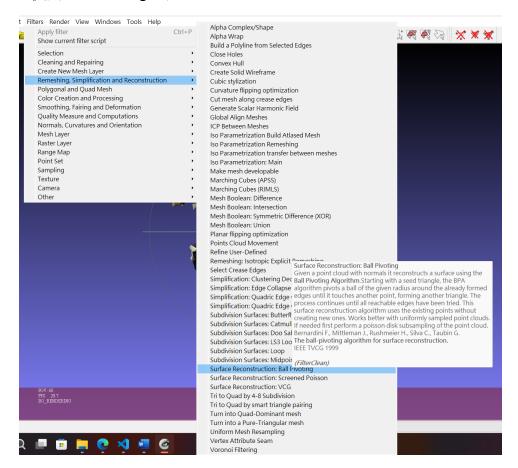
result:



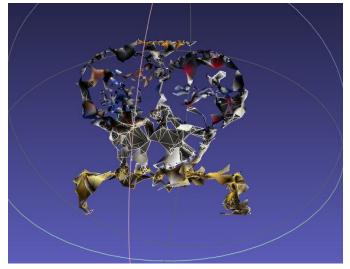
#### 1-2

### 用 meshlab 重建

- 1.把多餘的點手動清除
- 2.使用 Ball Pivoting 重建 surface



#### result:



觀察:sparse model 的點較為稀疏,重建有一定難度

影片連結:https://www.youtube.com/watch?v=kS03sSNckk0

#### Problem2

使用 2d3dmathcing.py 完成 2-1 與 2-2

#### 2-1

Step1:算 world to camera [R|t]

```
def pnpsolver(query,model,cameraMatrix=0,distortion=0,self_flag = False):
    kp_query, desc_query = query
   kp_model, desc_model = model
   cameraMatrix = np.array([[1868.27,0,540],[0,1869.18,960],[0,0,1]])
   distCoeffs = np.array([0.0847023,-0.192929,-0.000201144,-0.000725352])
   # TODO: solve PnP problem using OpenCV
   # Hint: you may use "Descriptors Matching and ratio test" first
   matcher = cv2.BFMatcher()
   matches = matcher.knnMatch(desc query, desc model, k=2)
   good matches = []
    for m, n in matches:
        if m.distance < 0.75 * n.distance:</pre>
            good matches.append(m)
    good_matches = sorted(good_matches, key=lambda x: x.distance)
    pointsquery = np.array([kp_query[m.queryIdx] for m in good_matches])
    pointsmodel = np.array([kp_model[m.trainIdx] for m in good_matches])
```

用 hw1 的 match 方法選出 match 的 2D 點與 3D 點

```
self_flag = True
for i in tqdm(IMAGE_ID_LIST):
    # Load quaery image
    fname = f"valid_img{i*5}.jpg"
    idx = images_df.loc[images_df["NAME"] == fname]["IMAGE_ID"].values[0]
    rimg = cv2.imread("data/frames/" + fname)

# Load query keypoints and descriptors
    points = point_desc_df.loc[point_desc_df["IMAGE_ID"] == idx]
    kp_query = np.array(points["XY"].to_list())
    desc_query = np.array(points["XY"].to_list()).astype(np.float32)

# Find correspondance and solve pnp
    retval, rvec, tvec, inliers = pnpsolver((kp_query, desc_query), (kp_model, desc_model),self_flag=self_flag)
    if not retval:
        continue
```

用 self\_flag 決定用自己的 p3p\_ransac 還是 opencv 的 solvePnPRansac function 解 出[R|t]

#### 自己實作 p3p(distortion 部分用 chatGPT 得出):

```
def World2Plane(world_pts, r, t, K, distCoeffs):
    #world to camera
    pts_cam = (r @ world_pts.T + t.reshape(3,1)).T

#camera normalize
    x = pts_cam[:,0] / pts_cam[:,2]
    y = pts_cam[:,1] / pts_cam[:,2]

#distortion
    k1, k2, p1, p2 = distCoeffs
    r2 = x**2 + y**2
    radial = 1 + k1*r2 + k2*r2**2
    x_dist = x * radial + 2*p1*x*y + p2*(r2 + 2*x**2)
    y_dist = y * radial + p1*(r2 + 2*y**2) + 2*p2*x*y

u = K[0,0]*x_dist + K[0,2]
    v = K[1,1]*y_dist + K[1,2]
    return np.vstack([u, v]).T #(points number, 2)
```

#### World2Plane:

- 1.把 world 座標轉乘 camera 座標
- 2.camera 座標標準化
- 3.用 k1,k2,p1,p2 與 instinct matrix 得到 distortion 後的 plane 座標

```
def undistort_points(pts, K, distCoeffs, max_iter=5):
    fx, fy = K[0,0], K[1,1]
    cx, cy = K[0,2], K[1,2]
    k1, k2, p1, p2 = distCoeffs
    undistorted = []
       #normalize
        x = (u - cx) / fx
        y = (v - cy) / fy
        x_u, y_u = x, y
        for _ in range(max_iter):#iteration solve undistort
            r2 = x_u^{**}2 + y_u^{**}2
            radial = 1 + k1*r2 + k2*r2**2
           x_u = (x - 2*p1*x_u*y_u - p2*(r2 + 2*x_u**2)) / radial
            y_u = (y - p1*(r2 + 2*y_u**2) - 2*p2*x_u*y_u) / radial
        undistorted.append([x_u, y_u, 1.0])
    return np.array(undistorted) / np.linalg.norm(undistorted, axis=1).reshape(-1,1)
    #normalize for p3p direction
```

### undistort\_points:

- 1.用 iteration 的方式估計 undistorted 的 camera 座標
- 2.將 camera 座標 normalize 成單位方向,p3p 要用

```
ef p3p_solver(world_pts, cam_dirs):
  poses = []
  perms = list(itertools.permutations([0,1,2]))
      i1,i2,i3 = perm
          and np.dot(cam_dirs[i1], cam_dirs[i2]) <= np.dot(cam_dirs[i2], cam_dirs[i3]):</pre>
  m1, m2, m3 = cam_dirs[reindex]
  m12 = np.dot(m1, m2)
  m13 = np.dot(m1,m3)
  m23 = np.dot(m2,m3)
  X1, X2, X3 = world_pts[reindex]
  X1 = X1.reshape(1,3)
  X2 = X2.reshape(1,3)
  X3 = X3.reshape(1,3)
  m1 = m1.reshape(1,3)
  m2 = m2.reshape(1,3)
  m3 = m3.reshape(1,3)
  s12 = np.sum((X1-X2)**2)
  s13 = np.sum((X1-X3)**2)
```

```
(A^*x^{**2} + B^*x + C) / (2^*s13^*(m12^*x - m23))
+ 4*s13*s23*m12**2 - 2*s13*s23 - s23**2
c3 = 4*s12**2*m13 - 4*s12*s13*m12*m23 - 4*s12*s13*m13\
                                                                                        d3 = np.sqrt(s12/(x**2-2*x*y*m12+y**2))
d1 = x*d3
    - 8*s12*s23*m13 + 4*s13**2*m12*m23\
      8*s13*s23*m12**2*m13 - 4*s13*s23*m12*m23\
    + 4*s13*s23*m13 + 4*s23**2*m13
                                                                                        d2 = y*d3
    -4*s12**2*m13**2 - 2*s12**2 + 8*s12*s13*m12*m13*m23\
                                                                                        + 4*s12*s13*m23**2 + 8*s12*s23*m13**2 + 4*s12*s23\
- 4*s13**2*m12**2 - 4*s13**2*m23**2 + 2*s13**2\
    + 4*s13*s23*m12**2 + 8*s13*s23*m12*m13*m23\
     4*s23**2*m13**2 - 2*s23**2
                                                                                            c1 = 4*s12**2*m13 - 4*s12*s13*m12*m23\
    - 8*s12*s13*m13*m23**2 + 4*s12*s13*m13\
- 8*s12*s23*m13 + 4*s13**2*m12*m23\
    - 4*s13*s23*m12*m23 - 4*s13*s23*m13\
                                                                                             dd = -np.linalg.inv(J.T @ J) @ J.T @ fd.reshape((3,1))
d1,d2,d3 = np.array([d1,d2,d3]) + dd.reshape(3)
    + 4*s23**2*m13
c\theta = -s12^{**}2 + 4^*s12^*s13^*m23^{**}2 - 2^*s12^*s13
    + 2*s12*s23 - s13**2 + 2*s13*s23 - s23**2
                                                                                        Y = np.hstack[[Y1.T,Y2.T,np.cross(Y1,Y2).T]]
r = Y @ np.linalg.inv(X)
t = d1*m1.T - r@X1.T
poses.append((r,t))
roots = [r.real for r in roots if np.isreal(r) and r.real > 0]
3 = 2*(s12-s23)*m13
```

#### p3p\_solver:

## 根據 P3P Made Easy

- 1.reindex points 直到滿足 m13 ≤ m12 ≤m23(mij = I,j dir 的內積)
- 2.使用 world points+對應 camera dir,求出對應 c4,c3,c2,c1,c0 後求根 x
- 3.用 x 求出 y 與三個點的深度 d1,d2,d3
- 4. 用 Gauss-Newton method 來 refine 深度 d1,d2,d3 (由 gemini 得出)
- 5.用 d1,d2,d3 與其他參數算出 world to camera 的 R,t

```
def ransac_p3p(world_pts, image_pts, K, distCoeffs,
               iterations=100, threshold=8, confidence=0.99):
   best_inliers = []
   best_pose = None
   dirs = undistort_points(image_pts, K, distCoeffs)
   N = world_pts.shape[0]
   best_error = np.inf
    for _ in range(iterations):#N iterations
        idx = np.random.choice(N, 3, replace=False)#sample S point
        sols = p3p solver(world pts[idx], dirs[idx])#fit
        if len(sols) == 0:
           continue
        for r, t in sols:
           proj = World2Plane(world_pts, r, t, K, distCoeffs)
            err = np.linalg.norm(proj - image_pts, axis=1)
            inliers = np.where(err < threshold)[0]#threshold d</pre>
            if len(inliers) >= N*confidence:#good fit
                err = np.mean(np.linalg.norm(proj[inliers] - image_pts[inliers], axis=1))
                if err<best error:
                    best_inliers = inliers
                    best_pose = (r, t)
                    best_error = err
    if best_pose is None:
   r, t = best_pose
   rvec = R.from_matrix(r).as_rotvec()
   tvec = t.reshape(3,1)
    inliers = np.array(best_inliers).reshape(-1,1)
   return True, rvec, tvec, inliers
```

## ransac\_p3p:

實作 ransac

在多次 iteraion 中

- 1. 每次隨機選 3 組點用 p3p\_solver 去 fit
- 2.fit 結果用來把 world 座標用 World2Plane 得到 plane 座標
- 3.算有多少點誤差在 threshold 內
- 4.如果在 threshold 內的 inliner 數量>總數\*confidence,則是 good fit 回傳最好的 fit 結果

#### Step2:error 計算

```
#calculate error
def rotation_error(R1, R2):
    #TODO: calculate rotation error
    R1 = R.from_quat(R1)
    R2 = R.from_quat(R2)
    R_rel = R1 * R2.inv()
    rotvecs = R_rel.as_rotvec()
    return np.median(np.abs(rotvecs))

def translation_error(t1, t2):
    #TODO: calculate translation error
    return np.sqrt(np.sum((t1 - t2) ** 2))
```

#### rotation error:

把 R1 與 R2 的 inverse 相乘後轉乘 rvec 形式,取中位數 translation error:

算 t1,t2 的 2-norm distance

### Step3:畫相機位置與軌跡

```
Camera2World_Transform_Matrixs = []
for r, t in zip(r_list, t_list):
    # TODO: calculate camera pose in world coordinate system
    c2w = np.zeros((3,4))
    c2w[:3,:3] = R.from_rotvec(r.reshape(1,3)).as_matrix().T.reshape(3,3)
    c2w[:3,3] = (-c2w[:3,:3] @ t.reshape(3,1)).flatten()
    Camera2World_Transform_Matrixs.append(c2w)

visualization(Camera2World_Transform_Matrixs, points3D_df)
```

先把 world\_to\_camera matrix 轉成 camera\_to\_world matrix

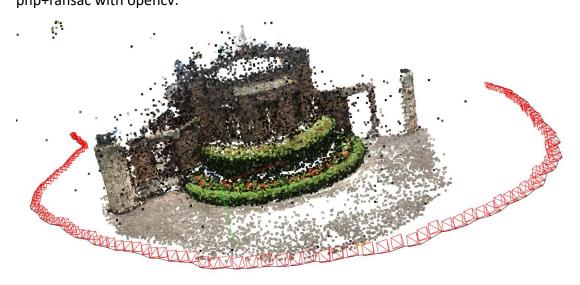
Xw = R-1 \* Xc - R-1 \* t

```
f = 0.1
    points = np.array([
    [0, 0, 0,1],
        [s, s, f,1],
[s, -s, f,1],
[s, s, f,1],
[-s, s, f,1]
    points = (c2w @ points.T).T
    track.append(points[0])
        [0, 1], [0, 2], [0, 3], [0, 4],
                                                            track_lines = [[i,i+1] for i in range(len(track)-1)]
    camera_pyramid = o3d.geometry.LineSet(
        points=o3d.utility.Vector3dVector(points),
lines=o3d.utility.Vector2iVector(lines),
                                                            trackline = o3d.geometry.LineSet(
                                                                  points=o3d.utility.Vector3dVector(track),
                                                                  lines=o3d.utility.Vector2iVector(track_lines),
    camera_pyramid.paint_uniform_color([1, 0, 0])
                                                             trackline.paint_uniform_color([0, 0, 0])
    vis.add_geometry(camera_pyramid)
                                                            vis.add_geometry(trackline)
```

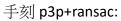
#### visualization:

用 camera\_to\_world matrix 轉換角錐點(points)位置後,用 points 與 lines 畫一個四角錐 camera\_pyramid,角錐頂點則一個一個連成線(trackline)

result: pnp+ransac with opencv:



rotation differences:2.1670244653495326e-05 translation differences:0.00016467364717986384





rotation differences:0.00030750389692665967 translation differences:0.0019143133395420225

```
[0,1,3,2],
                                                                                 [0,1,5,4],
                                                                                 [0,2,6,4],
box_maxtrix = np.load("cube_transform_mat.npy")
box_point = np.array([[0,0,0,1],
                       [1,0,0,1],
                       [0,1,0,1],
                       [1,1,0,1],
                       [0,0,1,1],
                                                                                 (255, 0, 0),
                                                                                 (0, 255, 0),
                       [1,0,1,1],
                                                                                 (0, 0, 255),
                       [0,1,1,1],
                                                                                 (255, 255, 0), # Cyan
                                                                                 (255, 0, 255), # Magenta
box_point = (box_maxtrix @ box_point.T).T
                                                                                 (0, 255, 255) # Yellow
box\_point = np.hstack([box\_point,np.ones((box\_point.shape[\emptyset],1))])
```

將 box point 的 8 個點,每面需要的點與顏色設定好 8 個點為 1\*1\*1 的立方體乘上 cube\_transform\_mat

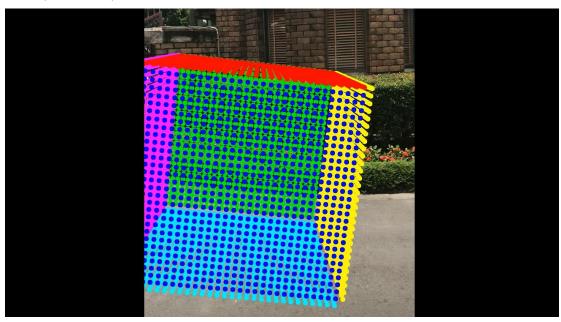
```
N = 30
x = np.arange(N)
y = np.arange(N)
X, Y = np.meshgrid(x, y, indexing='xy')
X, Y = X.reshape(-1,1)/N, Y.reshape(-1,1)/N
weights = np.hstack([1-X-Y,X,np.zeros(X.shape),Y])
```

- 1.用 world\_to\_camera matrix 與 instinct matrix of camera 把 box point 的點投射到 plane 上
- 2.接著用 meshgrid 得出每個面的點所需要的四頂點 weights,將每一面的平行四邊形分成 30\*30 個點
- 3.根據點的深度做排序,從深度高到低一點一點畫上去,並排除深度<0(在相機 後面)的點

## 方塊位置:



# result(影片截圖):



影片連結: <a href="https://youtu.be/YN1LazGENIk">https://youtu.be/YN1LazGENIk</a>