# Contents

# 1  Basic

## 1.1  .vimrc

```
syn on
se ai nu ru cul mouse=a
se cin et ts=2 sw=2 sts=2
so $VIMRUNTIME/mswin.vim
colo desert
se gfn=Monospace\ 14
```

## 1.2  Increase Stack Size

```
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
    const rlim_t ks = 64*1024*1024;
    struct rlimit rl;
    int res=getrlimit(RLIMIT_STACK, &rl);
    if(res==0){
        if(rl.rlim_cur<ks){
            rl.rlim_cur=ks;
            res=setrlimit(RLIMIT_STACK, &rl);
        }
    }
}
```

# 2  flow

## 2.1  Dinic

```
#include <bits/stdc++.h>
using namespace std;
#define N 5010
#define M 60010
#define ll long long
#define inf 1ll<<62
ll to[ M ] , next[ M ] , head[ M ];
ll cnt , ceng[ M ] , que[ M ] , w[ M ];
ll n , m , start , end;
void add( ll a , ll b , ll flow ){
    to[ cnt ] = b , next[ cnt ] = head[ a ] , w[ cnt ] =
        flow , head[ a ] = cnt ++;
    to[ cnt ] = a , next[ cnt ] = head[ b ] , w[ cnt ] =
        flow , head[ b ] = cnt ++;
}
void read(){
    memset(head,-1,sizeof head);
    //memset(next,-1,sizeof next);
    scanf( "%lld%lld" , &n , &m );
    ll a , b , flow;
    for( ll i = 1 ; i <= m ; i ++ ){
        scanf( "%lld%lld%lld" , &a , &b , &flow );
        add( a , b , flow );
    }
    end = n ,start = 1;
}
bool bfs(){
    memset( ceng , -1 , sizeof(ceng) );
    ll h = 1 , t = 2;
    ceng[ start ] = 0;
    que[ 1 ] = start;
    while( h < t ){
        ll sta = que[ h ++ ];
        for( ll i = head[ sta ] ; ~i ; i = next[ i ] )
            if( w[ i ] > 0 && ceng[ to[ i ] ] < 0 ){
                ceng[ to[ i ] ] = ceng[ sta ] + 1;
                que[ t ++ ] = to[ i ];
            }
    }
}
```

```
    return ceng[ end ] != -1;
}
ll find( ll x , ll low ){
  ll tmp = 0 , result = 0;
  if( x == end ) return low;
  for( ll i = head[ x ] ; ~i && result < low ; i = next
      [ i ] )
    if( w[ i ] > 0 && ceng[ to[ i ] ] == ceng[ x ] + 1
        ){
      tmp = find( to[ i ] , min( w[ i ] , low - result
          ) );
      w[ i ] -= tmp;
      w[ i^1 ] += tmp;
      result += tmp;
    }
  if( !result ) ceng[ x ] = -1;
  return result;
}
ll dinic(){
  ll ans = 0 , tmp;
  while( bfs() ) ans += find( start , inf );
  return ans;
}
int main(){
  read();
  cout << dinic() << endl;
}
```

## 2.2  DMST

```
/*
 * Edmond's algoirthm for Minimum Directed Spanning
     Tree
 * runs in O(VE)
 */
const int MAXV = 10010;
const int MAXE = 10010;
const int INF  = 2147483647;
struct Edge{
  int u, v, c;
  Edge(){}
  Edge(int x, int y, int z) :
    u(x), v(y), c(z){}
};
int V, E, root;
Edge edges[MAXE];
inline int newV(){
  V++;
  return V;
}
inline void addEdge(int u, int v, int c){
  E++;
  edges[E] = Edge(u, v, c);
}
bool con[MAXV];
int mnInW[MAXV], prv[MAXV], cyc[MAXV], vis[MAXV];
inline int DMST(){
  fill(con, con+V+1, 0);
  int r1 = 0, r2 = 0;
  while(1){
    fill(mnInW, mnInW+V+1, INF);
    fill(prv, prv+V+1, -1);
    REP(i, 1, E){
      int u = edges[i].u, v = edges[i].v, c = edges[i].
          c;
      if(u != v && v != root && c < mnInW[v])
        mnInW[v] = c, prv[v] = u;
    }
    fill(vis, vis+V+1, -1);
    fill(cyc, cyc+V+1, -1);
    r1 = 0;
    bool jf = 0;
    REP(i, 1, V){
      if(con[i]) continue ;
      if(prv[i] == -1 && i != root) return -1;
      if(prv[i] > 0) r1 += mnInW[i];
      int s;
      for(s = i; s != -1 && vis[s] == -1; s = prv[s])
        vis[s] = i;
      if(s > 0 && vis[s] == i){
```

```
        // get a cycle
        jf = 1;
        int v = s;
        do{
          cyc[v] = s, con[v] = 1;
          r2 += mnInW[v];
          v = prv[v];
        }while(v != s);
        con[s] = 0;
      }
    }
    if(!jf) break ;
    REP(i, 1, E){
      int &u = edges[i].u;
      int &v = edges[i].v;
      if(cyc[v] > 0) edges[i].c -= mnInW[edges[i].v];
      if(cyc[u] > 0) edges[i].u = cyc[edges[i].u];
      if(cyc[v] > 0) edges[i].v = cyc[edges[i].v];
      if(u == v) edges[i--] = edges[E--];
    }
  }
  return r1+r2;
}
```

## 2.3  ISAP

```
#include <bits/stdc++.h>
#define SZ(c) ((int)(c).size())
using namespace std;
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF  = 1000000;
  struct Edge {
    int v, c, r;
    Edge(int _v, int _c, int _r) : v(_v), c(_c), r(_r)
        {}
  };
  int s, t;
  vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void flowinit(int x) {
    tot = x+2;
    s = x+1, t = x+2;
    for(int i = 0; i <= tot; i++) {
      G[i].clear();
      iter[i] = d[i] = gap[i] = 0;
    }
  }
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v]) ));
    G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  }
  int dfs(int p, int flow) {
    if(p == t) return flow;
    for(int &i = iter[p]; i < SZ(G[p]); i++) {
      Edge &e = G[p][i];
      if(e.c > 0 && d[p] == d[e.v]+1) {
        int f = dfs(e.v, min(flow, e.c));
        if(f) {
          e.c -= f;
          G[e.v][e.r].c += f;
          return f;
        }
      }
    }
    if( (--gap[d[p]]) == 0) d[s] = tot;
    else {
      d[p]++;
      iter[p] = 0;
      ++gap[d[p]];
    }
    return 0;
  }

  int maxflow() {
    //puts("MF");
    int res = 0;
    gap[0] = tot;
    for(res = 0; d[s] < tot; res += dfs(s, INF));
    return res;
```

```
      }
} flow;

Maxflow::Edge e(1, 1, 1);
```

## 2.4  MinCostFlow

```
/*
  A template for Min Cost Max Flow
  tested with TIOJ 1724
*/
#include <bits/stdc++.h>
using namespace std;
struct MinCostMaxFlow{
  static const int MAXV = 20010;
  static const int INF  = 1000000000;
  struct Edge{
    int v, cap, w, rev;
    Edge(){}
    Edge(int t2, int t3, int t4, int t5)
    : v(t2), cap(t3), w(t4), rev(t5) {}
  };
  int V, s, t;
  vector<Edge> g[MAXV];
  void init(int n){
    V = n+2;
    s = n+1, t = n+2;
    for(int i = 1; i <= V; i++) g[i].clear();
  }
  void addEdge(int a, int b, int cap, int w){
    //printf("addEdge %d %d %d %d\n", a, b, cap, w);
    g[a].push_back(Edge(b, cap, w, (int) g[b].size()));
    g[b].push_back(Edge(a, 0, -w, ((int) g[a].size()) -
        1));
  }
  int d[MAXV], id[MAXV], mom[MAXV];
  bool inqu[MAXV];
  int qu[2000000], ql, qr;//the size of qu should be
      much large than MAXV
  int mncmxf(){
    int mxf = 0, mnc = 0;
    while(1){
      fill(d+1, d+1+V, -INF);
      fill(inqu+1, inqu+1+V, 0);
      fill(mom+1, mom+1+V, -1);
      mom[s] = s;
      d[s] = 0;
      ql = 1, qr = 0;
      qu[++qr] = s;
      inqu[s] = 1;
      while(ql <= qr){
        int u = qu[ql++];
        inqu[u] = 0;
        for(int i = 0; i < (int) g[u].size(); i++){
          Edge &e = g[u][i];
          int v = e.v;
          if(e.cap > 0 && d[v] < d[u]+e.w){
            // for min cost : d[v] > d[u]+e.w
            d[v] = d[u]+e.w;
            mom[v] = u;
            id[v] = i;
            if(!inqu[v]) qu[++qr] = v, inqu[v] = 1;
          }
        }
      }
      if(mom[t] == -1) break ;
      int df = INF;
      for(int u = t; u != s; u = mom[u])
        df = min(df, g[mom[u]][id[u]].cap);
      for(int u = t; u != s; u = mom[u]){
        Edge &e = g[mom[u]][id[u]];
        e.cap              -= df;
        g[e.v][e.rev].cap += df;
      }
      //printf("mxf %d mnc %d\n", mxf, mnc);
      mxf += df;
      mnc += df*d[t];
      //printf("mxf %d mnc %d\n", mxf, mnc);
    }
    return mnc;
```

## 2.5  SW min-cut

```
struct SW{ // O(V^3)
  static const int MXN = 514;
  int n,vst[MXN],del[MXN];
  int edge[MXN][MXN],wei[MXN];
  void init(int _n){
    n = _n;
    FZ(edge);
    FZ(del);
  }
  void add_edge(int u, int v, int w){
    edge[u][v] += w;
    edge[v][u] += w;
  }
  void search(int &s, int &t){
    FZ(vst); FZ(wei);
    s = t = -1;
    while (true){
      int mx=-1, cur=0;
      for (int i=0; i<n; i++)
        if (!del[i] && !vst[i] && mx<wei[i])
          cur = i, mx = wei[i];
      if (mx == -1) break;
      vst[cur] = 1;
      s = t;
      t = cur;
      for (int i=0; i<n; i++)
        if (!vst[i] && !del[i]) wei[i] += edge[cur][i];
    }
  }
  int solve(){
    int res = 2147483647;
    for (int i=0,x,y; i<n-1; i++){
      search(x,y);
      res = min(res,wei[y]);
      del[y] = 1;
      for (int j=0; j<n; j++)
        edge[x][j] = (edge[j][x] += edge[y][j]);
    }
    return res;
  }
}graph;
```

## 2.6  HLPPA

```
/* Highest-Label Preflow Push Algorithm */
// tested with sgu-212 (more testing suggested)
int n,m,src,sink;
int deg[MAXN],adj[MAXN][MAXN],res[MAXN][MAXN]; //
    residual capacity
// graph (i.e. all things above) should be constructed
    beforehand
int ef[MAXN],ht[MAXN]; // excess flow, height
int apt[MAXN]; // the next adj index to try push
int htodo; // highest label to check with
int hcnt[MAXN*2]; // number of nodes with height h
queue<int> ovque[MAXN*2]; // used to implement highest-
    label selection
bool inque[MAXN];
inline void push(int v,int u) {
  int a=min(ef[v],res[v][u]);
  ef[v]-=a; ef[u]+=a;
  res[v][u]-=a; res[u][v]+=a;
  if(!inque[u]) {
    inque[u]=1;
    ovque[ht[u]].push(u);
  }
}
inline void relabel(int v) {
  int i,u,oldh;
  oldh=ht[v]; ht[v]=2*n;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(res[v][u]) ht[v]=min(ht[u]+1,ht[v]);
```

```
    }
    // gap speedup
    hcnt[oldh]--; hcnt[ht[v]]++;
    if(0<oldh&&oldh<n&&hcnt[oldh]==0) {
        for(i=0;i<n;i++) {
            if(ht[i]>oldh&&ht[i]<n) {
                hcnt[ht[i]]--;
                hcnt[n]++;
                ht[i]=n;
            }
        }
    }
    // update queue
    htodo=ht[v]; ovque[ht[v]].push(v); inque[v]=1;
}
inline void initPreflow() {
    int i,u;
    for(i=0;i<n;i++) {
        ht[i]=ef[i]=0;
        apt[i]=0; inque[i]=0;
    }
    ht[src]=n;
    for(i=0;i<deg[src];i++) {
        u=adj[src][i];
        ef[u]=res[src][u];
        ef[src]-=ef[u];
        res[u][src]=ef[u];
        res[src][u]=0;
    }
    htodo=n-1;
    for(i=0;i<2*n;i++) {
        hcnt[i]=0;
        while(!ovque[i].empty()) ovque[i].pop();
    }
    for(i=0;i<n;i++) {
        if(i==src||i==sink) continue;
        if(ef[i]) {
            inque[i]=1;
            ovque[ht[i]].push(i);
        }
        hcnt[ht[i]]++;
    }
    // to ensure src & sink is never added to queue
    inque[src]=inque[sink]=1;
}
inline void discharge(int v) {
    int u;
    while(ef[v]) {
        if(apt[v]==deg[v]) {
            relabel(v);
            apt[v]=0;
            continue;
        }
        u=adj[v][apt[v]];
        if(res[v][u]&&ht[v]==ht[u]+1) push(v,u);
        else apt[v]++;
    }
}
inline void hlppa() {
    int v;
    list<int>::iterator it;
    initPreflow();
    while(htodo>=0) {
        if(!ovque[htodo].size()) {
            htodo--;
            continue;
        }
        v=ovque[htodo].front();
        ovque[htodo].pop();
        inque[v]=0;
        discharge(v);
    }
}
```

## 2.7  Hungarian

```
#define NIL -1
#define INF 100000000
int n,matched;
int cost[MAXNUM][MAXNUM];
```

```
bool sets[MAXNUM]; // whether x is in set S
bool sett[MAXNUM]; // whether y is in set T
int xlabel[MAXNUM],ylabel[MAXNUM];
int xy[MAXNUM],yx[MAXNUM]; // matched with whom
int slack[MAXNUM]; // given y: min{xlabel[x]+ylabel[y]-
    cost[x][y]} | x not in S
int prev[MAXNUM]; // for augmenting matching
inline void relabel() {
    int i,delta=INF;
    for(i=0;i<n;i++) if(!sett[i]) delta=min(slack[i],
        delta);
    for(i=0;i<n;i++) if(sets[i]) xlabel[i]-=delta;
    for(i=0;i<n;i++) {
        if(sett[i]) ylabel[i]+=delta;
        else slack[i]-=delta;
    }
}
inline void add_sets(int x) {
    int i;
    sets[x]=1;
    for(i=0;i<n;i++) {
        if(xlabel[x]+ylabel[i]-cost[x][i]<slack[i]) {
            slack[i]=xlabel[x]+ylabel[i]-cost[x][i];
            prev[i]=x;
        }
    }
}
inline void augment(int final) {
    int x=prev[final],y=final,tmp;
    matched++;
    while(1) {
        tmp=xy[x]; xy[x]=y; yx[y]=x; y=tmp;
        if(y==NIL) return;
        x=prev[y];
    }
}
inline void phase() {
    int i,y,root;
    for(i=0;i<n;i++) { sets[i]=sett[i]=0; slack[i]=INF; }
    for(root=0;root<n&&xy[root]!=NIL;root++);
    add_sets(root);
    while(1) {
        relabel();
        for(y=0;y<n;y++) if(!sett[y]&&slack[y]==0) break;
        if(yx[y]==NIL) { augment(y); return; }
        else { add_sets(yx[y]); sett[y]=1; }
    }
}
inline int hungarian() {
    int i,j,c=0;
    for(i=0;i<n;i++) {
        xy[i]=yx[i]=NIL;
        xlabel[i]=ylabel[i]=0;
        for(j=0;j<n;j++) xlabel[i]=max(cost[i][j],xlabel[i
            ]);
    }
    for(i=0;i<n;i++) phase();
    for(i=0;i<n;i++) c+=cost[i][xy[i]];
    return c;
}
```

## 2.8  Hungarian Unbalanced

```
const int nil = -1;
const int inf = 1000000000;
int xn,yn,matched;
int cost[MAXN][MAXN];
bool sets[MAXN]; // whether x is in set S
bool sett[MAXN]; // whether y is in set T
int xlabel[MAXN],ylabel[MAXN];
int xy[MAXN],yx[MAXN]; // matched with whom
int slack[MAXN]; // given y: min{xlabel[x]+ylabel[y]-
    cost[x][y]} | x not in S
int prev[MAXN]; // for augmenting matching
inline void relabel() {
    int i,delta=inf;
    for(i=0;i<yn;i++) if(!sett[i]) delta=min(slack[i],
        delta);
    for(i=0;i<xn;i++) if(sets[i]) xlabel[i]-=delta;
    for(i=0;i<yn;i++) {
```

```
      if(sett[i]) ylabel[i]+=delta;
      else slack[i]-=delta;
    }
  }
}
inline void add_sets(int x) {
  int i;
  sets[x]=1;
  for(i=0;i<yn;i++) {
    if(xlabel[x]+ylabel[i]-cost[x][i]<slack[i]) {
      slack[i]=xlabel[x]+ylabel[i]-cost[x][i];
      prev[i]=x;
    }
  }
}
inline void augment(int final) {
  int x=prev[final],y=final,tmp;
  matched++;
  while(1) {
    tmp=xy[x]; xy[x]=y; yx[y]=x; y=tmp;
    if(y==nil) return;
    x=prev[y];
  }
}
inline void phase() {
  int i,y,root;
  for(i=0;i<xn;i++) sets[i]=0;
  for(i=0;i<yn;i++) { sett[i]=0; slack[i]=inf; }
  for(root=0;root<xn&&xy[root]!=nil;root++);
  add_sets(root);
  while(1) {
    relabel();
    for(y=0;y<yn;y++) if(!sett[y]&&slack[y]==0) break;
    if(yx[y]==nil) { augment(y); return; }
    else { add_sets(yx[y]); sett[y]=1; }
  }
}
inline int hungarian() {
  int i,j,c=0;
  matched=0;
  // we must have "xn<yn"
  bool swapxy=0;
  if(xn>yn) {
    swapxy=1;
    int mn=max(xn,yn);
    swap(xn,yn);
    for(int i=0;i<mn;i++)
      for(int j=0;j<i;j++)
        swap(cost[i][j],cost[j][i]);
  }
  for(i=0;i<xn;i++) {
    xy[i]=nil;
    xlabel[i]=0;
    for(j=0;j<yn;j++) xlabel[i]=max(cost[i][j],xlabel[i
        ]);
  }
  for(i=0;i<yn;i++) {
    yx[i]=nil;
    ylabel[i]=0;
  }
  for(i=0;i<xn;i++) phase();
  for(i=0;i<xn;i++) c+=cost[i][xy[i]];
  // recover cost matrix (if necessary)
  if(swapxy) {
    int mn=max(xn,yn);
    swap(xn,yn);
    for(int i=0;i<mn;i++)
      for(int j=0;j<i;j++)
        swap(cost[i][j],cost[j][i]);
  }
  // need special recovery if we want more info than
      matching value
  return c;
}


## 2.9  Gusfield

#define SOURCE 0
#define SINK 1
const unsigned int inf=4000000000u;
int n,m,deg[MAXNUM],adj[MAXNUM][MAXNUM];
```

```
unsigned int res[MAXNUM][MAXNUM],cap[MAXNUM][MAXNUM];
int nei[MAXNUM],gdeg[MAXNUM],gadj[MAXNUM][MAXNUM];
unsigned int gres[MAXNUM][MAXNUM];
unsigned int cut[MAXNUM][MAXNUM];
unsigned int cutarr[MAXNUM*MAXNUM];
int cutn,ql,qr,que[MAXNUM],pred[MAXNUM];
unsigned int aug[MAXNUM];
bool cutset[MAXNUM];
int visited[MAXNUM],visid=0;
inline void augment(int src,int sink) {
  int v=sink; unsigned a=aug[sink];
  while(v!=src) {
    res[pred[v]][v]-=a;
    res[v][pred[v]]+=a;
    v=pred[v];
  }
}
inline bool bfs(int src,int sink) {
  int i,v,u; ++visid;
  ql=qr=0; que[qr++]=src;
  visited[src]=visid; aug[src]=inf;
  while(ql<qr) {
    v=que[ql++];
    for(i=0;i<deg[v];i++) {
      u=adj[v][i];
      if(visited[u]==visid||res[v][u]==0) continue;
      visited[u]=visid; pred[u]=v;
      aug[u]=min(aug[v],res[v][u]);
      que[qr++]=u;
      if(u==sink) return 1;
    }
  }
  return 0;
}
void dfs_src(int v) {
  int i,u;
  visited[v]=visid;
  cutset[v]=SOURCE;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(visited[u]<visid&&res[v][u]) dfs_src(u);
  }
}
inline unsigned int maxflow(int src,int sink) {
  int i,j;
  unsigned int f=0;
  for(i=0;i<n;i++) {
    for(j=0;j<deg[i];j++) res[i][adj[i][j]]=cap[i][adj[
        i][
      j]];
    cutset[i]=SINK;
  }
  while(bfs(src,sink)) {
    augment(src,sink);
    f+=aug[sink];
  }
  ++visid;
  dfs_src(src);
  return f;
}
inline void gusfield() {
  int i,j;
  unsigned int f;
  for(i=0;i<n;i++) { nei[i]=0; gdeg[i]=0; }
  for(i=1;i<n;i++) {
    f=maxflow(i,nei[i]);
    gres[i][nei[i]]=gres[nei[i]][i]=f;
    gadj[i][gdeg[i]++]=nei[i];
    gadj[nei[i]][gdeg[nei[i]]++]=i;
    for(j=i+1;j<n;j++)
      if(nei[j]==nei[i]&&cutset[j]==SOURCE) nei[j]=i;
  }
}
void dfs(int v,int pred,int src,unsigned int cur) {
  int i,u;
  cut[src][v]=cur;
  for(i=0;i<gdeg[v];i++) {
    u=gadj[v][i];
    if(u==pred) continue;
    dfs(u,v,src,min(cur,gres[v][u]));
  }
}
```

```cpp
inline void find_all_cuts() {
  int i;
  cutn=0; gusfield();
  for(i=0;i<n;i++) dfs(i,-1,i,inf);
}
```

## 2.10  Relabel to Front

```cpp
/* Relabel-to-Front */
// tested with sgu-212 (more testing suggested)
int n,m,layer,src,sink,lvl[MAXN];
Edge ed[MAXM];
int deg[MAXN],adj[MAXN][MAXN];
int res[MAXN][MAXN]; // residual capacity
// graph (i.e. all things above) should be constructed
    beforehand
list<int> lst; // discharge list
int ef[MAXN],ht[MAXN];
// excess flow, height
int apt[MAXN]; // the next adj index to try push
inline void push(int v,int u) {
  int a=min(ef[v],res[v][u]);
  ef[v]-=a; ef[u]+=a;
  res[v][u]-=a; res[u][v]+=a;
}
inline void relabel(int v) {
  int i,u;
  ht[v]=2*n;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(res[v][u]) ht[v]=min(ht[u]+1,ht[v]);
  }
}
inline void initPreflow() {
  int i,u;
  lst.clear();
  for(i=0;i<n;i++) {
    ht[i]=ef[i]=0; apt[i]=0;
    if(i!=src&&i!=sink) lst.push_back(i);
  }
  ht[src]=n;
  for(i=0;i<deg[src];i++) {
    u=adj[src][i];
    ef[u]=res[src][u];
    ef[src]-=ef[u];
    res[u][src]=ef[u];
    res[src][u]=0;
  }
}
inline void discharge(int v) {
  int u;
  while(ef[v]) {
    if(apt[v]==deg[v]) {
      relabel(v);
      apt[v]=0;
      continue;
    }
    u=adj[v][apt[v]];
    if(res[v][u]&&ht[v]==ht[u]+1) push(v,u);
    else apt[v]++;
  }
}
inline void relabelToFront() {
  int oldh,v;
  list<int>::iterator it;
  initPreflow();
  for(it=lst.begin();it!=lst.end();it++) {
    v=*it; oldh=ht[v]; discharge(v);
    if(ht[v]>oldh) {
      lst.push_front(v);
      lst.erase(it);
      it=lst.begin();
    }
  }
}
```

## 2.11  Flow Method

Maximize c^T x subject to Ax ≤ b, x ≥ 0;
with the corresponding symmetric dual problem,
Minimize b^T y subject to A^T y ≥ c, y ≥ 0.

Maximize c^T x subject to Ax ≤ b;
with the corresponding asymmetric dual problem,
Minimize b^T y subject to A^T y = c, y ≥ 0.

有源匯，有下界，最大流，無費用。

先從t連向s，容量設爲無限大。這樣就變成了無源匯的情
況。將每條有下界的邊先滿上下界的流量，然後更新盈餘
量（入的流量-出的流量）。新建超級源ss和超級匯tt，若
某個點u的盈餘量>0則ss--->u，容量爲u的盈餘量。否則u
--->tt，容量爲u的盈餘量的相反數。如果一個點的盈餘量
>0，則它是一定要流出去的，所以要從ss連向它，使它去
找這些流量的出路。建完了圖以後求一遍最大流，如果從
ss連出的所有邊都滿流，則有解。在得到的殘留網路（原
圖）上再求一次最大流即可。

# 3  Math

## 3.1  FFT

```cpp
typedef long long ll;
typedef unsigned int uint;
#define maxn 310010
#define nmaxn 141073
struct comp{
    double a , b ;
    comp( double a_ = 0.0 , double b_ = 0.0 ) : a( a_ )
        , b( b_ ){ }
} null ;
comp operator+ ( const comp &a , const comp &b ) {
    return comp(a.a+b.a,a.b+b.b); }
comp operator- ( const comp &a , const comp &b ) {
    return comp(a.a-b.a,a.b-b.b); }
comp operator* ( const comp &a , const comp &b ) {
    return comp(a.a*b.a-a.b*b.b,a.a*b.b+a.b*b.a); }
char s[ maxn ] ;
int n ;
comp A[ nmaxn ] , B[ nmaxn ] , C[ nmaxn ] ;
const double pi = acos( -1 ) ;
int L = 6 ;
ll base[ 10 ] , M = 1000000 ;
int get( comp *A ){
    if ( scanf( "%s" , s ) == EOF ) return 0 ;
    int a = 0 , p = 0 , l = 0 ;
    for ( register int i = strlen( s ) - 1 ; i >= 0 ; i
        -- ) {
        a += ( s[ i ] - '0' ) * base[ p ++ ] ;
        if( p == L ) A[ l ++ ] = comp( a , 0 ) , a = p = 0
            ;
    }
    if ( a ) A[ l ++ ] = comp( a , 0 ) ;
    return l;
}
bool init( ){
    base[ 0 ] = 1 ;
    for ( register int i = 1 ; i <= L ; i ++ ) base[ i ]
        = base[ i - 1 ] * 10 ;
    int l = get( A ) + get( B ) ;
    if ( l == 0 ) return false ;
    for ( n = 1 ; n < l ; n <<= 1 );
    //printf( "%d\n" , n ) ;
    return true ;
}
comp p[ 2 ][ nmaxn ]; int typ;
uint rev( uint a ){
    a = ( ( a & 0x55555555U ) << 1 ) | ( ( a & 0
        xAAAAAAAAU ) >> 1 ) ;
    a = ( ( a & 0x33333333U ) << 2 ) | ( ( a & 0
        xCCCCCCCCU ) >> 2 ) ;
    a = ( ( a & 0x0F0F0F0FU ) << 4 ) | ( ( a & 0
        xF0F0F0F0U ) >> 4 ) ;
    a = ( ( a & 0x00FF00FFU ) << 8 ) | ( ( a & 0
        xFF00FF00U ) >> 8 ) ;
```

```cpp
  a = ( ( a & 0x0000FFFFU ) << 16 ) | ( ( a & 0
      xFFFF0000U ) >> 16 ) ;
  return a;
}
void FFT( comp *s , comp *bac , int n ){
  register int d = log2( n );
  for ( register int i = 0 ; i < n ; i ++ ) s[ rev( i )
      >> ( 32 - d ) ] = bac[ i ];
  for ( register int i = 1 ; i <= d ; i ++ ) {
    int step = 1 << i , v = step >> 1 , rstep = n /
        step ;
    for ( register int j = 0 ; j <= n - 1 ; j += step )
        {
      comp *t = p[ typ ];
      for ( register int k = 0 ; k < v ; k ++ , t +=
          rstep ) {
        comp d = ( *t ) * s[ k + j + v ];
        s[ k + j + v ] = s[ k + j ] - d ;
        s[ k + j ] = s[ k + j ] + d ;
      }
    }
  }
}
ll ans[ 4 * maxn ];
bool work(){
  if ( !init() ) return false ;
  p[ 0 ][ 0 ] = comp( 1 , 0 ) , p[ 1 ][ 0 ] = comp( 1 ,
      0 );
  for ( register int i = 1 ; i < n ; i ++ ) {
    p[ 0 ][ i ] = comp( cos( 2 * i * pi / n ) , sin( 2
        * i * pi / n ) );
    p[ 1 ][ i ] = comp( cos( 2 * i * pi / n ) , -sin( 2
        * i * pi / n ) );
  }
  typ = 0; FFT( C , A , n ) , FFT( A , B , n ) ;
  for ( register int i = 0 ; i < n ; i ++ ) A[ i ] = A[
      i ] * C[ i ] ;
  typ = 1 ; FFT( C , A , n ) ;
  for ( register int i = 0 ; i < n ; i ++ )
    ans[ i ] = C[ i ].a / n + 0.1 , A[ i ] = null , B[
        i ] = null ;
  for ( register int i = 0 ; i < n ; i ++ )
    if ( ans[ i ] >= M ) ans[ i + 1 ] += ans[ i ] / M ,
        ans[ i ] %= M ;
  while ( n > 1 && ans[ n - 1 ] <= 0 ) n -- ;
  printf( "%lld" , ans[ n - 1 ] ) ;
  for( register int i = n - 2 ; i >= 0 ; i -- ) printf(
      "%06lld" , ans[ i ] );
  puts( "" ) ;
  return true ;
}
```

## 3.2  NTT

```cpp
ll P=2013265921,root=31;
int MAXNUM=4194304;
// Remember coefficient are mod P
/*
p=a*2^n+1
```

| n | 2^n | p | a | root | |
|---|---|---|---|---|---|
| 5 | 32 | 97 | 3 | 5 | |
| 6 | 64 | 193 | 3 | 5 | |
| 7 | 128 | 257 | 2 | 3 | |
| 8 | 256 | 257 | 1 | 3 | |
| 9 | 512 | 7681 | 15 | 17 | |
| 10 | 1024 | 12289 | 12 | 11 | |
| 11 | 2048 | 12289 | 6 | 11 | |
| 12 | 4096 | 12289 | 3 | 11 | |
| 13 | 8192 | 40961 | 5 | 3 | |
| 14 | 16384 | 65537 | 4 | 3 | |
| 15 | 32768 | 65537 | 2 | 3 | |
| 16 | 65536 | 65537 | 1 | 3 | |
| 17 | 131072 | 786433 | 6 | 10 | |
| 18 | 262144 | 786433 | 3 | 10 (605028353, 2308, 3) |
| 19 | 524288 | 5767169 | 11 | 3 | |
| 20 | 1048576 | 7340033 | 7 | 3 | |
| 21 | 2097152 | 23068673 | 11 | 3 | |
| 22 | 4194304 | 104857601 | 25 | 3 | |
| 23 | 8388608 | 167772161 | 20 | 3 | |
| 24 | 16777216 | 167772161 | 10 | 3 | |
| 25 | 33554432 | 167772161 | 5 | 3 (1107296257, 33, 10) |
| 26 | 67108864 | 469762049 | 7 | 3 | |
| 27 | 134217728 | 2013265921 | 15 | 31 | |

```cpp
*/
ll bigmod(ll a,ll b){
  if(b==0)return 1;
  return (bigmod((a*a)%P,b/2)*(b%2?a:1ll))%P;
}
ll inv(ll a,ll b){
  if(a==1)return 1;
  return (((long long)(a-inv(b%a,a))*b+1)/a)%b;
}
std::vector<ll> ps(MAXNUM);
std::vector<ll> rev(MAXNUM);
struct poly{
  std::vector<ll> co;
  int n;//polynomial degree = n
  poly(int d){n=d;co.resize(n+1,0);}
  void trans2(int NN){
    int r=0,st,N;
    unsigned int a,b;
    while((1<<r)<(NN>>1))++r;
    for(N=2;N<=NN;N<<=1,--r){
      for(st=0;st<NN;st+=N){
        int i,ss=st+(N>>1);
        for(i=(N>>1)-1;i>=0;--i){
          a=co[st+i]; b=(ps[i<<r]*co[ss+i])%P;
          co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
          co[ss+i]=a+P-b; if(co[ss+i]>=P)co[ss+i]-=P;
        }
      }
    }
  }
  void trans1(int NN){
    int r=0,st,N;
    unsigned int a,b;
    for(N=NN;N>1;N>>=1,++r){
      for(st=0;st<NN;st+=N){
        int i,ss=st+(N>>1);
        for(i=(N>>1)-1;i>=0;--i){
          a=co[st+i]; b=co[ss+i];
          co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
          co[ss+i]=((a+P-b)*ps[i<<r])%P;
        }
      }
    }
  }
  poly operator*(const poly& _b)const{
    poly a=*this,b=_b;
    int k=n+b.n,i,N=1;
    while(N<=k)N*=2;
    a.co.resize(N,0); b.co.resize(N,0);
    int r=bigmod(root,(P-1)/N),Ni=inv(N,P);
    ps[0]=1;
    for(i=1;i<N;++i)ps[i]=(ps[i-1]*r)%P;
    a.trans1(N);b.trans1(N);
    for(i=0;i<N;++i)a.co[i]=((long long)a.co[i]*b.co[i
        ])%P;
    r=inv(r,P);
    for(i=1;i<N/2;++i)std::swap(ps[i],ps[N-i]);
    a.trans2(N);
    for(i=0;i<N;++i)a.co[i]=((long long)a.co[i]*Ni)%P;
    a.n=n+_b.n; return a;
  }
};
```

## 3.3 BigInt

```cpp
struct Bigint{
  static const int LEN = 60;
  static const int BIGMOD = 10000;
  int s;
  int vl, v[LEN];
  //  vector<int> v;
  Bigint() : s(1) { vl = 0; }
  Bigint(long long a) {
    s = 1; vl = 0;
    if (a < 0) { s = -1; a = -a; }
    while (a) {
      push_back(a % BIGMOD);
      a /= BIGMOD;
    }
  }
  Bigint(string str) {
    s = 1; vl = 0;
    int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
      stPos = 1;
      s = -1;
    }
    for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
      num += (str[i] - '0') * q;
      if ((q *= 10) >= BIGMOD) {
        push_back(num);
        num = 0; q = 1;
      }
    }
    if (num) push_back(num);
  }
  int len() const { return vl; /* return SZ(v); */ }
  bool empty() const { return len() == 0; }
  void push_back(int x) { v[vl++] = x; /* v.PB(x); */ }
  void pop_back() { vl--; /* v.pop_back(); */ }
  int back() const { return v[vl-1]; /* return v.back()
    ; */ }
  void n() { while (!empty() && !back()) pop_back(); }
  void resize(int nl) {
    vl = nl; fill(v, v+vl, 0);
    //   v.resize(nl); // fill(ALL(v), 0);
  }
  void print() const {
    if (empty()) { putchar('0'); return; }
    if (s == -1) putchar('-');
    printf("%d", back());
    for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
  }
  friend std::ostream& operator << (std::ostream& out,
      const Bigint &a) {
    if (a.empty()) { out << "0"; return out; }
    if (a.s == -1) out << "-";
    out << a.back();
    for (int i=a.len()-2; i>=0; i--) {
      char str[10];
      snprintf(str, 5, "%.4d", a.v[i]);
      out << str;
    }
    return out;
  }
  int cp3(const Bigint &b)const {
    if (s != b.s) return s > b.s ? 1 : -1;
    if (s == -1) return -(-*this).cp3(-b);
    if (len() != b.len()) return len()>b.len()?1:-1;
    for (int i=len()-1; i>=0; i--)
      if (v[i]!=b.v[i]) return v[i]>b.v[i]?1:-1;
    return 0;
  }
  bool operator < (const Bigint &b)const{ return cp3(b)
      ==-1; }
  bool operator <= (const Bigint &b)const{ return cp3(b
      )<=0; }
  bool operator >= (const Bigint &b)const{ return cp3(b
      )>=0; }
  bool operator == (const Bigint &b)const{ return cp3(b
      )==0; }
  bool operator != (const Bigint &b)const{ return cp3(b
      )!=0; }
  bool operator > (const Bigint &b)const{ return cp3(b)
      ==1; }
  Bigint operator - () const {
    Bigint r = (*this);
    r.s = -r.s;
    return r;
  }
  Bigint operator + (const Bigint &b) const {
    if (s == -1) return -(-(*this)+(-b));
    if (b.s == -1) return (*this)-(-b);
    Bigint r;
    int nl = max(len(), b.len());
    r.resize(nl + 1);
    for (int i=0; i<nl; i++) {
      if (i < len()) r.v[i] += v[i];
      if (i < b.len()) r.v[i] += b.v[i];
      if(r.v[i] >= BIGMOD) {
        r.v[i+1] += r.v[i] / BIGMOD;
        r.v[i] %= BIGMOD;
      }
    }
    r.n();
    return r;
  }
  Bigint operator - (const Bigint &b) const {
    if (s == -1) return -(-(*this)-(-b));
    if (b.s == -1) return (*this)+(-b);
    if ((*this) < b) return -(b-(*this));
    Bigint r;
    r.resize(len());
    for (int i=0; i<len(); i++) {
      r.v[i] += v[i];
      if (i < b.len()) r.v[i] -= b.v[i];
      if (r.v[i] < 0) {
        r.v[i] += BIGMOD;
        r.v[i+1]--;
      }
    }
    r.n();
    return r;
  }
  Bigint operator * (const Bigint &b) {
    Bigint r;
    r.resize(len() + b.len() + 1);
    r.s = s * b.s;
    for (int i=0; i<len(); i++) {
      for (int j=0; j<b.len(); j++) {
        r.v[i+j] += v[i] * b.v[j];
        if(r.v[i+j] >= BIGMOD) {
          r.v[i+j+1] += r.v[i+j] / BIGMOD;
          r.v[i+j] %= BIGMOD;
        }
      }
    }
    r.n();
    return r;
  }
  Bigint operator / (const Bigint &b) {
    Bigint r;
    r.resize(max(1, len()-b.len()+1));
    int oriS = s;
    Bigint b2 = b; // b2 = abs(b)
    s = b2.s = r.s = 1;
    for (int i=r.len()-1; i>=0; i--) {
      int d=0, u=BIGMOD-1;
      while(d<u) {
        int m = (d+u+1)>>1;
        r.v[i] = m;
        if((r*b2) > (*this)) u = m-1;
        else d = m;
      }
      r.v[i] = d;
    }
    s = oriS;
    r.s = s * b.s;
    r.n();
    return r;
  }
  Bigint operator % (const Bigint &b) {
    return (*this)-(*this)/b*b;
  }
};
```

## 3.4  Linear Recurrence

```cpp
ll n, m;
ll dp[ N + N ];
void pre_dp(){
  dp[ 0 ] = 1;
  ll bdr = min( m + m , n );
  for( ll i = 1 ; i <= bdr ; i ++ )
    for( ll j = i - 1 ; j >= max( 0ll , i - m ) ; j --
        )
      dp[ i ] = add( dp[ i ] , dp[ j ] );
}
vector<ll> Mul( const vector<ll>& v1, const vector<ll>&
    v2 ){
  int _sz1 = (int)v1.size();
  int _sz2 = (int)v2.size();
  assert( _sz1 == m );
  assert( _sz2 == m );
  vector<ll> _v( m + m );
  for( int i = 0 ; i < m + m ; i ++ ) _v[ i ] = 0;
// expand
  for( int i = 0 ; i < _sz1 ; i ++ )
    for( int j = 0 ; j < _sz2 ; j ++ )
      _v[ i + j + 1 ] = add( _v[ i + j + 1 ] , mul( v1[
          i ] , v2[ j ] ) );
// shrink
  for( int i = 0 ; i < m ; i ++ )
    for( int j = 1 ; j <= m ; j ++ )
      _v[ i + j ] = add( _v[ i + j ] , _v[ i ] );
  for( int i = 0 ; i < m ; i ++ )
    _v[ i ] = _v[ i + m ];
  _v.resize( m );
  return _v;
}
vector<ll> I, A;
void solve(){
  pre_dp();
  if( n <= m + m ){
    printf( "%lld\n" , dp[ n ] );
    exit( 0 );
  }
  I.resize( m );
  A.resize( m );
  for( int i = 0 ; i < m ; i ++ ) I[ i ] = A[ i ] = 1;
// dp[ n ] = /Sum_{i=0}^{m-1} A_i * dp[ n - i - 1 ]
  ll dlt = ( n - m ) / m;
  ll rdlt = dlt * m;
  while( dlt ){
    if( dlt & 1ll ) I = Mul( I , A );
    A = Mul( A , A );
    dlt >>= 1;
  }
  ll ans = 0;
  for( int i = 0 ; i < m ; i ++ )
    ans = add( ans , mul( I[ i ] , dp[ n - i - 1 - rdlt
        ] ) );
  printf( "%lld\n" , ans );
}
```

## 3.5  Miller Rabin

```cpp
// n < 4,759,123,141        3 :  2, 7, 61
// n < 1,122,004,669,633    4 :  2, 13, 23, 1662803
// n < 3,474,749,660,383      6 :  pirmes <= 13
// n < 2^64                   7 :
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
ll power(ll x,ll p,ll mod){
  ll s=1,m=x;
  while(p) {
    if(p&1) s=mult(s,m,mod);
    p>>=1;
    m=mult(m,m,mod);
  }
  return s;
}
bool witness(ll a,ll n,ll u,int t){
  ll x=power(a,u,n);
  for(int i=0;i<t;i++) {
    ll nx=mult(x,x,n);
```

```cpp
    if(nx==1&&x!=1&&x!=n-1) return 1;
    x=nx;
  }
  return x!=1;
}
bool miller_rabin(ll n,int s=100) {
  // iterate s times of witness on n
  // return 1 if prime, 0 otherwise
  if(n<2) return 0;
  if(!(n&1)) return n==2;
  ll u=n-1;
  int t=0;
  // n-1 = u*2^t
  while(u&1) {
    u>>=1;
    t++;
  }
  while(s--) {
    ll a=randll()%(n-1)+1;
    if(witness(a,n,u,t)) return 0;
  }
  return 1;
}
```

## 3.6  Simplex

```cpp
const int maxn = 111;
const int maxm = 111;
const double eps = 1E-10;

double a[maxn][maxm], b[maxn], c[maxm], d[maxn][maxm];
double x[maxm];
int ix[maxn + maxm]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
//
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[maxn][maxm], double b[maxn],
    double c[maxm], int n, int m) {
  ++m;
  int r = n, s = m - 1;
  memset(d, 0, sizeof(d));
  for (int i = 0; i < n + m; ++i) ix[i] = i;
  for (int i = 0; i < n; ++i) {
    for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i
        ][j];
    d[i][m - 1] = 1;
    d[i][m] = b[i];
    if (d[r][m] > d[i][m]) r = i;
  }
  for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];
  d[n + 1][m - 1] = -1;
  for (double dd;; ) {
    if (r < n) {
      int t = ix[s]; ix[s] = ix[r + m]; ix[r + m]
          = t;
      d[r][s] = 1.0 / d[r][s];
      for (int j = 0; j <= m; ++j) if (j != s) d[
          r][j] *= -d[r][s];
      for (int i = 0; i <= n + 1; ++i) if (i != r
          ) {
        for (int j = 0; j <= m; ++j) if (j != s
            ) d[i][j] += d[r][j] * d[i][s];
        d[i][s] *= d[r][s];
      }
    }
    r = -1; s = -1;
    for (int j = 0; j < m; ++j) if (s < 0 || ix[s]
        > ix[j]) {
      if (d[n + 1][j] > eps || (d[n + 1][j] > -
          eps && d[n][j] > eps)) s = j;
    }
    if (s < 0) break;
    for (int i = 0; i < n; ++i) if (d[i][s] < -eps)
        {
      if (r < 0 || (dd = d[r][m] / d[r][s] - d[i
          ][m] / d[i][s]) < -eps || (dd < eps &&
          ix[r + m] > ix[i + m])) r = i;
```

```
        }
        if (r < 0) return -1; // not bounded
    }
    if (d[n + 1][m] < -eps) return -1; // not
        executable
    double ans = 0;
    for(int i=0; i<m; i++) x[i] = 0;
    for (int i = m; i < n + m; ++i) { // the missing
        enumerated x[i] = 0
        if (ix[i] < m - 1)
        {
            ans += d[i - m][m] * c[ix[i]];
            x[ix[i]] = d[i-m][m];
        }
    }
    return ans;
}
```

## 3.7  Faulhaber

```
/* faulhaber 's formula -
 * calculate power sum formula of all p=1~k in O(k^2)
    */
#define MAXK 2500
const int mod = 1000000007;
int b[MAXK];
// bernoulli number
int inv[MAXK+1];
// inverse
int cm[MAXK+1][MAXK+1]; // combinactories
int co[MAXK][MAXK+2];
// coeeficient of x^j when p=i
inline int add(int a,int b) { return a+b<mod?a+b:a+b-
    mod; }
inline int sub(int a,int b) { return a<b?a-b+mod:a-b; }
inline int getinv(int x) {
    int a=x,b=mod,a0=1,a1=0,b0=0,b1=1;
    while(b) {
        int q,t;
        q=a/b; t=b; b=a-b*q; a=t;
        t=b0; b0=a0-b0*q; a0=t;
        t=b1; b1=a1-b1*q; a1=t;
    }
    return a0<0?a0+mod:a0;
}
inline void pre() {
    /* combinational */
    for(int i=0;i<=MAXK;i++) {
        cm[i][0]=cm[i][i]=1;
        for(int j=1;j<i;j++) cm[i][j]=add(cm[i-1][j-1],cm[i
            -1][j]);
    }
    /* inverse */
    for(int i=1;i<=MAXK;i++) inv[i]=getinv(i);
    /* bernoulli */
    b[0]=1; b[1]=getinv(2); // with b[1] = 1/2
    for(int i=2;i<MAXK;i++) {
        if(i&1) { b[i]=0; continue; }
        b[i]=1;
        for(int j=0;j<i;j++)
            b[i]=sub(b[i],(long long)cm[i][j]*b[j]%mod*inv[i-
                j+1]%mod);
    }
    /* faulhaber */
    // sigma_x=1~n {x^p} = 1/(p+1) * sigma_j=0~p { C(p+1,
        j) * Bj * n^(p-j+1)}
    for(int i=1;i<MAXK;i++) {
        co[i][0]=0;
        for(int j=0;j<=i;j++)
            co[i][i-j+1]=(long long)inv[i+1]%mod*cm[i+1][j]%
                mod*b[j]%mod;
    }
}
inline int power(int x,int p) {
    int s=1,m=x;
    while(p) {
        if(p&1) s=(long long)s*m%mod;
        p>>=1; m=(long long)m*m%mod;
    }
    return s;
```

```
}
/* sample usage: return f(n,p) = sigma_x=1~n (x^p) */
inline int solve(int n,int p) {
    int sol=0,m=n;
    for(int i=1;i<=p+1;i++) {
        sol=add(sol,(long long)co[p][i]*m%mod);
        m=(long long)m*n%mod;
    }
    return sol;
}
```

## 3.8  Chinese Remainder

```
int pfn;
// number of distinct prime factors
int pf[MAXNUM]; // prime factor powers
int rem[MAXNUM]; // corresponding remainder
int pm[MAXNUM];
inline void generate_primes() {
    int i,j;
    pnum=1;
    prime[0]=2;
    for(i=3;i<MAXVAL;i+=2) {
        if(nprime[i]) continue;
        prime[pnum++]=i;
        for(j=i*i;j<MAXVAL;j+=i) nprime[j]=1;
    }
}
inline int inverse(int x,int p) {
    int q,tmp,a=x,b=p;
    int a0=1,a1=0,b0=0,b1=1;
    while(b) {
        q=a/b; tmp=b; b=a-b*q; a=tmp;
        tmp=b0; b0=a0-b0*q; a0=tmp;
        tmp=b1; b1=a1-b1*q; a1=tmp;
    }
    return a0;
}
inline void decompose_mod() {
    int i,p,t=mod;
    pfn=0;
    for(i=0;i<pnum&&prime[i]<=t;i++) {
        p=prime[i];
        if(t%p==0) {
            pf[pfn]=1;
            while(t%p==0) {
                t/=p;
                pf[pfn]*=p;
            }
            pfn++;
        }
    }
    if(t>1) pf[pfn++]=t;
}
inline int chinese_remainder() {
    int i,m,s=0;
    for(i=0;i<pfn;i++) {
        m=mod/pf[i];
        pm[i]=(long long)m*inverse(m,pf[i])%mod;
        s=(s+(long long)pm[i]*rem[i])%mod;
    }
    return s;
}
```

## 3.9  Pollard Rho

```
// does not work when n is prime
ll modit(ll x,ll mod) {
    if(x>=mod) x-=mod;
    //if(x<0) x+=mod;
    return x;
}
ll mult(ll x,ll y,ll mod) {
    ll s=0,m=x%mod;
    while(y) {
        if(y&1) s=modit(s+m,mod);
        y>>=1;
        m=modit(m+m,mod);
```

```
    }
    return s;
}
ll f(ll x,ll mod) {
    return modit(mult(x,x,mod)+1,mod);
}
ll pollard_rho(ll n) {
    if(!(n&1)) return 2;
    while (true) {
        ll y=2, x=rand()%(n-1)+1, res=1;
        for (int sz=2; res==1; sz*=2) {
            for (int i=0; i<sz && res<=1; i++) {
                x = f(x, n);
                res = __gcd(abs(x-y), n);
            }
            y = x;
        }
        if (res!=0 && res!=n) return res;
    }
}
```

### 3.10  ax+by=gcd

```
typedef pair<int, int> pii;
pii gcd(int a, int b){
    if(b == 0) return make_pair(1, 0);
    else{
        int p = a / b;
        pii q = gcd(b, a % b);
        return make_pair(q.second, q.first - q.second * p);
    }
}
```

### 3.11  Result

```
/*
Lucas ' Theorem:
  For non-negative integer n,m and prime P,
  C(m,n) mod P = C(m/M,n/M) * C(m%M,n%M) mod P
  = mult_i ( C(m_i,n_i) )
  where m_i is the i-th digit of m in base P.
--
Sum of Two Squares Thm (Legendre)
  For a given positive integer N, let
  D1 = (# of positive integers d dividing N that d=1(
      mod 4))
  D3 = (# of positive integers d dividing N that d=3(
      mod 4))
  then N can be written as a sum of two squares in
      exactly
  R(N) = 4(D1-D3) ways.
--
Difference of D1-D3 Thm
  let N = 2^t * [p1^e1 * ... * pr^er] * [q1^f1 * ... *
      qs^fs]
                 <- mod 4 = 1 prime ->   <- mod 4 = 3
                       prime ->
  then D1 - D3 = (e1+1)(e2+1)...(er+1) ... if (fi)s all
      even
                     0 ... if any fi is odd
*/


/*
* primes list
* 1097774749
* 1076767633
* 100102021
* 999997771
* 1001010013
* 1000512343
* 987654361
* 999991231
* 999888733
* 98789101
* 987777733
* 999991921
* 1010101333
```
```
* 1010102101
*/

Pick ' s Theorem
A = i + b/2 - 1
```

## 4  Geometry

### 4.1  halfPlaneIntersection

```cpp
#include<bits/stdc++.h>
#define N 100010
#define EPS 1e-8
#define SIDE 10000000
using namespace std;
struct PO{ double x , y ; } p[ N ], o ;
struct LI{
    PO a, b;
    double angle;
    void in( double x1 , double y1 , double x2 , double
        y2 ){
        a.x = x1 ; a.y = y1 ; b.x = x2 ; b.y = y2;
    }
}li[ N ] , deq[ N ];
int n , m , cnt;
inline int dc( double x ){
    if ( x > EPS ) return 1;
    else if ( x < -EPS ) return -1;
    return 0;
}
inline PO operator-( PO a, PO b ){
    PO c;
    c.x = a.x - b.x ; c.y = a.y - b.y;
    return c;
}
inline double cross( PO a , PO b , PO c ){
    return ( b.x - a.x ) * ( c.y - a.y ) - ( b.y - a.y )
        * ( c.x - a.x );
}
inline bool cmp( const LI &a , const LI &b ){
    if( dc( a.angle - b.angle ) == 0 ) return dc( cross(
        a.a , a.b , b.a ) ) < 0;
    return a.angle > b.angle;
}
inline PO getpoint( LI &a , LI &b ){
    double k1 = cross( a.a , b.b , b.a );
    double k2 = cross( a.b , b.a , b.b );
    PO tmp = a.b - a.a , ans;
    ans.x = a.a.x + tmp.x * k1 / ( k1 + k2 );
    ans.y = a.a.y + tmp.y * k1 / ( k1 + k2 );
    return ans;
}
inline void getcut(){
    sort( li + 1 , li + 1 + n , cmp ); m = 1;
    for( int i = 2 ; i <= n ; i ++ )
        if( dc( li[ i ].angle - li[ m ].angle ) != 0 )
            li[ ++ m ] = li[ i ];
    deq[ 1 ] = li[ 1 ]; deq[ 2 ] = li[ 2 ];
    int bot = 1 , top = 2;
    for( int i = 3 ; i <= m ; i ++ ){
        while( bot < top && dc( cross( li[ i ].a , li[ i ].
            b , getpoint( deq[ top ] , deq[ top - 1 ] ) ) )
             < 0 ) top -- ;
        while( bot < top && dc( cross( li[ i ].a , li[ i ].
            b , getpoint( deq[ bot ] , deq[ bot + 1 ] ) ) )
             < 0 ) bot ++ ;
        deq[ ++ top ] = li[ i ] ;
    }
    while( bot < top && dc( cross( deq[ bot ].a , deq[
        bot ].b , getpoint( deq[ top ] , deq[ top - 1 ] )
        ) ) < 0 ) top --;
    while( bot < top && dc( cross( deq[ top ].a , deq[
        top ].b , getpoint( deq[ bot ] , deq[ bot + 1 ] )
        ) ) < 0 ) bot ++;
    cnt = 0;
    if( bot == top ) return;
    for( int i = bot ; i < top ; i ++ ) p[ ++ cnt ] =
        getpoint( deq[ i ] , deq[ i + 1 ] );
```

```
  if( top - 1 > bot ) p[ ++ cnt ] = getpoint( deq[ bot
      ] , deq[ top ] );
}
double px[ N ] , py[ N ];
void read( int rm ) {
  for( int i = 1 ; i <= n ; i ++ ) px[ i + n ] = px[ i
      ] , py[ i + n ] = py[ i ];
  for( int i = 1 ; i <= n ; i ++ ){
    // half-plane from li[ i ].a -> li[ i ].b
    li[ i ].a.x = px[ i + rm + 1 ]; li[ i ].a.y = py[ i
        + rm + 1 ];
    li[ i ].b.x = px[ i ]; li[ i ].b.y = py[ i ];
    li[ i ].angle = atan2( li[ i ].b.y - li[ i ].a.y ,
        li[ i ].b.x - li[ i ].a.x ) ;
  }
}
inline double getarea( int rm ){
  read( rm ); getcut();
  double res = 0.0;
  p[ cnt + 1 ] = p[ 1 ];
  for( int i = 1 ; i <= cnt ; i ++ ) res += cross( o ,
      p[ i ] , p[ i + 1 ] ) ;
  if( res < 0.0 ) res *= -1.0;
  return res;
}
```

## 4.2  Convex Hull

```
double cross(Point o, Point a, Point b){
  return (a-o) % (b-o);
}
vector<Point> convex_hull(vector<Point> pt){
  sort(pt.begin(),pt.end());
  int top=0;
  vector<Point> stk(2*pt.size());
  for (int i=0; i<(int)pt.size(); i++){
    while (top >= 2 && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
    stk[top++] = pt[i];
  }
  for (int i=pt.size()-2, t=top+1; i>=0; i--){
    while (top >= t && cross(stk[top-2],stk[top-1],pt[i
        ]) <= 0)
      top--;
    stk[top++] = pt[i];
  }
  stk.resize(top-1);
  return stk;
}
```

## 4.3  Intersection of 2 lines

```
const double EPS = 1e-9;
pdd interPnt(pdd p1, pdd p2, pdd q1, pdd q2){
  double f1 = (p2 - p1) ^ (q1 - p1); // cross
  double f2 = (p2 - p1) ^ (p1 - q2); // cross
  double f = (f1 + f2);
  if(fabs(f) < EPS) return pdd(nan(""), nan(""));
  return (f2 / f) * q1 + (f1 / f) * q2;
}
```

## 4.4  KD Tree

```
const int MXN = 100005;

struct KDTree {
  struct Node {
    int x,y,x1,y1,x2,y2;
    int id,f;
    Node *L, *R;
  }tree[MXN];
  int n;
  Node *root;

  long long dis2(int x1, int y1, int x2, int y2) {
```

```
    long long dx = x1-x2;
    long long dy = y1-y2;
    return dx*dx+dy*dy;
  }
  static bool cmpx(Node& a, Node& b){ return a.x<b.x; }
  static bool cmpy(Node& a, Node& b){ return a.y<b.y; }
  void init(vector<pair<int,int>> ip) {
    n = ip.size();
    for (int i=0; i<n; i++) {
      tree[i].id = i;
      tree[i].x = ip[i].first;
      tree[i].y = ip[i].second;
    }
    root = build_tree(0, n-1, 0);
  }
  Node* build_tree(int L, int R, int dep) {
    if (L>R) return nullptr;
    int M = (L+R)/2;
    tree[M].f = dep%2;
    nth_element(tree+L, tree+M, tree+R+1, tree[M].f ?
        cmpy : cmpx);
    tree[M].x1 = tree[M].x2 = tree[M].x;
    tree[M].y1 = tree[M].y2 = tree[M].y;

    tree[M].L = build_tree(L, M-1, dep+1);
    if (tree[M].L) {
      tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
    }

    tree[M].R = build_tree(M+1, R, dep+1);
    if (tree[M].R) {
      tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
    }

    return tree+M;
  }
  int touch(Node* r, int x, int y, long long d2){
    long long dis = sqrt(d2)+1;
    if (x<r->x1-dis || x>r->x2+dis || y<r->y1-dis || y>
        r->y2+dis)
      return 0;
    return 1;
  }
  void nearest(Node* r, int x, int y, int &mID, long
      long &md2) {
    if (!r || !touch(r, x, y, md2)) return;
    long long d2 = dis2(r->x, r->y, x, y);
    if (d2 < md2 || (d2 == md2 && mID < r->id)) {
      mID = r->id;
      md2 = d2;
    }
    // search order depends on split dim
    if ((r->f == 0 && x < r->x) ||
        (r->f == 1 && y < r->y)) {
      nearest(r->L, x, y, mID, md2);
      nearest(r->R, x, y, mID, md2);
    } else {
      nearest(r->R, x, y, mID, md2);
      nearest(r->L, x, y, mID, md2);
    }
  }
  int query(int x, int y) {
    int id = 1029384756;
    long long d2 = 102938475612345678LL;
    nearest(root, x, y, id, d2);
    return id;
  }
}tree;
```

## 4.5  Poly Union

```cpp
#define EPS 1E-8
class PT{ public: double x,y; };
class PY{ public:
  int n;
  PT pt[5];
  PT& operator[](const int x){ return pt[x]; }
  void input(){
    int i; n=4;
    for(i=0;i<n;i++) scanf("%lf %lf",&pt[i].x,&pt[i].y)
      ;
  }
  double getArea(){
    int i; double s=pt[n-1]^pt[0];
    for(i=0;i<n-1;i++) s+=pt[i]^pt[i+1];
    return s/2;
  }
};
PY py[500];
pair<double,int> c[5000];
inline double segP(PT &p,PT &p1,PT &p2){
  if(SG(p1.x-p2.x)==0) return (p.y-p1.y)/(p2.y-p1.y);
  return (p.x-p1.x)/(p2.x-p1.x);
}
double polyUnion(int n){
  int i,j,ii,jj,ta,tb,r,d;
  double z,w,s,sum,tc,td;
  for(i=0;i<n;i++) py[i][py[i].n]=py[i][0];
  sum=0;
  for(i=0;i<n;i++){
    for(ii=0;ii<py[i].n;ii++){
      r=0;
      c[r++]=make_pair(0.0,0);
      c[r++]=make_pair(1.0,0);
      for(j=0;j<n;j++){
        if(i==j) continue;
        for(jj=0;jj<py[j].n;jj++){
          ta=SG(tri(py[i][ii],py[i][ii+1],py[j][jj
            ]));
          tb=SG(tri(py[i][ii],py[i][ii+1],py[j][jj
            +1]));
          if(ta==0 && tb==0){
            if((py[j][jj+1]-py[j][jj])*(py[i][ii
                +1]-py[i][ii])>0 && j<i){
              c[r++]=make_pair(segP(py[j][jj],
                  py[i][ii],py[i][ii+1]),1);
              c[r++]=make_pair(segP(py[j][jj
                  +1],py[i][ii],py[i][ii+1])
                  ,-1);
            }
          }else if(ta>=0 && tb<0){
            tc=tri(py[j][jj],py[j][jj+1],py[i][
              ii]);
            td=tri(py[j][jj],py[j][jj+1],py[i][
              ii+1]);
            c[r++]=make_pair(tc/(tc-td),1);
          }else if(ta<0 && tb>=0){
            tc=tri(py[j][jj],py[j][jj+1],py[i][
              ii]);
            td=tri(py[j][jj],py[j][jj+1],py[i][
              ii+1]);
            c[r++]=make_pair(tc/(tc-td),-1);
          }
        }
      }
      sort(c,c+r);
      z=min(max(c[0].first,0.0),1.0);
      d=c[0].second; s=0;
      for(j=1;j<r;j++){
        w=min(max(c[j].first,0.0),1.0);
        if(!d) s+=w-z;
        d+=c[j].second; z=w;
      }
      sum+=(py[i][ii]^py[i][ii+1])*s;
    }
  }
  return sum/2;
}
int main(){
  int n,i,j,k;
  double sum,ds;
  scanf("%d",&n); sum=0;
  for(i=0;i<n;i++){
    py[i].input();
    ds=py[i].getArea();
    if(ds<0){
      for(j=0,k=py[i].n-1;j<k;j++,k--) swap(py[i][j],
          py[i][k]);
      ds=-ds;
    } sum+=ds;
  } printf("%.9f\n",sum/polyUnion(n));
}
```

## 4.6  Lower Concave Hull

```cpp
/****
  maintain a "concave hull" that support the following
  1. insertion of a line
  2. query of height(y) on specific x on the hull
 ****/
/* set as needed */
const long double eps=1e-9;
const long double inf=1e19;
class Segment {
 public:
  long double m,c,x1,x2; // y=mx+c
  bool flag;
  Segment(long double _m,long double _c,long double _x1
      =-inf,long double _x2=inf,bool _flag=0)
    :m(_m),c(_c),x1(_x1),x2(_x2),flag(_flag) {}
  long double evaly(long double x) const {
    return m*x+c;
  }
  const bool operator<(long double x) const {
    return x2-eps<x;
  }
  const bool operator<(const Segment &b) const {
    if(flag||b.flag) return *this<b.x1;
    return m+eps<b.m;
  }
};
class LowerConcaveHull { // maintain a hull like: \__/
 public:
  set<Segment> hull;
  /* functions */
  long double xintersection(Segment a,Segment b) {
    return (a.c-b.c)/(b.m-a.m);
  }
  inline set<Segment>::iterator replace(set<Segment> &
      hull,set<Segment>::iterator it,Segment s) {
    hull.erase(it);
    return hull.insert(s).first;
  }
  void insert(Segment s) { // insert a line and update
      hull
    set<Segment>::iterator it=hull.find(s);
    // check for same slope
    if(it!=hull.end()) {
      if(it->c+eps>=s.c) return;
      hull.erase(it);
    }
    // check if below whole hull
    it=hull.lower_bound(s);
    if(it!=hull.end()&&s.evaly(it->x1)<=it->evaly(it->
        x1)+eps) return;
    // update right hull
    while(it!=hull.end()) {
      long double x=xintersection(s,*it);
      if(x>=it->x2-eps) hull.erase(it++);
      else {
        s.x2=x;
        it=replace(hull,it,Segment(it->m,it->c,x,it->x2
            ));
        break;
      }
    }
    // update left hull
    while(it!=hull.begin()) {
      long double x=xintersection(s,*(--it));
      if(x<=it->x1+eps) hull.erase(it++);
```

```cpp
      else {
        s.x1=x;
        it=replace(hull,it,Segment(it->m,it->c,it->x1,x
            ));
        break;
      }
    }
    // insert s
    hull.insert(s);
  }
  void insert(long double m,long double c) { insert(
      Segment(m,c)); }
  long double query(long double x) { // return y @
      given x
    set<Segment>::iterator it=hull.lower_bound(
        Segment(0.0,0.0,x,x,1));
    return it->evaly(x);
  }
};
```

## 4.7  MCC

```cpp
struct Mcc{
  // return pair of center and r^2
  static const int MAXN = 1000100;
  int n;
  Point p[MAXN],cen;
  double r2;
  void init(int _n, Point _p[]){
    n = _n;
    memcpy(p,_p,sizeof(Point)*n);
  }
  double sqr(double a){ return a*a; }
  Point center(Point p0, Point p1, Point p2) {
    Point a = p1-p0;
    Point b = p2-p0;
    double c1=a.len2()*0.5;
    double c2=b.len2()*0.5;
    double d = a % b;
    double x = p0.x + (c1 * b.y - c2 * a.y) / d;
    double y = p0.y + (a.x * c2 - b.x * c1) / d;
    return Point(x,y);
  }
  pair<Point,double> solve(){
    random_shuffle(p,p+n);
    r2=0;
    for (int i=0; i<n; i++){
      if ((cen-p[i]).len2() <= r2) continue;
      cen = p[i];
      r2 = 0;
      for (int j=0; j<i; j++){
        if ((cen-p[j]).len2() <= r2) continue;
        cen = Point((p[i].x+p[j].x)*0.5, (p[i].y+p[j].y
            )*0.5);
        r2 = (cen-p[j]).len2();
        for (int k=0; k<j; k++){
          if ((cen-p[k]).len2() <= r2) continue;
          cen = center(p[i],p[j],p[k]);
          r2 = (cen-p[k]).len2();
        }
      }
    }
    return {cen,r2};
  }
}mcc;
```

## 4.8  Minkowski sum

```cpp
/* convex hull Minkowski Sum*/
#define INF 100000000000000LL
class PT{ public:
  long long x,y;
  int POS(){
    if(y==0) return x>0?0:1;
    return y>0?0:1;
  }
};
PT pt[300000],qt[300000],rt[300000];
```

```cpp
long long Lx,Rx;
int dn,un;
inline bool cmp(PT a,PT b){
  int pa=a.POS(),pb=b.POS();
  if(pa==pb) return (a^b)>0;
  return pa<pb;
}
int minkowskiSum(int n,int m){
  int i,j,r,p,q,fi,fj;
  for(i=1,p=0;i<n;i++){
    if(pt[i].y<pt[p].y || (pt[i].y==pt[p].y && pt[i].x<
        pt[p].x)) p=i; }
  for(i=1,q=0;i<m;i++){
    if(qt[i].y<qt[q].y || (qt[i].y==qt[q].y && qt[i].x<
        qt[q].x)) q=i; }
  rt[0]=pt[p]+qt[q];
  r=1; i=p; j=q; fi=fj=0;
  while(1){
    if((fj&&j==q) || ((!fi||i!=p) && cmp(pt[(p+1)%n]-pt
        [
          p],qt[(q+1)%m]-qt[q]))){
      rt[r]=rt[r-1]+pt[(p+1)%n]-pt[p];
      p=(p+1)%n;
      fi=1;
    }else{
      rt[r]=rt[r-1]+qt[(q+1)%m]-qt[q];
      q=(q+1)%m;
      fj=1;
    }
    if(r<=1 || ((rt[r]-rt[r-1])^(rt[r-1]-rt[r-2]))!=0)
        r
      ++;
    else rt[r-1]=rt[r];
    if(i==p && j==q) break;
  }
  return r-1;
}
void initInConvex(int n){
  int i,p,q;
  long long Ly,Ry;
  Lx=INF; Rx=-INF;
  for(i=0;i<n;i++){
    if(pt[i].x<Lx) Lx=pt[i].x;
    if(pt[i].x>Rx) Rx=pt[i].x;
  }
  Ly=Ry=INF;
  for(i=0;i<n;i++){
    if(pt[i].x==Lx && pt[i].y<Ly){ Ly=pt[i].y; p=i; }
    if(pt[i].x==Rx && pt[i].y<Ry){ Ry=pt[i].y; q=i; }
  }
  for(dn=0,i=p;i!=q;i=(i+1)%n){ qt[dn++]=pt[i]; }
  qt[dn]=pt[q]; Ly=Ry=-INF;
  for(i=0;i<n;i++){
    if(pt[i].x==Lx && pt[i].y>Ly){ Ly=pt[i].y; p=i; }
    if(pt[i].x==Rx && pt[i].y>Ry){ Ry=pt[i].y; q=i; }
  }
  for(un=0,i=p;i!=q;i=(i+n-1)%n){ rt[un++]=pt[i]; }
  rt[un]=pt[q];
}
inline int inConvex(PT p){
  int L,R,M;
  if(p.x<Lx || p.x>Rx) return 0;
  L=0;R=dn;
  while(L<R-1){ M=(L+R)/2;
    if(p.x<qt[M].x) R=M; else L=M; }
  if(tri(qt[L],qt[R],p)<0) return 0;
  L=0;R=un;
  while(L<R-1){ M=(L+R)/2;
    if(p.x<rt[M].x) R=M; else L=M; }
  if(tri(rt[L],rt[R],p)>0) return 0;
  return 1;
}
int main(){
  int n,m,i;
  PT p;
  scanf("%d",&n);
  for(i=0;i<n;i++) scanf("%I64d %I64d",&pt[i].x,&pt[i].
      y);
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%I64d %I64d",&qt[i].x,&qt[i].
      y);
  n=minkowskiSum(n,m);
```

```
  for(i=0;i<n;i++) pt[i]=rt[i];
  scanf("%d",&m);
  for(i=0;i<m;i++) scanf("%I64d %I64d",&qt[i].x,&qt[i].
      y);
  n=minkowskiSum(n,m);
  for(i=0;i<n;i++) pt[i]=rt[i];
  initInConvex(n);
  scanf("%d",&m);
  for(i=0;i<m;i++){
    scanf("%I64d %I64d",&p.x,&p.y);
    p.x*=3; p.y*=3;
    puts(inConvex(p)?"YES":"NO");
  }
}
```

## 4.9  Min Enclosing Circle

```
/* minimum enclosing circle */
int n;
Coor p[MAXNUM];
const Circle circumcircle(Coor a,Coor b,Coor c){
  Circle cir;
  double fa,fb,fc,fd,fe,ff,dx,dy,dd;
  if(iszero(cross(a,b,c))) {
    if(dot(a,b,c)<=0) return Circle((b+c)/2,(b-c).len()
        /2)
        ;
    if(dot(b,c,a)<=0) return Circle((c+a)/2,(c-a).len()
        /2)
        ;
    if(dot(c,a,b)<=0) return Circle((a+b)/2,(a-b).len()
        /2)
        ;
  } else {
    fa=2*(a.x-b.x);
    fb=2*(a.y-b.y);
    fc=a.len2()-b.len2();
    fd=2*(a.x-c.x);
    fe=2*(a.y-c.y);
    ff=a.len2()-c.len2();
    dx=fc*fe-ff*fb;
    dy=fa*ff-fd*fc;
    dd=fa*fe-fd*fb;
    cir.o=Coor(dx/dd,dy/dd);
    cir.r=(a-cir.o).len();
    return cir;
  }
}
inline Circle mec(int fixed,int num){
  int i;
  Circle cir;
  if(fixed==3) return circumcircle(p[0],p[1],p[2]);
  cir=circumcircle(p[0],p[0],p[1]);
  for(i=fixed;i<num;i++) {
    if(cir.inside(p[i])) continue;
    swap(p[i],p[fixed]);
    cir=mec(fixed+1,i+1);
  }
  return cir;
}
inline double min_radius() {
  if(n<=1) return 0.0;
  if(n==2) return (p[0]-p[1]).len()/2;
  scramble();
  return mec(0,n).r;
}
```

## 4.10  Min/Max Enclosing Rectangle

```
/******* NEED REVISION *******/
/* uva819 - gifts large and small */
#define MAXNUM 100005
const double eps=1e-8;
const double inf=1e15;
class Coor {
 public:
  double x,y;
  Coor() {}
```

```
  Coor(double xi,double yi) { x=xi; y=yi; }
  Coor& operator+=(const Coor &b) { x+=b.x; y+=b.y;
      return *this; }
  const Coor operator+(const Coor &b) const { return (
      Coor)*this+=b; }
  Coor& operator-=(const Coor &b) { x-=b.x; y-=b.y;
      return *this; }
  const Coor operator-(const Coor &b) const { return (
      Coor)*this-=b; }
  Coor& operator*=(const double b) { x*=b; y*=b; return
       *this; }
  const Coor operator*(const double b) const { return (
      Coor)*this*=b; }
  Coor& operator/=(const double b) { x/=b; y/=b; return
       *this; }
  const Coor operator/(const double b) const { return (
      Coor)*this/=b; }
  const bool operator<(const Coor& b) const { return y<
      b.y-eps||fabs(y-b.y)<eps&&x<b.x; }
  const double len2() const { return x*x+y*y; }
  const double len() const { return sqrt(len2()); }
  const Coor perp() const { return Coor(y,-x); }
  Coor& standardize() {
    if(y<0||y==0&&x<0) {
      x=-x;
      y=-y;
    }
    return *this;
  }
  const Coor standardize() const { return ((Coor)*this)
      .standardize(); }
};
double dot(const Coor &a,const Coor &b) { return a.x*b.
    x+a.y*b.y; }
double dot(const Coor &o,const Coor &a,const Coor &b) {
    return dot(a-o,b-o); }
double cross(const Coor &a,const Coor &b) { return a.x*
    b.y-a.y*b.x; }
double cross(const Coor &o,const Coor &a,const Coor &b)
    { return cross(a-o,b-o); }
Coor cmpo;
const bool cmpf(const Coor &a,const Coor &b) {
  return cross(cmpo,a,b)>eps||fabs(cross(cmpo,a,b))<eps
      &&
    dot(a,cmpo,b)<-eps;
}
class Polygon {
 public:
  int pn;
  Coor p[MAXNUM];
  void convex_hull() {
    int i,tn=pn;
    for(i=1;i<pn;++i) if(p[i]<p[0]) swap(p[0],p[i]);
    cmpo=p[0];
    std::sort(p+1,p+pn,cmpf);
    for(i=pn=1;i<tn;++i) {
      while(pn>2&&cross(p[pn-2],p[pn-1],p[i])<=eps) --
          pn;
      p[pn++]=p[i];
    }
    p[pn]=p[0];
  }
};
Polygon pol;
double minarea,maxarea;
int slpn;
Coor slope[MAXNUM*2];
Coor lrec[MAXNUM*2],rrec[MAXNUM*2],trec[MAXNUM*2],brec[
    MAXNUM*2];
inline double xproject(Coor p,Coor slp) { return dot(p,
    slp)/slp.len(); }
inline double yproject(Coor p,Coor slp) { return cross(
    p,slp)/slp.len(); }
inline double calcarea(Coor lp,Coor rp,Coor bp,Coor tp,
    Coor slp) {
  return (xproject(rp,slp)-xproject(lp,slp))*(yproject(
      tp,slp)-yproject(bp,slp)); }
inline void solve(){
  int i,lind,rind,tind,bind,tn;
  double pro,area1,area2,l,r,m1,m2;
  Coor s1,s2;
  pol.convex_hull();
```

```
    slpn=0; /* generate all critical slope */
    slope[slpn++]=Coor(1.0,0.0);
    slope[slpn++]=Coor(0.0,1.0);
    for(i=0;i<pol.pn;i++) {
      slope[slpn]=(pol.p[i+1]-pol.p[i]).standardize();
      if(slope[slpn].x>0) slpn++;
      slope[slpn]=(pol.p[i+1]-pol.p[i]).perp().
        standardize();
      if(slope[slpn].x>0) slpn++;
    }
    cmpo=Coor(0,0);
    std::sort(slope,slope+slpn,cmpf);
    tn=slpn;
    for(i=slpn=1;i<tn;i++)
      if(cross(cmpo,slope[i-1],slope[i])>0) slope[slpn
        ++]=slope[i];
    lind=rind=0; /* find critical touchpoints */
    for(i=0;i<pol.pn;i++) {
      pro=xproject(pol.p[i],slope[0]);
      if(pro<xproject(pol.p[lind],slope[0])) lind=i;
      if(pro>xproject(pol.p[rind],slope[0])) rind=i;
    }
    tind=bind=0;
    for(i=0;i<pol.pn;i++) {
      pro=yproject(pol.p[i],slope[0]);
      if(pro<yproject(pol.p[bind],slope[0])) bind=i;
      if(pro>yproject(pol.p[tind],slope[0])) tind=i;
    }
    for(i=0;i<slpn;i++) {
      while(xproject(pol.p[lind+1],slope[i])<=xproject(
          pol.p[lind],slope[i])+eps)
        lind=(lind==pol.pn-1?0:lind+1);
      while(xproject(pol.p[rind+1],slope[i])>=xproject(
          pol.p[rind],slope[i])-eps)
        rind=(rind==pol.pn-1?0:rind+1);
      while(yproject(pol.p[bind+1],slope[i])<=yproject(
          pol.p[bind],slope[i])+eps)
        bind=(bind==pol.pn-1?0:bind+1);
      while(yproject(pol.p[tind+1],slope[i])>=yproject(
          pol.p[tind],slope[i])-eps)
        tind=(tind==pol.pn-1?0:tind+1);
      lrec[i]=pol.p[lind];
      rrec[i]=pol.p[rind];
      brec[i]=pol.p[bind];
      trec[i]=pol.p[tind];
    }
    minarea=inf; /* find minimum area */
    for(i=0;i<slpn;i++) {
      area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],
          slope[i]);
      if(area1<minarea) minarea=area1;
    }
    maxarea=minarea; /* find maximum area */
    for(i=0;i<slpn-1;i++) {
      l=0.0; r=1.0;
      while(l<r-eps) {
        m1=l+(r-l)/3;
        m2=l+(r-l)*2/3;
        s1=slope[i]*(1.0-m1)+slope[i+1]*m1;
        area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],
            s1);
        s2=slope[i]*(1.0-m2)+slope[i+1]*m2;
        area2=calcarea(lrec[i],rrec[i],brec[i],trec[i],
            s2);
        if(area1<area2) l=m1;
        else r=m2;
      }
      s1=slope[i]*(1.0-l)+slope[i+1]*l;
      area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],s1
          );
      if(area1>maxarea) maxarea=area1;
    }
  }
}
int main(){
  int i,casenum=1;
  while(scanf("%d",&pol.pn)==1&&pol.pn) {
    for(i=0;i<pol.pn;i++)
      scanf("%lf %lf",&pol.p[i].x,&pol.p[i].y);
    solve();
    //minarea, maxarea
  }
}
```

# 5 Graph

## 5.1 HeavyLightDecomp

```cpp
#include <bits/stdc++.h>
using namespace std;
#define SZ(c) (int)(c).size()
#define ALL(c) (c).begin(), (c).end()
#define REP(i, s, e) for(int i = (s); i <= (e); i++)
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
typedef tuple< int , int > tii;

const int MAXN = 100010;
const int LOG  = 19;

struct HLD
{
  int n;
  vector<int> g[MAXN];
  int sz[MAXN], dep[MAXN];
  int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
  // ts : timestamp , useless after yutruli
  // tid[ u ] : pos. of node u in the seq.
  // tdi[ i ] : node at pos i of the seq.
  // tl , tr[ u ] : subtree interval in the seq. of
  //     node u
  int mom[MAXN][LOG], head[MAXN];
  // head[ u ] : head of the chain contains u
  void dfssz(int u, int p){
    dep[u] = dep[p] + 1;
    mom[u][0] = p;
    sz[u] = 1;
    head[u] = u;
    for(int& v:g[u]) if(v != p){
      dep[v] = dep[u] + 1;
      dfssz(v, u);
      sz[u] += sz[v];
    }
  }
  void dfshl(int u){
    //printf("dfshl %d\n", u);
    ts++;
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
    sort(ALL(g[u]), [&](int a, int b){return sz[a] > sz
        [b];});
    bool flag = 1;
    for(int& v:g[u]) if(v != mom[u][0]){
      if(flag) head[v] = head[u], flag = 0;
      dfshl(v);
      tr[u] = tr[v];
    }
  }
  inline int lca(int a, int b){
    if(dep[a] > dep[b]) swap(a, b);
    //printf("lca %d %d\n", a, b);
    int diff = dep[b] - dep[a];
    REPD(k, LOG-1, 0) if(diff & (1<<k)){
      //printf("b %d\n", mom[b][k]);
      b = mom[b][k];
    }
    if(a == b) return a;
    REPD(k, LOG-1, 0) if(mom[a][k] != mom[b][k]){
      a = mom[a][k];
      b = mom[b][k];
    }
    return mom[a][0];
  }
  void init( int _n ){
    n = _n;
    REP( i , 1 , n ) g[ i ].clear();
  }
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
    g[ v ].push_back( u );
  }
  void yutruli(){
    dfssz(1, 0);
    ts = 0;
    dfshl(1);
```

```
    REP(k, 1, LOG-1) REP(i, 1, n)
      mom[i][k] = mom[mom[i][k-1]][k-1];
  }
  vector< tii > getPath( int u , int v ){
    vector< tii > res;
    while( tid[ u ] < tid[ head[ v ] ] ){
      res.push_back( tii( tid[ head[ v ] ] , tid[ v ] )
          );
      v = mom[ head[ v ] ][ 0 ];
    }
    res.push_back( tii( tid[ u ] , tid[ v ] ) );
    reverse( ALL( res ) );
    return res;
    /*
     * res : list of intervals from u to v
     * u must be ancestor of v
     * usage :
     * vector< tii >& path = tree.getPath( u , v )
     * for( tii tp : path ) {
     *   int l , r;tie( l , r ) = tp;
     *   upd( l , r );
     *   uu = tree.tdi[ l ] , vv = tree.tdi[ r ];
     *   uu ~> vv is a heavy path on tree
     * }
     */
  }
} tree;
```

## 5.2  DominatorTree

```
const int MAXN = 100010;
struct DominatorTree{
#define REP(i,s,e) for(int i=(s);i<=(e);i++)
#define REPD(i,s,e) for(int i=(s);i>=(e);i--)
  int n , m , s;
  vector< int > g[ MAXN ] , pred[ MAXN ];
  vector< int > cov[ MAXN ];
  int dfn[ MAXN ] , nfd[ MAXN ] , ts;
  int par[ MAXN ];
  int sdom[ MAXN ] , idom[ MAXN ];
  int mom[ MAXN ] , mn[ MAXN ];

  inline bool cmp( int u , int v )
  { return dfn[ u ] < dfn[ v ]; }

  int eval( int u ){
    if( mom[ u ] == u ) return u;
    int res = eval( mom[ u ] );
    if( cmp( sdom[ mn[ mom[ u ] ] ] , sdom[ mn[ u ] ] )
        )
      mn[ u ] = mn[ mom[ u ] ];
    return mom[ u ] = res;
  }

  void init( int _n , int _m , int _s ){
    ts = 0; n = _n; m = _m; s = _s;
    REP( i , 1 , n ) g[ i ].clear() , pred[ i ].clear()
        ;
  }
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
    pred[ v ].push_back( u );
  }
  void dfs( int u ){
    ts++;
    dfn[ u ] = ts;
    nfd[ ts ] = u;
    for( int v : g[ u ] ) if( dfn[ v ] == 0 ){
      par[ v ] = u;
      dfs( v );
    }
  }
  void build(){
    REP( i , 1 , n ){
      dfn[ i ] = nfd[ i ] = 0;
      cov[ i ].clear();
      mom[ i ] = mn[ i ] = sdom[ i ] = i;
    }
    dfs( s );
    REPD( i , n , 2 ){
```

```
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      for( int v : pred[ u ] ) if( dfn[ v ] ){
        eval( v );
        if( cmp( sdom[ mn[ v ] ] , sdom[ u ] ) ) sdom[
            u ] = sdom[ mn[ v ] ];
      }
      cov[ sdom[ u ] ].push_back( u );
      mom[ u ] = par[ u ];
      for( int w : cov[ par[ u ] ] ){
        eval( w );
        if( cmp( sdom[ mn[ w ] ] , par[ u ] ) ) idom[ w
            ] = mn[ w ];
        else idom[ w ] = par[ u ];
      }
      cov[ par[ u ] ].clear();
    }
    REP( i , 2 , n ){
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      if( idom[ u ] != sdom[ u ] ) idom[ u ] = idom[
          idom[ u ] ];
    }
  }
} domT;
```

## 5.3  generalWeightedGraphMaxmatching

```
#include <bits/stdc++.h>
using namespace std;
#define N 110
#define inf 0x3f3f3f3f
int G[ N ][ N ] , ID[ N ];
int match[ N ] , stk[ N ];
int vis[ N ] , dis[ N ];
int n , m , k , top;
bool SPFA( int u ){
  stk[ top ++ ] = u;
  if( vis[ u ] ) return true;
  vis[ u ] = true;
  for( int i = 1 ; i <= k ; i ++ ){
    if( i != u && i != match[ u ] && !vis[ i ] ){
      int v = match[ i ];
      if( dis[ v ] < dis[ u ] + G[ u ][ i ] - G[ i ][ v
          ] ){
        dis[ v ] = dis[ u ] + G[ u ][ i ] - G[ i ][ v
            ];
        if( SPFA( v ) ) return true;
      }
    }
  }
  top --; vis[ u ] = false;
  return false;
}
int MaxWeightMatch() {
  for( int i = 1 ; i <= k ; i ++ ) ID[ i ] = i;
  for( int i = 1 ; i <= k ; i += 2 ) match[ i ] = i + 1
      , match[ i + 1 ] = i;
  for( int times = 0 , flag ; times < 3 ; ){
    memset( dis , 0 , sizeof( dis ) );
    memset( vis , 0 , sizeof( vis ) );
    top = 0; flag = 0;
    for( int i = 1 ; i <= k ; i ++ ){
      if( SPFA( ID[ i ] ) ){
        flag = 1;
        int t = match[ stk[ top - 1 ] ] , j = top - 2;
        while( stk[ j ] != stk[ top - 1 ] ){
          match[ t ] = stk[ j ];
          swap( t , match[ stk[ j ] ] );
          j --;
        }
        match[ t ] = stk[ j ]; match[ stk[ j ] ] = t;
        break;
      }
    }
    if( !flag ) times ++;
    if( !flag ) random_shuffle( ID + 1 , ID + k + 1 );
  }
  int ret = 0;
  for( int i = 1 ; i <= k ; i ++ )
```

```cpp
      if( i < match[ i ] ) ret += G[ i ][ match[ i ] ];
    return ret;
}
int main(){
  int T; scanf("%d", &T);
  for ( int cs = 1 ; cs <= T ; cs ++ ){
    scanf( "%d%d%d" , &n , &m , &k );
    memset( G , 0x3f , sizeof( G ) );
    for( int i = 1 ; i <= n ; i ++ ) G[ i ][ i ] = 0;
    for( int i = 0 ; i < m ; i ++ ){
      int u, v, w;
            scanf( "%d%d%d" , &u , &v , &w );
      G[ u ][ v ] = G[ v ][ u ] = w;
    }
    printf( "Case %d: " , cs );
    if( k & 1 ){
      puts( "Impossible" );
      continue;
    }
    for( int tk = 1; tk <= n ; tk ++ )
      for( int i = 1 ; i <= n ; i ++ )
        for( int j = 1 ; j <= n ; j ++ )
          G[ i ][ j ] = min( G[ i ][ j ] , G[ i ][ tk ]
                  + G[ tk ][ j ] );
    for( int i = 1 ; i <= k ; i ++ ){
      for( int j = 1 ; j <= k ; j ++ )
        G[ i ][ j ] = -G[ i ][ j ];
      G[ i ][ i ] = -inf;
    }
    printf( "%d\n" , -MaxWeightMatch() );
  }
}
```

## 5.4  MaxClique

```cpp
// max N = 64
typedef unsigned long long ll;
struct MaxClique{
  ll nb[ N ] , n , ans;
  void init( ll _n ){
    n = _n;
    for( int i = 0 ; i < n ; i ++ ) nb[ i ] = 0LLU;
  }
  void add_edge( ll _u , ll _v ){
    nb[ _u ] |= ( 1LLU << _v );
    nb[ _v ] |= ( 1LLU << _u );
  }
  void B( ll r , ll p , ll x , ll cnt , ll res ){
    if( cnt + res < ans ) return;
    if( p == 0LLU && x == 0LLU ){
      if( cnt > ans ) ans = cnt;
      return;
    }
    ll y = p | x; y &= -y;
    ll q = p & ( ~nb[ int( log2( y ) ) ] );
    while( q ){
      ll i = int( log2( q & (-q) ) );
      B( r | ( 1LLU << i ) , p & nb[ i ] , x & nb[ i ]
          , cnt + 1LLU , __builtin_popcountll( p & nb[
            i ] ) );
      q &= ~( 1LLU << i );
      p &= ~( 1LLU << i );
      x |= ( 1LLU << i );
    }
  }
  int solve(){
    ans = 0;
    ll _set = 0;
    if( n < 64 ) _set = ( 1LLU << n ) - 1;
    else{
      for( ll i = 0 ; i < n ; i ++ ) _set |= ( 1LLU <<
          i );
    }
    B( 0LLU , _set , 0LLU , 0LLU , n );
    return ans;
  }
}maxClique;

class MaxClique {
public:
```

```cpp
  static const int MV = 210;
  int V , ans;
  int el[MV][MV/30+1];
  int dp[MV];
  int s[MV][MV/30+1];
  vector<int> sol;
  void init(int v) {
    V = v; ans = 0;
    FZ(el); FZ(dp);
  }
  /* Zero Base */
  void addEdge(int u, int v) {
    if(u > v) swap(u, v);
    if(u == v) return;
    el[u][v/32] |= (1<<(v%32));
  }
  bool dfs(int v, int k) {
    int c = 0, d = 0;
    for(int i=0; i<(V+31)/32; i++) {
      s[k][i] = el[v][i];
      if(k != 1) s[k][i] &= s[k-1][i];
      c += __builtin_popcount(s[k][i]);
    }
    if(c == 0) {
      if(k > ans) {
        ans = k;
        sol.clear();
        sol.push_back(v);
        return 1;
      }
      return 0;
    }
    for(int i=0; i<(V+31)/32; i++) {
      for(int a = s[k][i]; a ; d++) {
        if(k + (c-d) <= ans) return 0;
        int lb = a&(-a), lg = 0;
        a ^= lb;
        while(lb!=1) {
          lb = (unsigned int)(lb) >> 1;
          lg ++;
        }
        int u = i*32 + lg;
        if(k + dp[u] <= ans) return 0;
        if(dfs(u, k+1)) {
          sol.push_back(v);
          return 1;
        }
      }
    }
    return 0;
  }
  int solve() {
    for(int i=V-1; i>=0; i--) {
      dfs(i, 1);
      dp[i] = ans;
    }
    return ans;
  }
};
```

## 5.5  Kosaraju

```cpp
struct Scc{
  int n, nScc, vst[MXN], bln[MXN];
  vector<int> E[MXN], rE[MXN], vec;
  void init(int _n){
    n = _n;
    for (int i=0; i<MXN; i++){
      E[i].clear();
      rE[i].clear();
    }
  }
  void add_edge(int u, int v){
    E[u].PB(v);
    rE[v].PB(u);
  }
  void DFS(int u){
    vst[u]=1;
    for (auto v : E[u])
      if (!vst[v]) DFS(v);
```

```
      vec.PB(u);
  }
  void rDFS(int u){
    vst[u] = 1;
    bln[u] = nScc;
    for (auto v : rE[u])
      if (!vst[v]) rDFS(v);
  }
  void solve(){
    nScc = 0;
    vec.clear();
    FZ(vst);
    for (int i=0; i<n; i++)
      if (!vst[i]) DFS(i);
    reverse(vec.begin(),vec.end());
    FZ(vst);
    for (auto v : vec){
      if (!vst[v]){
        rDFS(v);
        nScc++;
      }
    }
  }
};
```

# 6  String

## 6.1  PalTree

```
const int MAXN = 200010;
struct PalT{
  struct Node{
    int nxt[ 33 ] , len , fail;
    ll cnt;
  };
  int tot , lst;
  Node nd[ MAXN * 2 ];
  char* s;
  int newNode( int l , int _fail ){
    int res = ++tot;
    memset( nd[ res ].nxt , 0 , sizeof nd[ res ].nxt );
    nd[ res ].len = l;
    nd[ res ].cnt = 0;
    nd[ res ].fail = _fail;
    return res;
  }
  void push( int p ){
    int np = lst;
    int c = s[ p ] - 'a';
    while( p - nd[ np ].len - 1 < 0
        || s[ p ] != s[ p - nd[ np ].len - 1 ] )
      np = nd[ np ].fail;

    if( nd[ np ].nxt[ c ] ){
      nd[ nd[ np ].nxt[ c ] ].cnt++;
      lst = nd[ np ].nxt[ c ];
      return ;
    }
    int nq = newNode( nd[ np ].len + 2 , 0 );
    nd[ nq ].cnt++;
    nd[ np ].nxt[ c ] = nq;
    lst = nq;
    if( nd[ nq ].len == 1 ){
      nd[ nq ].fail = 2;
      return ;
    }
    int tf = nd[ np ].fail;
    while( p - nd[ tf ].len - 1 < 0
        || s[ p ] != s[ p - nd[ tf ].len - 1 ] )
      tf = nd[ tf ].fail;

    nd[ nq ].fail = nd[ tf ].nxt[ c ];
    return ;
  }
  void init( char* _s ){
    s = _s;
    tot = 0;
    newNode( -1 , 1 );
```

```
    newNode( 0 , 1 );
    lst = 2;
    for( int i = 0 ; s[ i ] ; i++ )
      push( i );
  }
  void yutruli(){
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
    REPD( i , tot , 1 )
      nd[ nd[ i ].fail ].cnt += nd[ i ].cnt;
    nd[ 1 ].cnt = nd[ 2 ].cnt = 0ll;
  }
} pA;
int main(){
  pA.init( sa );
}
```

## 6.2  SuffixArray

```
const int MAX = 1020304;
int ct[MAX], he[MAX], rk[MAX], sa[MAX], tsa[MAX], tp[
    MAX][2];
void suffix_array(char *ip){
  int len = strlen(ip);
  int alp = 256;
  memset(ct, 0, sizeof(ct));
  for(int i=0;i<len;i++) ct[ip[i]+1]++;
  for(int i=1;i<alp;i++) ct[i]+=ct[i-1];
  for(int i=0;i<len;i++) rk[i]=ct[ip[i]];

  for(int i=1;i<len;i*=2){
    for(int j=0;j<len;j++){
      if(j+i>=len) tp[j][1]=0;
      else tp[j][1]=rk[j+i]+1;

      tp[j][0]=rk[j];
    }
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][1]+1]++;
    for(int j=1;j<len+2;j++) ct[j]+=ct[j-1];
    for(int j=0;j<len;j++) tsa[ct[tp[j][1]]++]=j;

    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][0]+1]++;
    for(int j=1;j<len+1;j++) ct[j]+=ct[j-1];
    for(int j=0;j<len;j++) sa[ct[tp[tsa[j]][0]]++]=tsa[
        j];

    rk[sa[0]]=0;
    for(int j=1;j<len;j++){
      if( tp[sa[j]][0] == tp[sa[j-1]][0] &&
        tp[sa[j]][1] == tp[sa[j-1]][1] )
        rk[sa[j]] = rk[sa[j-1]];
      else
        rk[sa[j]] = j;
    }
  }

  for(int i=0,h=0;i<len;i++){
    if(rk[i]==0) h=0;
    else{
      int j=sa[rk[i]-1];
      h=max(0,h-1);
      for(;ip[i+h]==ip[j+h];h++);
    }
    he[rk[i]]=h;
  }
}
```

## 6.3  SAIS

```cpp
// Suffix array by Induced-Sorting, O(n)
const int MAXL=200000+1000; // Max Length
// input: S[0..n-1], n; output: SA[0..n-1]
// S[n-1] MUST be an unique smallest item!!!!
// Max alphabet should be < MAXL.
int S[MAXL*2],SA[MAXL*2];
bool _iss[MAXL*2];
int _p[MAXL*2],_pb[MAXL*2],cnt[MAXL],qe[MAXL];
inline void isort(int n,int *s,int *sa,bool *iss,int *p
    ,int pc){
  int a=0,i;
  for(i=0;i<n;i++)a=max(a,s[i]); a++;
  memset(cnt,0,sizeof(int)*a);
  for(i=0;i<n;i++)cnt[s[i]]++;
  qe[0]=cnt[0]; for(i=1;i<a;i++)qe[i]=qe[i-1]+cnt[i];
  memset(sa,-1,sizeof(int)*n);
  for(i=pc-1;i>=0;i--)sa[--qe[s[p[i]]]]=p[i];
  qe[0]=0; for(i=1;i<a;i++)qe[i]=qe[i-1]+cnt[i-1];
  for(i=0;i<n;i++)if(sa[i]>0&&!iss[sa[i]-1])sa[qe[s[sa[
      i]-1]]++]=sa[i]-1;
  qe[0]=cnt[0]; for(i=1;i<a;i++)qe[i]=qe[i-1]+cnt[i];
  for(i=n-1;i>=0;i--)if(sa[i]>0&&iss[sa[i]-1])sa[--qe[s
      [sa[i]-1]]]=sa[i]-1;
}
inline bool eq(int *s,bool *iss,int *pp,int *pb,int pc,
    int x,int p){
  if(pb[p]==pc-1 || pb[x]==pc-1 || pp[pb[p]+1]-p!=pp[pb
      [x]+1]-x)return 0;
  for(int j=0;j<=pp[pb[p]+1]-p;j++)if(s[j+p]!=s[j+x]||
      iss[j+p]!=iss[j+x]) return 0;
  return 1;
}
void suffixArray(int n,int a1=0){
  int i;
  int *s=S+a1,*sa=SA+a1,*pp=_p+a1,*pb=_pb+a1;
  bool *iss=_iss+a1;
  iss[n-1]=1;
  for(i=n-2;i>=0;i--)iss[i]=s[i]<s[i+1]||(s[i]==s[i
      +1]&&iss[i+1]);
  int pc=0;
  for(i=1;i<n;i++)if(iss[i]&&!iss[i-1]){ pp[pc]=i; pb[i
      ]=pc; pc++; }
  isort(n,s,sa,iss,pp,pc);
  int p=-1,c=-1;
  for(i=0;i<n;i++){
    int x=sa[i];
    if(x&&iss[x]&&!iss[x-1]){
      if(p==-1||!eq(s,iss,pp,pb,pc,x,p))c++;
      s[n+pb[x]]=c;
      p=x;
    }
  }
  if(c==pc-1)for(i=0;i<pc;i++)sa[n+s[n+i]]=i;
  else suffixArray(pc,a1+n);
  for(i=0;i<pc;i++)pb[i]=pp[sa[n+i]];
  isort(n,s,sa,iss,pb,pc);
}
int rk[MAXL],DA[MAXL];
void depthArray(int n){
  int i,j;
  for(i=0;i<n;i++) rk[SA[i]]=i;
  for(i=j=0;i<n;i++){
    if(!rk[i]){ j=0; }
    else{
      if(j) j--;
      for(;S[i+j]==S[SA[rk[i]-1]+j];j++);
    }
    DA[rk[i]]=j;
  }
}
```

## 6.4  SuffixAutomata

```cpp
const int MAXM = 1000010;
struct SAM{
  int tot, root, lst, mom[MAXM], mx[MAXM];
  int acc[MAXM], nxt[MAXM][33];
```

```cpp
  int newNode(){
    int res = ++tot;
    fill(nxt[res], nxt[res]+33, 0);
    mom[res] = mx[res] = acc[res] = 0;
    return res;
  }
  void init(){
    tot = 0;
    root = newNode();
    mom[root] = 0, mx[root] = 0;
    lst = root;
  }
  void push(int c){
    int p = lst;
    int np = newNode();
    mx[np] = mx[p]+1;
    for(; p && nxt[p][c] == 0; p = mom[p])
      nxt[p][c] = np;
    if(p == 0) mom[np] = root;
    else{
      int q = nxt[p][c];
      if(mx[p]+1 == mx[q]) mom[np] = q;
      else{
        int nq = newNode();
        mx[nq] = mx[p]+1;
        for(int i = 0; i < 33; i++)
          nxt[nq][i] = nxt[q][i];
        mom[nq] = mom[q];
        mom[q] = nq;
        mom[np] = nq;
        for(; p && nxt[p][c] == q; p = mom[p])
          nxt[p][c] = nq;
      }
    }
    lst = np;
  }
  void print(){
    REP(i, 1, tot){
      printf("node %d :\n", i);
      printf("mx %d, mom %d\n", mx[i], mom[i]);
      REP(j, 1, 26) if(nxt[i][j])
        printf("nxt %c %d\n", 'a'+j-1, nxt[i][j]);
      puts("--------------------------");
    }
  }
  void push(char *str){
    for(int i = 0; str[i]; i++)
      push(str[i]-'a'+1);
  }
};

SAM sam;
```

## 6.5  Aho-Corasick

```cpp
struct ACautomata{
  struct Node{
    int cnt,dp;
    Node *go[26], *fail;
    Node (){
      cnt = 0;
      dp = -1;
      memset(go,0,sizeof(go));
      fail = 0;
    }
  };
  Node *root, pool[1048576];
  int nMem;
  Node* new_Node(){
    pool[nMem] = Node();
    return &pool[nMem++];
  }
  void init(){
    nMem = 0;
    root = new_Node();
  }
  void add(const string &str){
    insert(root,str,0);
  }
  void insert(Node *cur, const string &str, int pos){
```

```
      if (pos >= (int)str.size()){
        cur->cnt++;
        return;
      }
      int c = str[pos]-'a';
      if (cur->go[c] == 0){
        cur->go[c] = new_Node();
      }
      insert(cur->go[c],str,pos+1);
    }
    void make_fail(){
      queue<Node*> que;
      que.push(root);
      while (!que.empty()){
        Node* fr=que.front();
        que.pop();
        for (int i=0; i<26; i++){
          if (fr->go[i]){
            Node *ptr = fr->fail;
            while (ptr && !ptr->go[i]) ptr = ptr->fail;
            if (!ptr) fr->go[i]->fail = root;
            else fr->go[i]->fail = ptr->go[i];
            que.push(fr->go[i]);
          }
        }
      }
    }
};
```

## 6.6 Z Value

```
char s[MAXLEN];
int len,z[MAXLEN];
void Z_value() {
  int i,j,left,right;
  left=right=0; z[0]=len;
  for(i=1;i<len;i++) {
    j=max(min(z[i-left],right-i),0);
    for(;i+j<len&&s[i+j]==s[j];j++);
    z[i]=j;
    if(i+z[i]>right) {
      right=i+z[i];
      left=i;
    }
  }
}
```

## 6.7 ZValue Palindrome

```
const int MAX = 1000;
int len;
char ip[MAX];
char op[MAX*2];
int zv[MAX*2];
int main(){
  cin >> ip;
  len = strlen(ip);
  int l2 = len*2 - 1;
  for(int i=0; i<l2; i++){
    if(i&1) op[i] = '@';
    else op[i] = ip[i/2];
  }
  int l=0, r=0;
  zv[0] = 1;
  for(int i=1; i<l2; i++){
    if( i > r ){
      l = r = i;
      while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){
        l --;
        r ++;
      }
      zv[i] = (r-l+1);
    }else{
      int md = (l+r)/2;
      int j = md + md - i;
      zv[i] = zv[j];
      int q = zv[i] / 2;
      int nr = i + q;
```

```
      if( nr == r ){
        l = i + i - r;
        while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){
          l --;
          r ++;
        }
        zv[i] = r - l + 1;
      }else if( nr > r ){
        zv[i] = (r - i) * 2 + 1;
      }
    }
  }
}
```

## 6.8 Smallest Rotation

```
string mcp(string s){
  int n = s.length();
  s += s;
  int i=0, j=1, k=0;
  while (j<n && k<n){
    if (s[i+k] == s[j+k]) k++;
    else {
      if (s[i+k] < s[j+k]) {
        j += k + 1;
      } else {
        i = j;
        j = max(j+1, j+k);
      }
      k = 0;
    }
  }
  return s.substr(i, n);
}
```

## 6.9 Baker Bird

```
class Node { public:
  Node *fail;
  map<char,Node*> _next;
  int out;
  Node() { fail=NULL; out=-1; }
  ~Node() {
    for(map<char,Node*>::iterator it=_next.begin();it!=
        _next.end();it++)
      delete it->second;
  }
  Node* build(char ch) {
    if(_next.find(ch)==_next.end()) _next[ch]=new Node;
    return _next[ch];
  }
  Node* next(char ch) {
    if(_next.find(ch)==_next.end()) return NULL;
    return _next[ch];
  }
};
int srn,scn,prn,pcn,mrn,mcn;
char s[MAXLEN][MAXLEN],p[MAXLEN][MAXLEN];
int rm[MAXLEN][MAXLEN]; // rank matrix
int maxrank;
int seq[MAXLEN]; // index of patterns for radix sort
int rank[MAXLEN]; // rank of pattern on row r
int cnt[SIGMA+1],tmp[MAXLEN];
int pre[MAXLEN]; // pre-matrix for kmp
int ql,qr;
Node* que[MAXLEN*MAXLEN];
inline void radix_pass(int j,int *from,int *to) {
  int i;
  for(i=0;i<SIGMA;i++) cnt[i]=0;
  for(i=0;i<prn;i++) cnt[p[from[i]][j]+1]++;
  for(i=0;i<SIGMA;i++) cnt[i+1]+=cnt[i];
  for(i=0;i<prn;i++) to[cnt[p[from[i]][j]]++]=from[i];
}
inline void radix_sort_patterns() {
  int i,j;
  for(i=0;i<prn;i++) ((pcn&1)?tmp[i]:seq[i])=i;
  for(j=pcn-1;j>=0;j--) {
    if(j&1) radix_pass(j,seq,tmp);
```

```
    else radix_pass(j,tmp,seq);
  }
  maxrank=0;
  for(i=0;i<prn;i++) {
    if(i&&strcmp(p[seq[i-1]],p[seq[i]])) ++maxrank;
    rank[seq[i]]=maxrank;
  }
}
inline void construct(Node *v,char *p,int ind) {
  while(*p) { v=v->build(*p); p++; }
  v->out=ind;
}
inline void construct_all(Node *ac) {
  for(int i=0;i<prn;i++) construct(ac,p[i],rank[i]);
}
inline void find_fail(Node *ac) {
  Node *v,*u,*f;
  map<char,Node*>::iterator it;
  char ch;
  ql=qr=0; ac->fail=ac;
  for(it=ac->_next.begin();it!=ac->_next.end();it++) {
    u=it->second;
    u->fail=ac;
    que[qr++]=u;
  }
  while(ql<qr) {
    v=que[ql++];
    for(it=v->_next.begin();it!=v->_next.end();it++) {
      ch=it->first; u=it->second;
      f=v->fail;
      while(f!=ac&&f->next(ch)==NULL) f=f->fail;
      if(f->next(ch)) u->fail=f->next(ch);
      else u->fail=ac;
      que[qr++]=u;
    }
  }
}
inline void ac_match(Node *ac,char *s,int *arr) {
  int i;
  Node *v=ac;
  for(i=0;i<scn;i++) {
    while(v!=ac&&v->next(s[i])==NULL) v=v->fail;
    if(v->next(s[i])) v=v->next(s[i]);
    if(i>=pcn-1) arr[i-pcn+1]=v->out;
  }
}
inline void find_rank_matrix() {
  Node ac;
  radix_sort_patterns();
  construct_all(&ac);
  find_fail(&ac);
  mrn=srn; mcn=scn-pcn+1;
  for(int i=0;i<srn;i++) ac_match(&ac,s[i],rm[i]);
}
inline void find_pre(int *p,int plen) {
  int i,x;
  x=pre[0]=-1;
  for(i=1;i<plen;i++) {
    while(x>=0&&p[x+1]!=p[i]) x=pre[x];
    if(p[x+1]==p[i]) x++;
    pre[i]=x;
  }
}
inline int kmp_match(int col,int *p,int plen) {
  int i,x=-1,occ=0;
  for(i=0;i<mrn;i++) {
    while(x>=0&&p[x+1]!=rm[i][col]) x=pre[x];
    if(p[x+1]==rm[i][col]) x++;
    if(x==plen-1) { occ++; x=pre[x]; }
  }
  return occ;
}
inline int baker_bird() {
  int i,occ=0;
  find_rank_matrix();
  find_pre(rank,prn);
  for(i=0;i<mcn;i++) occ+=kmp_match(i,rank,prn);
  return occ;
}
```

## 6.10 Cyclic LCS

```
#define L 0
#define LU 1
#define U 2
const int mov[3][2]={0,-1, -1,-1, -1,0};
int al,bl;
char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
char pred[MAXL*2][MAXL];
inline int lcs_length(int r) {
  int i=r+al,j=bl,l=0;
  while(i>r) {
    char dir=pred[i][j];
    if(dir==LU) l++;
    i+=mov[dir][0];
    j+=mov[dir][1];
  }
  return l;
}
inline void reroot(int r) { // r = new base row
  int i=r,j=1;
  while(j<=bl&&pred[i][j]!=LU) j++;
  if(j>bl) return;
  pred[i][j]=L;
  while(i<2*al&&j<=bl) {
    if(pred[i+1][j]==U) {
      i++;
      pred[i][j]=L;
    } else if(j<bl&&pred[i+1][j+1]==LU) {
      i++;
      j++;
      pred[i][j]=L;
    } else {
      j++;
    }
  }
}
int cyclic_lcs() {
  // a, b, al, bl should be properly filled
  // note: a WILL be altered in process -- concatenated
  //       after itself
  char tmp[MAXL];
  if(al>bl) {
    swap(al,bl);
    strcpy(tmp,a);
    strcpy(a,b);
    strcpy(b,tmp);
  }
  strcpy(tmp,a);
  strcat(a,tmp);
  // basic lcs
  for(int i=0;i<=2*al;i++) {
    dp[i][0]=0;
    pred[i][0]=U;
  }
  for(int j=0;j<=bl;j++) {
    dp[0][j]=0;
    pred[0][j]=L;
  }
  for(int i=1;i<=2*al;i++) {
    for(int j=1;j<=bl;j++) {
      if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
      else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
      if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;
      else if(a[i-1]==b[j-1]) pred[i][j]=LU;
      else pred[i][j]=U;
    }
  }
  // do cyclic lcs
  int clcs=0;
  for(int i=0;i<al;i++) {
    clcs=max(clcs,lcs_length(i));
    reroot(i+1);
  }
  // recover a
  a[al]='\0';
  return clcs;
}
```

# 7 Data Structure

## 7.1 Treap

```
struct Treap{
  int sz , val , pri , tag;
  Treap *l , *r;
  Treap( int _val ){
    val = _val; sz = 1;
    pri = rand(); l = r = NULL; tag = 0;
  }
};
void push( Treap * a ){
  if( a->tag ){
    Treap *swp = a->l; a->l = a->r; a->r = swp;
    int swp2;
    if( a->l ) a->l->tag ^= 1;
    if( a->r ) a->r->tag ^= 1;
    a->tag = 0;
  }
}
int Size( Treap * a ){ return a ? a->sz : 0; }
void pull( Treap * a ){
  a->sz = Size( a->l ) + Size( a->r ) + 1;
}
Treap* merge( Treap *a , Treap *b ){
  if( !a || !b ) return a ? a : b;
  if( a->pri > b->pri ){
    push( a );
    a->r = merge( a->r , b );
    pull( a );
    return a;
  }else{
    push( b );
    b->l = merge( a , b->l );
    pull( b );
    return b;
  }
}
void split( Treap *t , int k , Treap*&a , Treap*&b ){
  if( !t ){ a = b = NULL; return; }
  push( t );
  if( Size( t->l ) + 1 <= k ){
    a = t;
    split( t->r , k - Size( t->l ) - 1 , a->r , b );
    pull( a );
  }else{
    b = t;
    split( t->l , k , a , b->l );
    pull( b );
  }
}
```

## 7.2 Link-Cut Tree

```
const int MXN = 100005;
const int MEM = 100005;
struct Splay {
  static Splay nil, mem[MEM], *pmem;
  Splay *ch[2], *f;
  int val, rev, size;
  Splay () : val(-1), rev(0), size(0){
    f = ch[0] = ch[1] = &nil;
  }
  Splay (int _val) : val(_val), rev(0), size(1){
    f = ch[0] = ch[1] = &nil;
  }
  bool isr(){
    return f->ch[0] != this && f->ch[1] != this;
  }
  int dir(){
    return f->ch[0] == this ? 0 : 1;
  }
  void setCh(Splay *c, int d){
    ch[d] = c;
    if (c != &nil) c->f = this;
    pull();
  }
```

```
  void push(){
    if (rev){
      swap(ch[0], ch[1]);
      if (ch[0] != &nil) ch[0]->rev ^= 1;
      if (ch[1] != &nil) ch[1]->rev ^= 1;
      rev=0;
    }
  }
  void pull(){
    size = ch[0]->size + ch[1]->size + 1;
    if (ch[0] != &nil) ch[0]->f = this;
    if (ch[1] != &nil) ch[1]->f = this;
  }
} Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::
    mem;
Splay *nil = &Splay::nil;
void rotate(Splay *x){
  Splay *p = x->f;
  int d = x->dir();
  if (!p->isr()) p->f->setCh(x, p->dir());
  else x->f = p->f;
  p->setCh(x->ch[!d], d);
  x->setCh(p, !d);
  p->pull(); x->pull();
}

vector<Splay*> splayVec;
void splay(Splay *x){
  splayVec.clear();
  for (Splay *q=x;; q=q->f){
    splayVec.push_back(q);
    if (q->isr()) break;
  }
  reverse(begin(splayVec), end(splayVec));
  for (auto it : splayVec) it->push();
  while (!x->isr()) {
    if (x->f->isr()) rotate(x);
    else if (x->dir()==x->f->dir()) rotate(x->f),rotate
        (x);
    else rotate(x),rotate(x);
  }
}
Splay* access(Splay *x){
  Splay *q = nil;
  for (;x!=nil;x=x->f){
    splay(x);
    x->setCh(q, 1);
    q = x;
  }
  return q;
}
void evert(Splay *x){
  access(x);
  splay(x);
  x->rev ^= 1;
  x->push(); x->pull();
}
void link(Splay *x, Splay *y){
//  evert(x);
  access(x);
  splay(x);
  evert(y);
  x->setCh(y, 1);
}
void cut(Splay *x, Splay *y){
//  evert(x);
  access(y);
  splay(y);
  y->push();
  y->ch[0] = y->ch[0]->f = nil;
}
int N, Q;
Splay *vt[MXN];
int ask(Splay *x, Splay *y){
  access(x);
  access(y);
  splay(x);
  int res = x->f->val;
  if (res == -1) res=x->val;
  return res;
}
int main(int argc, char** argv){
```

```
  scanf("%d%d", &N, &Q);
  for (int i=1; i<=N; i++)
    vt[i] = new (Splay::pmem++) Splay(i);
  while (Q--) {
    char cmd[105];
    int u, v;
    scanf("%s", cmd);
    if (cmd[1] == 'i') {
      scanf("%d%d", &u, &v);
      link(vt[v], vt[u]);
    } else if (cmd[0] == 'c') {
      scanf("%d", &v);
      cut(vt[1], vt[v]);
    } else {
      scanf("%d%d", &u, &v);
      int res=ask(vt[u], vt[v]);
      printf("%d\n", res);
    }
  }
}
```

## 7.3  Black Magic

```
#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> set_t;

int main(){
  // Insert some entries into s.
  set_t s;
  s.insert(12);
  s.insert(505);
  // The order of the keys should be: 12, 505.
  assert(*s.find_by_order(0) == 12);
  assert(*s.find_by_order(3) == 505);
  // The order of the keys should be: 12, 505.
  assert(s.order_of_key(12) == 0);
  assert(s.order_of_key(505) == 1);
  // Erase an entry.
  s.erase(12);
  // The order of the keys should be: 505.
  assert(*s.find_by_order(0) == 505);
  // The order of the keys should be: 505.
  assert(s.order_of_key(505) == 0);
}
```

# 8  Others

## 8.1  Find max tangent(x,y is increasing)

```
typedef long long LL;
const int MAXN = 100010;
struct Coord{
  LL x, y;
  Coord operator - (Coord ag) const{
    Coord res;
    res.x = x - ag.x;
    res.y = y - ag.y;
    return res;
  }
}sum[MAXN], pnt[MAXN], ans, calc;

inline bool cross(Coord a, Coord b, Coord c){
  return (c.y - a.y) * (c.x - b.x) > (c.x - a.x) * (c.y
      - b.y);
}

int main(){
  int n, l, np, st, ed, now;
  scanf("%d %d\n", &n, &l);
  sum[0].x = sum[0].y = np = st = ed = 0;
  for (int i = 1, v; i <= n; i++){
    scanf("%d", &v);
    sum[i].y = sum[i - 1].y + v;
    sum[i].x = i;
```

```
  }
  ans.x = now = 1;
  ans.y = -1;
  for (int i = 0; i <= n - l; i++){
    while (np > 1 && cross(pnt[np - 2], pnt[np - 1],
        sum[i]))
      np--;
    if (np < now && np != 0) now = np;
    pnt[np++] = sum[i];
    while (now < np && !cross(pnt[now - 1], pnt[now],
        sum[i + l]))
      now++;
    calc = sum[i + l] - pnt[now - 1];
    if (ans.y * calc.x < ans.x * calc.y){
      ans = calc;
      st = pnt[now - 1].x;
      ed = i + l;
    }
  }
  double res = (sum[ed].y-sum[st].y)/(sum[ed].x-sum[st
      ].x);
  printf("%f\n", res);
  return 0;
}
```