Contents

1 Basic

1.1 .vimrc

```
syn on
se ai nu ru cul mouse=a
se cin et ts=2 sw=2 sts=2
so $VIMRUNTIME/mswin.vim
colo desert
se gfn=Monospace\ 14
```

1.2 Increase Stack Size

```cpp
//stack resize
asm( "mov %0,%%esp\n" ::"g"(mem+10000000) );
//change esp to rsp if 64-bit system

//stack resize (linux)
#include <sys/resource.h>
void increase_stack_size() {
  const rlim_t ks = 64*1024*1024;
  struct rlimit rl;
  int res=getrlimit(RLIMIT_STACK, &rl);
  if(res==0){
    if(rl.rlim_cur<ks){
      rl.rlim_cur=ks;
      res=setrlimit(RLIMIT_STACK, &rl);
    }
  }
}
```

2 flow

2.1 DMST

```cpp
/*
 * Edmond's algoirthm for Directed MST
 * runs in O(VE)
 */
const int MAXV = 10010;
const int MAXE = 10010;
const int INF  = 2147483647;
struct Edge{
  int u, v, c;
  Edge(){}
  Edge(int x, int y, int z) :
    u(x), v(y), c(z){}
};
int V, E, root;
Edge edges[MAXE];
inline int newV(){
  V++;
  return V;
}
inline void addEdge(int u, int v, int c){
  E++;
  edges[E] = Edge(u, v, c);
}
bool con[MAXV];
int mnInW[MAXV], prv[MAXV], cyc[MAXV], vis[MAXV];
inline int DMST(){
  fill(con, con+V+1, 0);
  int r1 = 0, r2 = 0;
  while(1){
    fill(mnInW, mnInW+V+1, INF);
    fill(prv, prv+V+1, -1);
    REP(i, 1, E){
      int u=edges[i].u, v=edges[i].v, c=edges[i].c;
      if(u != v && v != root && c < mnInW[v])
        mnInW[v] = c, prv[v] = u;
    }
    fill(vis, vis+V+1, -1);
    fill(cyc, cyc+V+1, -1);
    r1 = 0;
    bool jf = 0;
```

```
    REP(i, 1, V){
      if(con[i]) continue ;
      if(prv[i] == -1 && i != root) return -1;
      if(prv[i] > 0) r1 += mnInW[i];
      int s;
      for(s = i; s != -1 && vis[s] == -1; s = prv[s])
        vis[s] = i;
      if(s > 0 && vis[s] == i){
         // get a cycle
        jf = 1;
        int v = s;
        do{
          cyc[v] = s, con[v] = 1;
          r2 += mnInW[v];
          v = prv[v];
        }while(v != s);
        con[s] = 0;
      }
    }
    if(!jf) break ;
    REP(i, 1, E){
      int &u = edges[i].u;
      int &v = edges[i].v;
      if(cyc[v] > 0) edges[i].c -= mnInW[edges[i].v];
      if(cyc[u] > 0) edges[i].u = cyc[edges[i].u];
      if(cyc[v] > 0) edges[i].v = cyc[edges[i].v];
      if(u == v) edges[i--] = edges[E--];
    }
  }
  return r1+r2;
}
```

2.2 ISAP

```
#define SZ(c) ((int)(c).size())
struct Maxflow {
  static const int MAXV = 20010;
  static const int INF  = 1000000;
  struct Edge {
    int v, c, r;
    Edge(int _v, int _c, int _r):
      v(_v), c(_c), r(_r) {}
  };
  int s, t;
  vector<Edge> G[MAXV*2];
  int iter[MAXV*2], d[MAXV*2], gap[MAXV*2], tot;
  void flowinit(int x) {
    tot = x+2;
    s = x+1, t = x+2;
    for(int i = 0; i <= tot; i++) {
      G[i].clear();
      iter[i] = d[i] = gap[i] = 0;
    }
  }
  void addEdge(int u, int v, int c) {
    G[u].push_back(Edge(v, c, SZ(G[v]) ));
    G[v].push_back(Edge(u, 0, SZ(G[u]) - 1));
  }
  int dfs(int p, int flow) {
    if(p == t) return flow;
    for(int &i = iter[p]; i < SZ(G[p]); i++) {
      Edge &e = G[p][i];
      if(e.c > 0 && d[p] == d[e.v]+1) {
        int f = dfs(e.v, min(flow, e.c));
        if(f) {
          e.c -= f;
          G[e.v][e.r].c += f;
          return f;
        }
      }
    }
    if( (--gap[d[p]]) == 0) d[s] = tot;
    else {
      d[p]++;
      iter[p] = 0;
      ++gap[d[p]];
    }
    return 0;
  }
  int maxflow() {
```

```
    //puts("MF");
    int res = 0;
    gap[0] = tot;
    for(res = 0; d[s] < tot; res += dfs(s, INF));
    return res;
  }
} flow;
Maxflow::Edge e(1, 1, 1);
```

2.3 MinCostFlow

```
/*
  A template for Min Cost Max Flow
  tested with TIOJ 1724
*/
struct MinCostMaxFlow{
  static const int MAXV = 20010;
  static const int INF  = 1000000000;
  struct Edge{
    int v, cap, w, rev;
    Edge(){}
    Edge(int t2, int t3, int t4, int t5)
    : v(t2), cap(t3), w(t4), rev(t5) {}
  };
  int V, s, t;
  vector<Edge> g[MAXV];
  void init(int n){
    V = n+2;
    s = n+1, t = n+2;
    for(int i = 1; i <= V; i++) g[i].clear();
  }
  void addEdge(int a, int b, int cap, int w){
    g[a].push_back(Edge(b, cap, w, (int)g[b].size()));
    g[b].push_back(Edge(a, 0, -w, (int)g[a].size()-1));
  }
  int d[MAXV], id[MAXV], mom[MAXV];
  bool inqu[MAXV];
  int qu[2000000], ql, qr;
  //the size of qu should be much large than MAXV
  int mncmxf(){
    int mxf = 0, mnc = 0;
    while(1){
      fill(d+1, d+1+V, INF);
      fill(inqu+1, inqu+1+V, 0);
      fill(mom+1, mom+1+V, -1);
      mom[s] = s;
      d[s] = 0;
      ql = 1, qr = 0;
      qu[++qr] = s;
      inqu[s] = 1;
      while(ql <= qr){
        int u = qu[ql++];
        inqu[u] = 0;
        for(int i = 0; i < (int) g[u].size(); i++){
          Edge &e = g[u][i];
          int v = e.v;
          if(e.cap > 0 && d[v] > d[u]+e.w){
            d[v] = d[u]+e.w;
            mom[v] = u;
            id[v] = i;
            if(!inqu[v]) qu[++qr] = v, inqu[v] = 1;
          }
        }
      }
      if(mom[t] == -1) break ;
      int df = INF;
      for(int u = t; u != s; u = mom[u])
        df = min(df, g[mom[u]][id[u]].cap);
      for(int u = t; u != s; u = mom[u]){
        Edge &e = g[mom[u]][id[u]];
        e.cap            -= df;
        g[e.v][e.rev].cap += df;
      }
      mxf += df;
      mnc += df*d[t];
    }
    return mnc;
  }
} flow;
```

2.4 SW min-cut

```cpp
struct SW{ // O(V^3)
  static const int MXN = 514;
  int n,vst[MXN],del[MXN];
  int edge[MXN][MXN],wei[MXN];
  void init(int _n){
    n = _n;
    FZ(edge);
    FZ(del);
  }
  void add_edge(int u, int v, int w){
    edge[u][v] += w;
    edge[v][u] += w;
  }
  void search(int &s, int &t){
    FZ(vst); FZ(wei);
    s = t = -1;
    while (true){
      int mx=-1, cur=0;
      for (int i=0; i<n; i++)
        if (!del[i] && !vst[i] && mx<wei[i])
          cur = i, mx = wei[i];
      if (mx == -1) break;
      vst[cur] = 1;
      s = t;
      t = cur;
      for (int i=0; i<n; i++)
        if (!vst[i] && !del[i]) wei[i] += edge[cur][i];
    }
  }
  int solve(){
    int res = 2147483647;
    for (int i=0,x,y; i<n-1; i++){
      search(x,y);
      res = min(res,wei[y]);
      del[y] = 1;
      for (int j=0; j<n; j++)
        edge[x][j] = (edge[j][x] += edge[y][j]);
    }
    return res;
  }
}graph;
```

2.5 HLPPA

```cpp
/* Highest-Label Preflow Push Algorithm */
// tested with sgu-212 (more testing suggested)
int n,m,src,sink;
int deg[MAXN],adj[MAXN][MAXN],res[MAXN][MAXN]; //
    residual capacity
// graph (i.e. all things above) should be constructed
    beforehand
int ef[MAXN],ht[MAXN]; // excess flow, height
int apt[MAXN]; // the next adj index to try push
int htodo; // highest label to check with
int hcnt[MAXN*2]; // number of nodes with height h
queue<int> ovque[MAXN*2]; // used to implement highest-
    label selection
bool inque[MAXN];
inline void push(int v,int u) {
  int a=min(ef[v],res[v][u]);
  ef[v]-=a; ef[u]+=a;
  res[v][u]-=a; res[u][v]+=a;
  if(!inque[u]) {
    inque[u]=1;
    ovque[ht[u]].push(u);
  }
}
inline void relabel(int v) {
  int i,u,oldh;
  oldh=ht[v]; ht[v]=2*n;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(res[v][u]) ht[v]=min(ht[u]+1,ht[v]);
  }
  // gap speedup
  hcnt[oldh]--; hcnt[ht[v]]++;
  if(0<oldh&&oldh<n&&hcnt[oldh]==0) {
```

```cpp
    for(i=0;i<n;i++) {
      if(ht[i]>oldh&&ht[i]<n) {
        hcnt[ht[i]]--;
        hcnt[n]++;
        ht[i]=n;
      }
    }
  }
  // update queue
  htodo=ht[v]; ovque[ht[v]].push(v); inque[v]=1;
}
inline void initPreflow() {
  int i,u;
  for(i=0;i<n;i++) {
    ht[i]=ef[i]=0;
    apt[i]=0; inque[i]=0;
  }
  ht[src]=n;
  for(i=0;i<deg[src];i++) {
    u=adj[src][i];
    ef[u]=res[src][u];
    ef[src]-=ef[u];
    res[u][src]=ef[u];
    res[src][u]=0;
  }
  htodo=n-1;
  for(i=0;i<2*n;i++) {
    hcnt[i]=0;
    while(!ovque[i].empty()) ovque[i].pop();
  }
  for(i=0;i<n;i++) {
    if(i==src||i==sink) continue;
    if(ef[i]) {
      inque[i]=1;
      ovque[ht[i]].push(i);
    }
    hcnt[ht[i]]++;
  }
  // to ensure src & sink is never added to queue
  inque[src]=inque[sink]=1;
}
inline void discharge(int v) {
  int u;
  while(ef[v]) {
    if(apt[v]==deg[v]) {
      relabel(v);
      apt[v]=0;
      continue;
    }
    u=adj[v][apt[v]];
    if(res[v][u]&&ht[v]==ht[u]+1) push(v,u);
    else apt[v]++;
  }
}
inline void hlppa() {
  int v;
  list<int>::iterator it;
  initPreflow();
  while(htodo>=0) {
    if(!ovque[htodo].size()) {
      htodo--;
      continue;
    }
    v=ovque[htodo].front();
    ovque[htodo].pop();
    inque[v]=0;
    discharge(v);
  }
}
```

2.6 Hungarian

```cpp
#define NIL -1
#define INF 100000000
int n,matched;
int cost[MAXN][MAXN];
bool sets[MAXN]; // whether x is in set S
bool sett[MAXN]; // whether y is in set T
int xlabel[MAXN],ylabel[MAXN];
int xy[MAXN],yx[MAXN]; // matched with whom
int slack[MAXN]; // given y: min{xlabel[x]+ylabel[y]-
    cost[x][y]} | x not in S
int prev[MAXN]; // for augmenting matching
inline void relabel() {
  int i,delta=INF;
  for(i=0;i<n;i++) if(!sett[i]) delta=min(slack[i],
      delta);
  for(i=0;i<n;i++) if(sets[i]) xlabel[i]-=delta;
  for(i=0;i<n;i++) {
    if(sett[i]) ylabel[i]+=delta;
    else slack[i]-=delta;
  }
}
inline void add_sets(int x) {
  int i;
  sets[x]=1;
  for(i=0;i<n;i++) {
    if(xlabel[x]+ylabel[i]-cost[x][i]<slack[i]) {
      slack[i]=xlabel[x]+ylabel[i]-cost[x][i];
      prev[i]=x;
    }
  }
}
inline void augment(int final) {
  int x=prev[final],y=final,tmp;
  matched++;
  while(1) {
    tmp=xy[x]; xy[x]=y; yx[y]=x; y=tmp;
    if(y==NIL) return;
    x=prev[y];
  }
}
inline void phase() {
  int i,y,root;
  for(i=0;i<n;i++) { sets[i]=sett[i]=0; slack[i]=INF; }
  for(root=0;root<n&&xy[root]!=NIL;root++);
  add_sets(root);
  while(1) {
    relabel();
    for(y=0;y<n;y++) if(!sett[y]&&slack[y]==0) break;
    if(yx[y]==NIL) { augment(y); return; }
    else { add_sets(yx[y]); sett[y]=1; }
  }
}
inline int hungarian() {
  int i,j,c=0;
  for(i=0;i<n;i++) {
    xy[i]=yx[i]=NIL;
    xlabel[i]=ylabel[i]=0;
    for(j=0;j<n;j++) xlabel[i]=max(cost[i][j],xlabel[i
        ]);
  }
  for(i=0;i<n;i++) phase();
  for(i=0;i<n;i++) c+=cost[i][xy[i]];
  return c;
}
```

2.7 Hungarian Unbalanced

```cpp
const int nil = -1;
const int inf = 1000000000;
int xn,yn,matched;
int cost[MAXN][MAXN];
bool sets[MAXN]; // whether x is in set S
bool sett[MAXN]; // whether y is in set T
int xlabel[MAXN],ylabel[MAXN];
int xy[MAXN],yx[MAXN]; // matched with whom
int slack[MAXN]; // given y: min{xlabel[x]+ylabel[y]-
    cost[x][y]} | x not in S
```

```cpp
int prev[MAXN]; // for augmenting matching
inline void relabel() {
  int i,delta=inf;
  for(i=0;i<yn;i++) if(!sett[i]) delta=min(slack[i],
      delta);
  for(i=0;i<xn;i++) if(sets[i]) xlabel[i]-=delta;
  for(i=0;i<yn;i++) {
    if(sett[i]) ylabel[i]+=delta;
    else slack[i]-=delta;
  }
}
inline void add_sets(int x) {
  int i;
  sets[x]=1;
  for(i=0;i<yn;i++) {
    if(xlabel[x]+ylabel[i]-cost[x][i]<slack[i]) {
      slack[i]=xlabel[x]+ylabel[i]-cost[x][i];
      prev[i]=x;
    }
  }
}
inline void augment(int final) {
  int x=prev[final],y=final,tmp;
  matched++;
  while(1) {
    tmp=xy[x]; xy[x]=y; yx[y]=x; y=tmp;
    if(y==nil) return;
    x=prev[y];
  }
}
inline void phase() {
  int i,y,root;
  for(i=0;i<xn;i++) sets[i]=0;
  for(i=0;i<yn;i++) { sett[i]=0; slack[i]=inf; }
  for(root=0;root<xn&&xy[root]!=nil;root++);
  add_sets(root);
  while(1) {
    relabel();
    for(y=0;y<yn;y++) if(!sett[y]&&slack[y]==0) break;
    if(yx[y]==nil) { augment(y); return; }
    else { add_sets(yx[y]); sett[y]=1; }
  }
}
inline int hungarian() {
  int i,j,c=0;
  matched=0;
  // we must have "xn<yn"
  bool swapxy=0;
  if(xn>yn) {
    swapxy=1;
    int mn=max(xn,yn);
    swap(xn,yn);
    for(int i=0;i<mn;i++)
      for(int j=0;j<i;j++)
        swap(cost[i][j],cost[j][i]);
  }
  for(i=0;i<xn;i++) {
    xy[i]=nil;
    xlabel[i]=0;
    for(j=0;j<yn;j++) xlabel[i]=max(cost[i][j],xlabel[i
        ]);
  }
  for(i=0;i<yn;i++) {
    yx[i]=nil;
    ylabel[i]=0;
  }
  for(i=0;i<xn;i++) phase();
  for(i=0;i<xn;i++) c+=cost[i][xy[i]];
  // recover cost matrix (if necessary)
  if(swapxy) {
    int mn=max(xn,yn);
    swap(xn,yn);
    for(int i=0;i<mn;i++)
      for(int j=0;j<i;j++)
        swap(cost[i][j],cost[j][i]);
  }
  // need special recovery if we want more info than
      matching value
  return c;
}
```

2.8 Gusfield

```cpp
#define SOURCE 0
#define SINK 1
const unsigned int inf=4000000000u;
int n,m,deg[MAXN],adj[MAXN][MAXN];
unsigned int res[MAXN][MAXN],cap[MAXN][MAXN];
int nei[MAXN],gdeg[MAXN],gadj[MAXN][MAXN];
unsigned int gres[MAXN][MAXN];
unsigned int cut[MAXN][MAXN];
unsigned int cutarr[MAXN*MAXN];
int cutn,ql,qr,que[MAXN],pred[MAXN];
unsigned int aug[MAXN];
bool cutset[MAXN];
int visited[MAXN],visid=0;
inline void augment(int src,int sink) {
  int v=sink; unsigned a=aug[sink];
  while(v!=src) {
    res[pred[v]][v]-=a;
    res[v][pred[v]]+=a;
    v=pred[v];
  }
}
inline bool bfs(int src,int sink) {
  int i,v,u; ++visid;
  ql=qr=0; que[qr++]=src;
  visited[src]=visid; aug[src]=inf;
  while(ql<qr) {
    v=que[ql++];
    for(i=0;i<deg[v];i++) {
      u=adj[v][i];
      if(visited[u]==visid||res[v][u]==0) continue;
      visited[u]=visid; pred[u]=v;
      aug[u]=min(aug[v],res[v][u]);
      que[qr++]=u;
      if(u==sink) return 1;
    }
  }
  return 0;
}
void dfs_src(int v) {
  int i,u;
  visited[v]=visid;
  cutset[v]=SOURCE;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(visited[u]<visid&&res[v][u]) dfs_src(u);
  }
}
inline unsigned int maxflow(int src,int sink) {
  int i,j;
  unsigned int f=0;
  for(i=0;i<n;i++) {
    for(j=0;j<deg[i];j++) res[i][adj[i][j]]=cap[i][adj[
        i][j]];
    cutset[i]=SINK;
  }
  while(bfs(src,sink)) {
    augment(src,sink);
    f+=aug[sink];
  }
  ++visid;
  dfs_src(src);
  return f;
}
inline void gusfield() {
  int i,j;
  unsigned int f;
  for(i=0;i<n;i++) { nei[i]=0; gdeg[i]=0; }
  for(i=1;i<n;i++) {
    f=maxflow(i,nei[i]);
    gres[i][nei[i]]=gres[nei[i]][i]=f;
    gadj[i][gdeg[i]++]=nei[i];
    gadj[nei[i]][gdeg[nei[i]]++]=i;
    for(j=i+1;j<n;j++)
      if(nei[j]==nei[i]&&cutset[j]==SOURCE) nei[j]=i;
  }
}
void dfs(int v,int pred,int src,unsigned int cur) {
  int i,u;
  cut[src][v]=cur;
  for(i=0;i<gdeg[v];i++) {
    u=gadj[v][i];
    if(u==pred) continue;
    dfs(u,v,src,min(cur,gres[v][u]));
  }
}
inline void find_all_cuts() {
  int i;
  cutn=0; gusfield();
  for(i=0;i<n;i++) dfs(i,-1,i,inf);
}
```

2.9 Max flow with lower/upper bound

```cpp
// Max flow with lower/upper bound on edges
// source = 1 , sink = n
int in[ N ] , out[ N ];
int l[ M ] , r[ M ] , a[ M ] , b[ M ];
int solve(){
  flow.init( n );
  for( int i = 0 ; i < m ; i ++ ){
    in[ r[ i ] ] += a[ i ];
    out[ l[ i ] ] += a[ i ];
    flow.addEdge( l[ i ] , r[ i ] , b[ i ] - a[ i ] );
    // flow on edge from l[ i ] to r[ i ] should
    // be in [a[ i ], b[ i ]].
  }
  int nd = 0;
  for( int i = 1 ; i <= n ; i ++ ){
    if( in[ i ] < out[ i ] ){
      flow.addEdge( i , flow.t , out[ i ] - in[ i ] );
      nd += out[ i ] - in[ i ];
    }
    if( out[ i ] < in[ i ] )
      flow.addEdge( flow.s , i , in[ i ] - out[ i ] );
  }
  // original sink to source
  flow.addEdge( n , 1 , INF );
  if( flow.maxflow() != nd )
    // no solution
    return -1;
  int ans = flow.G[ 1 ].back().c; // source to sink
  flow.G[ 1 ].back().c = flow.G[ n ].back().c = 0;
  // take out super source and super sink
  for( size_t i = 0 ; i < flow.G[ flow.s ].size() ; i
      ++ ){
    flow.G[ flow.s ][ i ].c = 0;
    Edge &e = flow.G[ flow.s ][ i ];
    flow.G[ e.v ][ e.r ].c = 0;
  }
  for( size_t i = 0 ; i < flow.G[ flow.t ].size() ; i
      ++ ){
    flow.G[ flow.t ][ i ].c = 0;
    Edge &e = flow.G[ flow.t ][ i ];
    flow.G[ e.v ][ e.r ].c = 0;
  }
  flow.addEdge( flow.s , 1 , INF );
  flow.addEdge( n , flow.t , INF );
  flow.reset();
  return ans + flow.maxflow();
}
```

2.10 Relabel to Front

```cpp
/* Relabel-to-Front */
// tested with sgu-212 (more testing suggested)
int n,m,layer,src,sink,lvl[MAXN];
Edge ed[MAXM];
int deg[MAXN],adj[MAXN][MAXN];
int res[MAXN][MAXN]; // residual capacity
// graph (i.e. all things above) should be constructed
    beforehand
list<int> lst; // discharge list
int ef[MAXN],ht[MAXN];
// excess flow, height
int apt[MAXN]; // the next adj index to try push
inline void push(int v,int u) {
```

```
  int a=min(ef[v],res[v][u]);
  ef[v]-=a; ef[u]+=a;
  res[v][u]-=a; res[u][v]+=a;
}
inline void relabel(int v) {
  int i,u;
  ht[v]=2*n;
  for(i=0;i<deg[v];i++) {
    u=adj[v][i];
    if(res[v][u]) ht[v]=min(ht[u]+1,ht[v]);
  }
}
inline void initPreflow() {
  int i,u;
  lst.clear();
  for(i=0;i<n;i++) {
    ht[i]=ef[i]=0; apt[i]=0;
    if(i!=src&&i!=sink) lst.push_back(i);
  }
  ht[src]=n;
  for(i=0;i<deg[src];i++) {
    u=adj[src][i];
    ef[u]=res[src][u];
    ef[src]-=ef[u];
    res[u][src]=ef[u];
    res[src][u]=0;
  }
}
inline void discharge(int v) {
  int u;
  while(ef[v]) {
    if(apt[v]==deg[v]) {
      relabel(v);
      apt[v]=0;
      continue;
    }
    u=adj[v][apt[v]];
    if(res[v][u]&&ht[v]==ht[u]+1) push(v,u);
    else apt[v]++;
  }
}
inline void relabelToFront() {
  int oldh,v;
  list<int>::iterator it;
  initPreflow();
  for(it=lst.begin();it!=lst.end();it++) {
    v=*it; oldh=ht[v]; discharge(v);
    if(ht[v]>oldh) {
      lst.push_front(v);
      lst.erase(it);
      it=lst.begin();
    }
  }
}
```

2.11 Flow Method

```
Maximize c^T x subject to Ax ≤ b, x ≥ 0;
with the corresponding symmetric dual problem,
Minimize b^T y subject to A^T y ≥ c, y ≥ 0.

Maximize c^T x subject to Ax ≤ b;
with the corresponding asymmetric dual problem,
Minimize b^T y subject to A^T y = c, y ≥ 0.


Minimum vertex cover on bipartite graph =
Maximum matching on bipartite graph =
Max flow with source to one side, other side to sink

To reconstruct the minimum vertex cover, dfs from each
unmatched vertex on the left side and with unused edges
only. Equivalently, dfs from source with unused edges
only and without visiting sink. Then, a vertex is
    chosen
iff. it is on the left side and without visited or on
the right side and visited through dfs.
```

有源匯，有下界，最大流，無費用。

先從t連向s，容量設爲無限大。這樣就變成了無源匯的情況。將每條有下界的邊先滿上下界的流量，然後更新盈餘量（入的流量-出的流量）。新建超級源ss和超級匯tt，若某個點u的盈餘量>0則ss--->u，容量爲u的盈餘量。否則u--->tt，容量爲u的盈餘量的相反數。如果一個點的盈餘量>0，則它是一定要流出去的，所以要從ss連向它，使它去找這些流量的出路。建完了圖以後求一遍最大流，如果從ss連出的所有邊都滿流，則有解。在得到的殘留網路（原圖）上再求一次最大流即可。

3 Math

3.1 FFT

```
// const int MAXN = 262144;
// (must be 2^k)
// before any usage, run pre_fft() first
//
// To implement poly. multiply:
//
// fft( n , a );
// fft( n , b );
// for( int i = 0 ; i < n ; i++ )
//   c[ i ] = a[ i ] * b[ i ];
// fft( n , c , 1 );
//
// then you have the result in c :: [cplx]
typedef long double ld;
typedef complex<ld> cplx;
const ld PI = acosl(-1);
const cplx I(0, 1);
cplx omega[MAXN+1];
void pre_fft(){
  for(int i=0; i<=MAXN; i++)
    omega[i] = exp(i * 2 * PI / MAXN * I);
}
// n must be 2^k
void fft(int n, cplx a[], bool inv=false){
  int basic = MAXN / n;
  int theta = basic;
  for (int m = n; m >= 2; m >>= 1) {
    int mh = m >> 1;
    for (int i = 0; i < mh; i++) {
      cplx w = omega[inv ? MAXN-(i*theta%MAXN)
                         : i*theta%MAXN];
      for (int j = i; j < n; j += m) {
        int k = j + mh;
        cplx x = a[j] - a[k];
        a[j] += a[k];
        a[k] = w * x;
      }
    }
    theta = (theta * 2) % MAXN;
  }
  int i = 0;
  for (int j = 1; j < n - 1; j++) {
    for (int k = n >> 1; k > (i ^= k); k >>= 1);
    if (j < i) swap(a[i], a[j]);
  }
  if (inv)
    for (i = 0; i < n; i++)
      a[i] /= n;
}
```

3.2 NTT

```
LL P=2013265921,root=31;
int MAXNUM=4194304;
// Remember coefficient are mod P
/*
p=a*2^n+1
n   2^n            p              a      root
5   32             97             3      5
```

```
6    64          193         3    5
7    128         257         2    3
8    256         257         1    3
9    512         7681        15   17
10   1024        12289       12   11
11   2048        12289       6    11
12   4096        12289       3    11
13   8192        40961       5    3
14   16384       65537       4    3
15   32768       65537       2    3
16   65536       65537       1    3
17   131072      786433      6    10
18   262144      786433      3    10 (605028353,
     2308, 3)
19   524288      5767169     11   3
20   1048576     7340033     7    3
21   2097152     23068673    11   3
22   4194304     104857601   25   3
23   8388608     167772161   20   3
24   16777216    167772161   10   3
25   33554432    167772161   5    3 (1107296257, 33,
     10)
26   67108864    469762049   7    3
27   134217728   2013265921  15   31
*/
LL bigmod(LL a,LL b){
  if(b==0)return 1;
  return (bigmod((a*a)%P,b/2)*(b%2?a:1LL))%P;
}
LL inv(LL a,LL b){
  if(a==1)return 1;
  return (((LL)(a-inv(b%a,a))*b+1)/a)%b;
}
std::vector<LL> ps(MAXNUM);
std::vector<LL> rev(MAXNUM);
struct poly{
  std::vector<LL> co;
  int n;//polynomial degree = n
  poly(int d){n=d;co.resize(n+1,0);}
  void trans2(int NN){
    int r=0,st,N;
    unsigned int a,b;
    while((1<<r)<(NN>>1))++r;
    for(N=2;N<=NN;N<<=1,--r){
      for(st=0;st<NN;st+=N){
        int i,ss=st+(N>>1);
        for(i=(N>>1)-1;i>=0;--i){
          a=co[st+i]; b=(ps[i<<r]*co[ss+i])%P;
          co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
          co[ss+i]=a+P-b; if(co[ss+i]>=P)co[ss+i]-=P;
        }
      }
    }
  }
  void trans1(int NN){
    int r=0,st,N;
    unsigned int a,b;
    for(N=NN;N>1;N>>=1,++r){
      for(st=0;st<NN;st+=N){
        int i,ss=st+(N>>1);
        for(i=(N>>1)-1;i>=0;--i){
          a=co[st+i]; b=co[ss+i];
          co[st+i]=a+b; if(co[st+i]>=P)co[st+i]-=P;
          co[ss+i]=((a+P-b)*ps[i<<r])%P;
        }
      }
    }
  }
  poly operator*(const poly& _b)const{
    poly a=*this,b=_b;
    int k=n+b.n,i,N=1;
    while(N<=k)N*=2;
    a.co.resize(N,0); b.co.resize(N,0);
    int r=bigmod(root,(P-1)/N),Ni=inv(N,P);
    ps[0]=1;
    for(i=1;i<N;++i)ps[i]=(ps[i-1]*r)%P;
    a.trans1(N);b.trans1(N);
    for(i=0;i<N;++i)a.co[i]=((LL)a.co[i]*b.co[i])%P;
    r=inv(r,P);
    for(i=1;i<N/2;++i)std::swap(ps[i],ps[N-i]);
    a.trans2(N);
    for(i=0;i<N;++i)a.co[i]=((LL)a.co[i]*Ni)%P;
```

```
    a.n=n+_b.n; return a;
  }
};
```

3.3 Fast Walsh Transform

```
/*
 * xor convolution:
 * x = (x0,x1) , y = (y0,y1)
 * z = ( x0y0 + x1y1 , x0y1 + x1y0 )
 * =>
 * x' = ( x0+x1 , x0-x1 ) , y' = ( y0+y1 , y0-y1 )
 * z' = ( ( x0+x1 )( y0+y1 ) , ( x0-x1 )( y0-y1 ) )
 * z = (1/2) * z''
 * or convolution:
 * x = ( x0 , x0+x1 )
 * and convolution:
 * x = ( x0+x1 , x1 )
 */
typedef long long LL;
const int MAXN = (1<<20)+10;
const LL MOD = 1e9+7;
inline LL pw( LL x , LL k ) {
  LL res = 1;
  for( LL bs = x ; k ; k >>= 1, bs = (bs * bs)%MOD ){
    if( k&1 ) res = ( res * bs ) % MOD;
  }
  return res;
}
inline LL inv( LL x ) {
  return pw( x , MOD-2 );
}
inline void fwt( LL x[ MAXN ] , int N , bool inv=0 ) {
  for( int d = 1 ; d < N ; d <<= 1 ) {
    int d2 = d<<1;
    for( int s = 0 ; s < N ; s += d2 ) {
      for( int i = s , j = s+d ; i < s+d ; i++, j++ ){
        LL ta = x[ i ] , tb = x[ j ];
        x[ i ] = ta+tb;
        x[ j ] = ta-tb;
        if( x[ i ] >= MOD ) x[ i ] -= MOD;
        if( x[ j ] < 0 ) x[ j ] += MOD;
      }
    }
  }
  if( inv )
    for( int i = 0 ; i < N ; i++ ) {
      x[ i ] *= inv( N );
      x[ i ] %= MOD;
    }
}
```

3.4 BigInt

```
struct Bigint{
  static const int LEN = 60;
  static const int BIGMOD = 10000;
  int s;
  int vl, v[LEN];
  // vector<int> v;
  Bigint() : s(1) { vl = 0; }
  Bigint(long long a) {
    s = 1; vl = 0;
    if (a < 0) { s = -1; a = -a; }
    while (a) {
      push_back(a % BIGMOD);
      a /= BIGMOD;
    }
  }
  Bigint(string str) {
    s = 1; vl = 0;
    int stPos = 0, num = 0;
    if (!str.empty() && str[0] == '-') {
      stPos = 1;
      s = -1;
    }
    for (int i=SZ(str)-1, q=1; i>=stPos; i--) {
      num += (str[i] - '0') * q;
```

```cpp
      if ((q *= 10) >= BIGMOD) {
        push_back(num);
        num = 0; q = 1;
      }
    }
    if (num) push_back(num);
    n();
  }
  int len() const {
    return vl;
    //    return SZ(v);
  }
  bool empty() const { return len() == 0; }
  void push_back(int x) {
    v[vl++] = x;
    //    v.PB(x);
  }
  void pop_back() {
    vl--;
    //    v.pop_back();
  }
  int back() const {
    return v[vl-1];
    //    return v.back();
  }
  void n() {
    while (!empty() && !back()) pop_back();
  }
  void resize(int nl) {
    vl = nl;
    fill(v, v+vl, 0);
    //    v.resize(nl);
    //    fill(ALL(v), 0);
  }
  void print() const {
    if (empty()) { putchar('0'); return; }
    if (s == -1) putchar('-');
    printf("%d", back());
    for (int i=len()-2; i>=0; i--) printf("%.4d",v[i]);
  }
  friend std::ostream& operator << (std::ostream& out,
      const Bigint &a) {
    if (a.empty()) { out << "0"; return out; }
    if (a.s == -1) out << "-";
    out << a.back();
    for (int i=a.len()-2; i>=0; i--) {
      char str[10];
      snprintf(str, 5, "%.4d", a.v[i]);
      out << str;
    }
    return out;
  }
  int cp3(const Bigint &b)const {
    if (s != b.s) return s - b.s;
    if (s == -1) return -(*this).cp3(-b);
    if (len() != b.len()) return len()-b.len();//int
    for (int i=len()-1; i>=0; i--)
      if (v[i]!=b.v[i]) return v[i]-b.v[i];
    return 0;
  }
  bool operator<(const Bigint &b)const
    { return cp3(b)<0; }
  bool operator<=(const Bigint &b)const
    { return cp3(b)<=0; }
  bool operator==(const Bigint &b)const
    { return cp3(b)==0; }
  bool operator!=(const Bigint &b)const
    { return cp3(b)!=0; }
  bool operator>(const Bigint &b)const
    { return cp3(b)>0; }
  bool operator>=(const Bigint &b)const
    { return cp3(b)>=0; }
  Bigint operator - () const {
    Bigint r = (*this);
    r.s = -r.s;
    return r;
  }
  Bigint operator + (const Bigint &b) const {
    if (s == -1) return -(-(*this)+(-b));
    if (b.s == -1) return (*this)-(-b);
    Bigint r;
    int nl = max(len(), b.len());
```

```cpp
    r.resize(nl + 1);
    for (int i=0; i<nl; i++) {
      if (i < len()) r.v[i] += v[i];
      if (i < b.len()) r.v[i] += b.v[i];
      if(r.v[i] >= BIGMOD) {
        r.v[i+1] += r.v[i] / BIGMOD;
        r.v[i] %= BIGMOD;
      }
    }
    r.n();
    return r;
  }
  Bigint operator - (const Bigint &b) const {
    if (s == -1) return -(-(*this)-(-b));
    if (b.s == -1) return (*this)+(-b);
    if ((*this) < b) return -(b-(*this));
    Bigint r;
    r.resize(len());
    for (int i=0; i<len(); i++) {
      r.v[i] += v[i];
      if (i < b.len()) r.v[i] -= b.v[i];
      if (r.v[i] < 0) {
        r.v[i] += BIGMOD;
        r.v[i+1]--;
      }
    }
    r.n();
    return r;
  }
  Bigint operator * (const Bigint &b) {
    Bigint r;
    r.resize(len() + b.len() + 1);
    r.s = s * b.s;
    for (int i=0; i<len(); i++) {
      for (int j=0; j<b.len(); j++) {
        r.v[i+j] += v[i] * b.v[j];
        if(r.v[i+j] >= BIGMOD) {
          r.v[i+j+1] += r.v[i+j] / BIGMOD;
          r.v[i+j] %= BIGMOD;
        }
      }
    }
    r.n();
    return r;
  }
  Bigint operator / (const Bigint &b) {
    Bigint r;
    r.resize(max(1, len()-b.len()+1));
    int oriS = s;
    Bigint b2 = b; // b2 = abs(b)
    s = b2.s = r.s = 1;
    for (int i=r.len()-1; i>=0; i--) {
      int d=0, u=BIGMOD-1;
      while(d<u) {
        int m = (d+u+1)>>1;
        r.v[i] = m;
        if((r*b2) > (*this)) u = m-1;
        else d = m;
      }
      r.v[i] = d;
    }
    s = oriS;
    r.s = s * b.s;
    r.n();
    return r;
  }
  Bigint operator % (const Bigint &b) {
    return (*this)-(*this)/b*b;
  }
};
```

3.5 Linear Recurrence

```cpp
LL n, m;
LL dp[ N + N ];
void pre_dp(){
  dp[ 0 ] = 1;
  LL bdr = min( m + m , n );
  for( LL i = 1 ; i <= bdr ; i ++ )
    for( LL j = i - 1 ; j >= max(0LL , i - m) ; j -- )
```

```cpp
        dp[ i ] = add( dp[ i ] , dp[ j ] );
}
vector<LL> Mul( vector<LL>& v1, vector<LL>& v2 ){
  int _sz1 = (int)v1.size();
  int _sz2 = (int)v2.size();
  assert( _sz1 == m );
  assert( _sz2 == m );
  vector<LL> _v( m + m );
  for( int i = 0 ; i < m + m ; i ++ ) _v[ i ] = 0;
// expand
  for( int i = 0 ; i < _sz1 ; i ++ )
    for( int j = 0 ; j < _sz2 ; j ++ )
      _v[ i + j + 1 ] = add( _v[ i + j + 1 ] ,
                             mul(v1[ i ] , v2[ j ]) );
// shrink
  for( int i = 0 ; i < m ; i ++ )
    for( int j = 1 ; j <= m ; j ++ )
      _v[ i + j ] = add( _v[ i + j ] , _v[ i ] );
  for( int i = 0 ; i < m ; i ++ )
    _v[ i ] = _v[ i + m ];
  _v.resize( m );
  return _v;
}
vector<LL> I, A;
void solve(){
  pre_dp();
  if( n <= m + m ){
    printf( "%lld\n" , dp[ n ] );
    exit( 0 );
  }
  I.resize( m );
  A.resize( m );
  for( int i = 0 ; i < m ; i ++ ) I[ i ] = A[ i ] = 1;
// dp[ n ] = /Sum_{i=0}^{m-1} A_i * dp[ n - i - 1 ]
  LL dlt = ( n - m ) / m;
  LL rdlt = dlt * m;
  while( dlt ){
    if( dlt & 1LL ) I = Mul( I , A );
    A = Mul( A , A );
    dlt >>= 1;
  }
  LL ans = 0;
  for( int i = 0 ; i < m ; i ++ )
    ans = add(ans, mul(I[i], dp[n - i - 1 - rdlt]));
  printf( "%lld\n" , ans );
}
```

3.6 Miller Rabin

```cpp
// n < 4,759,123,141        3 :  2, 7, 61
// n < 1,122,004,669,633    4 :  2, 13, 23, 1662803
// n < 3,474,749,660,383       6 :  pirmes <= 13
// n < 2^64                 7 :
// 2, 325, 9375, 28178, 450775, 9780504, 1795265022
// Make sure testing integer is in range [2, n-2] if
// you want to use magic.
LL power(LL x,LL p,LL mod){
  LL s=1,m=x;
  while(p) {
    if(p&1) s=mult(s,m,mod);
    p>>=1;
    m=mult(m,m,mod);
  }
  return s;
}
bool witness(LL a,LL n,LL u,int t){
  LL x=power(a,u,n);
  for(int i=0;i<t;i++) {
    LL nx=mult(x,x,n);
    if(nx==1&&x!=1&&x!=n-1) return 1;
    x=nx;
  }
  return x!=1;
}
bool miller_rabin(LL n,int s=100) {
  // iterate s times of witness on n
  // return 1 if prime, 0 otherwise
  if(n<2) return 0;
  if(!(n&1)) return n==2;
  LL u=n-1;
  int t=0;
  // n-1 = u*2^t
  while(!(u&1)) {
    u>>=1;
    t++;
  }
  while(s--) {
    LL a=randll()%(n-1)+1;
    if(witness(a,n,u,t)) return 0;
  }
  return 1;
}
```

3.7 Simplex

```cpp
const int MAXN = 111;
const int MAXM = 111;
const double eps = 1E-10;
double a[MAXN][MAXM], b[MAXN], c[MAXM], d[MAXN][MAXM];
double x[MAXM];
int ix[MAXN + MAXM]; // !!! array all indexed from 0
// max{cx} subject to {Ax<=b,x>=0}
// n: constraints, m: vars !!!
// x[] is the optimal solution vector
//
// usage :
// value = simplex(a, b, c, N, M);
double simplex(double a[MAXN][MAXM], double b[MAXN],
               double c[MAXM], int n, int m){
  ++m;
  int r = n, s = m - 1;
  memset(d, 0, sizeof(d));
  for (int i = 0; i < n + m; ++i) ix[i] = i;
  for (int i = 0; i < n; ++i) {
    for (int j = 0; j < m - 1; ++j) d[i][j] = -a[i][j];
    d[i][m - 1] = 1;
    d[i][m] = b[i];
    if (d[r][m] > d[i][m]) r = i;
  }
  for (int j = 0; j < m - 1; ++j) d[n][j] = c[j];
  d[n + 1][m - 1] = -1;
  for (double dd;; ) {
    if (r < n) {
      int t = ix[s]; ix[s] = ix[r + m]; ix[r + m] = t;
      d[r][s] = 1.0 / d[r][s];
      for (int j = 0; j <= m; ++j)
        if (j != s) d[r][j] *= -d[r][s];
      for (int i = 0; i <= n + 1; ++i) if (i != r) {
        for (int j = 0; j <= m; ++j) if (j != s)
          d[i][j] += d[r][j] * d[i][s];
        d[i][s] *= d[r][s];
      }
    }
    r = -1; s = -1;
    for (int j = 0; j < m; ++j)
      if (s < 0 || ix[s] > ix[j]) {
        if (d[n + 1][j] > eps ||
            (d[n + 1][j] > -eps && d[n][j] > eps))
          s = j;
      }
    if (s < 0) break;
    for (int i = 0; i < n; ++i) if (d[i][s] < -eps) {
      if (r < 0 ||
          (dd = d[r][m] / d[r][s] - d[i][m] / d[i][s])
              < -eps ||
          (dd < eps && ix[r + m] > ix[i + m]))
        r = i;
    }
    if (r < 0) return -1; // not bounded
  }
  if (d[n + 1][m] < -eps) return -1; // not executable
  double ans = 0;
  for(int i=0; i<m; i++) x[i] = 0;
  for (int i = m; i < n + m; ++i) { // the missing
      enumerated x[i] = 0
    if (ix[i] < m - 1){
      ans += d[i - m][m] * c[ix[i]];
      x[ix[i]] = d[i-m][m];
    }
  }
}
```

```
    return ans;
}
```

3.8 Faulhaber

```
/* faulhaber's formula -
 * cal power sum formula of all p=1~k in O(k^2) */
#define MAXK 2500
const int mod = 1000000007;
int b[MAXK];
// bernoulli number
int inv[MAXK+1];
// inverse
int cm[MAXK+1][MAXK+1]; // combinactories
int co[MAXK][MAXK+2];
// coeeficient of x^j when p=i
int add(int a,int b) { return a+b<mod?a+b:a+b-mod; }
int sub(int a,int b) { return a<b?a-b+mod:a-b; }
inline int getinv(int x) {
  int a=x,b=mod,a0=1,a1=0,b0=0,b1=1;
  while(b) {
    int q,t;
    q=a/b; t=b; b=a-b*q; a=t;
    t=b0; b0=a0-b0*q; a0=t;
    t=b1; b1=a1-b1*q; a1=t;
  }
  return a0<0?a0+mod:a0;
}
inline void pre() {
  /* combinational */
  for(int i=0;i<=MAXK;i++) {
    cm[i][0]=cm[i][i]=1;
    for(int j=1;j<i;j++)
      cm[i][j]=add(cm[i-1][j-1],cm[i-1][j]);
  }
  /* inverse */
  for(int i=1;i<=MAXK;i++) inv[i]=getinv(i);
  /* bernoulli */
  b[0]=1; b[1]=getinv(2); // with b[1] = 1/2
  for(int i=2;i<MAXK;i++) {
    if(i&1) { b[i]=0; continue; }
    b[i]=1;
    for(int j=0;j<i;j++)
      b[i]=sub(b[i],
              (LL)cm[i][j]*b[j]%mod*inv[i-j+1]%mod);
  }
  /* faulhaber */
  // sigma_x=1~n {x^p} = 1/(p+1) * sigma_j=0~p { C(p+1,
      j) * Bj * n^(p-j+1)}
  for(int i=1;i<MAXK;i++) {
    co[i][0]=0;
    for(int j=0;j<=i;j++)
      co[i][i-j+1]=
        (LL)inv[i+1]%mod*cm[i+1][j]%mod*b[j]%mod;
  }
}
inline int power(int x,int p) {
  int s=1,m=x;
  while(p) {
    if(p&1) s=(LL)s*m%mod;
    p>>=1; m=(LL)m*m%mod;
  }
  return s;
}
/* sample usage: return f(n,p) = sigma_x=1~n (x^p) */
inline int solve(int n,int p) {
  int sol=0,m=n;
  for(int i=1;i<=p+1;i++) {
    sol=add(sol,(LL)co[p][i]*m%mod);
    m=(LL)m*n%mod;
  }
  return sol;
}
```

3.9 Chinese Remainder

```
int pfn;
// number of distinct prime factors
```

```
int pf[MAXN]; // prime factor powers
int rem[MAXN]; // corresponding remainder
int pm[MAXN];
inline void generate_primes() {
  int i,j;
  pnum=1;
  prime[0]=2;
  for(i=3;i<MAXVAL;i+=2) {
    if(nprime[i]) continue;
    prime[pnum++]=i;
    for(j=i*i;j<MAXVAL;j+=i) nprime[j]=1;
  }
}
inline int inverse(int x,int p) {
  int q,tmp,a=x,b=p;
  int a0=1,a1=0,b0=0,b1=1;
  while(b) {
    q=a/b; tmp=b; b=a-b*q; a=tmp;
    tmp=b0; b0=a0-b0*q; a0=tmp;
    tmp=b1; b1=a1-b1*q; a1=tmp;
  }
  return a0;
}
inline void decompose_mod() {
  int i,p,t=mod;
  pfn=0;
  for(i=0;i<pnum&&prime[i]<=t;i++) {
    p=prime[i];
    if(t%p==0) {
      pf[pfn]=1;
      while(t%p==0) {
        t/=p;
        pf[pfn]*=p;
      }
      pfn++;
    }
  }
  if(t>1) pf[pfn++]=t;
}
inline int chinese_remainder() {
  int i,m,s=0;
  for(i=0;i<pfn;i++) {
    m=mod/pf[i];
    pm[i]=(LL)m*inverse(m,pf[i])%mod;
    s=(s+(LL)pm[i]*rem[i])%mod;
  }
  return s;
}
```

3.10 Pollard Rho

```
// does not work when n is prime
LL modit(LL x,LL mod) {
  if(x>=mod) x-=mod;
  //if(x<0) x+=mod;
  return x;
}
LL mult(LL x,LL y,LL mod) {
  LL s=0,m=x%mod;
  while(y) {
    if(y&1) s=modit(s+m,mod);
    y>>=1;
    m=modit(m+m,mod);
  }
  return s;
}
LL f(LL x,LL mod) {
  return modit(mult(x,x,mod)+1,mod);
}
LL pollard_rho(LL n) {
  if(!(n&1)) return 2;
  while (true) {
    LL y=2, x=rand()%(n-1)+1, res=1;
    for (int sz=2; res==1; sz*=2) {
      for (int i=0; i<sz && res<=1; i++) {
        x = f(x, n);
        res = __gcd(abs(x-y), n);
      }
      y = x;
    }
```

```
      if (res!=0 && res!=n) return res;
    }
  }
}
```

3.11 Poly Generator

```
class PolyGen {
  /* for a nth-order polynomial f(x), *
   * given f(0), f(1), ..., f(n) *
   * express f(x) as sigma_i{c_i*C(x,i)} */
 public:
  int n;
  vector<LL> coef;
  // initialize and calculate f(x), vector _fx should
  // be filled with f(0) to f(n)
  PolyGen(int _n,vector<LL> _fx):n(_n),coef(_fx){
    for(int i=0;i<n;i++)
      for(int j=n;j>i;j--)
        coef[j]-=coef[j-1];
  }
  // evaluate f(x), runs in O(n)
  LL eval(int x) {
    LL m=1,ret=0;
    for(int i=0;i<=n;i++) {
      ret+=coef[i]*m;
      m=m*(x-i)/(i+1);
    }
    return ret;
  }
};
```

3.12 Matrix Pseudo Inverse

```
Mat pinv( Mat m ){
  Mat res = I;
  FZ( used );
  for( int i = 0 ; i < W ; i ++ ){
    int piv = -1;
    for( int j = 0 ; j < W ; j ++ ){
      if( used[ j ] ) continue;
      if( abs( m.v[ j ][ i ] ) > EPS ){
        piv = j;
        break;
      }
    }
    if( piv == -1 ) continue;
    used[ i ] = true;
    swap( m.v[ piv ], m.v[ i ] );
    swap( res.v[ piv ], res.v[ i ] );
    LD rat = m.v[ i ][ i ];
    for( int j = 0 ; j < W ; j ++ ){
      m.v[ i ][ j ] /= rat;
      res.v[ i ][ j ] /= rat;
    }
    for( int j = 0 ; j < W ; j ++ ){
      if( j == i ) continue;
      rat = m.v[ j ][ i ];
      for( int k = 0 ; k < W ; k ++ ){
        m.v[ j ][ k ] -= rat * m.v[ i ][ k ];
        res.v[ j ][ k ] -= rat * res.v[ i ][ k ];
      }
    }
  }
  for( int i = 0 ; i < W ; i ++ ){
    if( used[ i ] ) continue;
    for( int j = 0 ; j < W ; j ++ )
      res.v[ i ][ j ] = 0;
  }
  return res;
}
```

3.13 ax+by=gcd

```
typedef pair<int, int> PII;
PII gcd(int a, int b){
  if(b == 0) return make_pair(1, 0);
```

```
  else{
    int p = a / b;
    PII q = gcd(b, a % b);
    return make_pair(q.second, q.first - q.second * p);
  }
}
```

3.14 Mod

```
/// _fd(a,b)  floor(a/b).
/// _rd(a,m)  a-floor(a/m)*m.
/// _pv(a,m,r) largest x s.t x<=a && x%m == r.
/// _nx(a,m,r) smallest x s.t x>=a && x%m == r.
/// _ct(a,b,m,r) |A| , A = { x : a<=x<=b && x%m == r }.
int _fd(int a,int b){ return a<0?(-~a/b-1):a/b; }
int _rd(int a,int m){ return a-_fd(a,m)*m; }
int _pv(int a,int m,int r){
    r=(r%m+m)%m;
    return _fd(a-r,m)*m+r;
}
int _nt(int a,int m,int r){
    m=abs(m);
    r=(r%m+m)%m;
    return _fd(a-r-1,m)*m+r+m;
}
int _ct(int a,int b,int m,int r){
    m=abs(m);
    a=_nt(a,m,r);
    b=_pv(b,m,r);
    return (a>b)?0:((b-a+m)/m);
}
```

3.15 Primes and μ function

```
/*
 * 12721
 * 13331
 * 14341
 * 75577
 * 123457
 * 222557
 * 556679
 * 999983
 * 1097774749
 * 1076767633
 * 100102021
 * 999997771
 * 1001010013
 * 1000512343
 * 987654361
 * 999991231
 * 999888733
 * 98789101
 * 987777733
 * 999991921
 * 1010101333
 * 1010102101
 * 1000000000039
 * 1000000000000037
 * 2305843009213693951
 * 4611686018427387847
 * 9223372036854775783
 * 18446744073709551557
 */
int mu[ N ] , p_tbl[ N ];
vector<int> primes;
void sieve() {
  mu[ 1 ] = p_tbl[ 1 ] = 1;
  for( int i = 2 ; i < N ; i ++ ){
    if( !p_tbl[ i ] ){
      p_tbl[ i ] = i;
      primes.push_back( i );
      mu[ i ] = -1;
    }
    for( int p : primes ){
      int x = i * p;
      if( x >= M ) break;
      p_tbl[ x ] = p;
```

```
        mu[ x ] = -mu[ i ];
        if( i % p == 0 ){
          mu[ x ] = 0;
          break;
        }
      }
    }
}
vector<int> factor( int x ){
  vector<int> fac{ 1 };
  while( x > 1 ){
    int fn = SZ(fac), p = p_tbl[ x ], pos = 0;
    while( x % p == 0 ){
      x /= p;
      for( int i = 0 ; i < fn ; i ++ )
        fac.PB( fac[ pos ++ ] * p );
    }
  }
  return fac;
}
```

3.16 Result

```
/*
Lucas ' Theorem:
  For non-negative integer n,m and prime P,
  C(m,n) mod P = C(m/M,n/M) * C(m%M,n%M) mod P
  = mult_i ( C(m_i,n_i) )
  where m_i is the i-th digit of m in base P.
--
Sum of Two Squares Thm (Legendre)
  For a given positive integer N, let
  D1 = (# of d \in \N dividing N that d=1(mod 4))
  D3 = (# of d \in \N dividing N that d=3(mod 4))
  then N can be written as a sum of two squares in
  exactly R(N) = 4(D1-D3) ways.
--
Difference of D1-D3 Thm
  let N=2^t * [p1^e1 *...* pr^er] * [q1^f1 *...* qs^fs]
              <-mod 4 = 1 prime->   <-mod 4 = 3 prime->
  then D1 - D3 = (e1+1)(e2+1)...(er+1) if fi all even
                 0                      if any fi is odd
--
Pick ' s Theorem
A = i + b/2 - 1
*/
```

4 Geometry

4.1 halfPlaneIntersection

4.2 Intersection of 2 lines

```
Pt interPnt( Line l1, Line l2, bool &res ){
  Pt p1, p2, q1, q2;
  tie(p1, p2) = l1;
  tie(q1, q2) = l2;
  double f1 = (p2 - p1) ^ (q1 - p1);
  double f2 = (p2 - p1) ^ (p1 - q2);
  double f = (f1 + f2);
  if( fabs(f) < eps) {
    res = false;
    return {0, 0};
  }
  res = true;
  return q1 * (f2 / f) + q2 * (f1 / f);
}
bool isin( Line l0, Line l1, Line l2 ){
  // Check inter(l1, l2) in l0
  bool res;
  Pt p = interPnt(l1, l2, res);
  return ( (l0.SE - l0.FI) ^ (p - l0.FI) ) > eps;
}
/* If no solution, check: 1. ret.size() < 3
 * Or more precisely, 2. interPnt(ret[0], ret[1])
 * in all the lines. (use (l.S - l.F) ^ (p - l.F) > 0
```

```
 */
/* --^-- Line.FI --^-- Line.SE --^-- */
vector<Line> halfPlaneInter( vector<Line> lines ){
  int sz = lines.size();
  vector<double> ata(sz), ord(sz);
  for( int i=0; i<sz; i++) {
    ord[i] = i;
    Pt d = lines[i].SE - lines[i].FI;
    ata[i] = atan2(d.Y, d.X);
  }
  sort( ord.begin(), ord.end(), [&](int i, int j) {
    if( fabs(ata[i] - ata[j]) < eps ){
      return ( (lines[i].SE - lines[i].FI) ^
               (lines[j].SE - lines[i].FI) ) < 0;
    }
    return ata[i] < ata[j];
  });
  vector<Line> fin;
  for (int i=0; i<sz; i++)
    if (!i or fabs(ata[ord[i]] - ata[ord[i-1]]) > eps)
      fin.PB(lines[ord[i]]);
  deque<Line> dq;
  for (int i=0; i<(int)(fin.size()); i++) {
    while((int)(dq.size()) >= 2 and
        not isin(fin[i], dq[(int)(dq.size())-2],
                         dq[(int)(dq.size())-1]))
      dq.pop_back();
    while((int)(dq.size()) >= 2 and
        not isin(fin[i], dq[0], dq[1]))
      dq.pop_front();
    dq.push_back(fin[i]);
  }
  while( (int)(dq.size()) >= 3 and
      not isin(dq[0], dq[(int)(dq.size())-2],
                      dq[(int)(dq.size())-1]))
    dq.pop_back();
  while( (int)(dq.size()) >= 3 and
      not isin(dq[(int)(dq.size())-1], dq[0], dq[1]))
    dq.pop_front();
  vector<Line> res(dq.begin(),dq.end());
  return res;
}
```

4.3 Intersection of 2 circles

```
vector<Pt> interCircle( Pt o1 , D r1 , Pt o2 , D r2 ){
  D d2 = ( o1 - o2 ) * ( o1 - o2 );
  D d = sqrt(d2);
  if( d > r1 + r2 ) return {};
  Pt u = (o1+o2)*0.5 + (o1-o2)*((r2*r2-r1*r1)/(2*d2));
  D A = sqrt((r1+r2+d)*(r1-r2+d)*(r1+r2-d)*(-r1+r2+d));
  Pt v = Pt( o1.Y-o2.Y , -o1.X + o2.X ) * A / (2*d2);
  return {u+v, u-v};
}
```

4.4 Intersection of 2 segments

```
int ori( const PLL& o , const PLL& a , const PLL& b ){
  LL ret = ( a - o ) ^ ( b - o );
  return ret / max( 1ll , abs( ret ) );
}
// p1 == p2 || q1 == q2 need to be handled
bool banana( const PLL& p1 , const PLL& p2 ,
             const PLL& q1 , const PLL& q2 ){
  if( ( ( p2 - p1 ) ^ ( q2 - q1 ) ) == 0 ){ // parallel
    if( ori( p1 , p2 , q1 ) ) return false;
    return ( ( p1 - q1 ) * ( p2 - q1 ) ) <= 0 ||
           ( ( p1 - q2 ) * ( p2 - q2 ) ) <= 0 ||
           ( ( q1 - p1 ) * ( q2 - p1 ) ) <= 0 ||
           ( ( q1 - p2 ) * ( q2 - p2 ) ) <= 0;
  }
  return (ori( p1, p2, q1 ) * ori( p1, p2, q2 )<=0) &&
         (ori( q1, q2, p1 ) * ori( q1, q2, p2 )<=0);
}
```

4.5 KD Tree

```cpp
const int MXN = 100005;
struct KDTree {
  struct Node {
    int x,y,x1,y1,x2,y2;
    int id,f;
    Node *L, *R;
  }tree[MXN];
  int n;
  Node *root;
  LL dis2(int x1, int y1, int x2, int y2) {
    LL dx = x1-x2;
    LL dy = y1-y2;
    return dx*dx+dy*dy;
  }
  static bool cmpx(Node& a, Node& b){ return a.x<b.x; }
  static bool cmpy(Node& a, Node& b){ return a.y<b.y; }
  void init(vector<pair<int,int>> ip) {
    n = ip.size();
    for (int i=0; i<n; i++) {
      tree[i].id = i;
      tree[i].x = ip[i].first;
      tree[i].y = ip[i].second;
    }
    root = build_tree(0, n-1, 0);
  }
  Node* build_tree(int L, int R, int dep) {
    if (L>R) return nullptr;
    int M = (L+R)/2;
    tree[M].f = dep%2;
    nth_element(tree+L, tree+M, tree+R+1, tree[M].f ?
        cmpy : cmpx);
    tree[M].x1 = tree[M].x2 = tree[M].x;
    tree[M].y1 = tree[M].y2 = tree[M].y;

    tree[M].L = build_tree(L, M-1, dep+1);
    if (tree[M].L) {
      tree[M].x1 = min(tree[M].x1, tree[M].L->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].L->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].L->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].L->y2);
    }
    tree[M].R = build_tree(M+1, R, dep+1);
    if (tree[M].R) {
      tree[M].x1 = min(tree[M].x1, tree[M].R->x1);
      tree[M].x2 = max(tree[M].x2, tree[M].R->x2);
      tree[M].y1 = min(tree[M].y1, tree[M].R->y1);
      tree[M].y2 = max(tree[M].y2, tree[M].R->y2);
    }
    return tree+M;
  }
  int touch(Node* r, int x, int y, LL d2){
    LL dis = sqrt(d2)+1;
    if (x<r->x1-dis || x>r->x2+dis ||
        y<r->y1-dis || y>r->y2+dis)
      return 0;
    return 1;
  }
  void nearest(Node* r, int x, int y,
               int &mID, LL &md2){
    if (!r || !touch(r, x, y, md2)) return;
    LL d2 = dis2(r->x, r->y, x, y);
    if (d2 < md2 || (d2 == md2 && mID < r->id)) {
      mID = r->id;
      md2 = d2;
    }
    // search order depends on split dim
    if ((r->f == 0 && x < r->x) ||
        (r->f == 1 && y < r->y)) {
      nearest(r->L, x, y, mID, md2);
      nearest(r->R, x, y, mID, md2);
    } else {
      nearest(r->R, x, y, mID, md2);
      nearest(r->L, x, y, mID, md2);
    }
  }
  int query(int x, int y) {
    int id = 1029384756;
    LL d2 = 102938475612345678LL;
    nearest(root, x, y, id, d2);
    return id;
  }
}tree;
```

4.6 Poly Union

```cpp
#define eps 1e-8
class PY{ public:
  int n;
  Pt pt[5];
  Pt& operator[](const int x){ return pt[x]; }
  void input(){
    int i; n=4;
    for(i=0;i<n;i++) scanf("%lf%lf",&pt[i].x,&pt[i].y);
  }
  double getArea(){
    int i; double s=pt[n-1]^pt[0];
    for(i=0;i<n-1;i++) s+=pt[i]^pt[i+1];
    return s/2;
  }
};
PY py[500];
pair<double,int> c[5000];
inline double segP(Pt &p,Pt &p1,Pt &p2){
  if(SG(p1.x-p2.x)==0) return (p.y-p1.y)/(p2.y-p1.y);
  return (p.x-p1.x)/(p2.x-p1.x);
}
double polyUnion(int n){
  int i,j,ii,jj,ta,tb,r,d;
  double z,w,s,sum,tc,td;
  for(i=0;i<n;i++) py[i][py[i].n]=py[i][0];
  sum=0;
  for(i=0;i<n;i++){
    for(ii=0;ii<py[i].n;ii++){
      r=0;
      c[r++]=make_pair(0.0,0);
      c[r++]=make_pair(1.0,0);
      for(j=0;j<n;j++){
        if(i==j) continue;
        for(jj=0;jj<py[j].n;jj++){
          ta=SG(tri(py[i][ii],py[i][ii+1],py[j][jj]));
          tb=SG(tri(py[i][ii],py[i][ii+1],py[j][jj+1]))
              ;
          if(ta==0 && tb==0){
            if((py[j][jj+1]-py[j][jj])*(py[i][ii+1]-py[
                i][ii])>0 && j<i){
              c[r++]=make_pair(segP(py[j][jj],py[i][ii
                  ],py[i][ii+1]),1);
              c[r++]=make_pair(segP(py[j][jj+1],py[i][
                  ii],py[i][ii+1]),-1);
            }
          }else if(ta>=0 && tb<0){
            tc=tri(py[j][jj],py[j][jj+1],py[i][ii]);
            td=tri(py[j][jj],py[j][jj+1],py[i][ii+1]);
            c[r++]=make_pair(tc/(tc-td),1);
          }else if(ta<0 && tb>=0){
            tc=tri(py[j][jj],py[j][jj+1],py[i][ii]);
            td=tri(py[j][jj],py[j][jj+1],py[i][ii+1]);
            c[r++]=make_pair(tc/(tc-td),-1);
          }
        }
      }
      sort(c,c+r);
      z=min(max(c[0].first,0.0),1.0);
      d=c[0].second; s=0;
      for(j=1;j<r;j++){
        w=min(max(c[j].first,0.0),1.0);
        if(!d) s+=w-z;
        d+=c[j].second; z=w;
      }
      sum+=(py[i][ii]^py[i][ii+1])*s;
    }
  }
  return sum/2;
}
int main(){
  int n,i,j,k;
  double sum,ds;
  scanf("%d",&n); sum=0;
  for(i=0;i<n;i++){
```

```
      py[i].input();
      ds=py[i].getArea();
      if(ds<0){
        for(j=0,k=py[i].n-1;j<k;j++,k--) swap(py[i][j],
            py[i][k]);
        ds=-ds;
      } sum+=ds;
    } printf("%.9f\n",sum/polyUnion(n));
}
```

4.7 Lower Concave Hull

```
/****
  maintain a "concave hull" that support the following
  1. insertion of a line
  2. query of height(y) on specific x on the hull
 ****/
/* set as needed */
typedef long double LD;
const LD eps=1e-9;
const LD inf=1e19;
class Seg {
 public:
  LD m,c,x1,x2; // y=mx+c
  bool flag;
  Seg(
    LD _m,LD _c,LD _x1=-inf,LD _x2=inf,bool _flag=0)
    :m(_m),c(_c),x1(_x1),x2(_x2),flag(_flag) {}
  LD evaly(LD x) const {
    return m*x+c;
  }
  const bool operator<(LD x) const {
    return x2-eps<x;
  }
  const bool operator<(const Seg &b) const {
    if(flag||b.flag) return *this<b.x1;
    return m+eps<b.m;
  }
};
class LowerConcaveHull { // maintain a hull like: \__/
 public:
  set<Seg> hull;
  /* functions */
  LD xintersection(Seg a,Seg b) {
    return (a.c-b.c)/(b.m-a.m);
  }
  inline set<Seg>::iterator replace(set<Seg> &
      hull,set<Seg>::iterator it,Seg s) {
    hull.erase(it);
    return hull.insert(s).first;
  }
  void insert(Seg s) {
    // insert a line and update hull
    set<Seg>::iterator it=hull.find(s);
    // check for same slope
    if(it!=hull.end()) {
      if(it->c+eps>=s.c) return;
      hull.erase(it);
    }
    // check if below whole hull
    it=hull.lower_bound(s);
    if(it!=hull.end()&&
       s.evaly(it->x1)<=it->evaly(it->x1)+eps) return;
    // update right hull
    while(it!=hull.end()) {
      LD x=xintersection(s,*it);
      if(x>=it->x2-eps) hull.erase(it++);
      else {
        s.x2=x;
        it=replace(hull,it,Seg(it->m,it->c,x,it->x2));
        break;
      }
    }
    // update left hull
    while(it!=hull.begin()) {
      LD x=xintersection(s,*(--it));
      if(x<=it->x1+eps) hull.erase(it++);
      else {
        s.x1=x;
        it=replace(hull,it,Seg(it->m,it->c,it->x1,x));
```

```
        break;
      }
    }
    // insert s
    hull.insert(s);
  }
  void insert(LD m,LD c) { insert(Seg(m,c)); }
  LD query(LD x) { // return y @ given x
    set<Seg>::iterator it =
      hull.lower_bound(Seg(0.0,0.0,x,x,1));
    return it->evaly(x);
  }
};
```

4.8 Min Enclosing Circle

```
struct Mec{
  // return pair of center and r
  static const int N = 101010;
  int n;
  Pt p[ N ], cen;
  double r2;
  void init( int _n , Pt _p[] ){
    n = _n;
    memcpy( p , _p , sizeof(Pt) * n );
  }
  double sqr(double a){ return a*a; }
  Pt center(Pt p0, Pt p1, Pt p2) {
    Pt a = p1-p0;
    Pt b = p2-p0;
    double c1=norm2( a ) * 0.5;
    double c2=norm2( b ) * 0.5;
    double d = a ^ b;
    double x = p0.X + (c1 * b.Y - c2 * a.Y) / d;
    double y = p0.Y + (a.X * c2 - b.X * c1) / d;
    return Pt(x,y);
  }
  pair<Pt,double> solve(){
    random_shuffle(p,p+n);
    r2=0;
    for (int i=0; i<n; i++){
      if (norm2(cen-p[i]) <= r2) continue;
      cen = p[i];
      r2 = 0;
      for (int j=0; j<i; j++){
        if (norm2(cen-p[j]) <= r2) continue;
        cen = Pt((p[i].X+p[j].X)*0.5, (p[i].Y+p[j].Y)
            *0.5);
        r2 = norm2(cen-p[j]);
        for (int k=0; k<j; k++){
          if (norm2(cen-p[k]) <= r2) continue;
          cen = center(p[i],p[j],p[k]);
          r2 = norm2(cen-p[k]);
        }
      }
    }
    return {cen,sqrt(r2)};
  }
} mec;
```

4.9 Minkowski sum

```
/* convex hull Minkowski Sum*/
#define INF 1000000000000000LL
int pos( const Pt& tp ){
  if( tp.Y == 0 ) return tp.X > 0 ? 0 : 1;
  return tp.Y > 0 ? 0 : 1;
}
#define N 300030
Pt pt[ N ], qt[ N ], rt[ N ];
LL Lx,Rx;
int dn,un;
inline bool cmp( Pt a, Pt b ){
  int pa=pos( a ),pb=pos( b );
  if(pa==pb) return (a^b)>0;
  return pa<pb;
}
int minkowskiSum(int n,int m){
```

```
   int i,j,r,p,q,fi,fj;
   for(i=1,p=0;i<n;i++){
     if( pt[i].Y<pt[p].Y ||
         (pt[i].Y==pt[p].Y && pt[i].X<pt[p].X) ) p=i; }
   for(i=1,q=0;i<m;i++){
     if( qt[i].Y<qt[q].Y ||
         (qt[i].Y==qt[q].Y && qt[i].X<qt[q].X) ) q=i; }
   rt[0]=pt[p]+qt[q];
   r=1; i=p; j=q; fi=fj=0;
   while(1){
     if((fj&&j==q) ||
        ( (!fi||i!=p) &&
          cmp(pt[(p+1)%n]-pt[p],qt[(q+1)%m]-qt[q]) ) ){
       rt[r]=rt[r-1]+pt[(p+1)%n]-pt[p];
       p=(p+1)%n;
       fi=1;
     }else{
       rt[r]=rt[r-1]+qt[(q+1)%m]-qt[q];
       q=(q+1)%m;
       fj=1;
     }
     if(r<=1 || ((rt[r]-rt[r-1])^(rt[r-1]-rt[r-2]))!=0)
       r++;
     else rt[r-1]=rt[r];
     if(i==p && j==q) break;
   }
   return r-1;
}
void initInConvex(int n){
   int i,p,q;
   LL Ly,Ry;
   Lx=INF; Rx=-INF;
   for(i=0;i<n;i++){
     if(pt[i].X<Lx) Lx=pt[i].X;
     if(pt[i].X>Rx) Rx=pt[i].X;
   }
   Ly=Ry=INF;
   for(i=0;i<n;i++){
     if(pt[i].X==Lx && pt[i].Y<Ly){ Ly=pt[i].Y; p=i; }
     if(pt[i].X==Rx && pt[i].Y<Ry){ Ry=pt[i].Y; q=i; }
   }
   for(dn=0,i=p;i!=q;i=(i+1)%n){ qt[dn++]=pt[i]; }
   qt[dn]=pt[q]; Ly=Ry=-INF;
   for(i=0;i<n;i++){
     if(pt[i].X==Lx && pt[i].Y>Ly){ Ly=pt[i].Y; p=i; }
     if(pt[i].X==Rx && pt[i].Y>Ry){ Ry=pt[i].Y; q=i; }
   }
   for(un=0,i=p;i!=q;i=(i+n-1)%n){ rt[un++]=pt[i]; }
   rt[un]=pt[q];
}
inline int inConvex(Pt p){
   int L,R,M;
   if(p.X<Lx || p.X>Rx) return 0;
   L=0;R=dn;
   while(L<R-1){ M=(L+R)/2;
     if(p.X<qt[M].X) R=M; else L=M; }
   if(tri(qt[L],qt[R],p)<0) return 0;
   L=0;R=un;
   while(L<R-1){ M=(L+R)/2;
     if(p.X<rt[M].X) R=M; else L=M; }
   if(tri(rt[L],rt[R],p)>0) return 0;
   return 1;
}
int main(){
   int n,m,i;
   Pt p;
   scanf("%d",&n);
   for(i=0;i<n;i++) scanf("%lld%lld",&pt[i].X,&pt[i].Y);
   scanf("%d",&m);
   for(i=0;i<m;i++) scanf("%lld%lld",&qt[i].X,&qt[i].Y);
   n=minkowskiSum(n,m);
   for(i=0;i<n;i++) pt[i]=rt[i];
   scanf("%d",&m);
   for(i=0;i<m;i++) scanf("%lld%lld",&qt[i].X,&qt[i].Y);
   n=minkowskiSum(n,m);
   for(i=0;i<n;i++) pt[i]=rt[i];
   initInConvex(n);
   scanf("%d",&m);
   for(i=0;i<m;i++){
     scanf("%lld %lld",&p.X,&p.Y);
     p.X*=3; p.Y*=3;
     puts(inConvex(p)?"YES":"NO");
```

```
   }
}
```

4.10 Min/Max Enclosing Rectangle

```
/******* NEED REVISION *******/
/* uva819 - gifts large and small */
#define MAXN 100005
const double eps=1e-8;
const double inf=1e15;
class Coor {
 public:
  double x,y;
  Coor() {}
  Coor(double xi,double yi) { x=xi; y=yi; }
  Coor& operator+=(const Coor &b) { x+=b.x; y+=b.y;
      return *this; }
  const Coor operator+(const Coor &b) const { return (
      Coor)*this+=b; }
  Coor& operator-=(const Coor &b) { x-=b.x; y-=b.y;
      return *this; }
  const Coor operator-(const Coor &b) const { return (
      Coor)*this-=b; }
  Coor& operator*=(const double b) { x*=b; y*=b; return
       *this; }
  const Coor operator*(const double b) const { return (
      Coor)*this*=b; }
  Coor& operator/=(const double b) { x/=b; y/=b; return
       *this; }
  const Coor operator/(const double b) const { return (
      Coor)*this/=b; }
  const bool operator<(const Coor& b) const { return y<
      b.y-eps||fabs(y-b.y)<eps&&x<b.x; }
  const double len2() const { return x*x+y*y; }
  const double len() const { return sqrt(len2()); }
  const Coor perp() const { return Coor(y,-x); }
  Coor& standardize() {
    if(y<0||y==0&&x<0) {
      x=-x;
      y=-y;
    }
    return *this;
  }
  const Coor standardize() const { return ((Coor)*this)
      .standardize(); }
};
double dot(const Coor &a,const Coor &b) { return a.x*b.
    x+a.y*b.y; }
double dot(const Coor &o,const Coor &a,const Coor &b) {
     return dot(a-o,b-o); }
double cross(const Coor &a,const Coor &b) { return a.x*
    b.y-a.y*b.x; }
double cross(const Coor &o,const Coor &a,const Coor &b)
    { return cross(a-o,b-o); }
Coor cmpo;
const bool cmpf(const Coor &a,const Coor &b) {
  return cross(cmpo,a,b)>eps||fabs(cross(cmpo,a,b))<eps
      &&
    dot(a,cmpo,b)<-eps;
}
class Polygon {
 public:
  int pn;
  Coor p[MAXN];
  void convex_hull() {
    int i,tn=pn;
    for(i=1;i<pn;++i) if(p[i]<p[0]) swap(p[0],p[i]);
    cmpo=p[0];
    std::sort(p+1,p+pn,cmpf);
    for(i=pn=1;i<tn;++i) {
      while(pn>2&&cross(p[pn-2],p[pn-1],p[i])<=eps) --
          pn;
      p[pn++]=p[i];
    }
    p[pn]=p[0];
  }
};
Polygon pol;
double minarea,maxarea;
int slpn;
```

```
Coor slope[MAXN*2];
Coor lrec[MAXN*2],rrec[MAXN*2],trec[MAXN*2],brec[MAXN
    *2];
inline double xproject(Coor p,Coor slp) { return dot(p,
    slp)/slp.len(); }
inline double yproject(Coor p,Coor slp) { return cross(
    p,slp)/slp.len(); }
inline double calcarea(Coor lp,Coor rp,Coor bp,Coor tp,
    Coor slp) {
  return (xproject(rp,slp)-xproject(lp,slp))*(yproject(
      tp,slp)-yproject(bp,slp)); }
  inline void solve(){
    int i,lind,rind,tind,bind,tn;
    double pro,area1,area2,l,r,m1,m2;
    Coor s1,s2;
    pol.convex_hull();
    slpn=0; /* generate all critical slope */
    slope[slpn++]=Coor(1.0,0.0);
    slope[slpn++]=Coor(0.0,1.0);
    for(i=0;i<pol.pn;i++) {
      slope[slpn]=(pol.p[i+1]-pol.p[i]).standardize();
      if(slope[slpn].x>0) slpn++;
      slope[slpn]=(pol.p[i+1]-pol.p[i]).perp().
          standardize();
      if(slope[slpn].x>0) slpn++;
    }
    cmpo=Coor(0,0);
    std::sort(slope,slope+slpn,cmpf);
    tn=slpn;
    for(i=slpn=1;i<tn;i++)
      if(cross(cmpo,slope[i-1],slope[i])>0) slope[slpn
          ++]=slope[i];
    lind=rind=0; /* find critical touchpoints */
    for(i=0;i<pol.pn;i++) {
      pro=xproject(pol.p[i],slope[0]);
      if(pro<xproject(pol.p[lind],slope[0])) lind=i;
      if(pro>xproject(pol.p[rind],slope[0])) rind=i;
    }
    tind=bind=0;
    for(i=0;i<pol.pn;i++) {
      pro=yproject(pol.p[i],slope[0]);
      if(pro<yproject(pol.p[bind],slope[0])) bind=i;
      if(pro>yproject(pol.p[tind],slope[0])) tind=i;
    }
    for(i=0;i<slpn;i++) {
      while(xproject(pol.p[lind+1],slope[i])<=xproject(
          pol.p[lind],slope[i])+eps)
        lind=(lind==pol.pn-1?0:lind+1);
      while(xproject(pol.p[rind+1],slope[i])>=xproject(
          pol.p[rind],slope[i])-eps)
        rind=(rind==pol.pn-1?0:rind+1);
      while(yproject(pol.p[bind+1],slope[i])<=yproject(
          pol.p[bind],slope[i])+eps)
        bind=(bind==pol.pn-1?0:bind+1);
      while(yproject(pol.p[tind+1],slope[i])>=yproject(
          pol.p[tind],slope[i])-eps)
        tind=(tind==pol.pn-1?0:tind+1);
      lrec[i]=pol.p[lind];
      rrec[i]=pol.p[rind];
      brec[i]=pol.p[bind];
      trec[i]=pol.p[tind];
    }
    minarea=inf; /* find minimum area */
    for(i=0;i<slpn;i++) {
      area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],
          slope[i]);
      if(area1<minarea) minarea=area1;
    }
    maxarea=minarea; /* find maximum area */
    for(i=0;i<slpn-1;i++) {
      l=0.0; r=1.0;
      while(l<r-eps) {
        m1=l+(r-l)/3;
        m2=l+(r-l)*2/3;
        s1=slope[i]*(1.0-m1)+slope[i+1]*m1;
        area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],
            s1);
        s2=slope[i]*(1.0-m2)+slope[i+1]*m2;
        area2=calcarea(lrec[i],rrec[i],brec[i],trec[i],
            s2);
        if(area1<area2) l=m1;
        else r=m2;
      }
      s1=slope[i]*(1.0-l)+slope[i+1]*l;
      area1=calcarea(lrec[i],rrec[i],brec[i],trec[i],s1
          );
      if(area1>maxarea) maxarea=area1;
    }
  }
}
int main(){
  int i,casenum=1;
  while(scanf("%d",&pol.pn)==1&&pol.pn) {
    for(i=0;i<pol.pn;i++)
      scanf("%lf %lf",&pol.p[i].x,&pol.p[i].y);
    solve();
    //minarea, maxarea
  }
}
```

5 Graph

5.1 HeavyLightDecomp

```
#define SZ(c) (int)(c).size()
#define ALL(c) (c).begin(), (c).end()
#define REP(i, s, e) for(int i = (s); i <= (e); i++)
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
typedef tuple< int , int > tii;
const int MAXN = 100010;
const int LOG  = 19;
struct HLD{
  int n;
  vector<int> g[MAXN];
  int sz[MAXN], dep[MAXN];
  int ts, tid[MAXN], tdi[MAXN], tl[MAXN], tr[MAXN];
  // ts : timestamp , useless after yutruli
  // tid[ u ] : pos. of node u in the seq.
  // tdi[ i ] : node at pos i of the seq.
  // tl , tr[ u ] : subtree interval in the seq. of
      node u
  int mom[MAXN][LOG], head[MAXN];
  // head[ u ] : head of the chain contains u
  void dfssz(int u, int p){
    dep[u] = dep[p] + 1;
    mom[u][0] = p;
    sz[u] = 1;
    head[u] = u;
    for(int& v:g[u]) if(v != p){
      dep[v] = dep[u] + 1;
      dfssz(v, u);
      sz[u] += sz[v];
    }
  }
  void dfshl(int u){
    //printf("dfshl %d\n", u);
    ts++;
    tid[u] = tl[u] = tr[u] = ts;
    tdi[tid[u]] = u;
    sort(ALL(g[u]),
        [&](int a, int b){return sz[a] > sz[b];});
    bool flag = 1;
    for(int& v:g[u]) if(v != mom[u][0]){
      if(flag) head[v] = head[u], flag = 0;
      dfshl(v);
      tr[u] = tr[v];
    }
  }
  inline int lca(int a, int b){
    if(dep[a] > dep[b]) swap(a, b);
    //printf("lca %d %d\n", a, b);
    int diff = dep[b] - dep[a];
    REPD(k, LOG-1, 0) if(diff & (1<<k)){
      //printf("b %d\n", mom[b][k]);
      b = mom[b][k];
    }
    if(a == b) return a;
    REPD(k, LOG-1, 0) if(mom[a][k] != mom[b][k]){
      a = mom[a][k];
      b = mom[b][k];
    }
```

```
      return mom[a][0];
  }
  void init( int _n ){
    n = _n;
    REP( i , 1 , n ) g[ i ].clear();
  }
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
    g[ v ].push_back( u );
  }
  void yutruli(){
    dfssz(1, 0);
    ts = 0;
    dfshl(1);
    REP(k, 1, LOG-1) REP(i, 1, n)
      mom[i][k] = mom[mom[i][k-1]][k-1];
  }
  vector< tii > getPath( int u , int v ){
    vector< tii > res;
    while( tid[ u ] < tid[ head[ v ] ] ){
      res.push_back( tii(tid[ head[ v ] ] , tid[ v ]) )
        ;
      v = mom[ head[ v ] ][ 0 ];
    }
    res.push_back( tii( tid[ u ] , tid[ v ] ) );
    reverse( ALL( res ) );
    return res;
    /*
     * res : list of intervals from u to v
     * u must be ancestor of v
     * usage :
     * vector< tii >& path = tree.getPath( u , v )
     * for( tii tp : path ) {
     *    int l , r;tie( l , r ) = tp;
     *    upd( l , r );
     *    uu = tree.tdi[ l ] , vv = tree.tdi[ r ];
     *    uu ~> vv is a heavy path on tree
     * }
     */
  }
} tree;
```

5.2 DominatorTree

```
const int MAXN = 100010;
struct DominatorTree{
#define REP(i,s,e) for(int i=(s);i<=(e);i++)
#define REPD(i,s,e) for(int i=(s);i>=(e);i--)
  int n , m , s;
  vector< int > g[ MAXN ] , pred[ MAXN ];
  vector< int > cov[ MAXN ];
  int dfn[ MAXN ] , nfd[ MAXN ] , ts;
  int par[ MAXN ];
  int sdom[ MAXN ] , idom[ MAXN ];
  int mom[ MAXN ] , mn[ MAXN ];

  inline bool cmp( int u , int v )
  { return dfn[ u ] < dfn[ v ]; }

  int eval( int u ){
    if( mom[ u ] == u ) return u;
    int res = eval( mom[ u ] );
    if(cmp( sdom[ mn[ mom[ u ] ] ] , sdom[ mn[ u ] ] ))
      mn[ u ] = mn[ mom[ u ] ];
    return mom[ u ] = res;
  }

  void init( int _n , int _m , int _s ){
    ts = 0; n = _n; m = _m; s = _s;
    REP( i, 1, n ) g[ i ].clear(), pred[ i ].clear();
  }
  void addEdge( int u , int v ){
    g[ u ].push_back( v );
    pred[ v ].push_back( u );
  }
  void dfs( int u ){
    ts++;
    dfn[ u ] = ts;
    nfd[ ts ] = u;
    for( int v : g[ u ] ) if( dfn[ v ] == 0 ){
```

```
      par[ v ] = u;
      dfs( v );
    }
  }
  void build(){
    REP( i , 1 , n ){
      dfn[ i ] = nfd[ i ] = 0;
      cov[ i ].clear();
      mom[ i ] = mn[ i ] = sdom[ i ] = i;
    }
    dfs( s );
    REPD( i , n , 2 ){
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      for( int v : pred[ u ] ) if( dfn[ v ] ){
        eval( v );
        if( cmp( sdom[ mn[ v ] ] , sdom[ u ] ) )
          sdom[ u ] = sdom[ mn[ v ] ];
      }
      cov[ sdom[ u ] ].push_back( u );
      mom[ u ] = par[ u ];
      for( int w : cov[ par[ u ] ] ){
        eval( w );
        if( cmp( sdom[ mn[ w ] ] , par[ u ] ) )
          idom[ w ] = mn[ w ];
        else idom[ w ] = par[ u ];
      }
      cov[ par[ u ] ].clear();
    }
    REP( i , 2 , n ){
      int u = nfd[ i ];
      if( u == 0 ) continue ;
      if( idom[ u ] != sdom[ u ] )
        idom[ u ] = idom[ idom[ u ] ];
    }
  }
} domT;
```

5.3 MaxClique

```
class MaxClique {
 public:
  static const int MV = 210;
  int V , ans;
  int el[MV][MV/30+1];
  int dp[MV];
  int s[MV][MV/30+1];
  vector<int> sol;
  void init(int v) {
    V = v; ans = 0;
    FZ(el); FZ(dp);
  }
  /* Zero Base */
  void addEdge(int u, int v) {
    if(u > v) swap(u, v);
    if(u == v) return;
    el[u][v/32] |= (1<<(v%32));
  }
  bool dfs(int v, int k) {
    int c = 0, d = 0;
    for(int i=0; i<(V+31)/32; i++) {
      s[k][i] = el[v][i];
      if(k != 1) s[k][i] &= s[k-1][i];
      c += __builtin_popcount(s[k][i]);
    }
    if(c == 0) {
      if(k > ans) {
        ans = k;
        sol.clear();
        sol.push_back(v);
        return 1;
      }
      return 0;
    }
    for(int i=0; i<(V+31)/32; i++) {
      for(int a = s[k][i]; a ; d++) {
        if(k + (c-d) <= ans) return 0;
        int lb = a&(-a), lg = 0;
        a ^= lb;
        while(lb!=1) {
```

```
        lb = (unsigned int)(lb) >> 1;
        lg ++;
      }
      int u = i*32 + lg;
      if(k + dp[u] <= ans) return 0;
      if(dfs(u, k+1)) {
        sol.push_back(v);
        return 1;
      }
    }
  }
  return 0;
}
int solve() {
  for(int i=V-1; i>=0; i--) {
    dfs(i, 1);
    dp[i] = ans;
  }
  return ans;
}
};
```

5.4 Strongly Connected Component

```
struct Scc{
  int n, nScc, vst[MXN], bln[MXN];
  vector<int> E[MXN], rE[MXN], vec;
  void init(int _n){
    n = _n;
    for (int i=0; i<MXN; i++){
      E[i].clear();
      rE[i].clear();
    }
  }
  void add_edge(int u, int v){
    E[u].PB(v);
    rE[v].PB(u);
  }
  void DFS(int u){
    vst[u]=1;
    for (auto v : E[u])
      if (!vst[v]) DFS(v);
    vec.PB(u);
  }
  void rDFS(int u){
    vst[u] = 1;
    bln[u] = nScc;
    for (auto v : rE[u])
      if (!vst[v]) rDFS(v);
  }
  void solve(){
    nScc = 0;
    vec.clear();
    FZ(vst);
    for (int i=0; i<n; i++)
      if (!vst[i]) DFS(i);
    reverse(vec.begin(),vec.end());
    FZ(vst);
    for (auto v : vec){
      if (!vst[v]){
        rDFS(v);
        nScc++;
      }
    }
  }
};
```

5.5 Minimum General Weighted Matching

```
struct Graph {
  // Minimum General Weighted Matching (Perfect Match)
  static const int MXN = 105;
  int n, edge[MXN][MXN];
  int match[MXN],dis[MXN],onstk[MXN];
  vector<int> stk;
  void init(int _n) {
    n = _n;
    for( int i = 0 ; i < n ; i ++ )
```

```
      for( int j = 0 ; j < n ; j ++ )
        edge[ i ][ j ] = 0;
  }
  void add_edge(int u, int v, int w) {
    edge[u][v] = edge[v][u] = w;
  }
  bool SPFA(int u){
    if (onstk[u]) return true;
    stk.PB(u);
    onstk[u] = 1;
    for (int v=0; v<n; v++){
      if (u != v && match[u] != v && !onstk[v]){
        int m = match[v];
        if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
          dis[m] = dis[u] - edge[v][m] + edge[u][v];
          onstk[v] = 1;
          stk.PB(v);
          if (SPFA(m)) return true;
          stk.pop_back();
          onstk[v] = 0;
        }
      }
    }
    onstk[u] = 0;
    stk.pop_back();
    return false;
  }
  int solve() {
    // find a match
    for (int i=0; i<n; i+=2){
      match[i] = i+1;
      match[i+1] = i;
    }
    while (true){
      int found = 0;
      for( int i = 0 ; i < n ; i ++ )
        onstk[ i ] = dis[ i ] = 0;
      for (int i=0; i<n; i++){
        stk.clear();
        if (!onstk[i] && SPFA(i)){
          found = 1;
          while (SZ(stk)>=2){
            int u = stk.back(); stk.pop_back();
            int v = stk.back(); stk.pop_back();
            match[u] = v;
            match[v] = u;
          }
        }
      }
      if (!found) break;
    }
    int ret = 0;
    for (int i=0; i<n; i++)
      ret += edge[i][match[i]];
    ret /= 2;
    return ret;
  }
}graph;
```

5.6 Minimum Steiner Tree

```
// Minimum Steiner Tree
// O(V 3^T + V^2 2^T)
struct SteinerTree{
#define V 33
#define T 8
#define INF 1023456789
  int n , dst[ V ][ V ] , dp[ 1 << T ][ V ] , tdst[ V
    ];
  void init( int _n ){
    n = _n;
    for( int i = 0 ; i < n ; i ++ ){
      for( int j = 0 ; j < n ; j ++ )
        dst[ i ][ j ] = INF;
      dst[ i ][ i ] = 0;
    }
  }
  void add_edge( int ui , int vi , int wi ){
    dst[ ui ][ vi ] = min( dst[ ui ][ vi ] , wi );
    dst[ vi ][ ui ] = min( dst[ vi ][ ui ] , wi );
```

```cpp
    }
    void shortest_path(){
      for( int k = 0 ; k < n ; k ++ )
        for( int i = 0 ; i < n ; i ++ )
          for( int j = 0 ; j < n ; j ++ )
            dst[ i ][ j ] = min( dst[ i ][ j ],
                    dst[ i ][ k ] + dst[ k ][ j ] );
    }
    int solve( const vector<int>& ter ){
      int t = (int)ter.size();
      for( int i = 0 ; i < ( 1 << t ) ; i ++ )
        for( int j = 0 ; j < n ; j ++ )
          dp[ i ][ j ] = INF;
      for( int i = 0 ; i < n ; i ++ )
        dp[ 0 ][ i ] = 0;
      for( int msk = 1 ; msk < ( 1 << t ) ; msk ++ ){
        if( msk == ( msk & (-msk) ) ){
          int who = __lg( msk );
          for( int i = 0 ; i < n ; i ++ )
            dp[ msk ][ i ] = dst[ ter[ who ] ][ i ];
          continue;
        }
        for( int i = 0 ; i < n ; i ++ )
          for( int submsk = ( msk - 1 ) & msk ; submsk ;
                  submsk = ( submsk - 1 ) & msk )
            dp[ msk ][ i ] = min( dp[ msk ][ i ],
                          dp[ submsk ][ i ] +
                          dp[ msk ^ submsk ][ i ] );
        for( int i = 0 ; i < n ; i ++ ){
          tdst[ i ] = INF;
          for( int j = 0 ; j < n ; j ++ )
            tdst[ i ] = min( tdst[ i ],
                        dp[ msk ][ j ] + dst[ j ][ i ] );
        }
        for( int i = 0 ; i < n ; i ++ )
          dp[ msk ][ i ] = tdst[ i ];
      }
      int ans = INF;
      for( int i = 0 ; i < n ; i ++ )
        ans = min( ans , dp[ ( 1 << t ) - 1 ][ i ] );
      return ans;
    }
  }
} solver;
```

6 String

6.1 PalTree

```cpp
const int MAXN = 200010;
struct PalT{
  struct Node{
    int nxt[ 33 ] , len , fail;
    ll cnt;
  };
  int tot , lst;
  Node nd[ MAXN * 2 ];
  char* s;
  int newNode( int l , int _fail ){
    int res = ++tot;
    memset( nd[ res ].nxt , 0 , sizeof nd[ res ].nxt );
    nd[ res ].len = l;
    nd[ res ].cnt = 0;
    nd[ res ].fail = _fail;
    return res;
  }
  void push( int p ){
    int np = lst;
    int c = s[ p ] - 'a';
    while( p - nd[ np ].len - 1 < 0
        || s[ p ] != s[ p - nd[ np ].len - 1 ] )
      np = nd[ np ].fail;

    if( nd[ np ].nxt[ c ] ){
      nd[ nd[ np ].nxt[ c ] ].cnt++;
      lst = nd[ np ].nxt[ c ];
      return ;
    }
    int nq = newNode( nd[ np ].len + 2 , 0 );
```

```cpp
    nd[ nq ].cnt++;
    nd[ np ].nxt[ c ] = nq;
    lst = nq;
    if( nd[ nq ].len == 1 ){
      nd[ nq ].fail = 2;
      return ;
    }
    int tf = nd[ np ].fail;
    while( p - nd[ tf ].len - 1 < 0
        || s[ p ] != s[ p - nd[ tf ].len - 1 ] )
      tf = nd[ tf ].fail;

    nd[ nq ].fail = nd[ tf ].nxt[ c ];
    return ;
  }
  void init( char* _s ){
    s = _s;
    tot = 0;
    newNode( -1 , 1 );
    newNode( 0 , 1 );
    lst = 2;
    for( int i = 0 ; s[ i ] ; i++ )
      push( i );
  }
  void yutruli(){
#define REPD(i, s, e) for(int i = (s); i >= (e); i--)
    REPD( i , tot , 1 )
      nd[ nd[ i ].fail ].cnt += nd[ i ].cnt;
    nd[ 1 ].cnt = nd[ 2 ].cnt = 0ll;
  }
} pA;
int main(){
  pA.init( sa );
}
```

6.2 SuffixArray

```cpp
const int MAX = 1020304;
int ct[MAX], he[MAX], rk[MAX];
int sa[MAX], tsa[MAX], tp[MAX][2];
void suffix_array(char *ip){
  int len = strlen(ip);
  int alp = 256;
  memset(ct, 0, sizeof(ct));
  for(int i=0;i<len;i++) ct[ip[i]+1]++;
  for(int i=1;i<alp;i++) ct[i]+=ct[i-1];
  for(int i=0;i<len;i++) rk[i]=ct[ip[i]];

  for(int i=1;i<len;i*=2){
    for(int j=0;j<len;j++){
      if(j+i>=len) tp[j][1]=0;
      else tp[j][1]=rk[j+i]+1;
      tp[j][0]=rk[j];
    }
    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][1]+1]++;
    for(int j=1;j<len+2;j++) ct[j]+=ct[j-1];
    for(int j=0;j<len;j++) tsa[ct[tp[j][1]]++]=j;

    memset(ct, 0, sizeof(ct));
    for(int j=0;j<len;j++) ct[tp[j][0]+1]++;
    for(int j=1;j<len+1;j++) ct[j]+=ct[j-1];
    for(int j=0;j<len;j++)
      sa[ct[tp[tsa[j]][0]]++]=tsa[j];

    rk[sa[0]]=0;
    for(int j=1;j<len;j++){
      if( tp[sa[j]][0] == tp[sa[j-1]][0] &&
        tp[sa[j]][1] == tp[sa[j-1]][1] )
        rk[sa[j]] = rk[sa[j-1]];
      else
        rk[sa[j]] = j;
    }
  }

  for(int i=0,h=0;i<len;i++){
    if(rk[i]==0) h=0;
    else{
      int j=sa[rk[i]-1];
      h=max(0,h-1);
```

```
      for(;ip[i+h]==ip[j+h];h++);
    }
    he[rk[i]]=h;
  }
}
```

6.3 SAIS

```
const int N = 300010;
struct SA{
#define REP(i,n) for ( int i=0; i<int(n); i++ )
#define REP1(i,a,b) for ( int i=(a); i<=int(b); i++ )
  bool _t[N*2];
  int _s[N*2], _sa[N*2], _c[N*2], x[N], _p[N], _q[N*2],
      hei[N], r[N];
  int operator [] (int i){ return _sa[i]; }
  void build(int *s, int n, int m){
    memcpy(_s, s, sizeof(int) * n);
    sais(_s, _sa, _p, _q, _t, _c, n, m);
    mkhei(n);
  }
  void mkhei(int n){
    REP(i,n) r[_sa[i]] = i;
    hei[0] = 0;
    REP(i,n) if(r[i]) {
      int ans = i>0 ? max(hei[r[i-1]] - 1, 0) : 0;
      while(_s[i+ans] == _s[_sa[r[i]-1]+ans]) ans++;
      hei[r[i]] = ans;
    }
  }
  void sais(int *s, int *sa, int *p, int *q, bool *t,
      int *c, int n, int z){
    bool uniq = t[n-1] = true, neq;
    int nn = 0, nmxz = -1, *nsa = sa + n, *ns = s + n,
        lst = -1;
#define MS0(x,n) memset((x),0,n*sizeof(*(x)))
#define MAGIC(XD) MS0(sa, n); \
    memcpy(x, c, sizeof(int) * z); \
    XD; \
    memcpy(x + 1, c, sizeof(int) * (z - 1)); \
    REP(i,n) if(sa[i] && !t[sa[i]-1]) sa[x[s[sa[i
        ]-1]]++] = sa[i]-1; \
    memcpy(x, c, sizeof(int) * z); \
    for(int i = n - 1; i >= 0; i--) if(sa[i] && t[sa[i
        ]-1]) sa[--x[s[sa[i]-1]]] = sa[i]-1;
    MS0(c, z);
    REP(i,n) uniq &= ++c[s[i]] < 2;
    REP(i,z-1) c[i+1] += c[i];
    if (uniq) { REP(i,n) sa[--c[s[i]]] = i; return; }
    for(int i = n - 2; i >= 0; i--) t[i] = (s[i]==s[i
        +1]) ? t[i+1] : s[i]<s[i+1]);
    MAGIC(REP1(i,1,n-1) if(t[i] && !t[i-1]) sa[--x[s[i
        ]]]=p[q[i]=nn++]=i);
    REP(i, n) if (sa[i] && t[sa[i]] && !t[sa[i]-1]) {
      neq=lst<0||memcmp(s+sa[i],s+lst,(p[q[sa[i]]+1]-sa
          [i])*sizeof(int));
      ns[q[lst=sa[i]]]=nmxz+=neq;
    }
    sais(ns, nsa, p + nn, q + n, t + n, c + z, nn, nmxz
        + 1);
    MAGIC(for(int i = nn - 1; i >= 0; i--) sa[--x[s[p[
        nsa[i]]]]] = p[nsa[i]]);
  }
}sa;
int H[ N ], SA[ N ];
void suffix_array(int* ip, int len) {
  // should padding a zero in the back
  // ip is int array, len is array length
  // ip[0..n-1] != 0, and ip[len] = 0
  ip[len++] = 0;
  sa.build(ip, len, 128);
  for (int i=0; i<len; i++) {
    H[i] = sa.hei[i + 1];
    SA[i] = sa._sa[i + 1];
  }
  // resulting height, sa array \in [0,len)
}
```

6.4 SuffixAutomata

```
const int MAXM = 1000010;
struct SAM{
  int tot, root, lst, mom[MAXM], mx[MAXM];
  int acc[MAXM], nxt[MAXM][33];
  int newNode(){
    int res = ++tot;
    fill(nxt[res], nxt[res]+33, 0);
    mom[res] = mx[res] = acc[res] = 0;
    return res;
  }
  void init(){
    tot = 0;
    root = newNode();
    mom[root] = 0, mx[root] = 0;
    lst = root;
  }
  void push(int c){
    int p = lst;
    int np = newNode();
    mx[np] = mx[p]+1;
    for(; p && nxt[p][c] == 0; p = mom[p])
      nxt[p][c] = np;
    if(p == 0) mom[np] = root;
    else{
      int q = nxt[p][c];
      if(mx[p]+1 == mx[q]) mom[np] = q;
      else{
        int nq = newNode();
        mx[nq] = mx[p]+1;
        for(int i = 0; i < 33; i++)
          nxt[nq][i] = nxt[q][i];
        mom[nq] = mom[q];
        mom[q] = nq;
        mom[np] = nq;
        for(; p && nxt[p][c] == q; p = mom[p])
          nxt[p][c] = nq;
      }
    }
    lst = np;
  }
  void print(){
    REP(i, 1, tot){
      printf("node %d :\n", i);
      printf("mx %d, mom %d\n", mx[i], mom[i]);
      REP(j, 1, 26) if(nxt[i][j])
        printf("nxt %c %d\n", 'a'+j-1, nxt[i][j]);
      puts("--------------------------");
    }
  }
  void push(char *str){
    for(int i = 0; str[i]; i++)
      push(str[i]-'a'+1);
  }
} sam;
```

6.5 Aho-Corasick

```
struct ACautomata{
  struct Node{
    int cnt,dp;
    Node *go[26], *fail;
    Node (){
      cnt = 0;
      dp = -1;
      memset(go,0,sizeof(go));
      fail = 0;
    }
  };
  Node *root, pool[1048576];
  int nMem;
  Node* new_Node(){
    pool[nMem] = Node();
    return &pool[nMem++];
  }
  void init(){
    nMem = 0;
    root = new_Node();
```

```cpp
  }
  void add(const string &str){
    insert(root,str,0);
  }
  void insert(Node *cur, const string &str, int pos){
    if (pos >= (int)str.size()){
      cur->cnt++;
      return;
    }
    int c = str[pos]-'a';
    if (cur->go[c] == 0){
      cur->go[c] = new_Node();
    }
    insert(cur->go[c],str,pos+1);
  }
  void make_fail(){
    queue<Node*> que;
    que.push(root);
    while (!que.empty()){
      Node* fr=que.front();
      que.pop();
      for (int i=0; i<26; i++){
        if (fr->go[i]){
          Node *ptr = fr->fail;
          while (ptr && !ptr->go[i]) ptr = ptr->fail;
          if (!ptr) fr->go[i]->fail = root;
          else fr->go[i]->fail = ptr->go[i];
          que.push(fr->go[i]);
        }
      }
    }
  }
};
```

6.6 Z Value

```cpp
char s[MAXN];
int len,z[MAXN];
void Z_value() {
  int i,j,left,right;
  left=right=0; z[0]=len;
  for(i=1;i<len;i++) {
    j=max(min(z[i-left],right-i),0);
    for(;i+j<len&&s[i+j]==s[j];j++);
    z[i]=j;
    if(i+z[i]>right) {
      right=i+z[i];
      left=i;
    }
  }
}
```

6.7 ZValue Palindrome

```cpp
const int MAX = 1000;
int len, zv[MAX*2];
char ip[MAX], op[MAX*2];
int main(){
  cin >> ip; len = strlen(ip);
  int l2 = len*2 - 1;
  for(int i=0; i<l2; i++){
    if(i&1) op[i] = '@';
    else op[i] = ip[i/2];
  }
  int l=0, r=0; zv[0] = 1;
  for(int i=1; i<l2; i++){
    if( i > r ){
      l = r = i;
      while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){
        l --; r ++;
      }
      zv[i] = (r-l+1);
    }else{
      int md = (l+r)/2;
      int j = md + md - i;
      zv[i] = zv[j];
      int q = zv[i] / 2;
      int nr = i + q;
```

```cpp
      if( nr == r ){
        l = i + i - r;
        while( l>0 && r<l2-1 && op[l-1] == op[r+1] ){
          l --; r ++;
        }
        zv[i] = r - l + 1;
      }else if( nr > r ){
        zv[i] = (r - i) * 2 + 1;
      }
    }
  }
}
```

6.8 Smallest Rotation

```cpp
string mcp(string s){
  int n = s.length();
  s += s;
  int i=0, j=1, k=0;
  while (j<n && k<n){
    if (s[i+k] == s[j+k]) k++;
    else {
      if (s[i+k] < s[j+k]) {
        j += k + 1;
      } else {
        i = j;
        j = max(j+1, j+k);
      }
      k = 0;
    }
  }
  return s.substr(i, n);
}
```

6.9 Baker Bird

```cpp
class Node { public:
  Node *fail;
  map<char,Node*> _next;
  int out;
  Node() { fail=NULL; out=-1; }
  ~Node() {
    for(map<char,Node*>::iterator it=_next.begin();it!=
        _next.end();it++)
      delete it->second;
  }
  Node* build(char ch) {
    if(_next.find(ch)==_next.end()) _next[ch]=new Node;
    return _next[ch];
  }
  Node* next(char ch) {
    if(_next.find(ch)==_next.end()) return NULL;
    return _next[ch];
  }
};
int srn,scn,prn,pcn,mrn,mcn;
char s[MAXN][MAXN],p[MAXN][MAXN];
int rm[MAXN][MAXN]; // rank matrix
int maxrank;
int seq[MAXN]; // index of patterns for radix sort
int rank[MAXN]; // rank of pattern on row r
int cnt[SIGMA+1],tmp[MAXN];
int pre[MAXN]; // pre-matrix for kmp
int ql,qr;
Node* que[MAXN*MAXN];
inline void radix_pass(int j,int *from,int *to) {
  int i;
  for(i=0;i<SIGMA;i++) cnt[i]=0;
  for(i=0;i<prn;i++) cnt[p[from[i]][j]+1]++;
  for(i=0;i<SIGMA;i++) cnt[i+1]+=cnt[i];
  for(i=0;i<prn;i++) to[cnt[p[from[i]][j]]++]=from[i];
}
inline void radix_sort_patterns() {
  int i,j;
  for(i=0;i<prn;i++) ((pcn&1)?tmp[i]:seq[i])=i;
  for(j=pcn-1;j>=0;j--) {
    if(j&1) radix_pass(j,seq,tmp);
    else radix_pass(j,tmp,seq);
```

```
  }
  maxrank=0;
  for(i=0;i<prn;i++) {
    if(i&&strcmp(p[seq[i-1]],p[seq[i]])) ++maxrank;
    rank[seq[i]]=maxrank;
  }
}
inline void construct(Node *v,char *p,int ind) {
  while(*p) { v=v->build(*p); p++; }
  v->out=ind;
}
inline void construct_all(Node *ac) {
  for(int i=0;i<prn;i++) construct(ac,p[i],rank[i]);
}
inline void find_fail(Node *ac) {
  Node *v,*u,*f;
  map<char,Node*>::iterator it;
  char ch;
  ql=qr=0; ac->fail=ac;
  for(it=ac->_next.begin();it!=ac->_next.end();it++) {
    u=it->second;
    u->fail=ac;
    que[qr++]=u;
  }
  while(ql<qr) {
    v=que[ql++];
    for(it=v->_next.begin();it!=v->_next.end();it++) {
      ch=it->first; u=it->second;
      f=v->fail;
      while(f!=ac&&f->next(ch)==NULL) f=f->fail;
      if(f->next(ch)) u->fail=f->next(ch);
      else u->fail=ac;
      que[qr++]=u;
    }
  }
}
inline void ac_match(Node *ac,char *s,int *arr) {
  int i;
  Node *v=ac;
  for(i=0;i<scn;i++) {
    while(v!=ac&&v->next(s[i])==NULL) v=v->fail;
    if(v->next(s[i])) v=v->next(s[i]);
    if(i>=pcn-1) arr[i-pcn+1]=v->out;
  }
}
inline void find_rank_matrix() {
  Node ac;
  radix_sort_patterns();
  construct_all(&ac);
  find_fail(&ac);
  mrn=srn; mcn=scn-pcn+1;
  for(int i=0;i<srn;i++) ac_match(&ac,s[i],rm[i]);
}
inline void find_pre(int *p,int plen) {
  int i,x;
  x=pre[0]=-1;
  for(i=1;i<plen;i++) {
    while(x>=0&&p[x+1]!=p[i]) x=pre[x];
    if(p[x+1]==p[i]) x++;
    pre[i]=x;
  }
}
inline int kmp_match(int col,int *p,int plen) {
  int i,x=-1,occ=0;
  for(i=0;i<mrn;i++) {
    while(x>=0&&p[x+1]!=rm[i][col]) x=pre[x];
    if(p[x+1]==rm[i][col]) x++;
    if(x==plen-1) { occ++; x=pre[x]; }
  }
  return occ;
}
inline int baker_bird() {
  int i,occ=0;
  find_rank_matrix();
  find_pre(rank,prn);
  for(i=0;i<mcn;i++) occ+=kmp_match(i,rank,prn);
  return occ;
}
```

6.10 Cyclic LCS

```
#define L 0
#define LU 1
#define U 2
const int mov[3][2]={0,-1, -1,-1, -1,0};
int al,bl;
char a[MAXL*2],b[MAXL*2]; // 0-indexed
int dp[MAXL*2][MAXL];
char pred[MAXL*2][MAXL];
inline int lcs_length(int r) {
  int i=r+al,j=bl,l=0;
  while(i>r) {
    char dir=pred[i][j];
    if(dir==LU) l++;
    i+=mov[dir][0];
    j+=mov[dir][1];
  }
  return l;
}
inline void reroot(int r) { // r = new base row
  int i=r,j=1;
  while(j<=bl&&pred[i][j]!=LU) j++;
  if(j>bl) return;
  pred[i][j]=L;
  while(i<2*al&&j<=bl) {
    if(pred[i+1][j]==U) {
      i++;
      pred[i][j]=L;
    } else if(j<bl&&pred[i+1][j+1]==LU) {
      i++;
      j++;
      pred[i][j]=L;
    } else {
      j++;
    }
  }
}
int cyclic_lcs() {
  // a, b, al, bl should be properly filled
  // note: a WILL be altered in process
  //       -- concatenated after itself
  char tmp[MAXL];
  if(al>bl) {
    swap(al,bl);
    strcpy(tmp,a);
    strcpy(a,b);
    strcpy(b,tmp);
  }
  strcpy(tmp,a);
  strcat(a,tmp);
  // basic lcs
  for(int i=0;i<=2*al;i++) {
    dp[i][0]=0;
    pred[i][0]=U;
  }
  for(int j=0;j<=bl;j++) {
    dp[0][j]=0;
    pred[0][j]=L;
  }
  for(int i=1;i<=2*al;i++) {
    for(int j=1;j<=bl;j++) {
      if(a[i-1]==b[j-1]) dp[i][j]=dp[i-1][j-1]+1;
      else dp[i][j]=max(dp[i-1][j],dp[i][j-1]);
      if(dp[i][j-1]==dp[i][j]) pred[i][j]=L;
      else if(a[i-1]==b[j-1]) pred[i][j]=LU;
      else pred[i][j]=U;
    }
  }
  // do cyclic lcs
  int clcs=0;
  for(int i=0;i<al;i++) {
    clcs=max(clcs,lcs_length(i));
    reroot(i+1);
  }
  // recover a
  a[al]='\0';
  return clcs;
}
```

7 Data Structure

7.1 Treap

```cpp
struct Treap{
  int sz , val , pri , tag;
  Treap *l , *r;
  Treap( int _val ){
    val = _val; sz = 1;
    pri = rand(); l = r = NULL; tag = 0;
  }
};
void push( Treap * a ){
  if( a->tag ){
    Treap *swp = a->l; a->l = a->r; a->r = swp;
    int swp2;
    if( a->l ) a->l->tag ^= 1;
    if( a->r ) a->r->tag ^= 1;
    a->tag = 0;
  }
}
int Size( Treap * a ){ return a ? a->sz : 0; }
void pull( Treap * a ){
  a->sz = Size( a->l ) + Size( a->r ) + 1;
}
Treap* merge( Treap *a , Treap *b ){
  if( !a || !b ) return a ? a : b;
  if( a->pri > b->pri ){
    push( a );
    a->r = merge( a->r , b );
    pull( a );
    return a;
  }else{
    push( b );
    b->l = merge( a , b->l );
    pull( b );
    return b;
  }
}
void split( Treap *t , int k , Treap*&a , Treap*&b ){
  if( !t ){ a = b = NULL; return; }
  push( t );
  if( Size( t->l ) + 1 <= k ){
    a = t;
    split( t->r , k - Size( t->l ) - 1 , a->r , b );
    pull( a );
  }else{
    b = t;
    split( t->l , k , a , b->l );
    pull( b );
  }
}
```

7.2 Link-Cut Tree

```cpp
const int MXN = 100005;
const int MEM = 100005;
struct Splay {
  static Splay nil, mem[MEM], *pmem;
  Splay *ch[2], *f;
  int val, rev, size;
  Splay () : val(-1), rev(0), size(0){
    f = ch[0] = ch[1] = &nil;
  }
  Splay (int _val) : val(_val), rev(0), size(1){
    f = ch[0] = ch[1] = &nil;
  }
  bool isr(){
    return f->ch[0] != this && f->ch[1] != this;
  }
  int dir(){
    return f->ch[0] == this ? 0 : 1;
  }
  void setCh(Splay *c, int d){
    ch[d] = c;
    if (c != &nil) c->f = this;
    pull();
  }
```

```cpp
  void push(){
    if (rev){
      swap(ch[0], ch[1]);
      if (ch[0] != &nil) ch[0]->rev ^= 1;
      if (ch[1] != &nil) ch[1]->rev ^= 1;
      rev=0;
    }
  }
  void pull(){
    size = ch[0]->size + ch[1]->size + 1;
    if (ch[0] != &nil) ch[0]->f = this;
    if (ch[1] != &nil) ch[1]->f = this;
  }
} Splay::nil, Splay::mem[MEM], *Splay::pmem = Splay::
    mem;
Splay *nil = &Splay::nil;
void rotate(Splay *x){
  Splay *p = x->f;
  int d = x->dir();
  if (!p->isr()) p->f->setCh(x, p->dir());
  else x->f = p->f;
  p->setCh(x->ch[!d], d);
  x->setCh(p, !d);
  p->pull(); x->pull();
}

vector<Splay*> splayVec;
void splay(Splay *x){
  splayVec.clear();
  for (Splay *q=x;; q=q->f){
    splayVec.push_back(q);
    if (q->isr()) break;
  }
  reverse(begin(splayVec), end(splayVec));
  for (auto it : splayVec) it->push();
  while (!x->isr()) {
    if (x->f->isr()) rotate(x);
    else if (x->dir()==x->f->dir())
      rotate(x->f),rotate(x);
    else rotate(x),rotate(x);
  }
}
Splay* access(Splay *x){
  Splay *q = nil;
  for (;x!=nil;x=x->f){
    splay(x);
    x->setCh(q, 1);
    q = x;
  }
  return q;
}
void evert(Splay *x){
  access(x);
  splay(x);
  x->rev ^= 1;
  x->push(); x->pull();
}
void link(Splay *x, Splay *y){
//  evert(x);
  access(x);
  splay(x);
  evert(y);
  x->setCh(y, 1);
}
void cut(Splay *x, Splay *y){
//  evert(x);
  access(y);
  splay(y);
  y->push();
  y->ch[0] = y->ch[0]->f = nil;
}
int N, Q;
Splay *vt[MXN];
int ask(Splay *x, Splay *y){
  access(x);
  access(y);
  splay(x);
  int res = x->f->val;
  if (res == -1) res=x->val;
  return res;
}
int main(int argc, char** argv){
```

```cpp
  scanf("%d%d", &N, &Q);
  for (int i=1; i<=N; i++)
    vt[i] = new (Splay::pmem++) Splay(i);
  while (Q--) {
    char cmd[105];
    int u, v;
    scanf("%s", cmd);
    if (cmd[1] == 'i') {
      scanf("%d%d", &u, &v);
      link(vt[v], vt[u]);
    } else if (cmd[0] == 'c') {
      scanf("%d", &v);
      cut(vt[1], vt[v]);
    } else {
      scanf("%d%d", &u, &v);
      int res=ask(vt[u], vt[v]);
      printf("%d\n", res);
    }
  }
}
```

7.3 Disjoint Set

```cpp
struct DisjointSet{
  // save() is like recursive
  // undo() is like return
  int n, fa[ N ], sz[ N ];
  vector< pair<int*,int> > h;
  vector<int> sp;
  void init( int tn ){
    n=tn;
    for( int i = 0 ; i < n ; i ++ ){
      fa[ i ]=i;
      sz[ i ]=1;
    }
    sp.clear(); h.clear();
  }
  void assign( int *k, int v ){
    h.PB( {k, *k} );
    *k = v;
  }
  void save(){ sp.PB(SZ(h)); }
  void undo(){
    assert(!sp.empty());
    int last=sp.back(); sp.pop_back();
    while( SZ(h)!=last ){
      auto x=h.back(); h.pop_back();
      *x.first = x.second;
    }
  }
  int f( int x ){
    while( fa[ x ] != x ) x = fa[ x ];
    return x;
  }
  void uni( int x , int y ){
    x = f( x ); y = f( y );
    if( x == y ) return;
    if( sz[ x ] < sz[ y ] ) swap( x, y );
    assign( &sz[ x ] , sz[ x ] + sz[ y ] );
    assign( &fa[ y ] , x);
  }
}djs;
```

7.4 Pairing Heap

```cpp
#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef priority_queue<int> heap;
int main(){
  heap h1 , h2;
  h1.push( 1 );
  h2.push( 4 );
  h1.join( h2 );
  h1.size(); // 2
  h2.size(); // 0
  h1.top(); // 4
}
```

7.5 Leftist Heap

```cpp
const int MAXN = 10000;
struct Node{
  int num,lc,rc;
  Node() : num(0), lc(-1), rc(-1){}
  Node( int _v ) : num(_v), lc(-1), rc(-1){}
}tree[ MAXN ];
int merge( int x, int y ){
  if( x == -1 ) return y;
  if( y == -1 ) return x;
  if( tree[ x ].num < tree[ y ].num )
    swap(x, y);
  tree[ x ].rc = merge(tree[ x ].rc, y);
  swap(tree[ x ].lc, tree[ x ].rc);
  return x;
}
/* Usage
merge: root = merge(x, y)
delmin: root = merge(root.lc, root.rc)
*/
```

7.6 Black Magic

```cpp
#include <bits/extc++.h>
using namespace __gnu_pbds;
typedef tree<int,null_type,less<int>,rb_tree_tag,
    tree_order_statistics_node_update> set_t;
int main(){
  // Insert some entries into s.
  set_t s;
  s.insert(12);
  s.insert(505);
  // The order of the keys should be: 12, 505.
  assert(*s.find_by_order(0) == 12);
  assert(*s.find_by_order(3) == 505);
  // The order of the keys should be: 12, 505.
  assert(s.order_of_key(12) == 0);
  assert(s.order_of_key(505) == 1);
  // Erase an entry.
  s.erase(12);
  // The order of the keys should be: 505.
  assert(*s.find_by_order(0) == 505);
  // The order of the keys should be: 505.
  assert(s.order_of_key(505) == 0);
}
```

8 Others

8.1 Find max tangent(x,y is increasing)

```cpp
typedef long long LL;
const int MAXN = 100010;
struct Coord{
  LL x, y;
  Coord operator - (Coord ag) const{
    Coord res;
    res.x = x - ag.x;
    res.y = y - ag.y;
    return res;
  }
}sum[MAXN], pnt[MAXN], ans, calc;

inline bool cross(Coord a, Coord b, Coord c){
  return (c.y-a.y)*(c.x-b.x) > (c.x-a.x)*(c.y-b.y);
}

int main(){
  int n, l, np, st, ed, now;
  scanf("%d %d\n", &n, &l);
  sum[0].x = sum[0].y = np = st = ed = 0;
  for (int i = 1, v; i <= n; i++){
    scanf("%d", &v);
    sum[i].y = sum[i - 1].y + v;
    sum[i].x = i;
  }
}
```

```
  ans.x = now = 1;
  ans.y = -1;
  for (int i = 0; i <= n - l; i++){
    while (np > 1 &&
            cross(pnt[np - 2], pnt[np - 1], sum[i]))
      np--;
    if (np < now && np != 0) now = np;
    pnt[np++] = sum[i];
    while (now < np &&
            !cross(pnt[now - 1], pnt[now], sum[i + l]))
      now++;
    calc = sum[i + l] - pnt[now - 1];
    if (ans.y * calc.x < ans.x * calc.y){
      ans = calc;
      st = pnt[now - 1].x;
      ed = i + l;
    }
  }
  double res = (sum[ed].y - sum[st].y) /
               (sum[ed].x - sum[st].x);
  printf("%f\n", res);
  return 0;
}
```

8.2 Exact Cover Set

```
// given n*m 0-1 matrix
// find a set of rows s.t.
// for each column, there's exactly one 1
#include <stdio.h>
#include <string.h>
#define N 1024 //row
#define M 1024 //column
#define NM ((N+2)*(M+2))
char A[N][M]; //n*m 0-1 matrix
int used[N]; //answer: the row used
int id[N][M];
int L[NM],R[NM],D[NM],U[NM],C[NM],S[NM],ROW[NM];
void remove(int c){
  L[R[c]]=L[c]; R[L[c]]=R[c];
  for( int i=D[c]; i!=c; i=D[i] )
    for( int j=R[i]; j!=i; j=R[j] ){
      U[D[j]]=U[j]; D[U[j]]=D[j]; S[C[j]]--;
    }
}
void resume(int c){
  for( int i=D[c]; i!=c; i=D[i] )
    for( int j=L[i]; j!=i; j=L[j] ){
      U[D[j]]=D[U[j]]=j; S[C[j]]++;
    }
  L[R[c]]=R[L[c]]=c;
}
int dfs(){
  if(R[0]==0) return 1;
  int md=100000000,c;
  for( int i=R[0]; i!=0; i=R[i] )
    if(S[i]<md){ md=S[i]; c=i; }
  if(md==0) return 0;
  remove(c);
  for( int i=D[c]; i!=c; i=D[i] ){
    used[ROW[i]]=1;
    for( int j=R[i]; j!=i; j=R[j] ) remove(C[j]);
    if(dfs()) return 1;
    for( int j=L[i]; j!=i; j=L[j] ) resume(C[j]);
    used[ROW[i]]=0;
  }
  resume(c);
  return 0;
}
int exact_cover(int n,int m){
  for( int i=0; i<=m; i++ ){
    R[i]=i+1; L[i]=i-1; U[i]=D[i]=i;
    S[i]=0; C[i]=i;
  }
  R[m]=0; L[0]=m;
  int t=m+1;
  for( int i=0; i<n; i++ ){
    int k=-1;
    for( int j=0; j<m; j++ ){
      if(!A[i][j]) continue;
```

```
      if(k==-1) L[t]=R[t]=t;
      else{ L[t]=k; R[t]=R[k]; }
      k=t; D[t]=j+1; U[t]=U[j+1];
      L[R[t]]=R[L[t]]=U[D[t]]=D[U[t]]=t;
      C[t]=j+1; S[C[t]]++; ROW[t]=i; id[i][j]=t++;
    }
  }
  for( int i=0; i<n; i++ ) used[i]=0;
  return dfs();
}
```