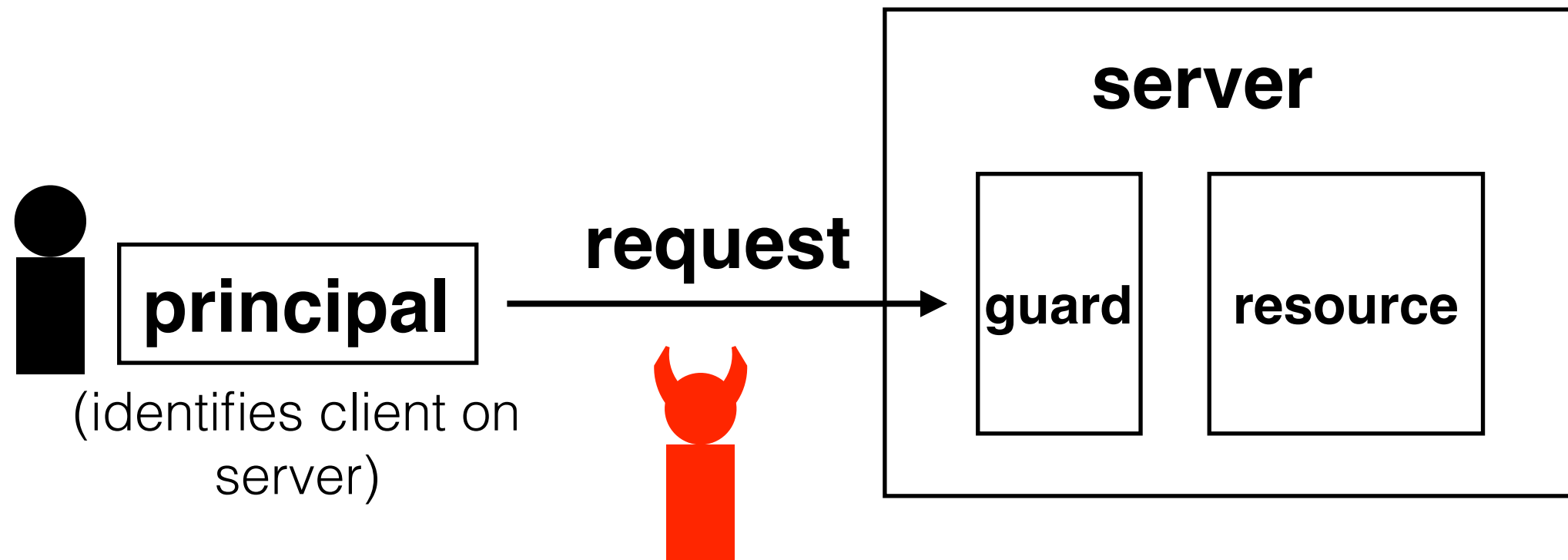


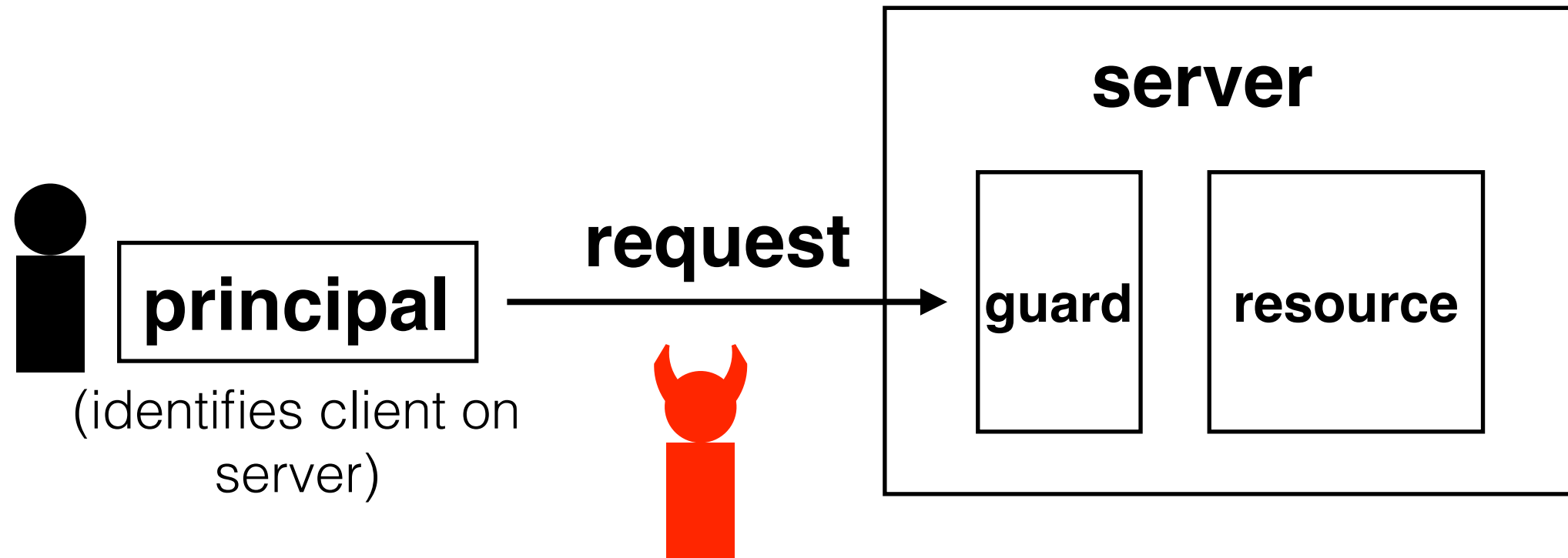
# 6.033 Spring 2019

## Lecture #22

- **Combating network adversaries**
  - **Secure Channels**
  - **Signatures**



**today we're going to focus on how to protect  
packet data from an adversary. in a future lecture,  
we'll talk about how you can protect meta-  
information (e.g., packet headers) from an  
adversary**



**confidentiality:** adversary cannot learn message contents

**integrity:** adversary cannot tamper with message contents  
(if they do, client and/or server will detect it)

**encrypt**(**key**, **message**) → **ciphertext**  
**decrypt**(**key**, **ciphertext**) → **message**

encrypt(34fbcbd1, "hello, world") = 0x47348f63a67926cd393d4b93c58f78c  
decrypt(34fbcbd1, "0x47348f63a67926cd393d4b93c58f78c") = hello, world

**property:** given the **ciphertext**, it is (virtually) impossible to obtain the **message** without knowing the **key**



adversary can't determine **message**, *but* might be able to cleverly alter **ciphertext** so that it decrypts to a different message

**encrypt**(**key**, **message**) → **ciphertext**  
**decrypt**(**key**, **ciphertext**) → **message**

encrypt(34fbcbd1, "hello, world") = 0x47348f63a67926cd393d4b93c58f78c  
decrypt(34fbcbd1, "0x47348f63a67926cd393d4b93c58f78c") = hello, world

**property:** given the **ciphertext**, it is (virtually) impossible to obtain the **message** without knowing the **key**



no good — if the adversary changes **ciphertext**, it can also (correctly) update the hash

**encrypt**(**key**, **message**) → **ciphertext**

**decrypt**(**key**, **ciphertext**) → **message**

encrypt(34fbcbd1, "hello, world") = 0x47348f63a67926cd393d4b93c58f78c

decrypt(34fbcbd1, "0x47348f63a67926cd393d4b93c58f78c") = hello, world

**property:** given the **ciphertext**, it is (virtually) impossible to obtain the **message** without knowing the **key**

**MAC**(**key**, **message**) → **token**

MAC(34fbcbd1, "hello, world") = 0x59cccc95723737f777e62bc756c8da5c

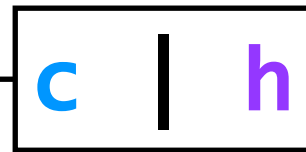
**property:** given the **message**, it is (virtually) impossible to obtain the **token** without knowing the **key**

(it is also impossible to go in the reverse direction)

alice

$c = \text{encrypt}(k, m)$   
 $h = \text{MAC}(k, m)$

in practice, we'd use one key to  
encrypt and a different one to MAC



bob

$m = \text{decrypt}(k, c)$   
 $\text{MAC}(k, m) == h ?$



alice

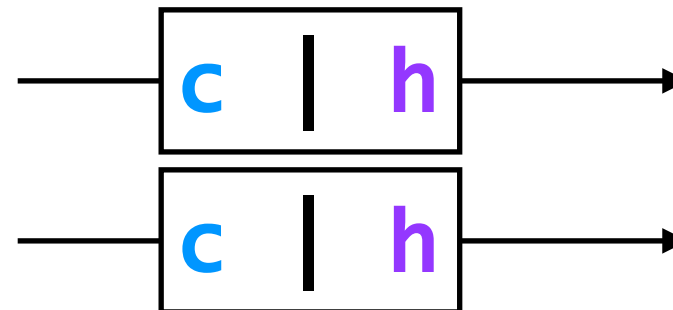
eve

bob

$c = \text{encrypt}(k, m)$   
 $h = \text{MAC}(k, m)$



$m = \text{decrypt}(k, c)$   
 $\text{MAC}(k, m) == h ?$



**problem:** replay attacks

(adversary could intercept a message, re-send it at a later time)

alice

$c = \text{encrypt}(k, m \mid \text{seq})$   
 $h = \text{MAC}(k, m \mid \text{seq})$



bob

$m \mid \text{seq} = \text{decrypt}(k, c)$   
 $\text{MAC}(k, m \mid \text{seq}) == h ?$

alice

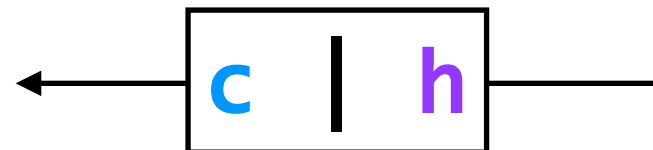
eve

bob

$c = \text{encrypt}(k, m \mid \text{seq})$   
 $h = \text{MAC}(k, m \mid \text{seq})$



$m \mid \text{seq} = \text{decrypt}(k, c)$   
 $\text{MAC}(k, m \mid \text{seq}) == h ?$



**problem:** reflection attacks

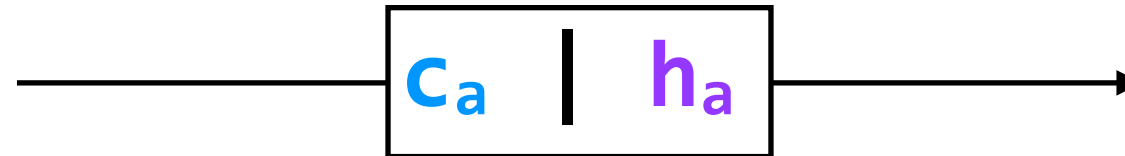
(adversary could intercept a message, re-send it at a later time in the opposite direction)

alice

bob

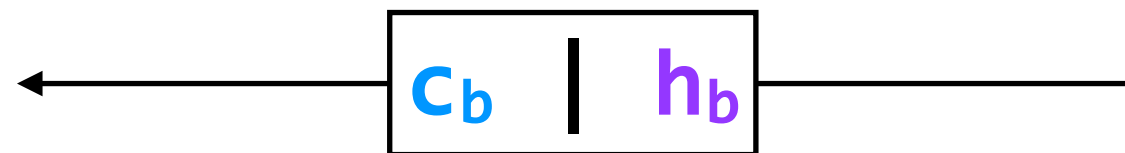
$c_a = \text{encrypt}(k_a, m_a \mid \text{seq}_a)$

$h_a = \text{MAC}(k_a, m_a \mid \text{seq}_a)$



$m_a \mid \text{seq}_a = \text{decrypt}(k_a, c_a)$   
 $\text{MAC}(k_a, m_a \mid \text{seq}_a) == h_a ?$

$c_b = \text{encrypt}(k_b, m_b \mid \text{seq}_b)$   
 $h_b = \text{MAC}(k_b, m_b \mid \text{seq}_b)$

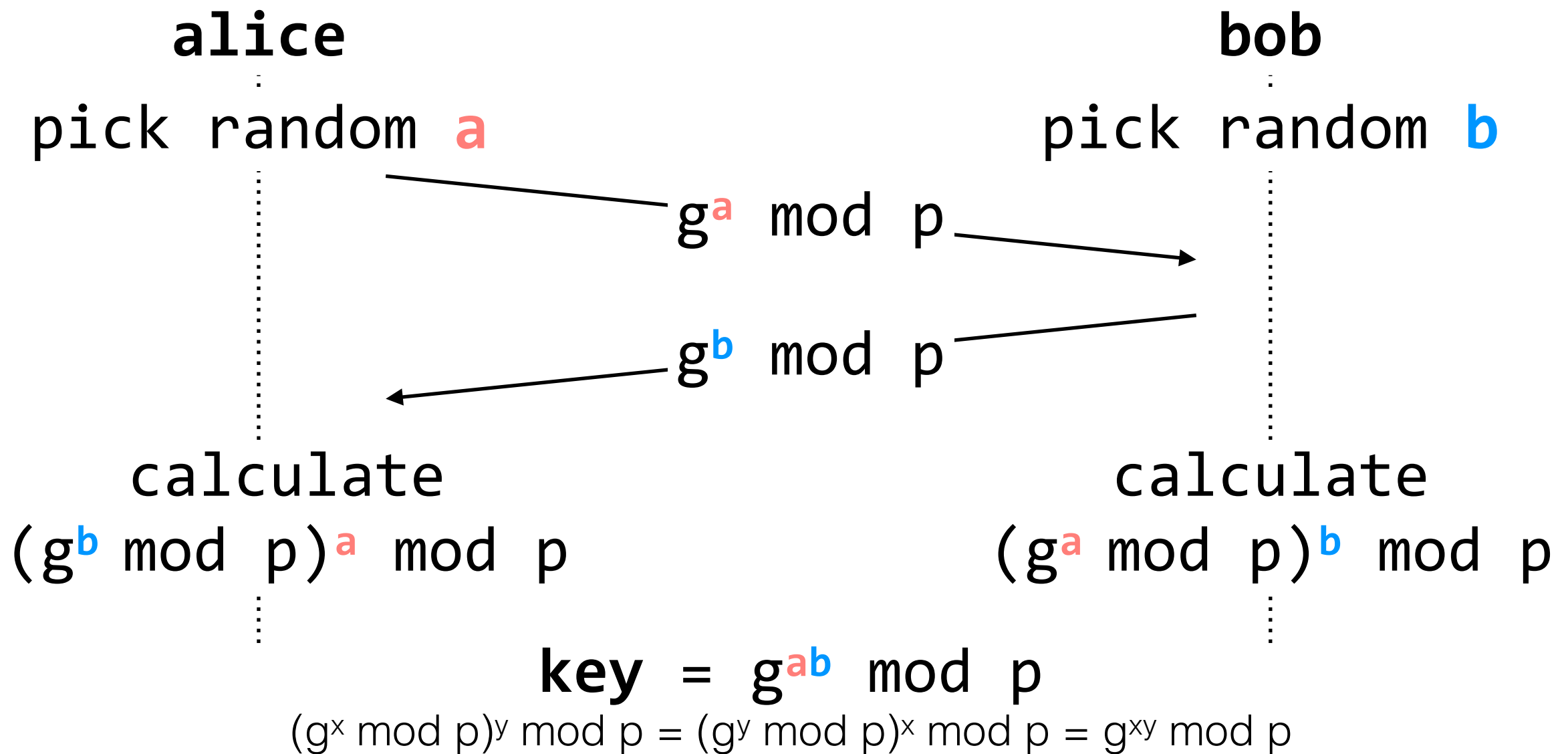


$m_b \mid \text{seq}_b = \text{decrypt}(k_b, c_b)$   
 $\text{MAC}(k_b, m_b \mid \text{seq}_b) == h_b ?$

**problem:** how do the parties know the keys?

**known:**  $p$  (prime),  $g$

**property:** given  $g^r \bmod p$ , it is (virtually) impossible to determine  $r$  *even if* you know  $g$  and  $p$



alice

eve

bob

pick random  $a$

pick random  $e$

pick random  $b$

$g^a \bmod p$

$g^b \bmod p$

$g^e \bmod p$

$g^e \bmod p$

$$k_1 = (g^e)^a \bmod p$$

$$k_2 = (g^e)^b \bmod p$$

eve can calculate  
 $k_1$  and  $k_2$

— encrypt( $k_1$ ,  $m$ ) →

decrypt  $m$

— encrypt( $k_2$ ,  $m$ ) →

**problem:** alice and bob don't know they're not communicating directly

# cryptographic signatures

allow users to verify identities using public-key cryptography

## users generate key pairs

the two keys in the pair are related mathematically

{**public\_key**, **secret\_key**}

**sign**(**secret\_key**, message) → **sig**

**verify**(**public\_key**, message, **sig**) → yes/no

**property:** it is (virtually) impossible to compute **sig** without  
**secret\_key**

alice

bob

$m$  = original message

$c$  =  $\text{encrypt}(k_a, m \mid \text{seq}_a)$

$h$  =  $\text{MAC}(k_a, m \mid \text{seq}_a)$

$\text{sig}$  =  $\text{sign}(\text{secret\_key}_a, m \mid \text{seq}_a)$



$m \mid \text{seq}_a = \text{decrypt}(k_a, c)$

$\text{MAC}(k_a, m \mid \text{seq}_a) == h ?$

$\text{verify}(m \mid \text{seq}_a, \text{public\_key}_a, \text{sig}) == \text{yes} ?$

**verify** will not check out if **sig** was not created with **secret\_key<sub>a</sub>**, the corresponding secret key to **public\_key<sub>a</sub>**



alice

bob

$m$  = original message

$c$  =  $\text{encrypt}(k_a, m \mid \text{seq}_a)$

$h$  =  $\text{MAC}(k_a, m \mid \text{seq}_a)$

$\text{sig}$  =  $\text{sign}(\text{secret\_key}_a, m \mid \text{seq}_a)$



$m \mid \text{seq}_a = \text{decrypt}(k_a, c)$

$\text{MAC}(k_a, m \mid \text{seq}_a) == h ?$

$\text{verify}(m \mid \text{seq}_a, \text{public\_key}_a, \text{sig}) == \text{yes} ?$

how do we distribute public keys?

client

# TLS handshake

server

ClientHello {version, **seq<sub>c</sub>**, session\_id, cipher suites, compression func}

ServerHello {version, **seq<sub>s</sub>**, session\_id, cipher suite, compression func}

{server certificate, CA certificates}

ServerHelloDone

client verifies authenticity of server

ClientKeyExchange {encrypt(server\_pub\_key, **pre\_master\_secret**)}

compute

master\_secret = PRF(**pre\_master\_secret**, "master secret", **seq<sub>c</sub>** | **seq<sub>s</sub>**)

key\_block = PRF(**master\_secret**, "key expansion", **seq<sub>c</sub>** | **seq<sub>s</sub>**)

= {client\_MAC\_key,  
server\_MAC\_key,  
client\_encrypt\_key,  
server\_encrypt\_key,  
...}

Finished {sign(client\_MAC\_key, encrypt(client\_encrypt\_key,  
MAC(master\_secret, previous\_messages)))}

Finished {sign(server\_MAC\_key, encrypt(server\_encrypt\_key,  
MAC(master\_secret, previous\_messages)))}

- **Secure channels** protect us from adversaries that can observe and tamper with packets in the network.
- Encrypting with **symmetric keys** provides secrecy, and using **MACs** provides integrity. **Diffie-Hellman key exchange** lets us exchange the symmetric key securely.
- To verify identities, we use **public-key cryptography** and cryptographic **signatures**. We often distribute public keys with **certificate authorities**, though this method is not perfect.