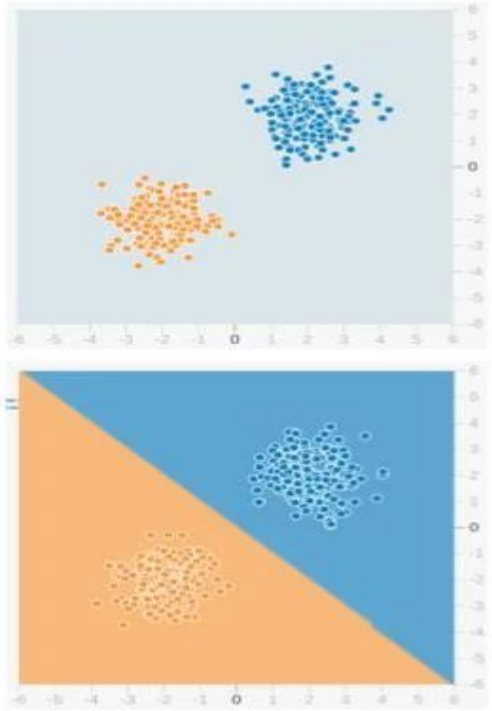
Deep Learning

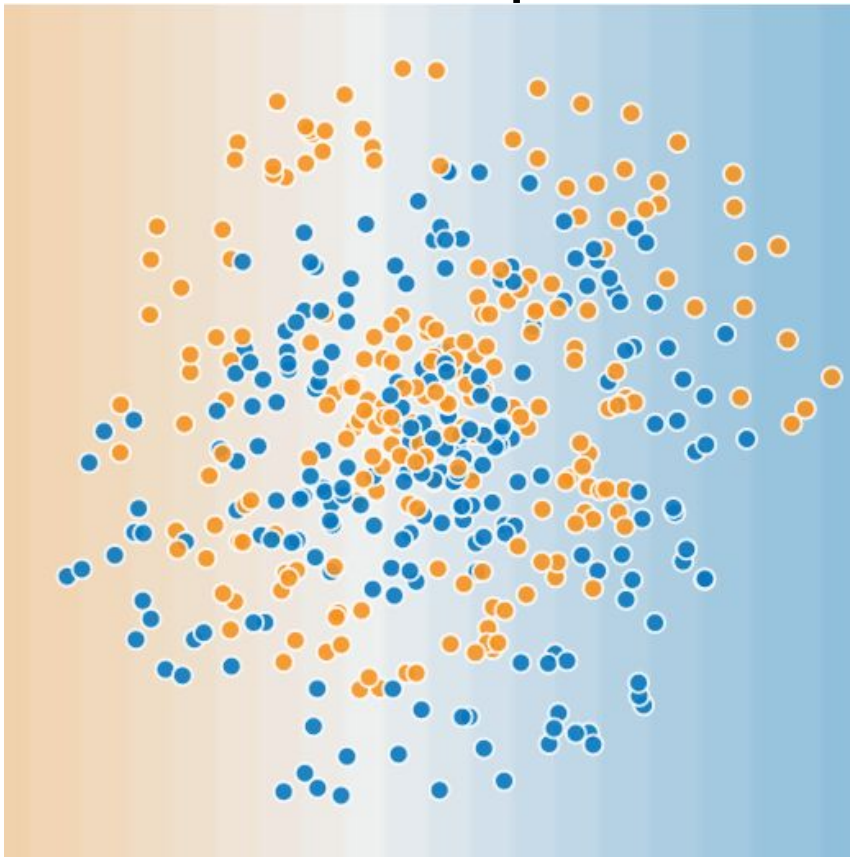
Neural Networks

A “Simple” Classification Problem



How about this classification problem?

Linear model can not solve the problem



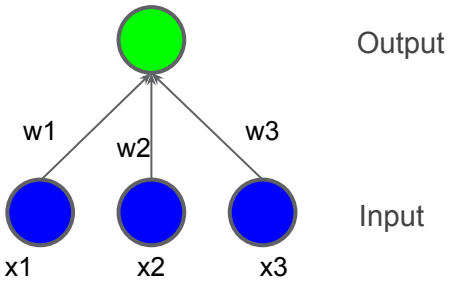
We need **non-linear models**

A Linear Model

- Linear Regression if output is continuous
- Logistic Regression if output is discrete

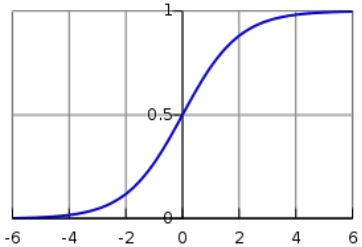
Linear Regression

$$y = \mathbf{w}\mathbf{x} + b$$

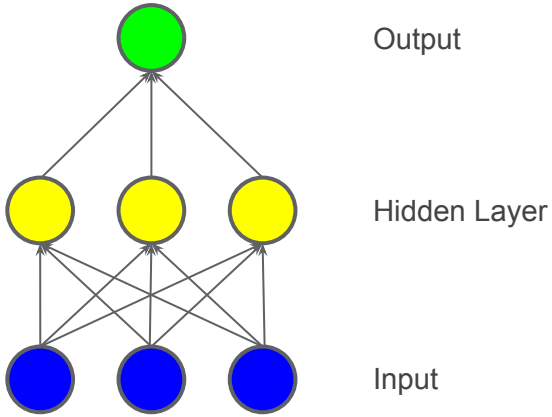


Logistic Regression

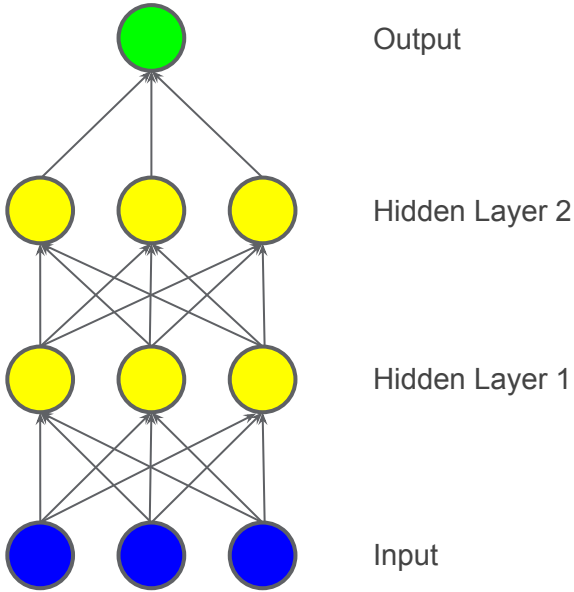
$$y = \sigma(\mathbf{w}\mathbf{x} + b)$$



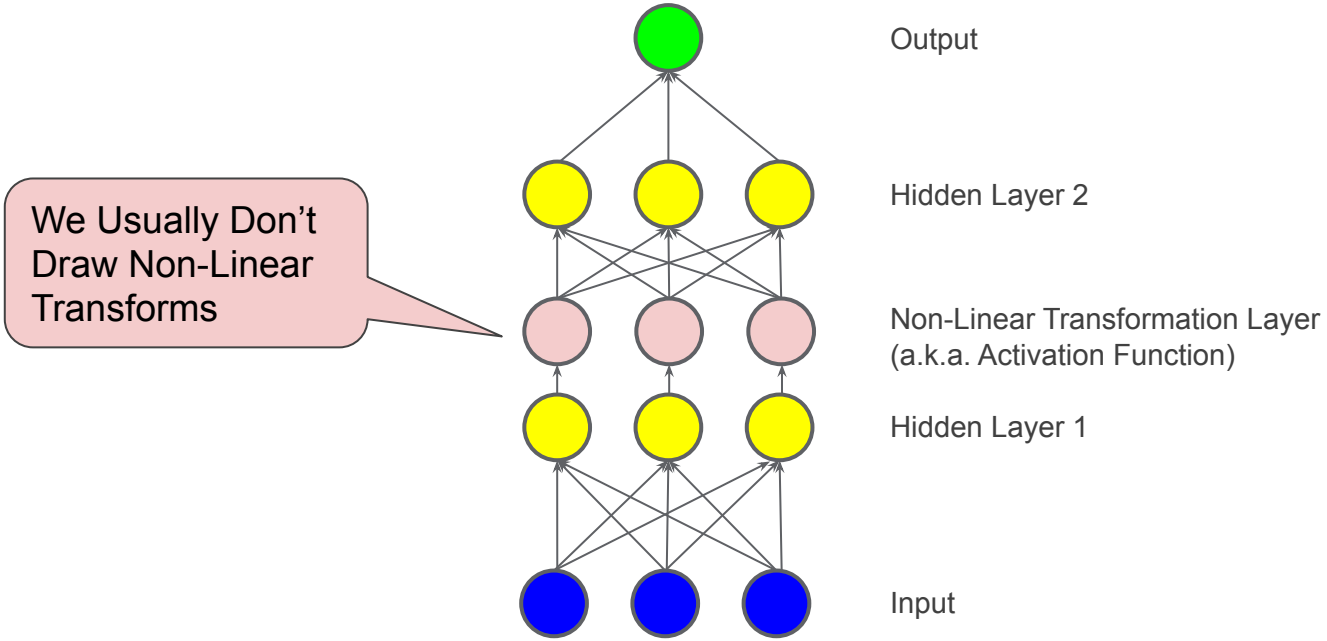
Add Complexity



How about now?



Make it non-linear

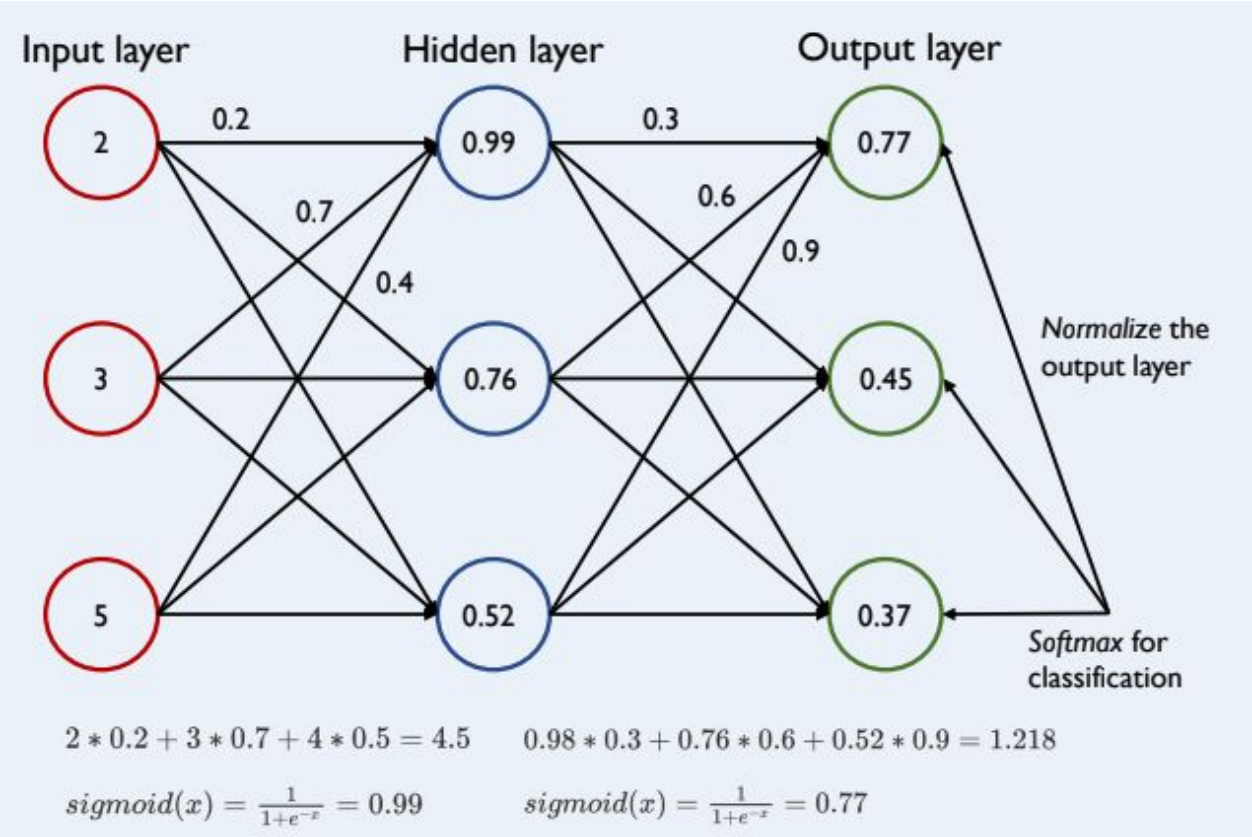


Why Non-linear Activation

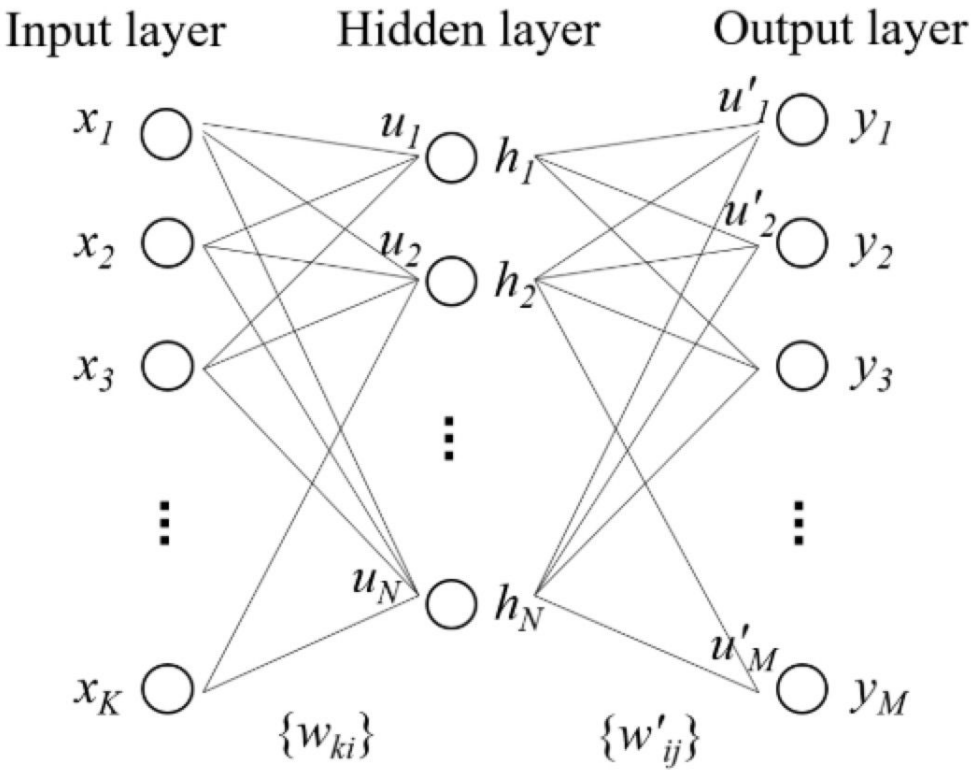
- The non-linearities activation function increases the capacity of model
- Without non-linearities, deep neural networks is meaningless: each extra layer is just one linear transform.
- How to select activation functions?

  You can select an activation function which will approximate the distribution faster leading to faster training process.

Forward Computation



Forward Computation



$$u_i = \sum_{k=1}^{K} w_{ki} x_k$$

$$h_i = f(u_i)$$

$$u'_j = \sum_{i=1}^{N} w'_{ij} h_i$$

$$y_j = f(u'_j)$$

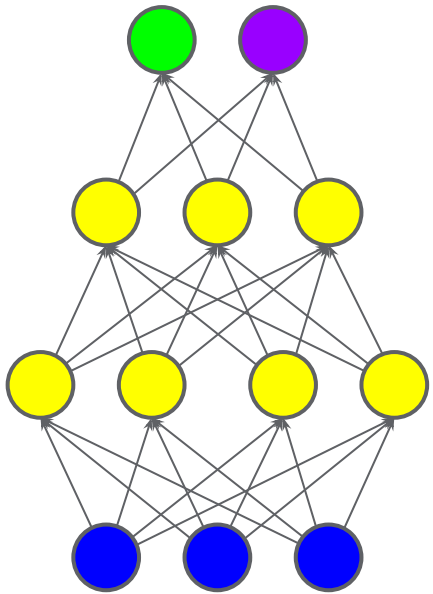
Forward Computation

1. Take f as the non-linear activation
2. Linear Transformation: $h = W_1 x$
3. 2-layer Neural Network: $h = W_2 f(W_1 x)$
4. 3-layer Neural Network: $h = W_3 f(W_2 f(W_1 x))$

- Neural Network is a model that **recursively** applies the matrix multiplication and non-linear activation function.

Backpropagation

Neural networks can be arbitrarily complex



Training done via BackProp algorithm: gradient descent in very non-convex space

$$\min E\big(f(x), t\big) + R$$

optimizer
error function
data
architecture
regularization term

Gradient Descent

Gradient for loss function f for $\mathbf{x}_n$, which computed by BP algorithm

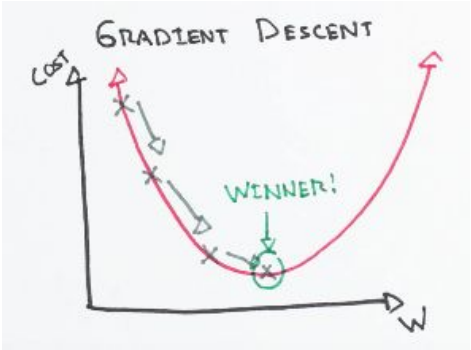
$$\mathbf{x}_{n+1} = \mathbf{x}_n - \alpha \nabla f(\mathbf{x}_n)$$

New Parameters Guess

Current Parameters Guess

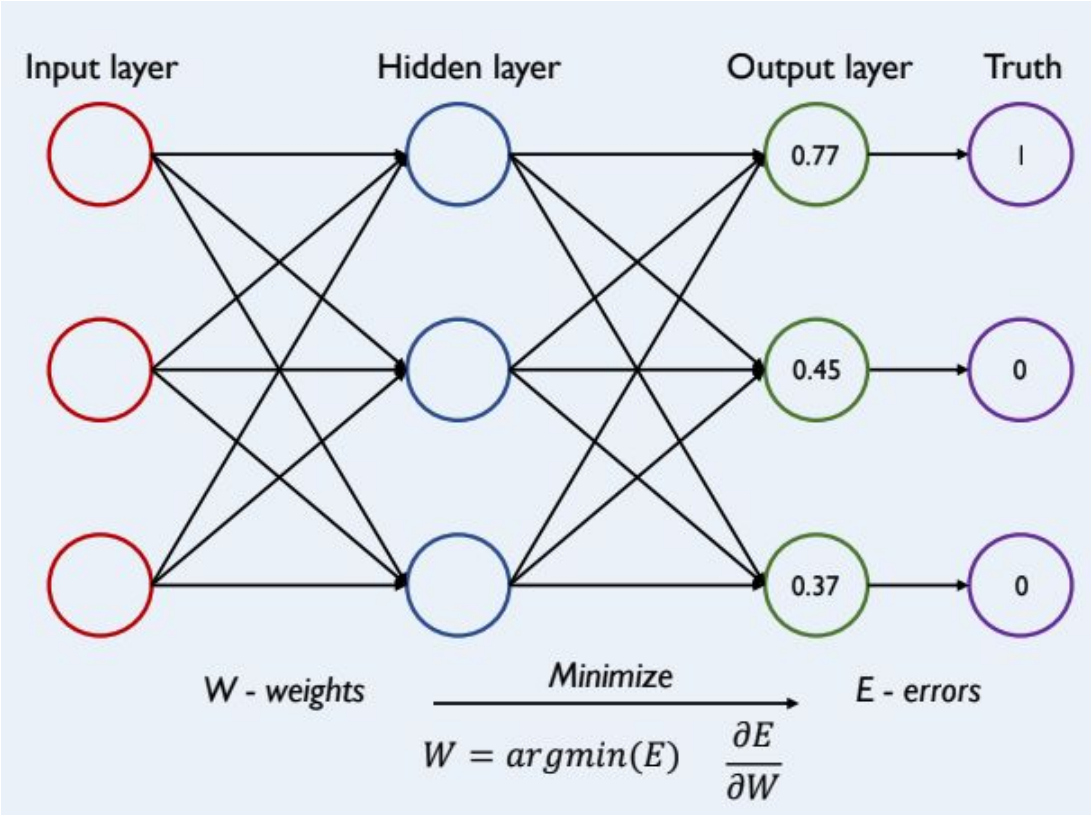
Learning Rate

Like hiking down a mountain



Credit: https://ml-cheatsheet.readthedocs.io/en/latest/gradient_descent.html

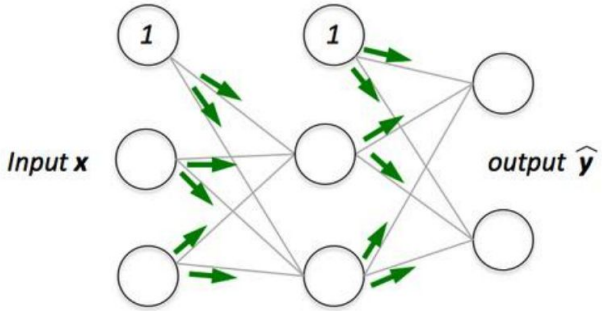
Backpropagation



Backpropagation

Step 1:

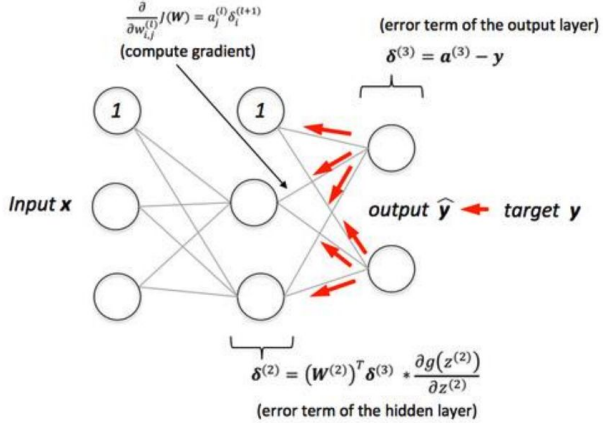
Forward pass to compute the network output and “error”



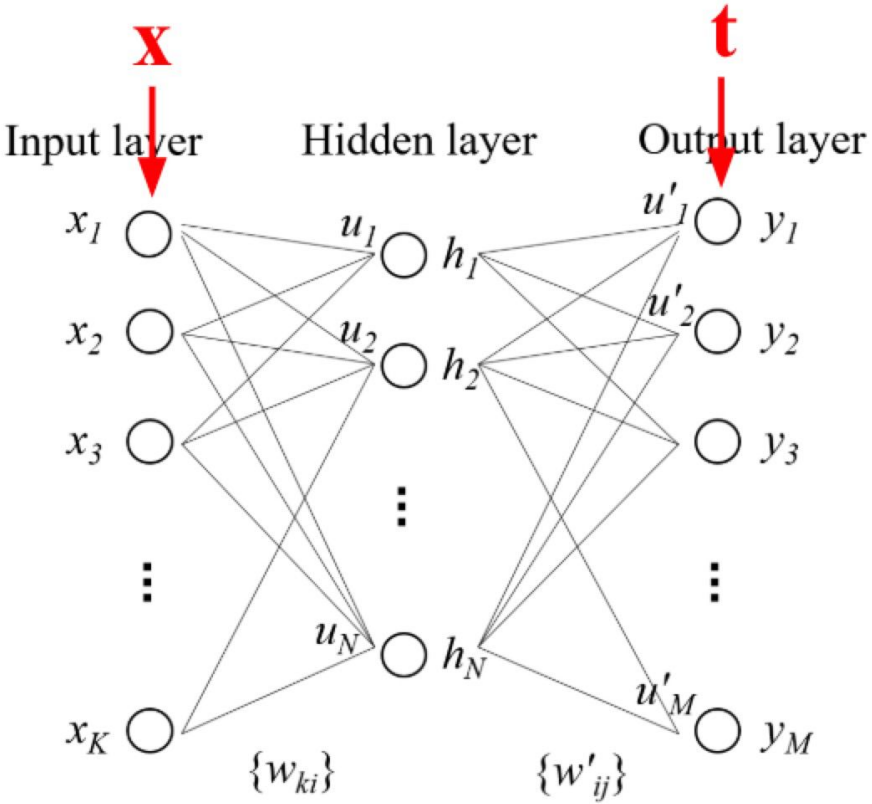
Step 2:

Backward pass to compute gradients

And update the model weights based on gradients.



Backpropagation



$$E = \frac{1}{2}\sum_{j=1}^{M}(y_j - t_j)^2$$

$$\frac{\partial E}{\partial y_j} = y_j - t_j$$

$$\frac{\partial E}{\partial u'_j} = \frac{\partial E}{\partial y_j} \cdot \frac{\partial y_j}{\partial u'_j}$$

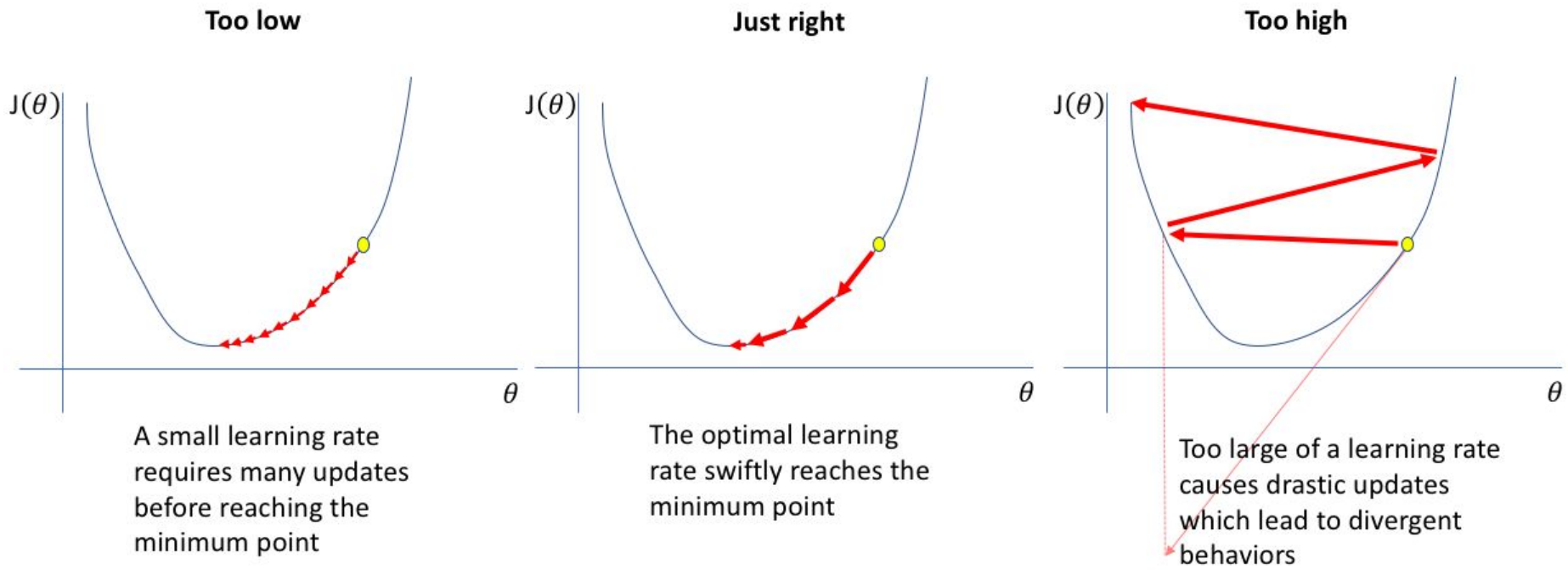
$$\frac{\partial E}{\partial w'_{ij}} = \frac{\partial E}{\partial u'_j} \cdot \frac{\partial u'_j}{\partial w'_{ij}}$$

$$\frac{\partial E}{\partial h_i} = \sum_{j=1}^{M} \frac{\partial E}{\partial u'_j} \frac{\partial u'_j}{\partial h_i}$$

$$\frac{\partial E}{\partial u_i} = \frac{\partial E}{\partial h_i} \cdot \frac{\partial h_i}{\partial u_i}$$

$$\frac{\partial E}{\partial w_{ki}} = \frac{\partial E}{\partial u_i} \cdot \frac{\partial u_i}{\partial w_{ki}}$$

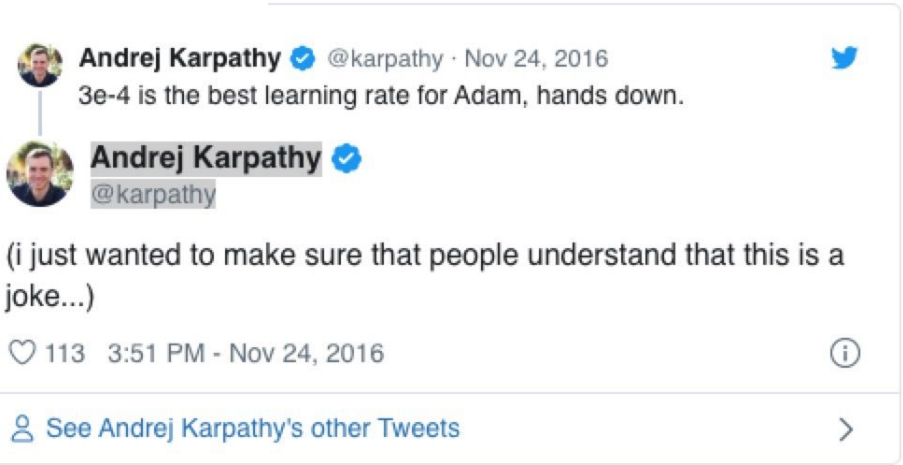
How to find learning rate?



https://machinelearningmastery.com/understand-the-dynamics-of-learning-rate-on-deep-learning-neural-networks/

A Joke

One variant of Gradient Descent Algorithm



Training Process

1. Initialize neural network randomly
2. Get output with input data
3. Compare outputs with ground truth in training data
4. Get loss function
5. Update weights with backpropagation and gradient descent algorithm

$$\mathbf{x}_{n+1} = \mathbf{x}_n - \alpha \bigtriangledown f(\mathbf{x}_n)$$

- Stochastic gradient descent (SGD)
  - Randomly shuffle the data
  - Batch size k: the number of data used for steps 2-5
  - One epoch: the full scan of all the training data. How many times will the weights be updated in one epoch?
  - Number of Epoch T: the number of iterations to stop training

Types of Gradient Descent Algorithms

1. Batch Gradient Descent — *batch size = Number of data*
2. Mini-batch Gradient Descent — *1<batch size< number of data*
3. Stochastic Gradient Descent — *batch size = 1*

Batch SGD

Batch SGD: batch size is the number of training data

1 only update model parameters after all training data have been evaluated.

2 stable error gradient

3 need a large memory

4 may lead to a less optimal solution

Mini-Batch SGD

Mini-batch SGD: split the dataset into small batches and take the average of the gradient over the batch and update the weights

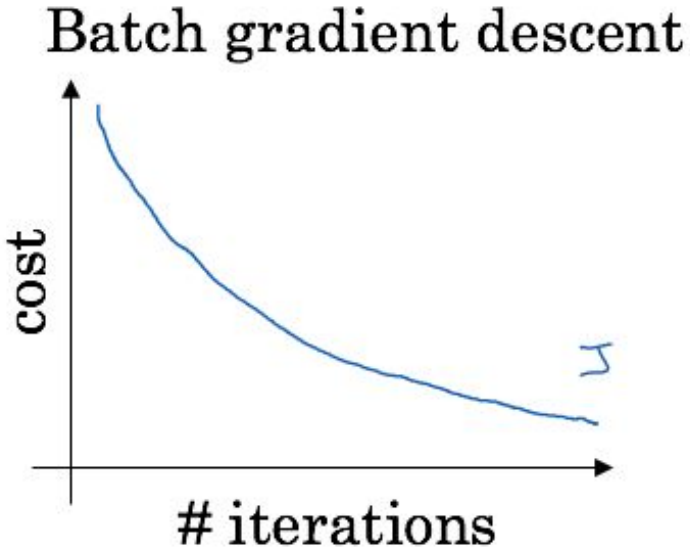
1 more efficient than SGD

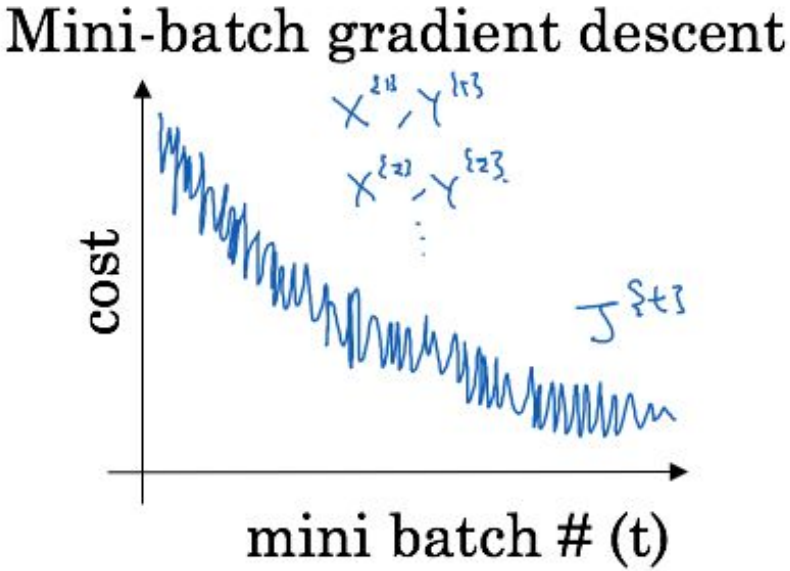
2 requires additional hyperparameter i.e. mini-batch size

3 hints on batch size:

* a power of two that fits the memory requirements of GPU or CPU.
* small -> a learning process that converges quickly at the cost of noise in the training
* large -> a learning process that converges slowly with accurate estimate of the error gradient

Mini-Batch vs Batch





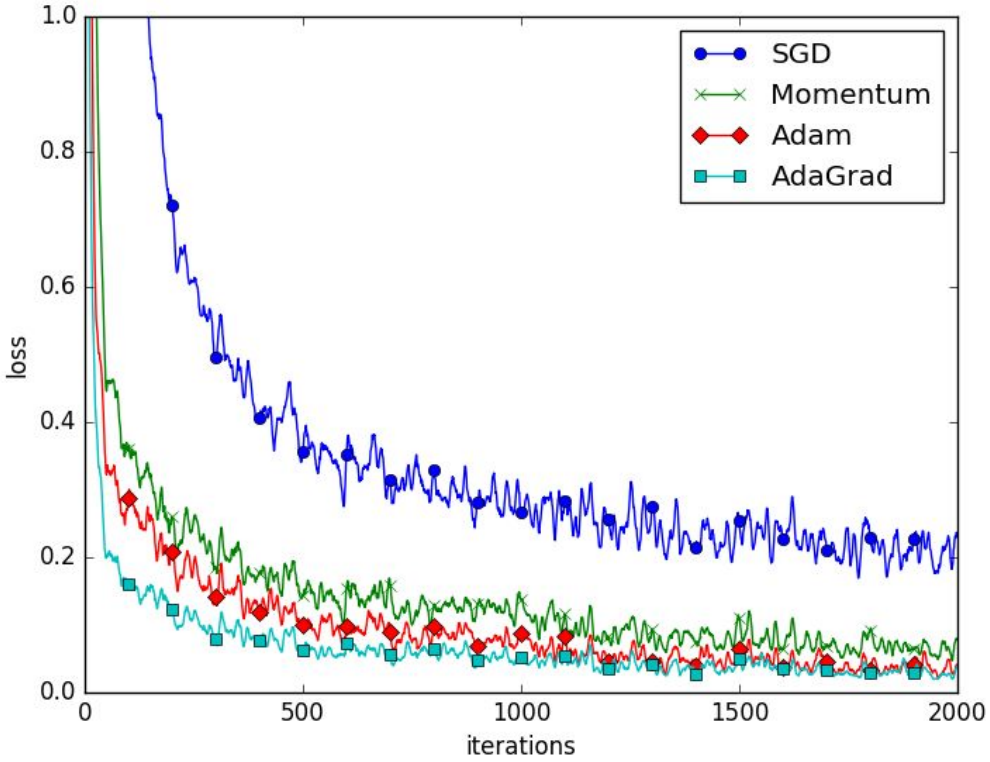
Except SGD

SGD

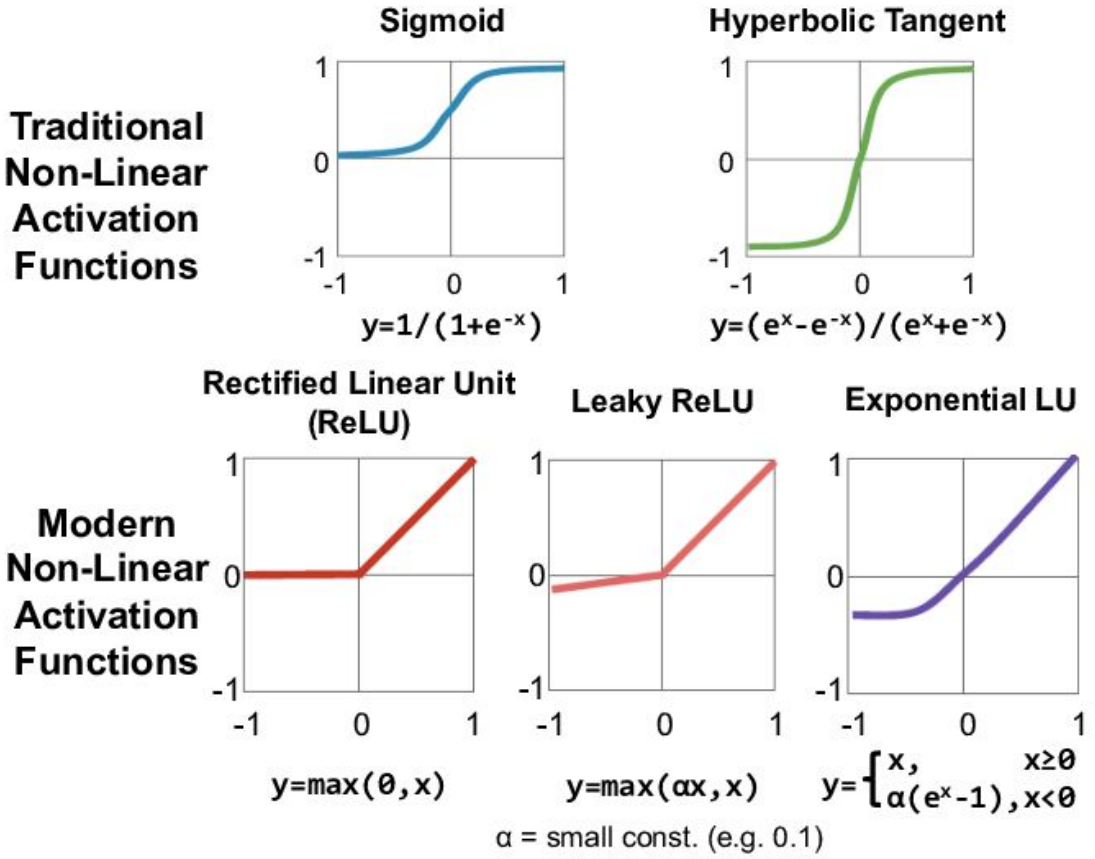
$$\mathbf{x}_{n+1} = \mathbf{x}_n - \alpha \bigtriangledown f(\mathbf{x}_n)$$

Different Variants

Momentum, Adam, AdaGrad, RMSProp



Non-linear Activation Functions

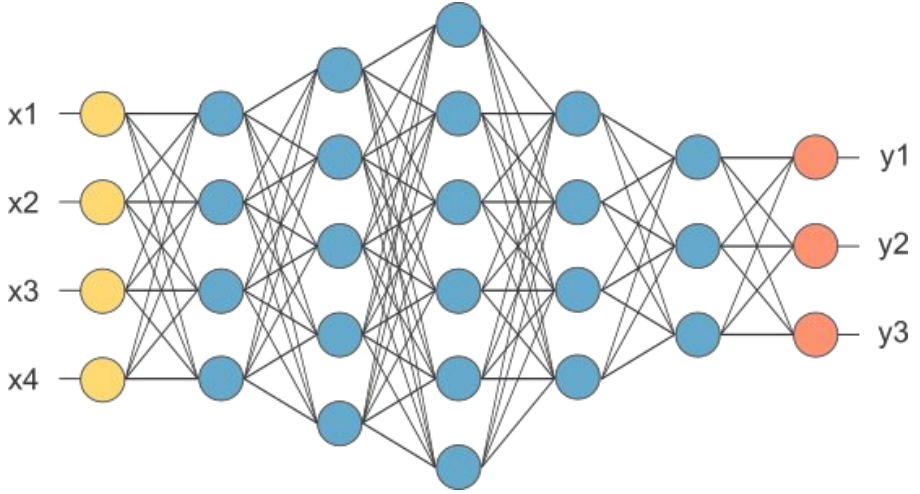


When Gradient is zero

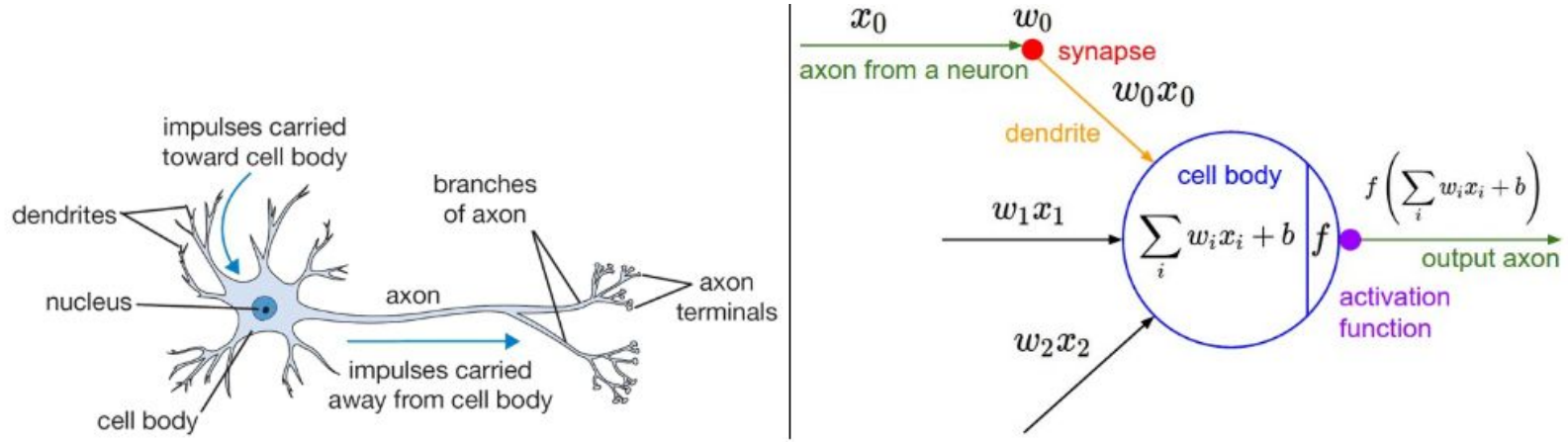
Neural Network

1. From Wiki:
   - NN is based on a collection of connected units of nodes called artificial **neurons** which loosely model the neurons in a biological brain.

2. From another way:
   - NN is running several ‘logistic regression’ at the same time (expanding at width and depth dimensions).



Neural Computation

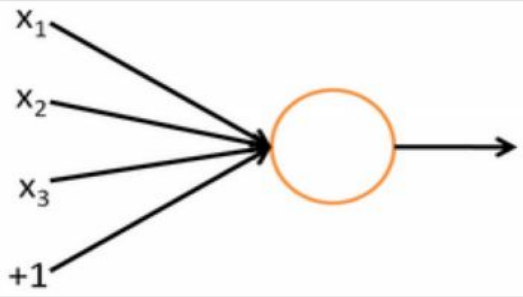


A cartoon drawing of a biological neuron (left) and its mathematical model (right).

The fact that a neuron is essentially a logistic regression unit:

1 performs a dot product with the input and its weights

2 adds the bias and apply the non-linearity

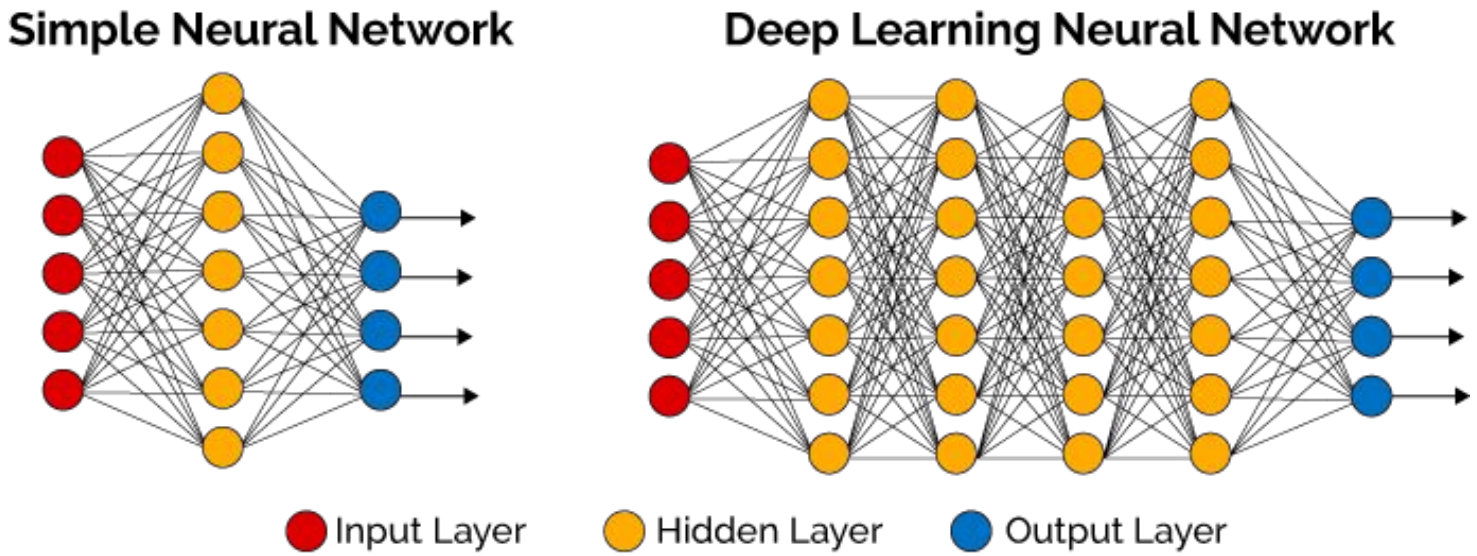


Neural Network Visualization

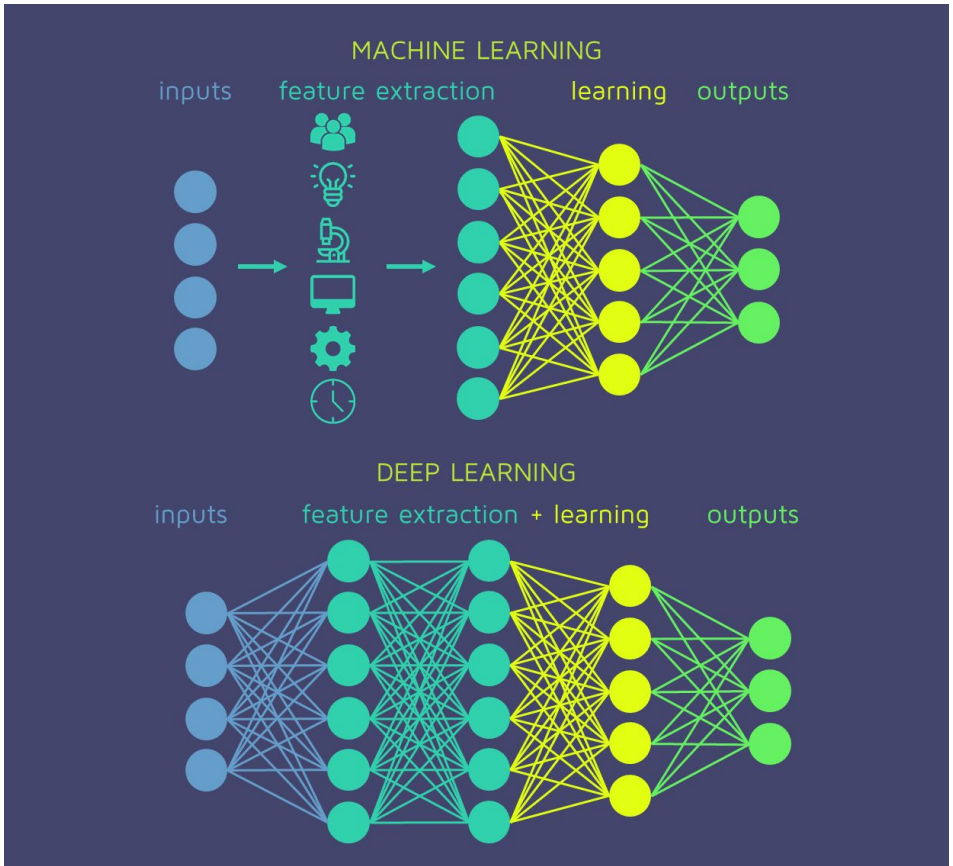
Playground

Deep Learning/Deep Neural Networks

Shallow vs Deep

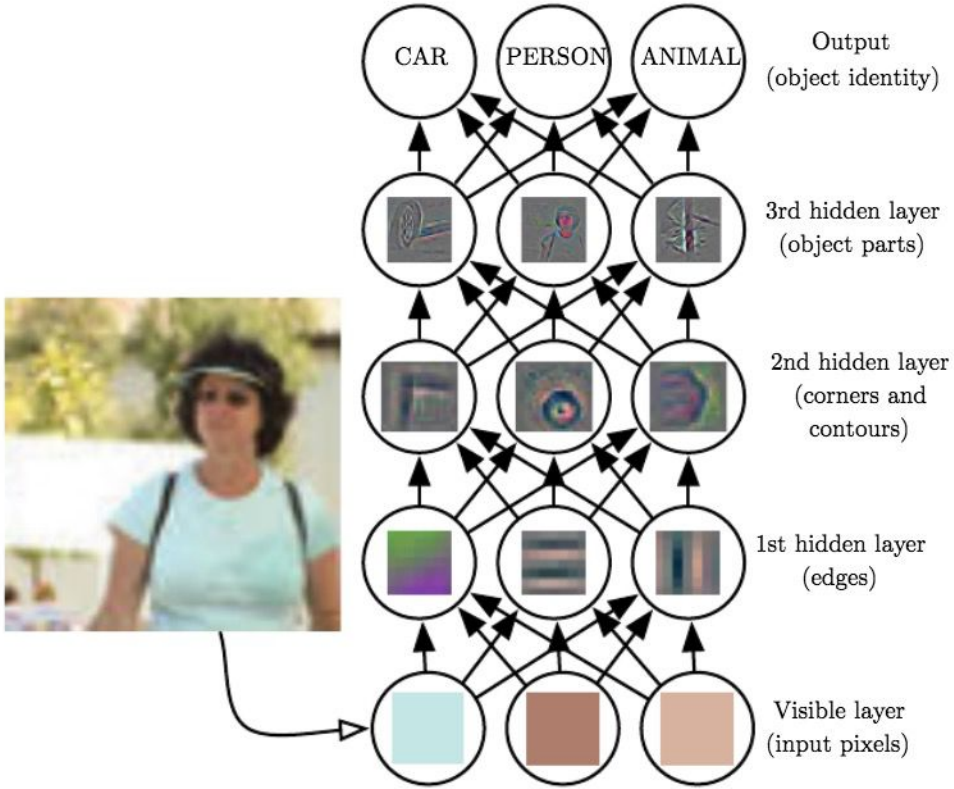


End-to-End Learning



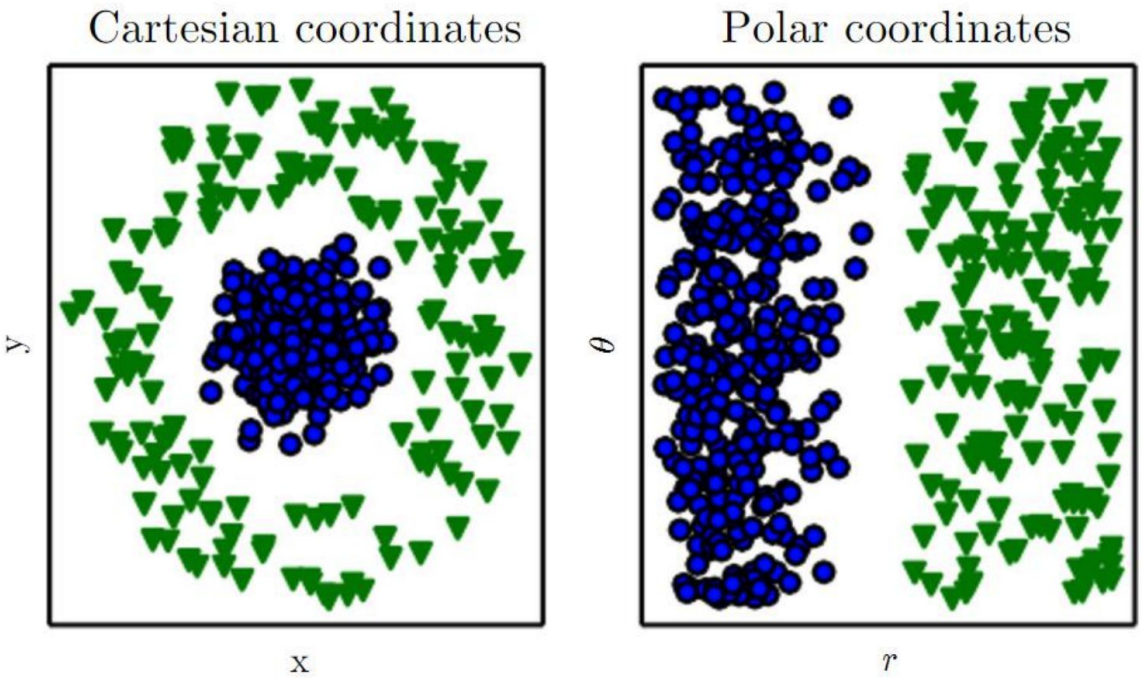
From Aporras

Representation Learning in DL

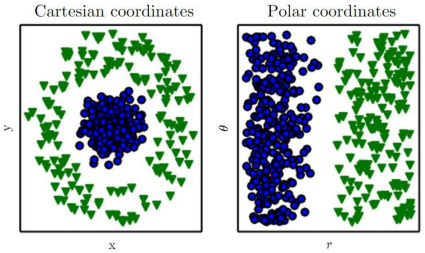


From Deep Learning (Goodfellow)

Representation Matters

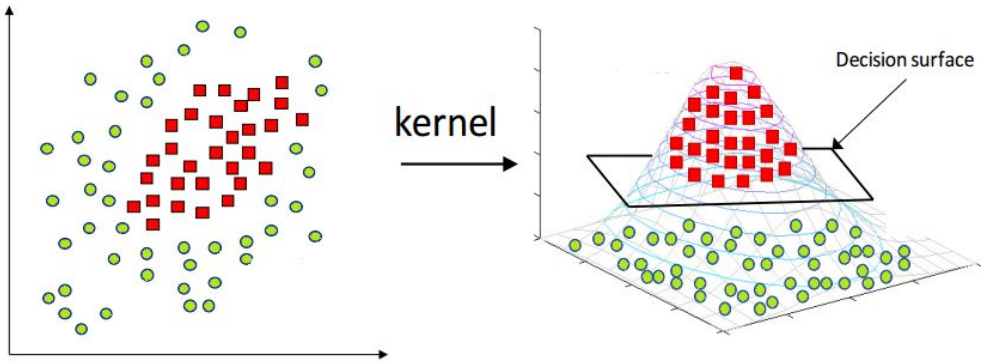


Task: Draw a line to separate the **green triangles** and **blue circles**.



We want to project the data into the new feature/vector space that data is linearly separated

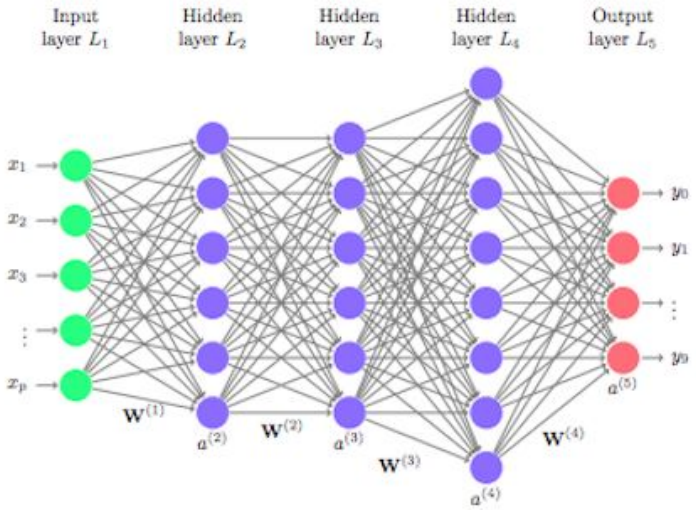
Kernel Tricks in SVM



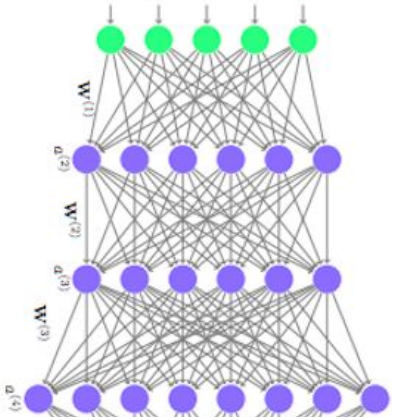
Low-dim, Original Space

High-dim, **Linearly Separated** Space

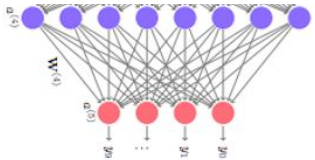
“Trick” in Deep Learning



Low-dim, Original Space

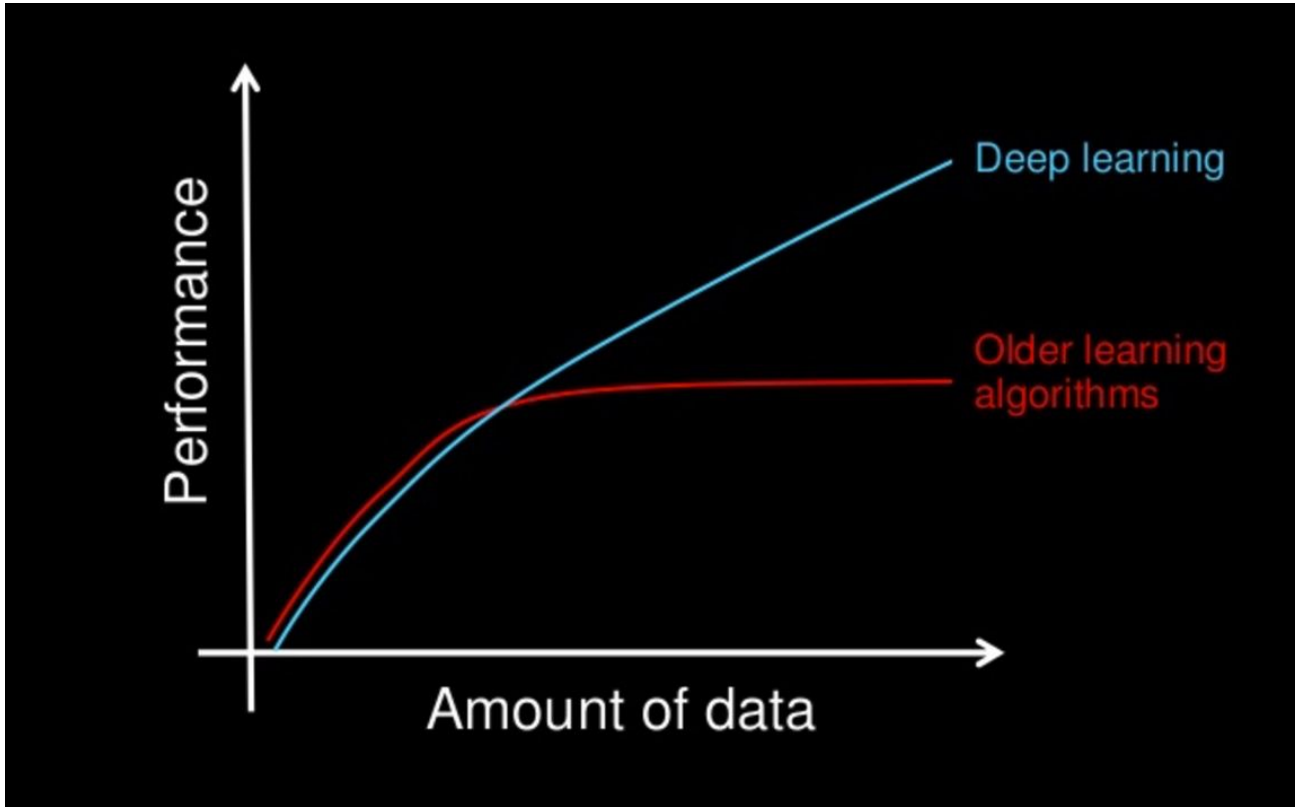


High-dim, **Linearly Separated** Space



Softmax Classifier
(Linear Model)

Why Deep Learning



From Andrew Ng

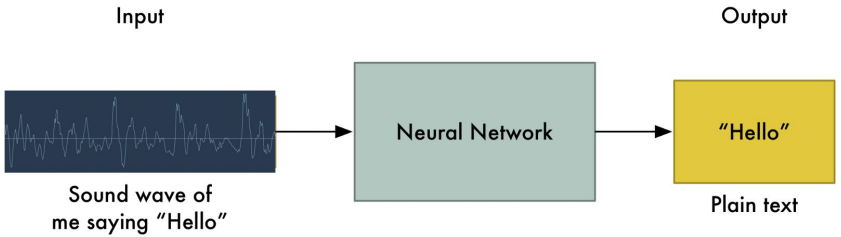
Deep Learning

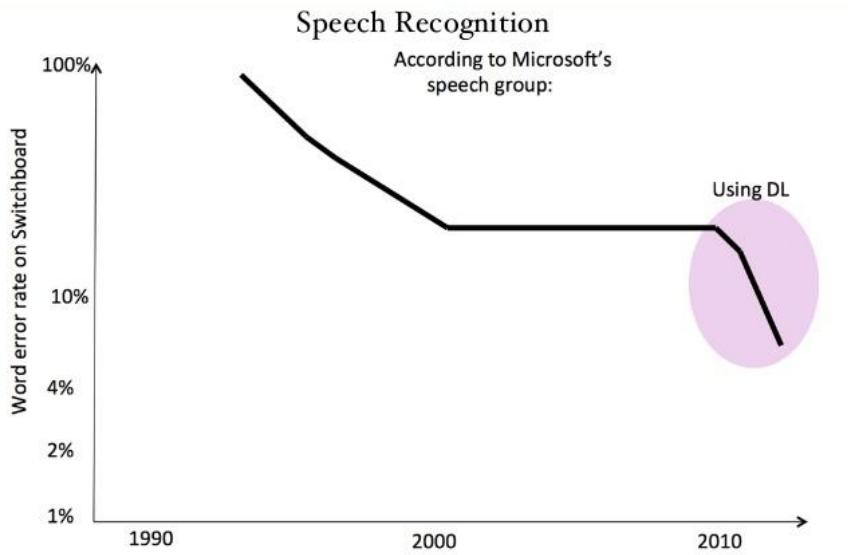
- Deep learning is a subfield of machine learning
- Most machine learning methods work well because of high-quality feature engineering/representation learning.
- Deep learning is an **end-to-end** structure, which supports automatic representation learning
- Different network structures: CNN, RNN, LSTM, GRU, Attention model, etc

Applications of DL

Deep Learning for Speech

The first real-world tasks addressed by deep learning is speech recognition

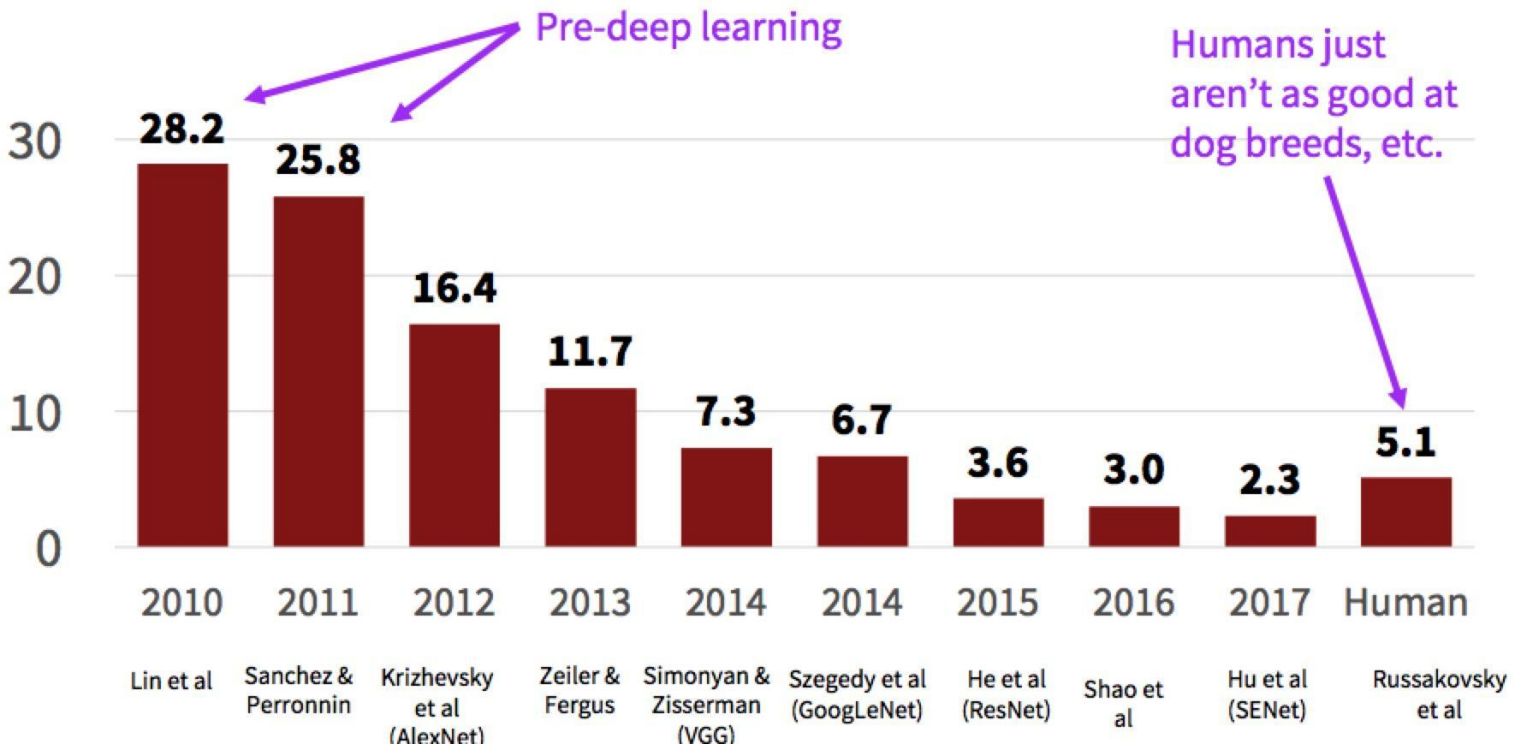




Deep Learning for Computer Vision

- Computer vision may be the most well-known breakthrough of DL.
- ImageNet Classification with Deep Convolutional Neural Networks.

ImageNet Scoreboard



Deep Learning For Arts

Style transfer based on Deep Learning: use one image to stylize another.

Original photo Reference photo Result

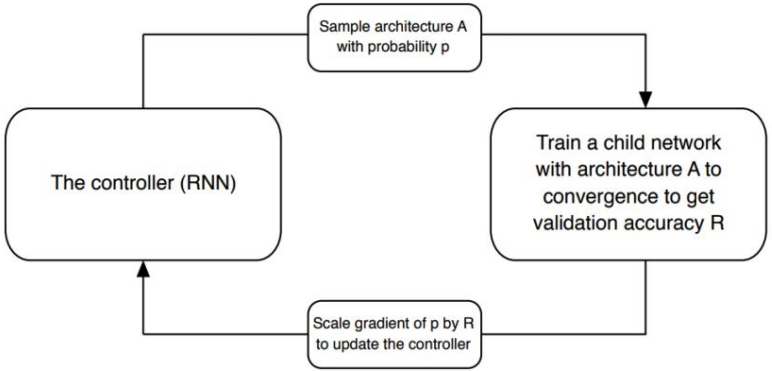
The now iconic examples from Figure 2 of Gatys et al (2015).

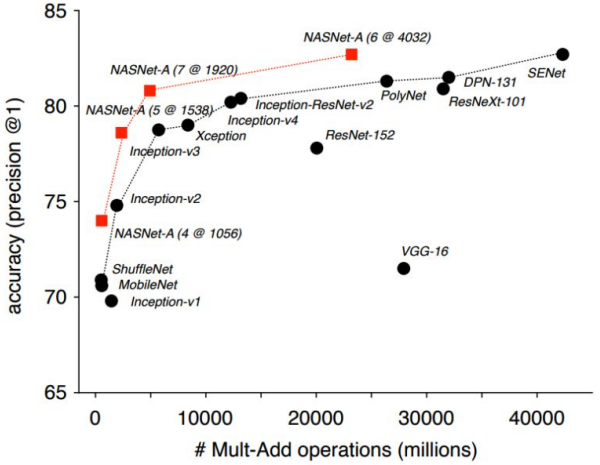
Deep Learning For Data Generation

Given training data, generate new data samples from same distribution

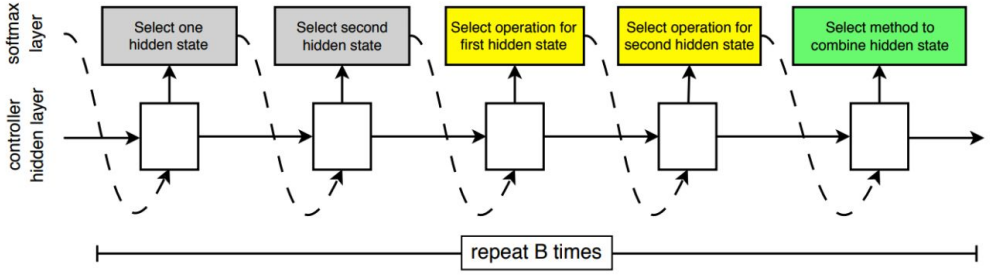
Examples of Photorealistic GAN-Generated Faces.

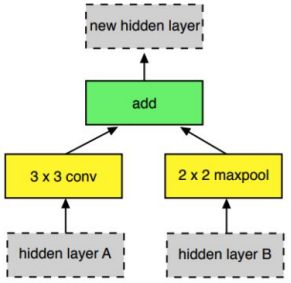
AutoML and Neural Architecture Search



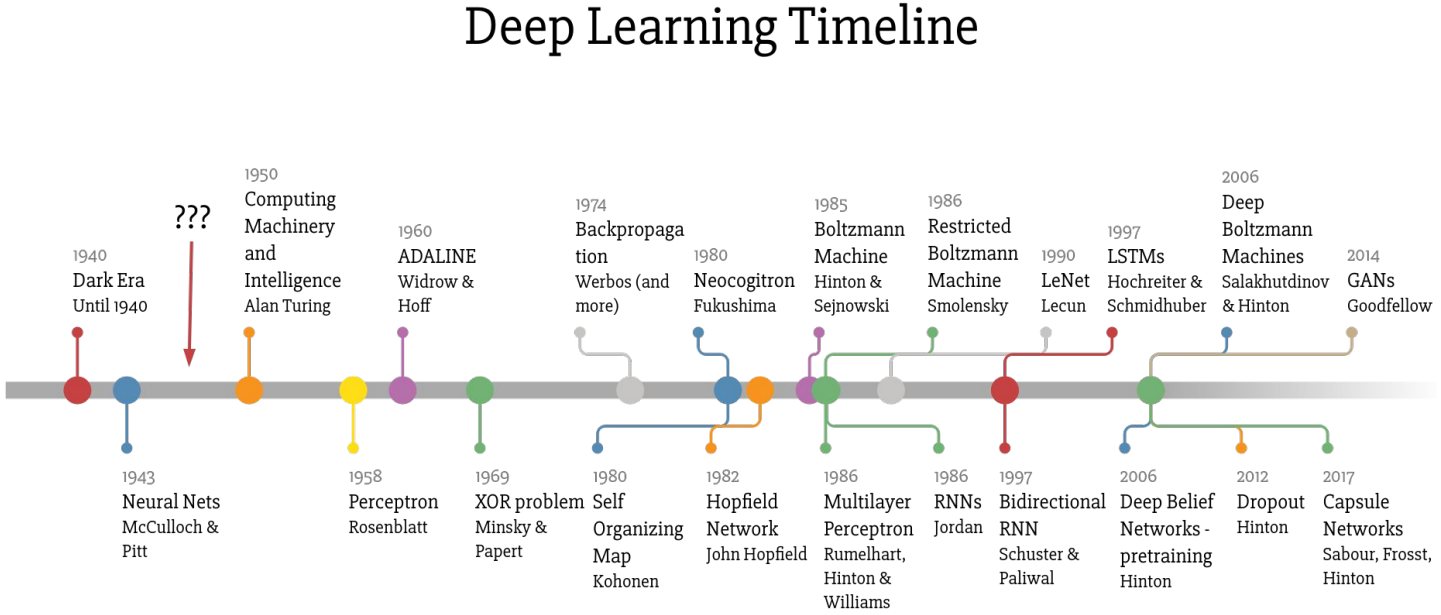


Source:Lex Fridman





DL/NN is not New



Made by Favio Vázquez

Why is Deep Learning Powerful Now?

- Feature engineering require high-level expert knowledge, which are easily over-specified and incomplete.
- Large amounts of training data
- Modern multi-core CPUs/GPUs/TPUs
- Better deep learning ‘tricks’ such as regularization, optimization, transfer learning etc.

When DL may not Work

You need to get off your non-motor vehicle when u pass the pedestrian crossing.

detected offender

The Challenge of Deep Learning

- **Ask the right question** and **know what the answer means**:

  Image classification is not scene understanding.

- **Select, collect, and organize the right data to train on**:



Efficient Teaching/Efficient Learning

- Humans can learn from few examples

- DL/machine require thousands/millions of examples
  - Data augmentation

Limitations

- DL always requires a large amount of annotated data

14 million

Pre-training, Transfer Learning, Data Augmentation

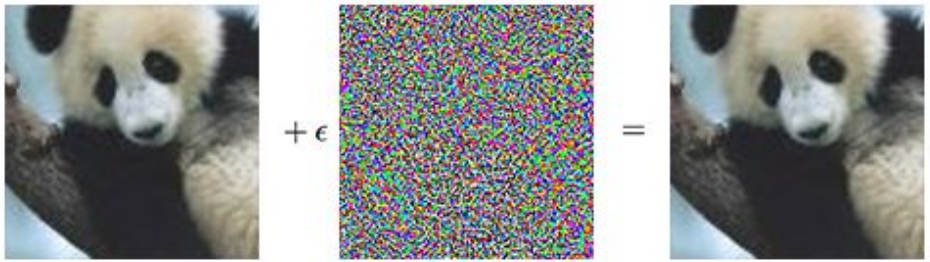
- Generalization capability is low, e.g. the model that perform well on benchmarked datasets fail badly on real world images

- Easily got attacked by random, tiny noise
- How to explain such huge black box

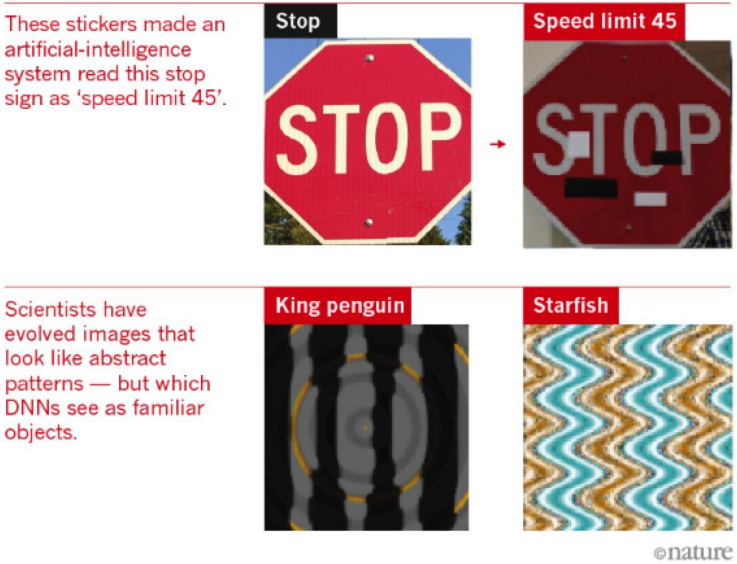
Attack Machine Learning

Attack Machine Learning

Adversarial Examples



Open AI



Why deep-learning AIs are so easy to fool

Three points behind Successful ML Application

Zhihua ZHOU

- Deep algorithms, i.e., deep learning
- Strong supervision information (data with high quality labels)
- Stable learning environment

Limitations of DL

Y. LeCun

Three challenges for Deep Learning

- **Deep Supervised Learning works well for perception**
  - When labeled data is abundant.
- **Deep Reinforcement Learning works well for action generation**
  - When trials are cheap, e.g. in simulation.
- **Three problems the community is working on:**
- **1. Learning with fewer labeled samples and/or fewer trials**
  - Self-supervised learning / unsup learning / learning to fill in the blanks
    - learning to represent the world before learning tasks
- **2. Learning to reason,** beyond "system 1" feed-forward computation.
  - Making reasoning compatible with gradient-based learning.
- **3. Learning to plan complex action sequences**
  - Learning hierarchical representations of action plans

Yann LeCun in AAAI 2020

Key Takeaways

- Neural Network is: 1 linear transformation 2 non-linear activation
- Gradient Descent plus Back-Propagation is used to find the model parameters of neural networks
- Deep learning: neural network with a deep structure (many layers)
- Deep learning is the method which tries to learn features by the model itself without human efforts