

20250528\_01

May 28, 2025

```
[9]: import numpy as np
import matplotlib.pyplot as plt

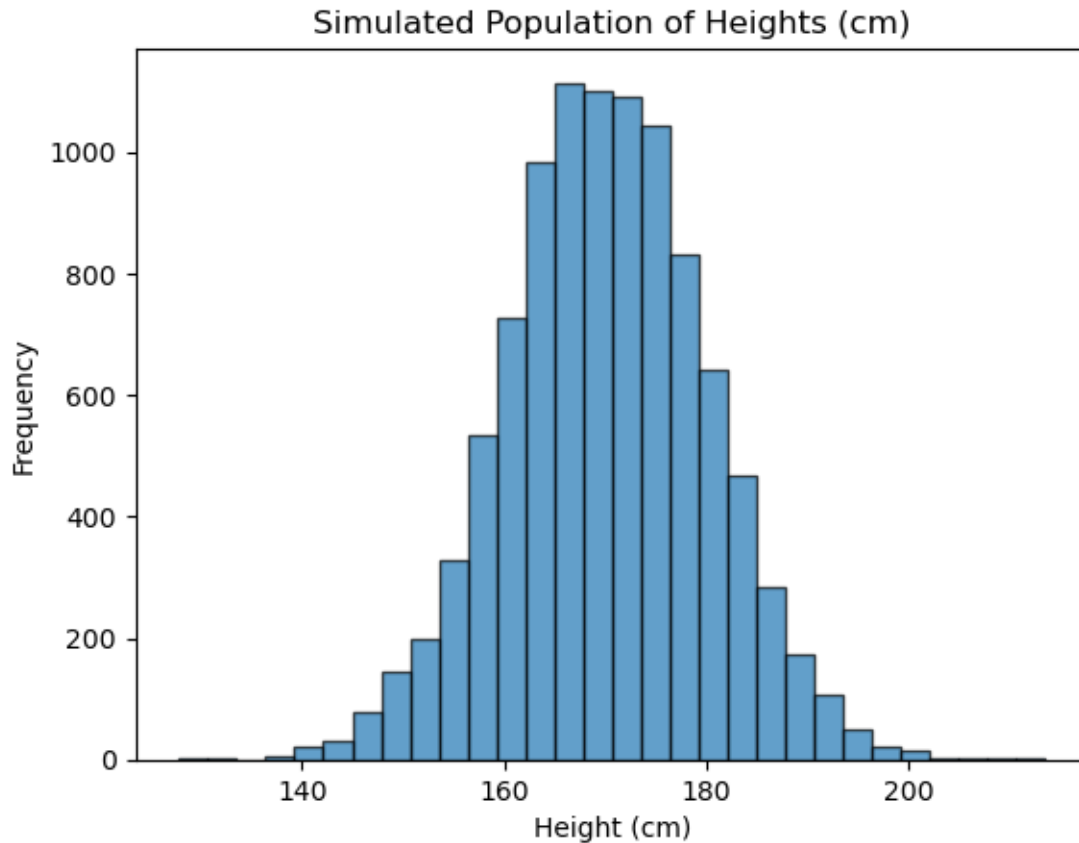
[10]: np.random.seed(420)

[13]: #To simulate population
population = np.random.normal(loc = 170, scale = 10, size = 10000)

[14]: plt.hist(population, bins = 30, edgecolor = 'black', alpha = 0.7)

plt.title("Simulated Population of Heights (cm)")
plt.xlabel("Height (cm)")
plt.ylabel("Frequency")

plt.show()
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[24]: #Store means from bootstrap
sample_means = []

#Bootstrap, 100 datas at a time, and can repeatedly chosen, because it's
↳bootstrap.
for _ in range(1000):
    sample = np.random.choice(population, size = 100, replace = True)
    sample_means.append(np.mean(sample))
```

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[16]: # Get 95% CI from percentiles
lower = np.percentile(sample_means, 2.5)
upper = np.percentile(sample_means, 97.5)

print(f"95% CI (bootstrap): [{lower:.2f}, {upper:.2f}]")
```

95% CI (bootstrap): [167.95, 171.89]

```
[30]: # Plot histogram of bootstrap means
plt.hist(sample_means, bins = 30, edgecolor = 'black', alpha = 0.7, label =
↳'Bootstrap Means')
```

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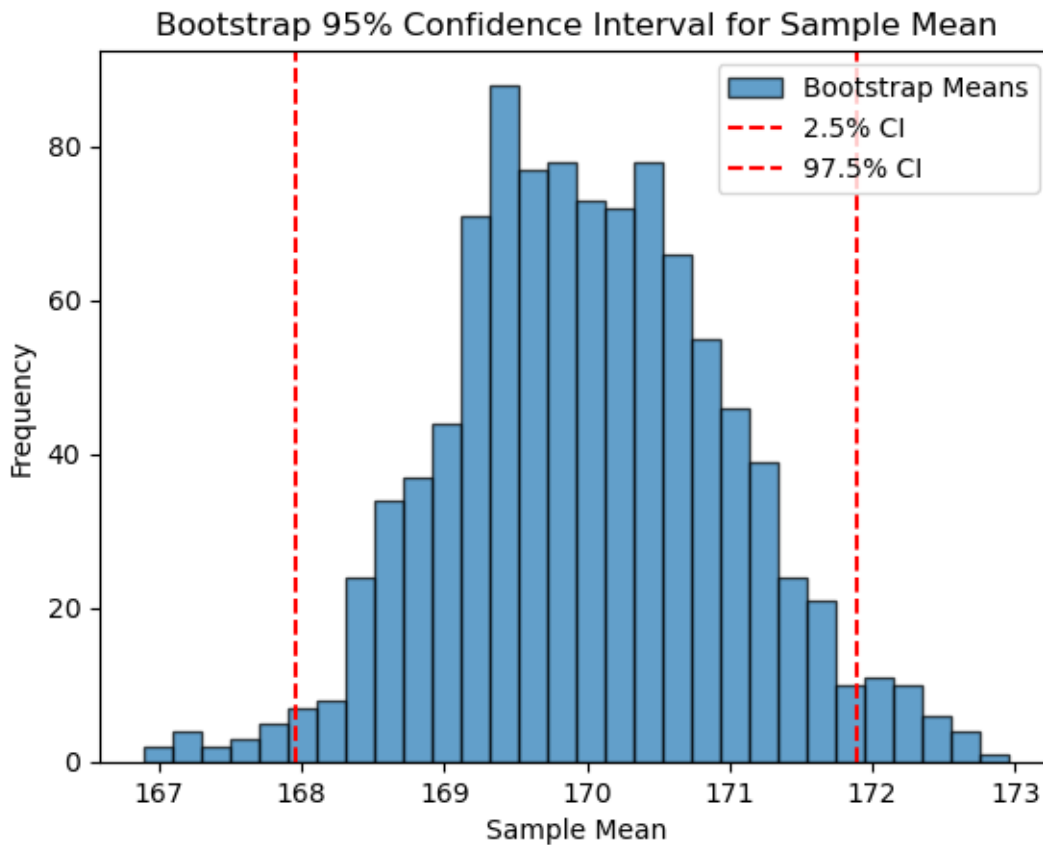
# Add CI boundaries
plt.axvline(lower, color = 'red', linestyle = '--', label = '2.5% CI')
plt.axvline(upper, color = 'red', linestyle = '--', label = '97.5% CI')

# Decorate plot
plt.title("Bootstrap 95% Confidence Interval for Sample Mean")

plt.xlabel("Sample Mean")
plt.ylabel("Frequency")

plt.legend()
plt.show()

```



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[26]: # Taking a single sample
sample = np.random.choice(population, size = 100, replace = False)

# Sample stats
sample_mean = np.mean(sample)

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sample_std = np.std(sample, ddof=1) # ddof = Delta Degree of Freedom, sample
    ↳ SD means that use ddof = 1, it's a theorem.
n = len(sample)
z = 1.96 # 95% confidence, derive from standard normal distribution where  $P(-1.96 < Z < 1.96) = 0.95$ . You don't really need to calculate this, just look up
    ↳ the chart.

# Confidence interval formula
ci_lower = sample_mean - z * (sample_std / np.sqrt(n))
ci_upper = sample_mean + z * (sample_std / np.sqrt(n))

print(f"95% CI (formula): [{ci_lower:.2f}, {ci_upper:.2f}]")

```

95% CI (formula): [167.81, 172.08]