

APT

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Arbitrage Pricing Theory, & Modelling

The history of asset pricing and associated models have witnessed numerous landmark developments over the past century, each standing on the shoulders of the previous and striving to reach above and beyond.

Arbitrage Pricing Theory (APT) proposed by economist Stephen Ross in 1976 and published with real world data in possible use case in the seminal work published in 1980 (<http://doi.wiley.com/10.1111/j.1540-6261.1980.tb02197.x>). This model builds forward on Markowitz Portfolio Theory (MPT), its application in selecting assets using Capital Asset Pricing Model (CAPM) and their limitations. While CAPM alongside with MPT considers previous individual asset returns, they don't allow to mathematically (& thus more objectively) to incorporate various macroeconomic and other factors in this model. Over long periods of time, even inflation eats into absolute returns observed over time. APT provides a mathematical framework to handle such issues, one of the first of its kind.

APT model uses the same mathematical strategy of linear regression as with CAPM except instead of being limited to just market risk measured in comparison to a market index, APT allows of any number of parameters. They can be market risk as in CAPM, additional parameters like *Small Minus Big (SMB) (market capitalization)* and *High Minus Low (HML) (book to market ratio)* like in **Fama-French model** and they can be disparately other factors like inflation or political risk in the market place of the country or build up inventory items on the accounting sheets of a company. The model allows such flexibility for users, often improved by leveraging insights from experienced fund managers.

APT model can thus be generalized and depicted by the following mathematical equation:

$$r_j = \alpha_j + \lambda_{j1}f_1 + \lambda_{j2}f_2 + \dots + \lambda_{jn}f_n + \epsilon_j$$

where the different linearly added terms can be different factors like political risk or inflation or SMB or HML or others. As linear regression model is used for prediction, the underlying assumptions of linear regression are also implied for feature selection in APT model.

As part of this assignment, we model **NIFTY monthly returns** as a function of **monthly 10 yr G-Ssec bond yields** and **monthly inflation**.

Data collection and preprocessing

Loading necessary libraries first as follows:

```
rm(list=ls())
knitr::opts_chunk$set(echo = TRUE)

setwd("~/QRS/Finance Stuff/APT")

libraries_required = c('lubridate', 'xts')

for(i in seq(libraries_required))
{
  if(!(libraries_required[i] %in% rownames(installed.packages())))
  {
    try(expr = install.packages('libraries_required[i]'), silent = T)
  }
  try(expr = library(libraries_required[i], character.only = T), silent = T)
}
```

```
##
## Attaching package: 'lubridate'
```

```
## The following object is masked from 'package:base':
##
##   date
```

```
## Loading required package: zoo
```

```
##
## Attaching package: 'zoo'
```

```
## The following objects are masked from 'package:base':
##
##   as.Date, as.Date.numeric
```

```
options(warn=-1)
```

Next, we obtain India's 10yr G-Sec bond yield from investing.com (<https://in.investing.com/rates-bonds/india-10-year-bond-yield-historical-data>). We save in file 'India 10-Year Bond Yield Historical Data Monthly.csv', load it and have a look.

```
India_10_yr_bond <- read.csv(file = "India 10-Year Bond Yield Historical Data Monthly.csv",
                             header = T, stringsAsFactors = F)

head(India_10_yr_bond,10)
```

```
##      Date Price  Open  High   Low Change..
## 1  01/08/19 6.390 6.369 6.432 6.324    0.33%
## 2  01/07/19 6.369 6.906 6.930 6.266   -7.41%
## 3  01/06/19 6.879 6.949 7.097 6.734   -2.18%
## 4  01/05/19 7.032 7.411 7.426 7.030   -5.15%
## 5  01/04/19 7.414 7.356 7.497 7.229    0.93%
## 6  01/03/19 7.346 7.588 7.590 7.301   -3.23%
## 7  01/02/19 7.591 7.470 7.699 7.425    1.44%
## 8  01/01/19 7.483 7.401 7.650 7.350    1.53%
## 9  01/12/18 7.370 7.646 7.703 7.218   -3.12%
## 10 01/11/18 7.607 7.831 7.840 7.576   -3.13%
```

Next, we utilise the date column to generate the time series. We also change the date to only year and month as our model is for monthly data (same frequency as inflation data, which we load later).

```
India_10_yr_bond$Date <- as.Date(India_10_yr_bond$Date, format="%d/%m/%y")

head(India_10_yr_bond)
```

```
##      Date Price  Open  High   Low Change..
## 1 2019-08-01 6.390 6.369 6.432 6.324    0.33%
## 2 2019-07-01 6.369 6.906 6.930 6.266   -7.41%
## 3 2019-06-01 6.879 6.949 7.097 6.734   -2.18%
## 4 2019-05-01 7.032 7.411 7.426 7.030   -5.15%
## 5 2019-04-01 7.414 7.356 7.497 7.229    0.93%
## 6 2019-03-01 7.346 7.588 7.590 7.301   -3.23%
```

```
India_10_yr_bond$Date <- format(India_10_yr_bond$Date, format="%y-%m")

head(India_10_yr_bond)
```

```
##      Date Price  Open  High   Low Change..
## 1 19-08 6.390 6.369 6.432 6.324    0.33%
## 2 19-07 6.369 6.906 6.930 6.266   -7.41%
## 3 19-06 6.879 6.949 7.097 6.734   -2.18%
## 4 19-05 7.032 7.411 7.426 7.030   -5.15%
## 5 19-04 7.414 7.356 7.497 7.229    0.93%
## 6 19-03 7.346 7.588 7.590 7.301   -3.23%
```

Next, we load our standard NIFTY time series data.

```
NIFTY_monthly <- read.csv(file = "NIFTY_monthly.csv", header = T, stringsAsFactors = F)

head(NIFTY_monthly)
```

```
##           Date    Open    High    Low   Close Shares.Traded
## 1 16 Jul 09 4223.50 4305.00 4205.50 4231.40    292288337
## 2 17 Jul 09 4231.45 4390.40 4230.15 4374.95    250233020
## 3 20 Jul 09 4377.90 4510.30 4377.90 4502.25    280309302
## 4 21 Jul 09 4501.50 4524.00 4436.60 4469.10    311984330
## 5 22 Jul 09 4469.30 4557.95 4380.45 4398.90    337796915
## 6 23 Jul 09 4409.70 4532.40 4405.95 4523.75    273052133
##   Turnover..Rs..Cr.
## 1           10209.96
## 2           9545.1
## 3           10151.33
## 4           10289.73
## 5           11688.74
## 6           10580
```

```
NIFTY_monthly$Date <- as.Date(NIFTY_monthly$Date, format="%d %b %y")

head(NIFTY_monthly)
```

```
##           Date    Open    High    Low   Close Shares.Traded
## 1 2009-07-16 4223.50 4305.00 4205.50 4231.40    292288337
## 2 2009-07-17 4231.45 4390.40 4230.15 4374.95    250233020
## 3 2009-07-20 4377.90 4510.30 4377.90 4502.25    280309302
## 4 2009-07-21 4501.50 4524.00 4436.60 4469.10    311984330
## 5 2009-07-22 4469.30 4557.95 4380.45 4398.90    337796915
## 6 2009-07-23 4409.70 4532.40 4405.95 4523.75    273052133
##   Turnover..Rs..Cr.
## 1           10209.96
## 2           9545.1
## 3           10151.33
## 4           10289.73
## 5           11688.74
## 6           10580
```

```
NIFTY_monthly$Date <- format(NIFTY_monthly$Date, format="%y-%m")

head(NIFTY_monthly)
```

```
##   Date    Open    High    Low   Close Shares.Traded Turnover..Rs..Cr.
## 1 09-07 4223.50 4305.00 4205.50 4231.40    292288337    10209.96
## 2 09-07 4231.45 4390.40 4230.15 4374.95    250233020     9545.1
## 3 09-07 4377.90 4510.30 4377.90 4502.25    280309302    10151.33
## 4 09-07 4501.50 4524.00 4436.60 4469.10    311984330    10289.73
## 5 09-07 4469.30 4557.95 4380.45 4398.90    337796915    11688.74
## 6 09-07 4409.70 4532.40 4405.95 4523.75    273052133    10580
```

```
NIFTY_monthly <- NIFTY_monthly[,1:5]

head(NIFTY_monthly)
```

```
##      Date      Open      High      Low      Close
## 1 09-07 4223.50 4305.00 4205.50 4231.40
## 2 09-07 4231.45 4390.40 4230.15 4374.95
## 3 09-07 4377.90 4510.30 4377.90 4502.25
## 4 09-07 4501.50 4524.00 4436.60 4469.10
## 5 09-07 4469.30 4557.95 4380.45 4398.90
## 6 09-07 4409.70 4532.40 4405.95 4523.75
```

```
temp_name <- colnames(NIFTY_monthly)

colnames(NIFTY_monthly) <- temp_name

head(NIFTY_monthly)
```

```
##      Date      Open      High      Low      Close
## 1 09-07 4223.50 4305.00 4205.50 4231.40
## 2 09-07 4231.45 4390.40 4230.15 4374.95
## 3 09-07 4377.90 4510.30 4377.90 4502.25
## 4 09-07 4501.50 4524.00 4436.60 4469.10
## 5 09-07 4469.30 4557.95 4380.45 4398.90
## 6 09-07 4409.70 4532.40 4405.95 4523.75
```

Next, we combine by 'Date' column, NIFTY returns and the bond yield data.

```
Combined <- merge(x = NIFTY_monthly[,c(1,5)], y = India_10_yr_bond[,1:2], by = "Date", all.y
= TRUE)

colnames(Combined) <- c("Date", "NIFTY_Close", "India_10_yr_bond_RF")

# head(Combined,40)
tail(Combined,40)
```

##	Date	NIFTY_Close	India_10_yr_bond_RF
## 2403	18-10	10198.40	7.853
## 2404	18-10	10386.60	7.853
## 2405	18-11	10380.45	7.607
## 2406	18-11	10553.00	7.607
## 2407	18-11	10524.00	7.607
## 2408	18-11	10530.00	7.607
## 2409	18-11	10585.20	7.607
## 2410	18-11	10482.20	7.607
## 2411	18-11	10582.50	7.607
## 2412	18-12	NA	7.370
## 2413	19-01	NA	7.483
## 2414	19-02	NA	7.591
## 2415	19-03	NA	7.346
## 2416	19-04	NA	7.414
## 2417	19-05	NA	7.032
## 2418	19-06	NA	6.879
## 2419	19-07	NA	6.369
## 2420	19-08	NA	6.390
## 2421	98-03	NA	12.086
## 2422	98-04	NA	11.781
## 2423	98-05	NA	12.049
## 2424	98-06	NA	12.117
## 2425	98-07	NA	12.200
## 2426	98-08	NA	12.241
## 2427	98-09	NA	12.287
## 2428	98-10	NA	12.302
## 2429	98-11	NA	12.221
## 2430	98-12	NA	12.213
## 2431	99-01	NA	12.219
## 2432	99-02	NA	12.223
## 2433	99-03	NA	11.994
## 2434	99-04	NA	11.886
## 2435	99-05	NA	11.700
## 2436	99-06	NA	11.851
## 2437	99-07	NA	11.673
## 2438	99-08	NA	11.588
## 2439	99-09	NA	11.634
## 2440	99-10	NA	11.521
## 2441	99-11	NA	11.384
## 2442	99-12	NA	11.197

```
Combined <- na.omit(Combined)
```

```
head(Combined)
```

##	Date	NIFTY_Close	India_10_yr_bond_RF
## 115	09-07	4231.40	6.998
## 116	09-07	4374.95	6.998
## 117	09-07	4502.25	6.998
## 118	09-07	4469.10	6.998
## 119	09-07	4398.90	6.998
## 120	09-07	4523.75	6.998

```
Combined$NIFTY_ret <- c(NA,100*diff(Combined$NIFTY_Close)/Combined$NIFTY_Close[-1])

head(Combined)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF  NIFTY_ret
## 115 09-07    4231.40          6.998          NA
## 116 09-07    4374.95          6.998    3.2811804
## 117 09-07    4502.25          6.998    2.8274752
## 118 09-07    4469.10          6.998   -0.7417601
## 119 09-07    4398.90          6.998   -1.5958535
## 120 09-07    4523.75          6.998    2.7598784
```

```
Combined <- na.omit(Combined)

head(Combined)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF  NIFTY_ret
## 116 09-07    4374.95          6.998    3.2811804
## 117 09-07    4502.25          6.998    2.8274752
## 118 09-07    4469.10          6.998   -0.7417601
## 119 09-07    4398.90          6.998   -1.5958535
## 120 09-07    4523.75          6.998    2.7598784
## 121 09-07    4568.55          6.998    0.9806175
```

Converting annual bond yield to monthly

```
Combined$India_10_yr_bond_RF_monthly <- (((((Combined$India_10_yr_bond_RF/100)+1)^10)^(1/(10*
12)))) - 1)*100

head(Combined,10)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF    NIFTY_ret
## 116 09-07      4374.95              6.998  3.28118036
## 117 09-07      4502.25              6.998  2.82747515
## 118 09-07      4469.10              6.998 -0.74176009
## 119 09-07      4398.90              6.998 -1.59585351
## 120 09-07      4523.75              6.998  2.75987842
## 121 09-07      4568.55              6.998  0.98061748
## 122 09-07      4572.30              6.998  0.08201562
## 123 09-07      4564.10              6.998 -0.17966302
## 124 09-07      4513.50              6.998 -1.12108120
## 125 09-07      4571.45              6.998  1.26765031
##      India_10_yr_bond_RF_monthly
## 116                      0.5652579
## 117                      0.5652579
## 118                      0.5652579
## 119                      0.5652579
## 120                      0.5652579
## 121                      0.5652579
## 122                      0.5652579
## 123                      0.5652579
## 124                      0.5652579
## 125                      0.5652579
```

Calculating market risk premium (MRP)

```
for (i in seq(dim(Combined)[1]))
{
  Combined[i,"MRP"] <- mean(Combined[1:i,"NIFTY_ret"]) - Combined[i,"India_10_yr_bond_RF_monthly"]
}

head(Combined,20)
```


##	Date	NIFTY_Close	India_10_yr_bond_RF	NIFTY_ret
## 116	09-07	4374.95	6.998	3.28118036
## 117	09-07	4502.25	6.998	2.82747515
## 118	09-07	4469.10	6.998	-0.74176009
## 119	09-07	4398.90	6.998	-1.59585351
## 120	09-07	4523.75	6.998	2.75987842
## 121	09-07	4568.55	6.998	0.98061748
## 122	09-07	4572.30	6.998	0.08201562
## 123	09-07	4564.10	6.998	-0.17966302
## 124	09-07	4513.50	6.998	-1.12108120
## 125	09-07	4571.45	6.998	1.26765031
## 126	09-07	4636.45	6.998	1.40193467
## 127	09-08	4711.40	7.434	1.59082226
## 128	09-08	4680.50	7.434	-0.66018588
## 129	09-08	4694.15	7.434	0.29078747
## 130	09-08	4585.50	7.434	-2.36942536
## 131	09-08	4481.40	7.434	-2.32293480
## 132	09-08	4437.65	7.434	-0.98588217
## 133	09-08	4471.35	7.434	0.75368737
## 134	09-08	4457.50	7.434	-0.31071228
## 135	09-08	4605.00	7.434	3.20304017
##	India_10_yr_bond_RF_monthly		MRP	
## 116		0.5652579		2.71592246
## 117		0.5652579		2.48906986
## 118		0.5652579		1.22370725
## 119		0.5652579		0.37750258
## 120		0.5652579		0.74092617
## 121		0.5652579		0.68666508
## 122		0.5652579		0.51953545
## 123		0.5652579		0.36147841
## 124		0.5652579		0.13394313
## 125		0.5652579		0.19078806
## 126		0.5652579		0.24950521
## 127		0.5993432		0.28009146
## 128		0.5993432		0.16165910
## 129		0.5993432		0.12807233
## 130		0.5993432		-0.07838374
## 131		0.5993432		-0.25612713
## 132		0.5993432		-0.33430938
## 133		0.5993432		-0.30716196
## 134		0.5993432		-0.33889321
## 135		0.5993432		-0.19176370

```
tail(Combined,20)
```

##	Date	NIFTY_Close	India_10_yr_bond_RF	NIFTY_ret
## 2392	18-10	10472.50	7.853	2.27118644
## 2393	18-10	10512.50	7.853	0.38049941
## 2394	18-10	10584.75	7.853	0.68258580
## 2395	18-10	10453.05	7.853	-1.25991935
## 2396	18-10	10303.55	7.853	-1.45095622
## 2397	18-10	10245.25	7.853	-0.56904419
## 2398	18-10	10146.80	7.853	-0.97025663
## 2399	18-10	10224.75	7.853	0.76236583
## 2400	18-10	10124.90	7.853	-0.98618258
## 2401	18-10	10030.00	7.853	-0.94616152
## 2402	18-10	10250.85	7.853	2.15445548
## 2403	18-10	10198.40	7.853	-0.51429636
## 2404	18-10	10386.60	7.853	1.81195001
## 2405	18-11	10380.45	7.607	-0.05924599
## 2406	18-11	10553.00	7.607	1.63508007
## 2407	18-11	10524.00	7.607	-0.27556062
## 2408	18-11	10530.00	7.607	0.05698006
## 2409	18-11	10585.20	7.607	0.52148283
## 2410	18-11	10482.20	7.607	-0.98261815
## 2411	18-11	10582.50	7.607	0.94779116
##	India_10_yr_bond_RF_monthly		MRP	
## 2392	0.6319803		-0.5972491	
## 2393	0.6319803		-0.5970973	
## 2394	0.6319803		-0.5968131	
## 2395	0.6319803		-0.5973811	
## 2396	0.6319803		-0.5980324	
## 2397	0.6319803		-0.5982966	
## 2398	0.6319803		-0.5987364	
## 2399	0.6319803		-0.5984171	
## 2400	0.6319803		-0.5988634	
## 2401	0.6319803		-0.5992918	
## 2402	0.6319803		-0.5983640	
## 2403	0.6319803		-0.5986035	
## 2404	0.6319803		-0.5978265	
## 2405	0.6128328		-0.5787198	
## 2406	0.6128328		-0.5780210	
## 2407	0.6128328		-0.5781564	
## 2408	0.6128328		-0.5781467	
## 2409	0.6128328		-0.5779345	
## 2410	0.6128328		-0.5783778	
## 2411	0.6128328		-0.5779800	

With Market Risk Premium and NIFTY index returns in place, we next proceed to add monthly inflation data to our time series for linear regression of the APT model. We obtain the monthly inflation data on India from the website: <https://www.inflation.eu/inflation-rates/india/historic-inflation/cpi-inflation-india-2019.aspx> (<https://www.inflation.eu/inflation-rates/india/historic-inflation/cpi-inflation-india-2019.aspx>)

We copy the monthly figures onto a csv and process it further to prepare for integration with the inflation time series data with NIFTY returns and 10-year G-Sec bond yields. **We also extract the current month from the first column and use it to build the time series.**

```
India_monthly_Inflation <- read.csv(file = "inflation_India_monthly_basis.csv", header = T,
                                   stringsAsFactors = F)
```

```
head(India_monthly_Inflation)
```

```
##           Monthly_basis inflation
## 1  january 2009 - december 2008    0.68%
## 2  february 2009 - january 2009    0.00%
## 3   march 2009 - february 2009    0.00%
## 4   april 2009 - march 2009      1.35%
## 5    may 2009 - april 2009      0.67%
## 6   june 2009 - may 2009       1.32%
```

```
for(j in seq(dim(India_monthly_Inflation)[1]))
{
  temp_vector <- rev(strsplit(India_monthly_Inflation[j,1], split = ' ')[[1]])[1:2]

  temp_vector_2 <- strsplit(temp_vector[2],split='')[[1]]

  temp_vector_2[1] <- toupper(temp_vector_2[1])

  temp_vector[2] <- paste0(temp_vector_2, collapse = '')

  temp_vector[3] <- "01"

  India_monthly_Inflation[j,"Date"] <- paste0(temp_vector, collapse = ' ')
}

head(India_monthly_Inflation)
```

```
##           Monthly_basis inflation           Date
## 1  january 2009 - december 2008    0.68% 2008 December 01
## 2  february 2009 - january 2009    0.00% 2009 January 01
## 3   march 2009 - february 2009    0.00% 2009 February 01
## 4   april 2009 - march 2009      1.35% 2009 March 01
## 5    may 2009 - april 2009      0.67% 2009 April 01
## 6   june 2009 - may 2009       1.32% 2009 May 01
```

```
tail(India_monthly_Inflation)
```

```
##           Monthly_basis inflation           Date
## 121 january 2019 - december 2018    1.99% 2018 December 01
## 122 february 2019 - january 2019    0.00% 2019 January 01
## 123  march 2019 - february 2019    0.65% 2019 February 01
## 124  april 2019 - march 2019      0.97% 2019 March 01
## 125   may 2019 - april 2019      0.64% 2019 April 01
## 126  june 2019 - may 2019       0.64% 2019 May 01
```

```
India_monthly_Inflation <- India_monthly_Inflation[2:3]

head(India_monthly_Inflation)
```

```
##      inflation      Date
## 1      0.68% 2008 December 01
## 2      0.00% 2009 January 01
## 3      0.00% 2009 February 01
## 4      1.35% 2009 March 01
## 5      0.67% 2009 April 01
## 6      1.32% 2009 May 01
```

```
tail(India_monthly_Inflation)
```

```
##      inflation      Date
## 121     1.99% 2018 December 01
## 122     0.00% 2019 January 01
## 123     0.65% 2019 February 01
## 124     0.97% 2019 March 01
## 125     0.64% 2019 April 01
## 126     0.64% 2019 May 01
```

```
India_monthly_Inflation$inflation <- as.numeric(gsub("%", "", India_monthly_Inflation$inflatio
n))
```

```
head(India_monthly_Inflation)
```

```
##      inflation      Date
## 1      0.68 2008 December 01
## 2      0.00 2009 January 01
## 3      0.00 2009 February 01
## 4      1.35 2009 March 01
## 5      0.67 2009 April 01
## 6      1.32 2009 May 01
```

```
tail(India_monthly_Inflation)
```

```
##      inflation      Date
## 121     1.99 2018 December 01
## 122     0.00 2019 January 01
## 123     0.65 2019 February 01
## 124     0.97 2019 March 01
## 125     0.64 2019 April 01
## 126     0.64 2019 May 01
```

```
colnames(India_monthly_Inflation) <- c("Inflation_%", "Date")
```

```
head(India_monthly_Inflation)
```

```
##      Inflation_%      Date
## 1          0.68 2008 December 01
## 2          0.00 2009 January 01
## 3          0.00 2009 February 01
## 4          1.35 2009 March 01
## 5          0.67 2009 April 01
## 6          1.32 2009 May 01
```

```
tail(India_monthly_Inflation)
```

```
##      Inflation_%      Date
## 121          1.99 2018 December 01
## 122          0.00 2019 January 01
## 123          0.65 2019 February 01
## 124          0.97 2019 March 01
## 125          0.64 2019 April 01
## 126          0.64 2019 May 01
```

```
India_monthly_Inflation$Date <- as.Date(India_monthly_Inflation$Date, format="%Y %B %d")
head(India_monthly_Inflation)
```

```
##      Inflation_%      Date
## 1          0.68 2008-12-01
## 2          0.00 2009-01-01
## 3          0.00 2009-02-01
## 4          1.35 2009-03-01
## 5          0.67 2009-04-01
## 6          1.32 2009-05-01
```

```
tail(India_monthly_Inflation)
```

```
##      Inflation_%      Date
## 121          1.99 2018-12-01
## 122          0.00 2019-01-01
## 123          0.65 2019-02-01
## 124          0.97 2019-03-01
## 125          0.64 2019-04-01
## 126          0.64 2019-05-01
```

```
India_monthly_Inflation$Date <- format(India_monthly_Inflation$Date, format="%y-%m")
head(India_monthly_Inflation)
```

```
##      Inflation_%      Date
## 1          0.68 08-12
## 2          0.00 09-01
## 3          0.00 09-02
## 4          1.35 09-03
## 5          0.67 09-04
## 6          1.32 09-05
```

```
tail(India_monthly_Inflation)
```

```
##      Inflation_% Date
## 121         1.99 18-12
## 122         0.00 19-01
## 123         0.65 19-02
## 124         0.97 19-03
## 125         0.64 19-04
## 126         0.64 19-05
```

```
head(Combined)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF NIFTY_ret
## 116 09-07      4374.95          6.998 3.2811804
## 117 09-07      4502.25          6.998 2.8274752
## 118 09-07      4469.10          6.998 -0.7417601
## 119 09-07      4398.90          6.998 -1.5958535
## 120 09-07      4523.75          6.998 2.7598784
## 121 09-07      4568.55          6.998 0.9806175
##      India_10_yr_bond_RF_monthly      MRP
## 116          0.5652579 2.7159225
## 117          0.5652579 2.4890699
## 118          0.5652579 1.2237072
## 119          0.5652579 0.3775026
## 120          0.5652579 0.7409262
## 121          0.5652579 0.6866651
```

```
tail(Combined)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF NIFTY_ret
## 2406 18-11      10553.0          7.607 1.63508007
## 2407 18-11      10524.0          7.607 -0.27556062
## 2408 18-11      10530.0          7.607 0.05698006
## 2409 18-11      10585.2          7.607 0.52148283
## 2410 18-11      10482.2          7.607 -0.98261815
## 2411 18-11      10582.5          7.607 0.94779116
##      India_10_yr_bond_RF_monthly      MRP
## 2406          0.6128328 -0.5780210
## 2407          0.6128328 -0.5781564
## 2408          0.6128328 -0.5781467
## 2409          0.6128328 -0.5779345
## 2410          0.6128328 -0.5783778
## 2411          0.6128328 -0.5779800
```

Now, with this inflation time series dataframe, we combine using left join with the previous data frame consisting of the NIFTY returns and 10-year bond yields.

```
All_Factors <- merge(x = Combined, y = India_monthly_Inflation, by = "Date", all.y = TRUE)

head(All_Factors)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF NIFTY_ret
## 1 08-12          NA          NA          NA
## 2 09-01          NA          NA          NA
## 3 09-02          NA          NA          NA
## 4 09-03          NA          NA          NA
## 5 09-04          NA          NA          NA
## 6 09-05          NA          NA          NA
##      India_10_yr_bond_RF_monthly MRP Inflation_%
## 1          NA NA          0.68
## 2          NA NA          0.00
## 3          NA NA          0.00
## 4          NA NA          1.35
## 5          NA NA          0.67
## 6          NA NA          1.32
```

```
tail(All_Factors)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF NIFTY_ret
## 2304 18-12          NA          NA          NA
## 2305 19-01          NA          NA          NA
## 2306 19-02          NA          NA          NA
## 2307 19-03          NA          NA          NA
## 2308 19-04          NA          NA          NA
## 2309 19-05          NA          NA          NA
##      India_10_yr_bond_RF_monthly MRP Inflation_%
## 2304          NA NA          1.99
## 2305          NA NA          0.00
## 2306          NA NA          0.65
## 2307          NA NA          0.97
## 2308          NA NA          0.64
## 2309          NA NA          0.64
```

```
All_Factors <- na.omit(All_Factors)
```

```
head(All_Factors)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF NIFTY_ret
## 8 09-07      4374.95          6.998 3.2811804
## 9 09-07      4502.25          6.998 2.8274752
## 10 09-07      4469.10          6.998 -0.7417601
## 11 09-07      4398.90          6.998 -1.5958535
## 12 09-07      4523.75          6.998 2.7598784
## 13 09-07      4568.55          6.998 0.9806175
##      India_10_yr_bond_RF_monthly MRP Inflation_%
## 8          0.5652579 2.7159225          1.25
## 9          0.5652579 2.4890699          1.25
## 10         0.5652579 1.2237072          1.25
## 11         0.5652579 0.3775026          1.25
## 12         0.5652579 0.7409262          1.25
## 13         0.5652579 0.6866651          1.25
```

```
tail(All_Factors)
```

```
##      Date NIFTY_Close India_10_yr_bond_RF   NIFTY_ret
## 2298 18-11      10553.0              7.607  1.63508007
## 2299 18-11      10524.0              7.607 -0.27556062
## 2300 18-11      10530.0              7.607  0.05698006
## 2301 18-11      10585.2              7.607  0.52148283
## 2302 18-11      10482.2              7.607 -0.98261815
## 2303 18-11      10582.5              7.607  0.94779116
##      India_10_yr_bond_RF_monthly      MRP Inflation_%
## 2298                0.6128328 -0.5780210      -0.33
## 2299                0.6128328 -0.5781564      -0.33
## 2300                0.6128328 -0.5781467      -0.33
## 2301                0.6128328 -0.5779345      -0.33
## 2302                0.6128328 -0.5783778      -0.33
## 2303                0.6128328 -0.5779800      -0.33
```

```
dim(All_Factors)
```

```
## [1] 2296      7
```

```
APT_data <- All_Factors[,c("NIFTY_ret", "MRP", "Inflation_%")]
```

```
head(APT_data)
```

```
##      NIFTY_ret      MRP Inflation_%
## 8    3.2811804  2.7159225      1.25
## 9    2.8274752  2.4890699      1.25
## 10   -0.7417601  1.2237072      1.25
## 11   -1.5958535  0.3775026      1.25
## 12    2.7598784  0.7409262      1.25
## 13    0.9806175  0.6866651      1.25
```

```
tail(APT_data)
```

```
##      NIFTY_ret      MRP Inflation_%
## 2298  1.63508007 -0.5780210      -0.33
## 2299 -0.27556062 -0.5781564      -0.33
## 2300  0.05698006 -0.5781467      -0.33
## 2301  0.52148283 -0.5779345      -0.33
## 2302 -0.98261815 -0.5783778      -0.33
## 2303  0.94779116 -0.5779800      -0.33
```

```
dim(APT_data)
```

```
## [1] 2296      3
```

With the data ready, we finally proceed onto the regression for APT as follows with NIFTY returns being the:

```
summary(lm(APT_data$NIFTY_ret~APT_data$MRP+APT_data$`Inflation_%`))
```



```
##
## Call:
## lm(formula = APT_data$NIFTY_ret ~ APT_data$MRP + APT_data$`Inflation_%`)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -6.3190 -0.5559  0.0140  0.5730  3.6619
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)    0.34575    0.08902   3.884 0.000106 ***
## APT_data$MRP    0.59516    0.14786   4.025 5.88e-05 ***
## APT_data$`Inflation_%` 0.05085    0.02607   1.951 0.051230 .
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.003 on 2293 degrees of freedom
## Multiple R-squared:  0.00899,    Adjusted R-squared:  0.008126
## F-statistic: 10.4 on 2 and 2293 DF,  p-value: 3.187e-05
```

Conclusion of our Arbitrage Pricing Theory modelling

We see that with $\alpha = 0.1$, both **Inflation** and **Market Risk Premium** are **significant**.

With $\alpha = 0.05$ cutoff, **Inflation** is **insignificant** whereas **Market Risk Premium** is **significant**.

Lastly, we close by clearing the workspace

```
rm(list=ls())
```