

# Terrain-Adaptive Cruise Control; A Human-Like Approach

Narayani Vedam

Advisors:

Dr. Shankar P Bhattacharyya, Dr. Reza Langari

10/13/2015



TEXAS A&M  
UNIVERSITY.

# OUTLINE

- ❑ **Objectives**
- ❑ **Introduction**
  - ❑ Conventional Cruise Control System
  - ❑ Human Driving Behavior
  - ❑ Prevalent Approaches
- ❑ **Preliminaries**
  - ❑ Vehicle Model
  - ❑ Road Grade
- ❑ **Proposed Method**
  - ❑ Model
  - ❑ Objective Function
  - ❑ Control Algorithm
  - ❑ Simulation Results
- ❑ **Summary**

# OBJECTIVES

- Design a speed control system that can:
  - *Track a set-speed along flat roads*
  - *Mimic human driving behavior along varying terrains*
- Ensure optimality of regulatory actions w.r.t (either or all),
  - *Fuel consumption,*
  - *Brake usage &*
  - *Acceleration.*

# OBJECTIVES

- In a typical approach:
  - *Fixed-weight* objective function is used
  - *Pre-processing* algorithms are needed
  - *To ensure speed tracking*
  - *Fuel savings of 2.5% over 127km*
- In this approach:
  - *Varying-weight* objective function is used
  - *No need* for pre-processing algorithms
  - *0.48%(downhill) and 0.44%(uphill) fuel savings over 2.5km*

# OUTLINE

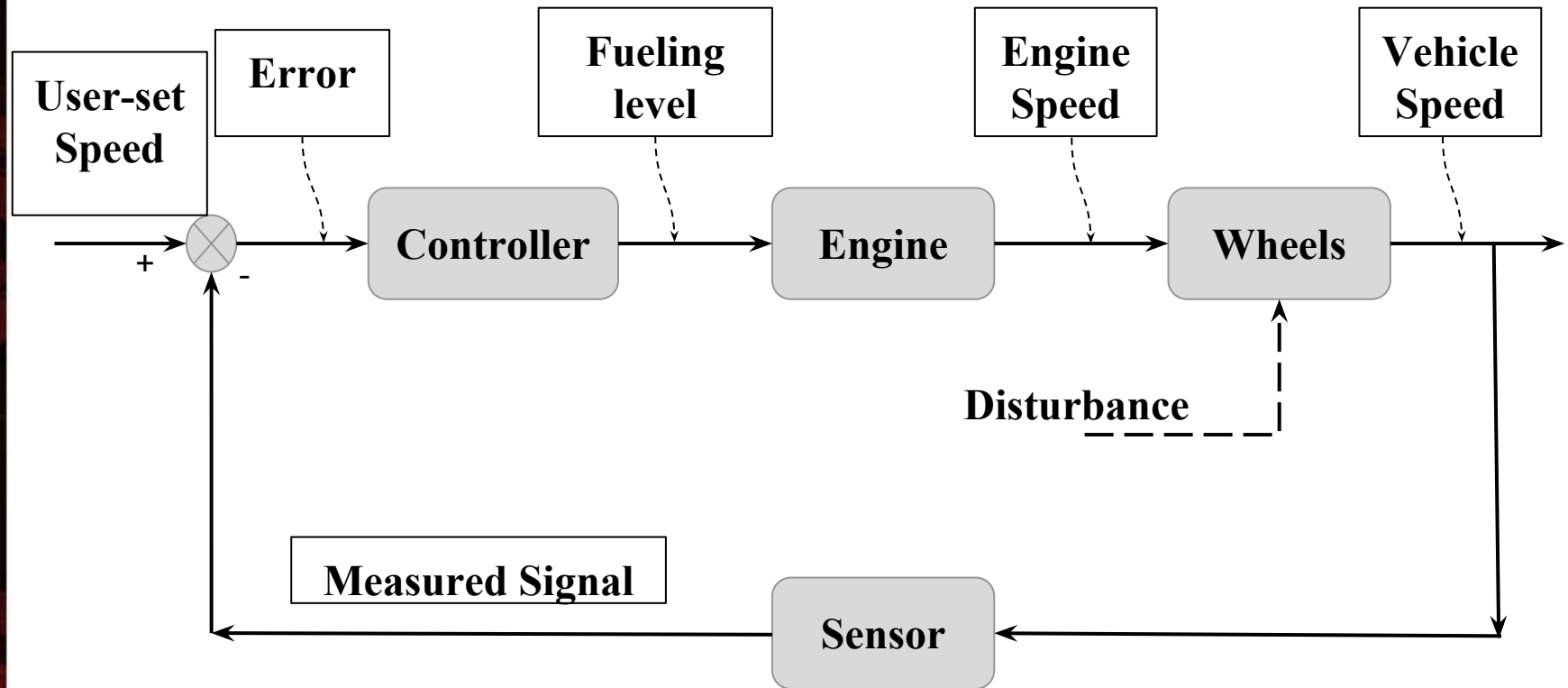
- ❑ Objectives
- ❑ Introduction
  - ❑ Conventional Cruise Control System
  - ❑ Human Driving Behavior
  - ❑ Prevalent Approaches
- ❑ Preliminaries
  - ❑ Vehicle Model
  - ❑ Road Grade
- ❑ Proposed Method
  - ❑ Model
  - ❑ Objective Function
  - ❑ Control Algorithm
  - ❑ Simulation Results
- ❑ Summary

# Conventional Speed Control

Aim	Maintain a user-set vehicle speed
Means	Controllers - PI, LQR, Fuzzy, ..., etc.
Actuators	Accelerator, Brakes
Sensors	Wheel Speed Sensor
Advantages	On flat roads: Robust tracking of set-speed Reduce driver fatigue Fuel efficient



# Conventional Speed Control



**Figure 1:** Block Diagram Of A Typical Conventional Speed Control System



# Conventional Speed Control

## Disadvantages

- *Oblivious to impending gradients*
  - Lot of energy is used up while going up a hill
  - Lot of energy is wasted while going down a hill
- *Unaware of curves along a route*
  - Set speed may not be safe along curvatures
  - Necessitates manual intervention
- *Always tries to maintain the highest possible gear*



# Human Driving Behavior

- *Preview Utilization*
- *Accelerate* before and during an uphill
- *Decelerate* before a downhill
- *Coast* during descent
- Right choice of *gear*

*Unfamiliar route, novice driver, bad driving practices?*

# Prevalent Approaches

## 1. Heuristic Algorithm<sup>1</sup>

- a. Road section is divided based on the terrain - *uphill, downhill and flat*
- b. Intuitive rules mapping inputs to the outputs are generated
- c. Computationally less intense
- d. Generation of rule base is tedious

[1] Mustafa Abdul Rasool, Master's Thesis in Automatic Control, KTH.

# Prevalent Approaches

## 2. Model Predictive Control Scheme

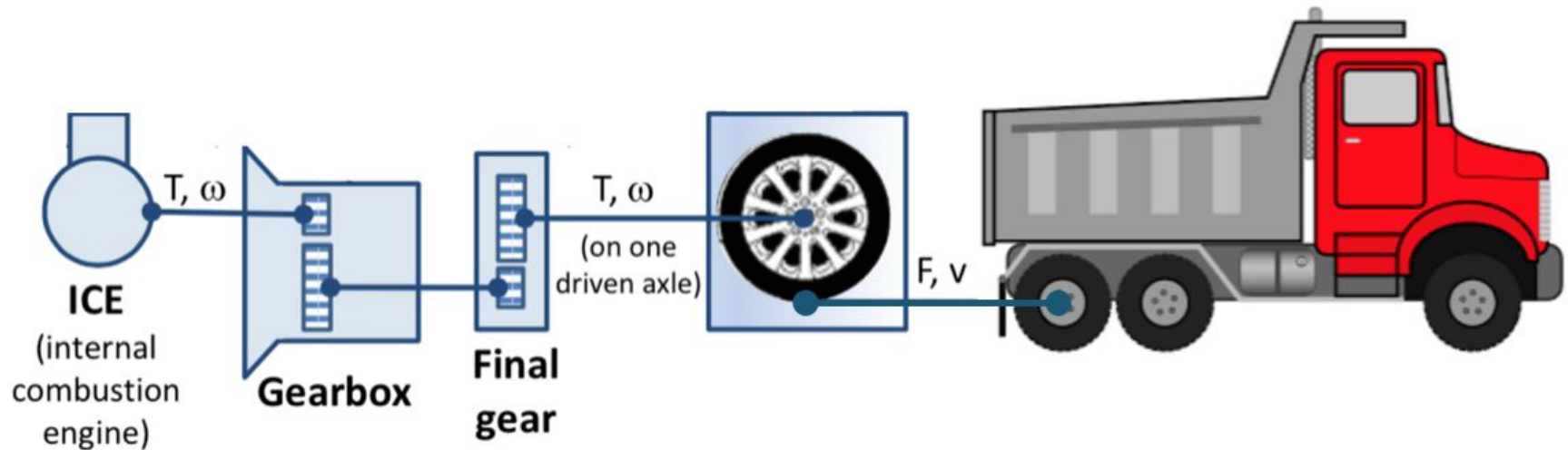
- a. Constrained optimization with gradient descent algorithm<sup>2</sup>
  - i. Local minimum
  - ii. Optimal velocity trajectory
  - iii. Linear controller with gain scheduling
- b. Discrete Dynamic Programming<sup>3</sup>
  - i. **Fixed** objective function
  - ii. State-space & Input-space are discretized
  - iii. **Pre-processing** algorithm is needed



# OUTLINE

- ❑ Objectives
- ❑ Introduction
  - ❑ Conventional Cruise Control System
  - ❑ Human Driving Behavior
  - ❑ Prevalent Approaches
- ❑ Preliminaries
  - ❑ Vehicle Model
  - ❑ Road Grade
- ❑ Proposed Method
  - ❑ Model
  - ❑ Objective Function
  - ❑ Control Algorithm
  - ❑ Simulation Results
- ❑ Summary

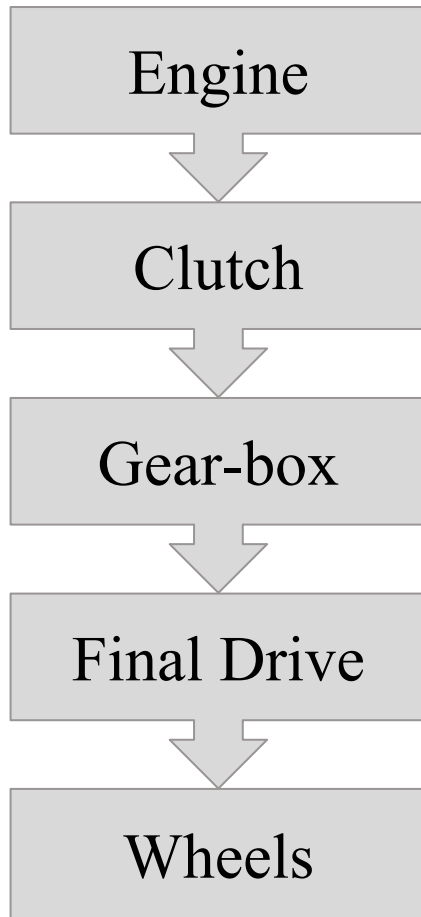
# Vehicle Model



**Figure 3: A Typical Automotive Power-train<sup>4</sup>**

[4] Jacobson, B. (2012), Chalmers University of Technology.

# Vehicle Model



$$T_e(P, N, G) = \begin{cases} a_e N + b_e P \delta_{max}(N) + c_e, & P > 0, G \neq 0 \\ a_d N + b_d, & P \leq 0, G \neq 0 \\ 0, & G = 0 \end{cases}$$

$$T_c = T_e$$

$$T_t = \eta_t i_t T_c$$

$$T_f = \eta_f i_f T_t$$

$$T_w = T_f$$

Parameter	Description
$T$	Torque Output ( $N\cdot m$ )
$P$	Accelerator Pedal
$G$	Gear Position
$N$	Engine Speed ( $RPM$ )
$a, b, c$	Empirical Constants
$i$	Conversion Ratio
$\eta$	Efficiency (%)

# Vehicle Model

Air Drag

$$F_d = \frac{1}{2} \rho c_d A v^2$$

Rolling  
Resistance

$$F_r = m g c_r \cos(\alpha)$$

Gradient  
Resistance

$$F_g = m g \sin(\alpha)$$


Parameter	Description
$c$	Friction Coefficient
$m$	Mass (kg)
$A$	Frontal Area (sq. m)
$v$	Velocity (m/s)
$g$	Acceleration due to gravity (m/s <sup>2</sup> )
$\rho$	Density of air (kg/m <sup>3</sup> )
$\alpha$	Road Grade (rads)

$$F_{total} = F_d + F_r + F_g$$



# Vehicle Model

Tractive Force  
at the wheels



$$T_w = F_w r_w$$

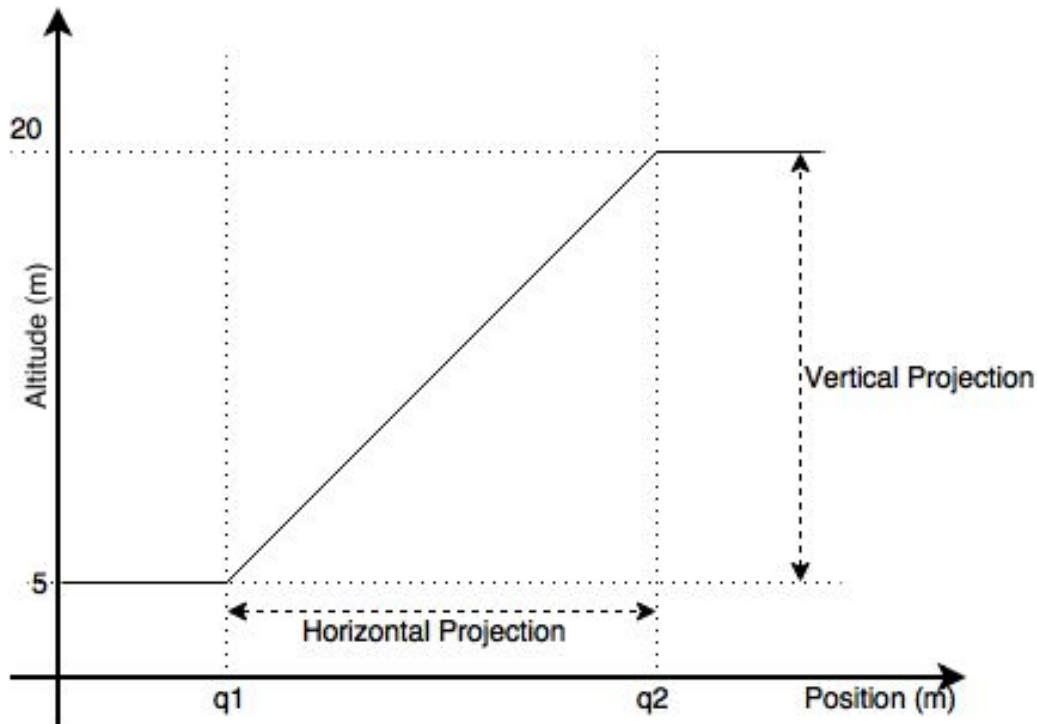
$$F_w = F_e - F_{total}$$

Parameter	Description
F	Tractive Force (kN)
J	Inertia ( $kg/m^2$ )
$r_w$	Wheel Radius (m)

$$\dot{v} = \frac{r_w}{J_w + m r_w^2 + \eta_t i_t^2 \eta_f i_f^2 J_e} (\eta_t i_t \eta_f i_f T_e(N, P, G) - B F_B - 0.5 \rho c_d r_w A v^2 - m g r_w \sqrt{1 + c_r^2} \sin(\alpha + \arctan(c_r)))$$

# Road Grade ( $\alpha$ )

$$\alpha(\text{rads}) = \frac{\text{Vertical Projection}}{\text{Horizontal Projection}}$$



**Figure 4:** Pictorial Representation Of Road Grade

# OUTLINE

- ❑ Objectives
- ❑ Introduction
  - ❑ Conventional Cruise Control System
  - ❑ Human Driving Behavior
  - ❑ Prevalent Approaches
- ❑ Preliminaries
  - ❑ Vehicle Model
  - ❑ Road Grade
- ❑ **Proposed Method**
  - ❑ Model
  - ❑ Objective Function
  - ❑ Control Algorithm
  - ❑ Simulation Results
- ❑ Summary

# Overview

1. Discretize the vehicle model
  - a. Define States, Inputs & Outputs
  - b. Define Constraints
2. Formulate an objective function
  - a. **Adaptively** vary the weights
3. Implement a MPC scheme with discrete dynamic programming
  - a. Apply the first instance of the control action
  - b. Measure the output
  - c. Recompute the control action



# Model

State: 
$$v_{k+1} = v_k + \frac{h}{v_k} f_1(v_k, u_k, \alpha_k), \quad k = 0, 1, 2, \dots, N - 1$$

Inputs: 
$$u_k = \begin{bmatrix} P_k \\ B_k \end{bmatrix}, \quad k = 0, 1, 2, \dots, N - 1$$

Outputs: 
$$y_k = \begin{bmatrix} v_k \\ m_{f,k} \end{bmatrix}, \quad k = 0, 1, 2, \dots, N - 1$$

Constraints: 
$$(v_{ref} - 5) \leq v_k \leq (v_{ref} + 5)$$

$$0 \leq P_k \leq 1$$

$$0 \leq B_k \leq 1$$



# Objective Function

Cost Criteria:  $B_k$ , Brake usage  
 $m_{f,k}$ , Fuel usage  
 $|v_k - v_{k+1}|$ , Acceleration  
 $|v_{ref} - v_k|$ , Deviation in velocity

## Objective Function:

$$\beta_k = L_1(\alpha_k)m_{f,k} + L_2(\alpha_k)|v_{ref} - v_k| + L_3(\alpha_k)|v_k - v_{k+1}| + L_4(\alpha_k)B_k$$

$L_1(\alpha_k)$ ,  $L_2(\alpha_k)$ ,  $L_3(\alpha_k)$  &  $L_4(\alpha_k)$  are *terrain dependent* penalties.



# Terrain Dependent Objectives

## ➤ Flat Stretch (F):

- Track Set-Speed

## ➤ Uphill (U):

- Accelerate Before Ascent
- Accelerate Upon Ascent
- Reduced Speed Drop

## ➤ Downhill (D):

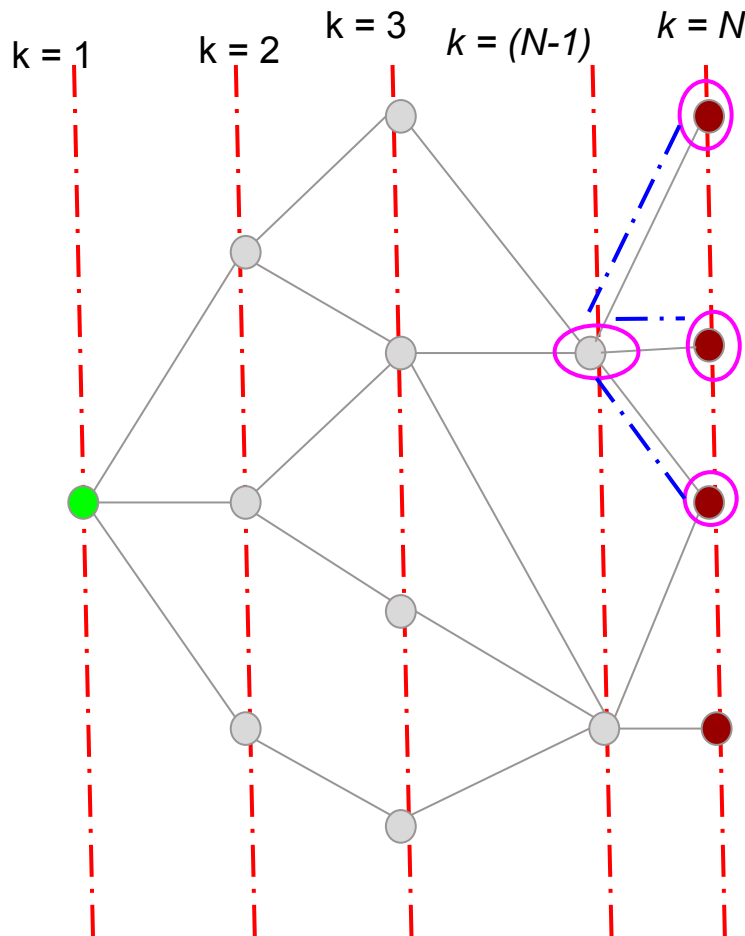
- Decelerate Before Descent
- Coast during descent
- Minimal Brake Usage
- Fuel Efficient



Gain	F	U	D
$L_1$	Low	Low	High
$L_2$	High	Low	Low
$L_3$	High	High	High
$L_4$	Low	Nil	High



# Discrete Dynamic Programming



1. At  $k = N$ ,  
 $J_N(v_N(i)) = \beta_N(v_N(i)) = 0$

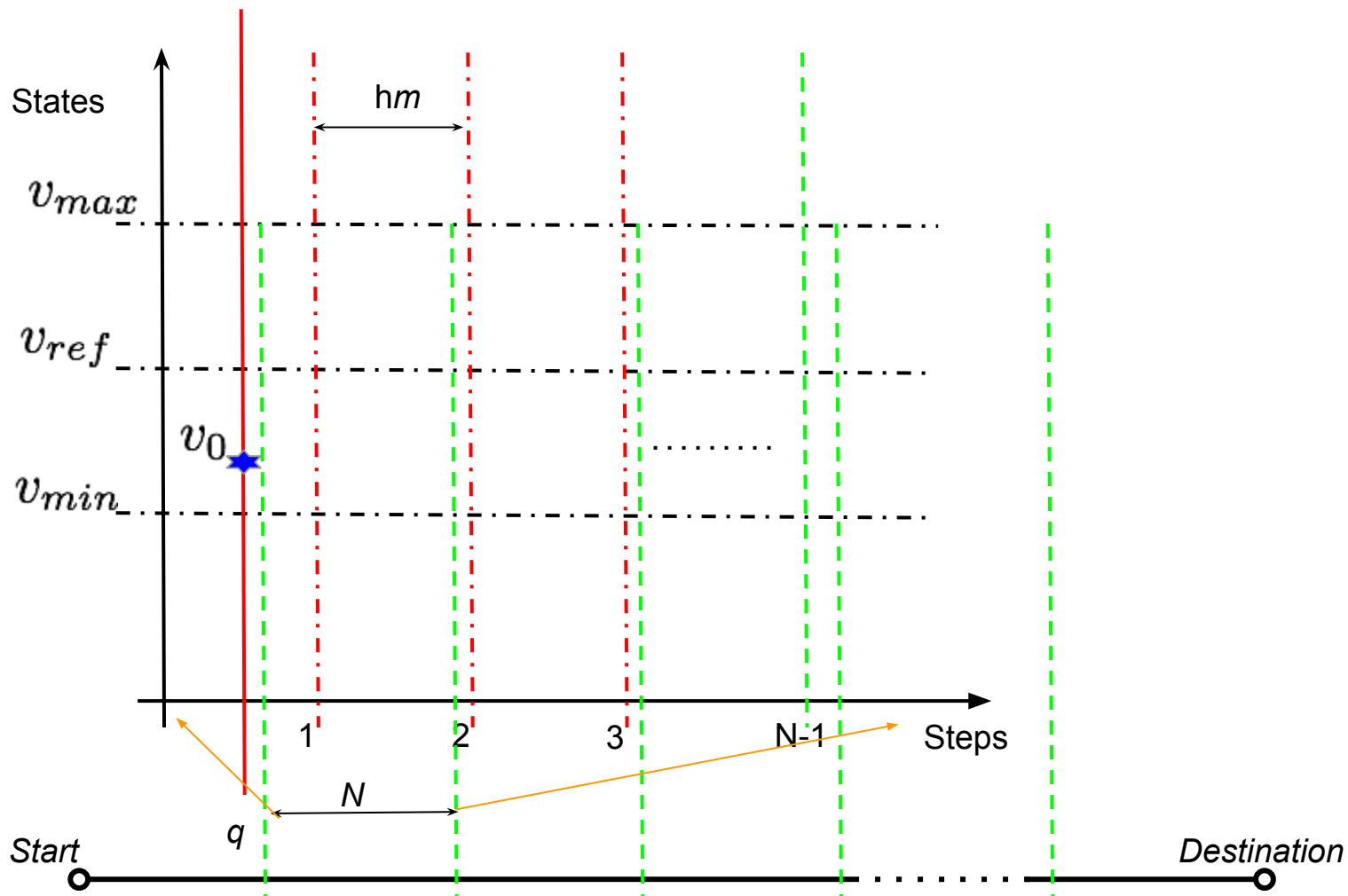
2. Take a step backward,  
 $k = N-1$ ,

$$J_k(v_k(i)) = \min_{v_{k+1}(j)} \{J_{k+1}(v_{k+1}(j)) + \beta_k^{i,j}\}$$

3. If  $k > 1$ , repeat step 2

**Figure 5:** N-step Dynamic Programming Problem

# Model Predictive Control



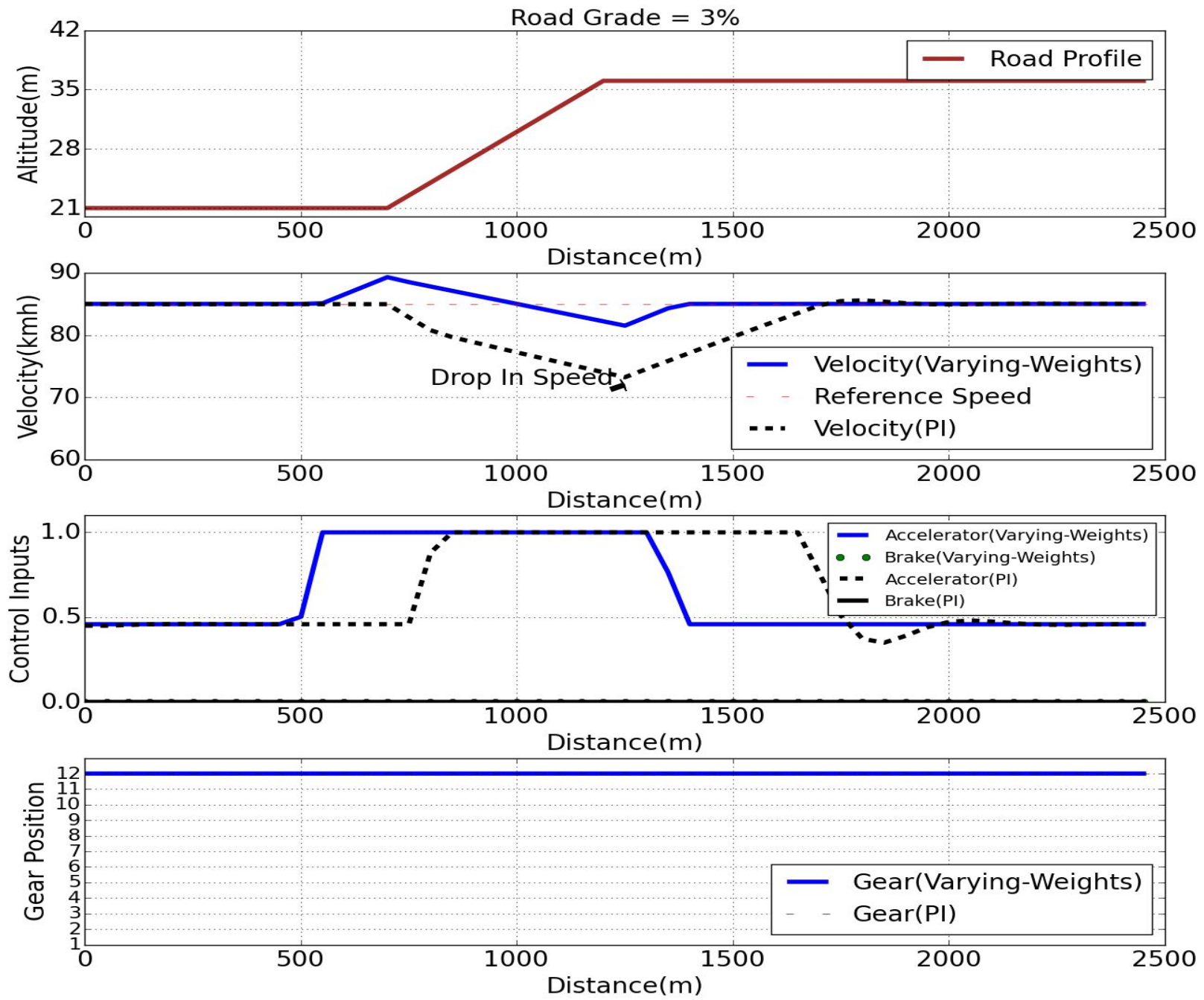
# Simulation

- Controllers (Julia):
  - PI Controller
  - Optimal Controller with fixed-weights
  - Optimal Controller with varying-weights
- Scenarios:
  - Uphill
  - Downhill

*Artificial road sections of length 2500m with 500m of varying grade (uphill/downhill)*

# Simulation Parameters

Parameter	Description	Value
$h$	Step length	50m
$N$	No. Of Steps	30
$v_{ref}$	Reference Velocity	85 km/h
$v_{min}$	Lower Bound	80 km/h
$v_{max}$	Upper Bound	90 km/h
$\alpha$	Road Grade	$\pm 3\%$



# *PI Vs Varying-Weights (Uphill)*

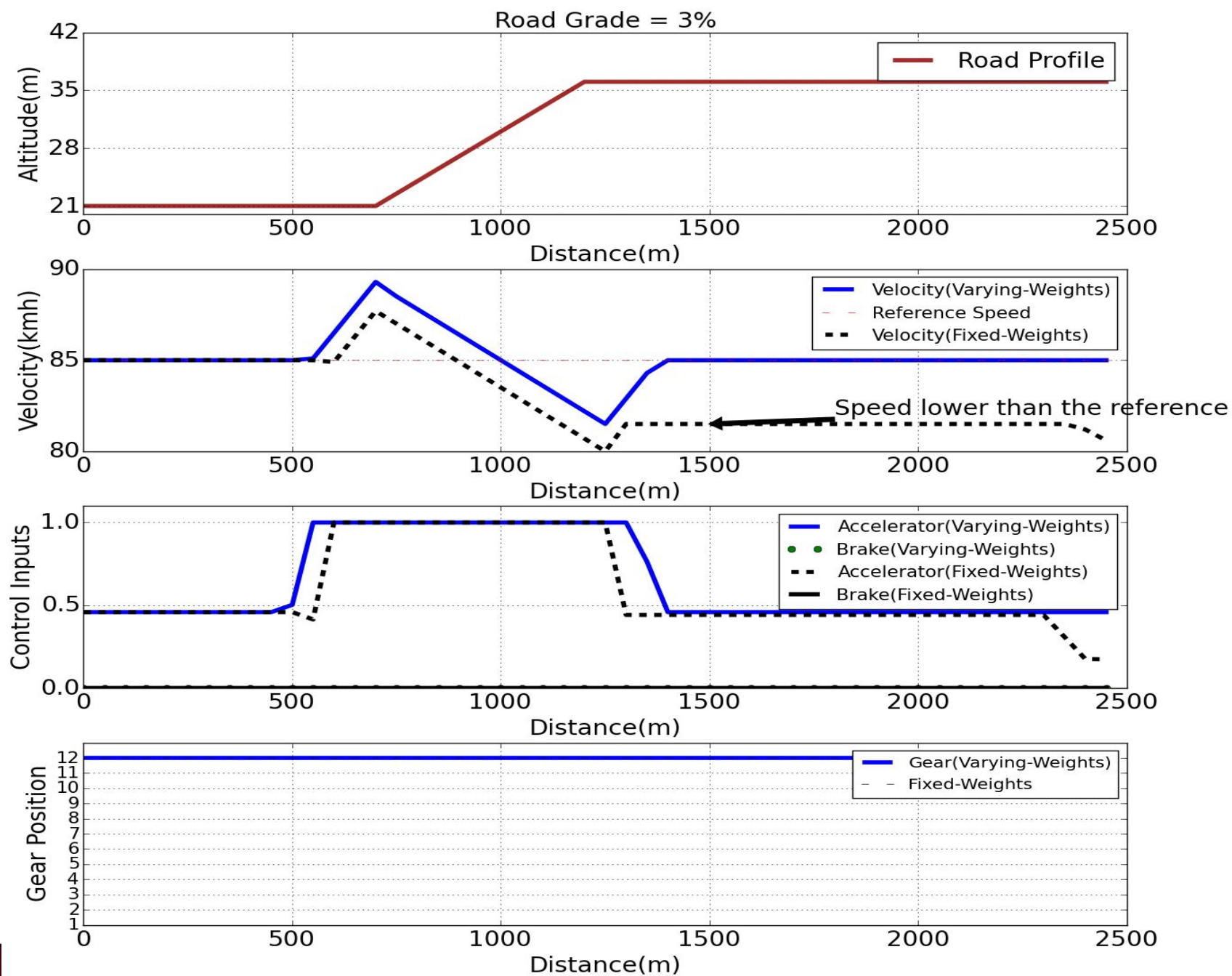
Gain	Uphill	Value
$L_1$	Low	1
$L_2$	Low	2
$L_3$	High	15
$L_4$	Nil	0



Desired Behavior	Observed Behavior
Accelerate Before Ascent	😊
Accelerate During Ascent	😊
Fuel Consumption	😊
Minimal Speed Drop	😊
Time	😊

$$\Delta_{fuel}(\%) = \frac{m_{f,VW} - m_{f,PI}}{m_{f,PI}} \times 100 = -0.44\%$$

# Performance Analyses Of Fixed-Weights Optimal Control Vs Varying-Weights Optimal Control










# Varying-Weights Vs Fixed-Weights (Uphill)

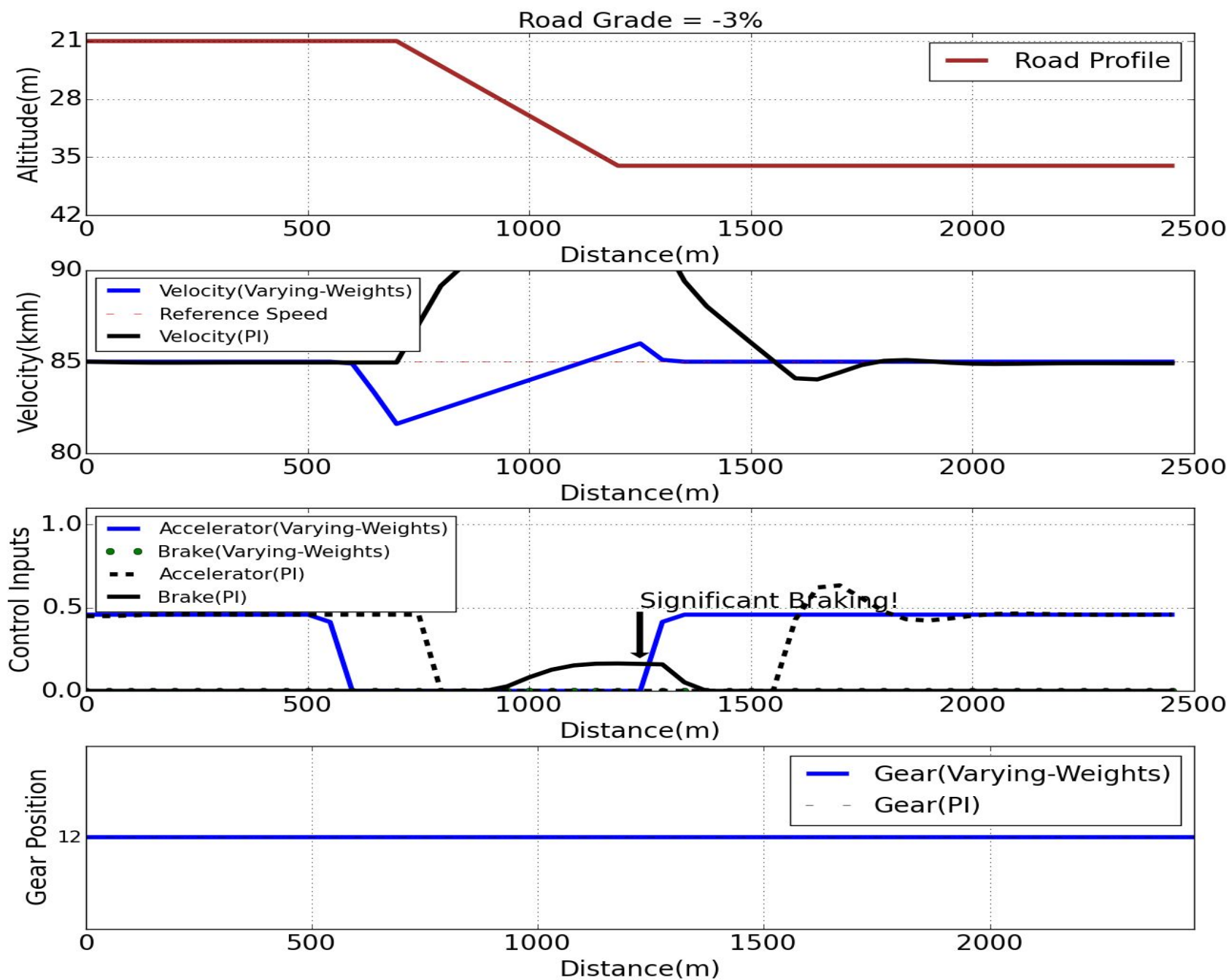
Gain	FW	VW	Value
$L_1$	2	Low	1
$L_2$	5	Low	2
$L_3$	15	High	15
$L_4$	100	Nil	0



Desired Behavior	Observed Behavior
Accelerate Before Ascent	
Accelerate During Ascent	
Fuel Consumption	
Minimal Speed Drop	
Time	

$$\Delta_{fuel}(\%) = \frac{m_{f,VW} - m_{f,PI}}{m_{f,PI}} \times 100 = 1.79\%$$

# Performance Analyses Of PI Vs Varying-Weights Optimal Control(Fuel Savings = -0.48%)



# Varying-Weights Vs PI (Downhill)

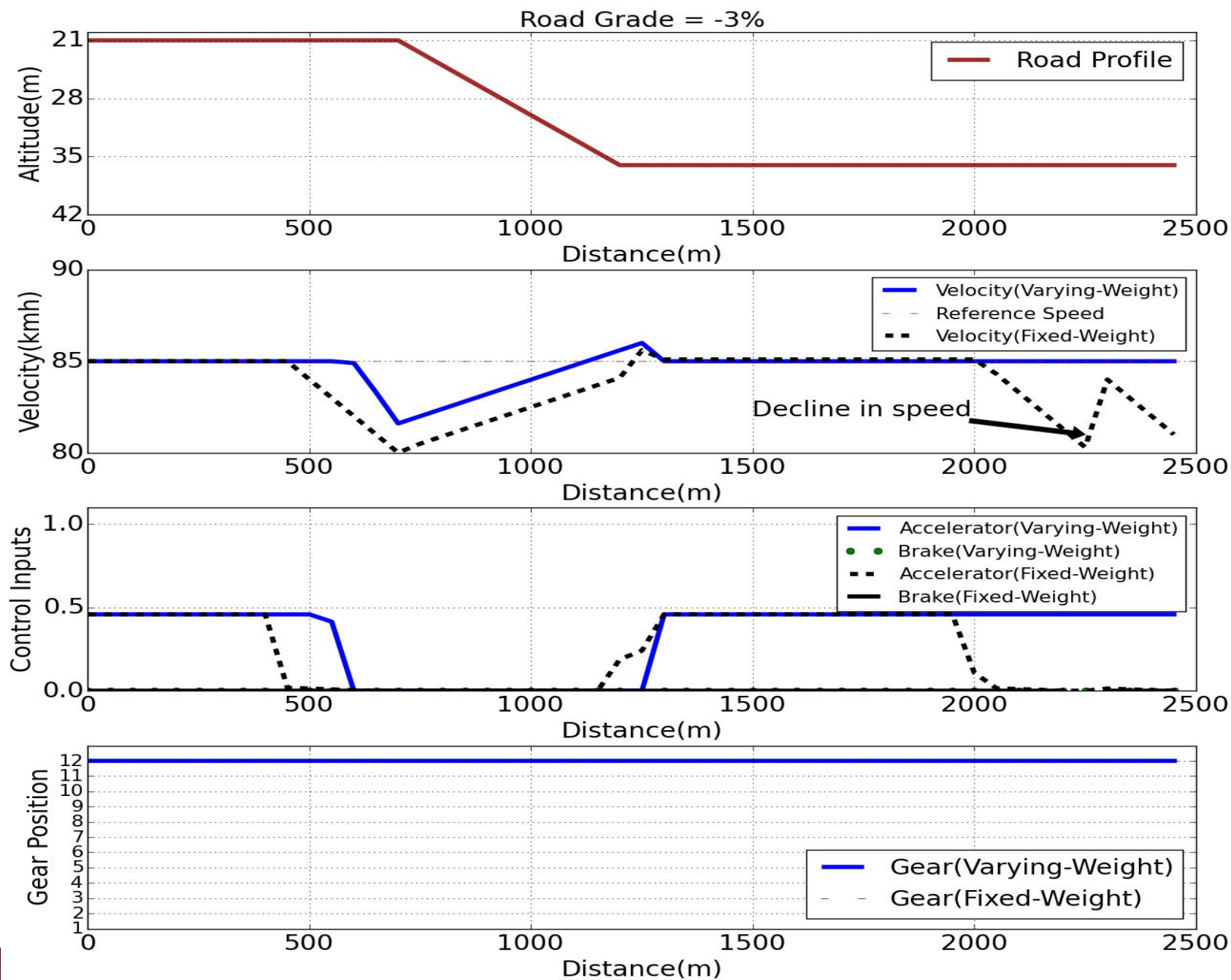
Gain	VW	Value
$L_1$	High	2.5
$L_2$	Low	1
$L_3$	High	15
$L_4$	High	100



Desired Behavior	Observed Behavior
Decelerate Before Descent	😊
Coasting During Descent	😊
Fuel Consumption	😊
Minimal Usage Of Brakes	😊
Time	😬

$$\Delta_{fuel}(\%) = \frac{m_{f,VW} - m_{f,PI}}{m_{f,PI}} \times 100 = -0.48\%$$






# Performance Analyses Of Fixed-Weight Optimal Control Vs Varying-Weight Optimal Control



# Varying-Weights Vs Fixed-Weights (Downhill)

Gain	FW	VW	Value
$L_1$	2	High	2.5
$L_2$	5	Low	1
$L_3$	15	High	15
$L_4$	100	High	100



Desired Behavior	Observed Behavior
Decelerate Before Descent	
Coasting During Descent	
Fuel Consumption	
Minimal Usage Of Brakes	
Time	

$$\Delta_{fuel}(\%) = \frac{m_{f,VW} - m_{f,PI}}{m_{f,PI}} \times 100 = 1\%$$

# OUTLINE

- ❑ Objectives
- ❑ Introduction
  - ❑ Conventional Cruise Control System
  - ❑ Human Driving Behavior
  - ❑ Prevalent Approaches
- ❑ Preliminaries
  - ❑ Vehicle Model
  - ❑ Road Grade
- ❑ Proposed Method
  - ❑ Model
  - ❑ Objective Function
  - ❑ Control Algorithm
  - ❑ Simulation Results
- ❑ Summary

# Summary

Terrain	Objective	Conventional Control	FW Control	VW Control
<i>Flat Stretch</i>	Speed Tracking	Good	Poor	Good
<i>Uphill</i>	Speed Drop	High	$>VW$	Minimal
	Fuel	$>FW/VW$	$<PI/VW$	$<PI$
	Time	High	$>VW$	Low
<i>Downhill</i>	Speed Increase	High	Low	Low
	Brake Use	High	Low	Low
	Fuel	$>FW/VW$	$<PI \& VW$	$<PI$
	Time	Low	$>PI/VW$	$<FW \& >PI$

*Varying-Weights Control is simpler since it needs no pre-processing algorithm!*





Thank you!



# Acknowledgement

- Advisory Committee:
  - Dr. Aniruddha Datta
  - Dr. Ben Zoghi
  - Dr. Reza Langari
  - Dr. Shankar P Bhattacharyya
  - Dr. Xingyong Song



TEXAS A&M  
UNIVERSITY.