Linear Regression_Coding Challenge 7

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Linear Model – 25 pts

Question 1

1. 4 pts. Read in the data called "PlantEmergence.csv" using a relative file path and load the following libraries. tidyverse, lme4, emmeans, multcomp, and multcompView. Turn the Treatment , DaysAfter-Planting and Rep into factors using the function as factor

```
# Read in data and set variable as a factor
data <- read.csv("PlantEmergence.csv",na="na")
str(data)</pre>
```

```
## 'data.frame':
                   144 obs. of 7 variables:
  $ Plot
                      : int 101 102 103 104 105 106 107 108 109 201 ...
                      : int 1234567896...
  $ Treatment
                            1 1 1 1 1 1 1 1 2 ...
##
   $ Rep
                      : int
   $ Emergence
##
                            180.5 54.5 195 198.5 202 ...
                      : num
                             "9-May-22" "9-May-22" "9-May-22" "9-May-22" ...
##
  $ DatePlanted
                      : chr
## $ DateCounted
                      : chr
                             "16-May-22" "16-May-22" "16-May-22" "16-May-22" ...
   $ DaysAfterPlanting: int
                            7 7 7 7 7 7 7 7 7 7 7 . . .
```

```
# Load necessary libraries
library(tidyverse)
```

```
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr 1.1.4 v readr
                                    2.1.5
                     v stringr
                                   1.5.1
## v forcats 1.0.0
## v ggplot2 3.5.1
                      v tibble
                                    3.2.1
## v lubridate 1.9.3
                        v tidyr
                                    1.3.1
              1.0.2
## v purrr
## -- Conflicts ----- tidyverse conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(lme4)
## Loading required package: Matrix
##
## Attaching package: 'Matrix'
##
## The following objects are masked from 'package:tidyr':
##
##
       expand, pack, unpack
library(emmeans)
## Welcome to emmeans.
## Caution: You lose important information if you filter this package's results.
## See '? untidy'
library(multcomp)
## Loading required package: mvtnorm
## Loading required package: survival
## Loading required package: TH.data
## Loading required package: MASS
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
##
##
## Attaching package: 'TH.data'
## The following object is masked from 'package:MASS':
##
##
       geyser
library(multcompView)
# Turn the Treatment , DaysAfterPlanting and Rep into factors
data <- data %>%
```

```
mutate(
    Treatment = as.factor(Treatment),
   DaysAfterPlanting = as.factor(DaysAfterPlanting),
    Rep = as.factor(Rep)
  )
str(data)
## 'data.frame':
                   144 obs. of 7 variables:
                       : int 101 102 103 104 105 106 107 108 109 201 ...
   $ Plot
##
##
                       : Factor w/ 9 levels "1","2","3","4",..: 1 2 3 4 5 6 7 8 9 6 ...
   $ Treatment
                       : Factor w/ 4 levels "1","2","3","4": 1 1 1 1 1 1 1 1 2 ...
   $ Rep
##
   $ Emergence
                      : num 180.5 54.5 195 198.5 202 ...
   $ DatePlanted
                              "9-May-22" "9-May-22" "9-May-22" ...
                       : chr
                             "16-May-22" "16-May-22" "16-May-22" "16-May-22" ...
## $ DateCounted
                       : chr
   $ DaysAfterPlanting: Factor w/ 4 levels "7", "14", "21", ...: 1 1 1 1 1 1 1 1 1 1 ...
```

Question 2

2. 5 pts. Fit a linear model to predict Emergence using Treatment and DaysAfterPlanting along with the interaction. Provide the summary of the linear model and ANOVA results.

```
lm_model <- lm(Emergence ~ Treatment*DaysAfterPlanting, data = data)
summary(lm_model)</pre>
```

```
##
## Call:
## lm(formula = Emergence ~ Treatment * DaysAfterPlanting, data = data)
## Residuals:
##
       Min
                10 Median
                                3Q
                                       Max
## -21.250
           -6.062 -0.875
                             6.750
                                    21.875
## Coefficients:
##
                                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                   1.823e+02 5.324e+00 34.229
                                                                   <2e-16 ***
## Treatment2
                                  -1.365e+02 7.530e+00 -18.128
                                                                   <2e-16 ***
## Treatment3
                                   1.112e+01 7.530e+00
                                                           1.477
                                                                    0.142
                                   2.500e+00
## Treatment4
                                              7.530e+00
                                                           0.332
                                                                    0.741
## Treatment5
                                   8.750e+00
                                             7.530e+00
                                                           1.162
                                                                    0.248
## Treatment6
                                   7.000e+00 7.530e+00
                                                           0.930
                                                                    0.355
## Treatment7
                                  -1.250e-01
                                              7.530e+00
                                                          -0.017
                                                                    0.987
## Treatment8
                                   9.125e+00
                                              7.530e+00
                                                           1.212
                                                                    0.228
## Treatment9
                                   2.375e+00
                                              7.530e+00
                                                           0.315
                                                                    0.753
                                                           1.328
## DaysAfterPlanting14
                                   1.000e+01
                                              7.530e+00
                                                                    0.187
## DaysAfterPlanting21
                                   1.062e+01
                                              7.530e+00
                                                           1.411
                                                                    0.161
## DaysAfterPlanting28
                                              7.530e+00
                                   1.100e+01
                                                           1.461
                                                                    0.147
## Treatment2:DaysAfterPlanting14 1.625e+00
                                              1.065e+01
                                                           0.153
                                                                    0.879
## Treatment3:DaysAfterPlanting14 -2.625e+00
                                              1.065e+01
                                                          -0.247
                                                                    0.806
## Treatment4:DaysAfterPlanting14 -6.250e-01
                                              1.065e+01
                                                          -0.059
                                                                    0.953
## Treatment5:DaysAfterPlanting14 2.500e+00
                                              1.065e+01
                                                           0.235
                                                                    0.815
## Treatment6:DaysAfterPlanting14 1.000e+00
                                              1.065e+01
                                                           0.094
                                                                    0.925
## Treatment7:DaysAfterPlanting14 -2.500e+00 1.065e+01
                                                          -0.235
                                                                    0.815
```

```
## Treatment8:DaysAfterPlanting14 -2.500e+00
                                              1.065e+01
                                                                    0.815
                                                          -0.235
## Treatment9:DaysAfterPlanting14 6.250e-01
                                              1.065e+01
                                                           0.059
                                                                    0.953
## Treatment2:DaysAfterPlanting21
                                  3.500e+00
                                              1.065e+01
                                                           0.329
                                                                    0.743
## Treatment3:DaysAfterPlanting21 -1.000e+00
                                                          -0.094
                                              1.065e+01
                                                                    0.925
## Treatment4:DaysAfterPlanting21
                                  1.500e+00
                                              1.065e+01
                                                           0.141
                                                                    0.888
## Treatment5:DaysAfterPlanting21
                                  2.875e+00
                                              1.065e+01
                                                           0.270
                                                                    0.788
## Treatment6:DaysAfterPlanting21
                                  4.125e+00
                                              1.065e+01
                                                           0.387
                                                                    0.699
## Treatment7:DaysAfterPlanting21 -2.125e+00
                                              1.065e+01
                                                          -0.200
                                                                    0.842
## Treatment8:DaysAfterPlanting21 -1.500e+00
                                              1.065e+01
                                                          -0.141
                                                                    0.888
## Treatment9:DaysAfterPlanting21 -1.250e+00
                                              1.065e+01
                                                         -0.117
                                                                    0.907
## Treatment2:DaysAfterPlanting28 2.750e+00
                                              1.065e+01
                                                           0.258
                                                                    0.797
## Treatment3:DaysAfterPlanting28 -1.875e+00
                                              1.065e+01
                                                          -0.176
                                                                    0.861
## Treatment4:DaysAfterPlanting28 3.123e-13
                                              1.065e+01
                                                           0.000
                                                                    1.000
                                  2.500e+00
## Treatment5:DaysAfterPlanting28
                                              1.065e+01
                                                           0.235
                                                                    0.815
## Treatment6:DaysAfterPlanting28
                                  2.125e+00
                                              1.065e+01
                                                           0.200
                                                                    0.842
## Treatment7:DaysAfterPlanting28 -3.625e+00
                                              1.065e+01
                                                          -0.340
                                                                    0.734
## Treatment8:DaysAfterPlanting28 -1.500e+00
                                                          -0.141
                                              1.065e+01
                                                                    0.888
## Treatment9:DaysAfterPlanting28 -8.750e-01
                                                          -0.082
                                                                    0.935
                                              1.065e+01
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 10.65 on 108 degrees of freedom
## Multiple R-squared: 0.9585, Adjusted R-squared: 0.945
## F-statistic: 71.21 on 35 and 108 DF, p-value: < 2.2e-16
```

anova(lm_model)

```
## Analysis of Variance Table
##
## Response: Emergence
##
                                Df Sum Sq Mean Sq F value
                                                               Pr(>F)
                                            34921 307.9516 < 2.2e-16 ***
## Treatment
                                 8 279366
## DaysAfterPlanting
                                 3
                                     3116
                                              1039
                                                    9.1603 1.877e-05 ***
## Treatment:DaysAfterPlanting
                                                 6
                                                    0.0522
                                24
                                      142
                                                                    1
## Residuals
                               108
                                    12247
                                              113
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

Question 3

3a. 5 pts. Based on the results of the linear model in question 2, do you need to fit the interaction term?

Based on the ANOVA results from Question 2, the interaction term (Treatment:DaysAfterPlanting) is not significant (p = 1), indicating that the effect of Treatment on Emergence does not significantly vary across different DaysAfterPlanting. Therefore, we can simplify the model by removing the interaction term and refitting it with only the main effects.

3b. Provide a simplified linear model without the interaction term but still testing both main effects. Provide the summary and ANOVA results. Then, interpret the intercept and the coefficient for Treatment 2.

```
lm_model2 <- lm(Emergence ~ Treatment+ DaysAfterPlanting, data = data)
summary(lm_model2)</pre>
```

```
##
## Call:
  lm(formula = Emergence ~ Treatment + DaysAfterPlanting, data = data)
##
##
  Residuals:
##
        Min
                  1Q
                       Median
                                     3Q
                                             Max
                      -0.8542
##
   -21.1632 -6.1536
                                 6.1823
                                         21.3958
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                         182.163
                                      2.797
                                             65.136
                                                     < 2e-16 ***
                       -134.531
                                      3.425 -39.277
                                                     < 2e-16 ***
## Treatment2
## Treatment3
                           9.750
                                      3.425
                                              2.847
                                                     0.00513 **
## Treatment4
                                              0.794
                           2.719
                                      3.425
                                                     0.42876
## Treatment5
                                      3.425
                                                     0.00216 **
                          10.719
                                              3.129
## Treatment6
                          8.812
                                      3.425
                                              2.573
                                                     0.01119 *
## Treatment7
                                      3.425
                                             -0.639
                                                     0.52416
                          -2.188
## Treatment8
                           7.750
                                      3.425
                                              2.263
                                                     0.02529 *
## Treatment9
                          2.000
                                      3.425
                                              0.584
                                                     0.56028
## DaysAfterPlanting14
                          9.722
                                      2.283
                                              4.258 3.89e-05 ***
## DaysAfterPlanting21
                          11.306
                                      2.283
                                              4.951 2.21e-06 ***
## DaysAfterPlanting28
                                              4.793 4.36e-06 ***
                          10.944
                                      2.283
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.688 on 132 degrees of freedom
## Multiple R-squared: 0.958, Adjusted R-squared:
## F-statistic: 273.6 on 11 and 132 DF, p-value: < 2.2e-16
```

anova(lm_model2)

```
## Analysis of Variance Table
##
##
  Response: Emergence
                      Df Sum Sq Mean Sq F value
                                                   Pr(>F)
                                  34921 372.070 < 2.2e-16 ***
                       8 279366
## Treatment
                           3116
## DaysAfterPlanting
                       3
                                   1039
                                        11.068 1.575e-06 ***
## Residuals
                     132
                          12389
                                     94
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

Result interpretation

The intercept of 182.163 represents the expected Emergence value when the treatment is at its reference level, which is Treatment 1, and the number of days after planting is at the reference level, which is 7 days. This means that when Treatment = 1 and DaysAfterPlanting = 7, the model predicts an Emergence value of 182.163. This is the baseline value for the response variable when both factors are at their reference levels.

The coefficient for Treatment 2 (-134.531) means that, compared to Treatment 1, Emergence is estimated to decrease by 134.531 units when Treatment 2 is applied, with the observation taken 7 days after planting. This difference is statistically significant, as indicated by the p-value (< 2e-16).

Question 4

4. 5 pts. Calculate the least square means for Treatment using the emmeans package and perform a Tukey separation with the compact letter display using the cld function. Interpret the results.

```
lsmeans <- emmeans(lm_model2, ~Treatment) # estimate lsmeans of variety within Treatment

Results_lsmeans <- cld(lsmeans, alpha = 0.05, reversed = TRUE, details = TRUE) # contrast with Tukey ad

Results_lsmeans
```

```
## $emmeans
   Treatment emmean
                       SE df lower.CL upper.CL .group
##
               200.9 2.42 132
                                 196.1
                                           205.7
##
   3
               199.9 2.42 132
                                 195.1
                                           204.7
                                                  1
##
   6
               199.0 2.42 132
                                 194.2
                                           203.8
               197.9 2.42 132
##
   8
                                          202.7
                                 193.1
                                                  12
##
   4
               192.9 2.42 132
                                 188.1
                                           197.7
##
   9
               192.2 2.42 132
                                 187.4
                                           196.9
                                                  12
               190.2 2.42 132
   1
                                 185.4
                                           194.9
                                                  12
               188.0 2.42 132
                                           192.8
                                                   2
##
   7
                                 183.2
##
                55.6 2.42 132
                                  50.8
                                           60.4
##
## Results are averaged over the levels of: DaysAfterPlanting
## Confidence level used: 0.95
## P value adjustment: tukey method for comparing a family of 9 estimates
## significance level used: alpha = 0.05
  NOTE: If two or more means share the same grouping symbol,
##
         then we cannot show them to be different.
##
         But we also did not show them to be the same.
##
## $comparisons
##
   contrast
                            estimate
                                       SE df t.ratio p.value
##
   Treatment7 - Treatment2 132.344 3.43 132
                                               38.638
                                                       <.0001
  Treatment1 - Treatment2 134.531 3.43 132
                                                39.277
                                                        <.0001
  Treatment1 - Treatment7
                                                        0.9993
##
                               2.188 3.43 132
                                                 0.639
   Treatment9 - Treatment2 136.531 3.43 132
                                               39.861
                                                        <.0001
##
  Treatment9 - Treatment7
                               4.188 3.43 132
                                                 1.223
                                                        0.9502
   Treatment9 - Treatment1
                               2.000 3.43 132
                                                 0.584
                                                        0.9997
   Treatment4 - Treatment2 137.250 3.43 132
##
                                                40.071
                                                        <.0001
   Treatment4 - Treatment7
                               4.906 3.43 132
                                                 1.432
                                                        0.8832
##
                               2.719 3.43 132
  Treatment4 - Treatment1
                                                 0.794
                                                        0.9969
  Treatment4 - Treatment9
                               0.719 3.43 132
                                                 0.210
                                                        1.0000
##
   Treatment8 - Treatment2 142.281 3.43 132
                                                41.540
                                                        <.0001
   Treatment8 - Treatment7
                               9.938 3.43 132
                                                 2.901
                                                        0.0978
##
  Treatment8 - Treatment1
                               7.750 3.43 132
                                                 2.263
                                                        0.3724
## Treatment8 - Treatment9
                               5.750 3.43 132
                                                 1.679
                                                        0.7583
##
   Treatment8 - Treatment4
                               5.031 3.43 132
                                                 1.469
                                                        0.8678
##
   Treatment6 - Treatment2 143.344 3.43 132
                                                41.850
                                                        <.0001
  Treatment6 - Treatment7
                              11.000 3.43 132
                                                 3.212
                                                        0.0425
##
  Treatment6 - Treatment1
                               8.812 3.43 132
                                                 2.573
                                                        0.2083
   Treatment6 - Treatment9
                               6.812 3.43 132
                                                 1.989
##
                                                        0.5538
##
  Treatment6 - Treatment4
                               6.094 3.43 132
                                                 1.779
                                                        0.6957
## Treatment6 - Treatment8
                               1.062 3.43 132
                                                 0.310
                                                        1.0000
## Treatment3 - Treatment2 144.281 3.43 132 42.124 <.0001
```

```
Treatment3 - Treatment7
                              11.938 3.43 132
                                                3.485
                                                      0.0187
   Treatment3 - Treatment1
##
                               9.750 3.43 132
                                                2.847
                                                      0.1120
##
  Treatment3 - Treatment9
                               7.750 3.43 132
                                                2.263
                                                       0.3724
## Treatment3 - Treatment4
                               7.031 3.43 132
                                                2.053
                                                       0.5099
   Treatment3 - Treatment8
                               2.000 3.43 132
                                                0.584
                                                       0.9997
## Treatment3 - Treatment6
                               0.938 3.43 132
                                                0.274
                                                       1.0000
## Treatment5 - Treatment2 145.250 3.43 132
                                               42.406
                                                       <.0001
## Treatment5 - Treatment7
                              12.906 3.43 132
                                                3.768
                                                       0.0074
##
   Treatment5 - Treatment1
                              10.719 3.43 132
                                                3.129
                                                       0.0535
## Treatment5 - Treatment9
                              8.719 3.43 132
                                                2.545
                                                       0.2204
## Treatment5 - Treatment4
                               8.000 3.43 132
                                                2.336
                                                       0.3288
## Treatment5 - Treatment8
                               2.969 3.43 132
                                                0.867
                                                       0.9943
   Treatment5 - Treatment6
                               1.906 3.43 132
                                                0.557
                                                       0.9998
  Treatment5 - Treatment3
                               0.969 3.43 132
##
                                                0.283
                                                      1.0000
##
## Results are averaged over the levels of: DaysAfterPlanting
## P value adjustment: tukey method for comparing a family of 9 estimates
```

Result interpretation

The LSMeans show that Treatment 2 has a significantly lower emergence (55.6) compared to all other treatments, which have similar means around 199-200. The compact letter display groups the treatments into two categories: Treatments 5, 3, 6, and 1 are not significantly different from each other, while Treatments 7, 2, and 8 differ significantly. Tukey's pairwise comparisons confirm that Treatment 2 is significantly lower than all other treatments, while differences within other treatments are generally not significant.

Question 5

5. 4 pts. The provided function lets you dynamically add a linear model plus one factor from that model and plots a bar chart with letters denoting treatment differences. Use this model to generate the plot shown below. Explain the significance of the letters.

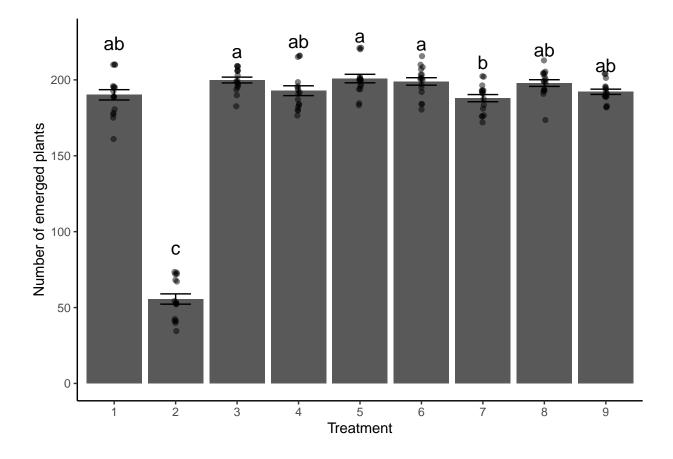
```
plot_cldbars_onefactor <- function(lm_model, factor) {</pre>
  data <- lm_model$model</pre>
  variables <- colnames(lm_model$model)</pre>
  dependent_var <- variables[1]</pre>
  independent var <- variables[2:length(variables)]</pre>
  lsmeans <- emmeans(lm_model, as.formula(paste("~", factor))) # estimate lsmeans
  Results_1smeans <- cld(1smeans, alpha = 0.05, reversed = TRUE, details = TRUE, Letters = letters) # c
  # Extracting the letters for the bars
  sig.diff.letters <- data.frame(Results_lsmeans$emmeans[,1],</pre>
                                   str_trim(Results_lsmeans$emmeans[,7]))
  colnames(sig.diff.letters) <- c(factor, "Letters")</pre>
  # for plotting with letters from significance test
  ave_stand2 <- lm_model$model %>%
    group_by(!!sym(factor)) %>%
    dplyr::summarize(
      ave.emerge = mean(.data[[dependent_var]], na.rm = TRUE),
      se = sd(.data[[dependent_var]]) / sqrt(n())
```

```
) %>%
  left_join(sig.diff.letters, by = factor) %>%
  mutate(letter_position = ave.emerge + 10 * se)

plot <- ggplot(data, aes(x = !! sym(factor), y = !! sym(dependent_var))) +
  stat_summary(fun = mean, geom = "bar") +
  stat_summary(fun.data = mean_se, geom = "errorbar", width = 0.5) +
  ylab("Number of emerged plants") +
  geom_jitter(width = 0.02, alpha = 0.5) +
  geom_text(data = ave_stand2, aes(label = Letters, y = letter_position), size = 5) +
  xlab(as.character(factor)) +
  theme_classic()

return(plot)
}

plot_cldbars_onefactor(lm_model2, "Treatment")</pre>
```



Result Interpretation - significance of letters

The letters help us know which treatments are significantly different from the others. Treatments with the same letter are not significantly different from each other, while treatments with different letters are significantly different.

In the above result, Treatments 1, 4, 8, and 9 share the "ab" label, indicating that they are not significantly

different from each other. Treatment 2, marked with a "c," is significantly different from all other treatments. Treatments 3, 5, and 6, labeled with "a," are significantly different from Treatments 2 and 7, but not from each other. Treatment 7, marked with a "b," is only significantly different from Treatments 1, 4, 8, and 9, and not from the others within its group.

Question 6

6. 2 pts. Generate the gfm .md file along with a .html, .docx, or .pdf. Commit, and push the .md file to github and turn in the .html, .docx, or .pdf to Canvas. Provide me a link here to your github.

Link to github