



- When the polynomial code method is employed, the sender and receiver must agree upon a **generator polynomial**,  $G(x)$ , in advance.
- Both the high- and low order bits of the generator must be 1.
- To compute the CRC for some frame with  $m$  bits corresponding to the polynomial  $M(x)$ , the frame must be longer than the generator polynomial.
- The idea is to append a CRC to the end of the frame in such a way that the polynomial represented by the checksummed frame is divisible by  $G(x)$ .
- When the receiver gets the checksummed frame, it tries dividing it by  $G(x)$ . If there is a remainder, there has been a transmission error.

- 1. Let  $r$  be the degree of  $G(x)$ . Append  $r$  zero bits to the low-order end of the frame so it now contains  $m + r$  bits and corresponds to the polynomial  $x^r M(x)$ .
- 2. Divide the bit string corresponding to  $G(x)$  into the bit string corresponding to  $x^r M(x)$ , using modulo 2 division.
- 3. Subtract the remainder (which is always  $r$  or fewer bits) from the bit string corresponding to  $x^r M(x)$  using modulo 2 subtraction. The result is the checksummed frame to be transmitted. Call its polynomial  $T(x)$ .

- calculation for a frame 1101011111 using the generator  $G(x) = x^4 + x^3 + 1$ .

Diagram illustrating the CRC-16 calculation:

Divisor: 1 1 0 1 0 1 1 1 1 1 0 0 0 0 (Frame with four zeros appended)

Dividend: 1 0 0 1 1

Quotient (thrown away): 1 1 0 0 0 0 1 1 1 0

Remainder: 1 0 0 1 1

Diagram illustrating the CRC-16 calculation using polynomial division:

Dividend: 1 0 0 1 1 (Data) followed by 0 0 0 0 (padding) → 1 0 0 1 1 0 0 0 0

Divisor: 1 1 0 0 0 0 1 1 1 0

Quotient (thrown away): 1 1 0 1 0 0 0 0

Remainder: 0 0 1 0 (labeled as 0010)

Transmitted frame: 1 1 0 1 0 1 1 1 1 1 0 0 1 0 ← Frame with four zeros appended  
minus remainder