

# Applicatives

## pure

`pure x` puts `x` into a functor (a container).

## (<\*>)

Called "ap".

Left associative by default.

You can also put functions inside functors: `Just succ`

How to apply such functions?

## Definitions

```
class Functor f => Applicative f where
  pure :: a -> f a
  (<*>) :: f (a -> b) -> f a -> f b
```

```
instance Applicative Maybe where
  pure :: a -> Maybe a
  pure x = Just x
  (<*>) :: Maybe (a -> b) -> Maybe a -> Maybe b
  Just f <*> Just x = Just (f x)
  _ <*> _ = Nothing
```

```
instance Applicative [] where
  pure :: a -> [a]
  pure x = [x]
  (<*>) :: [a -> b] -> [a] -> [b]
  (f : fs) <*> xs = map f xs ++ fs <*> xs
  _ <*> _ = []
```

## Rules

A valid instance of an Applicative must satisfy these laws:

## Applicatives

1. Homomorphism:  $\text{pure } f \lt * \text{ pure } x = \text{pure } (f \ x)$
2. Identity:  $\text{pure id} \lt * v = v$
3. Composition:  $\text{pure } (.) \lt * u \lt * v \lt * w = u \lt * (v \lt * w)$
4. Interchange:  $u \lt * \text{pure } x = \text{pure } (\$ \ x) \lt * u$