## **Diagonal Matrices**

$$\mathsf{D} = \begin{bmatrix} d_1 & 0 & 0 & 0 \\ 0 & d_2 & 0 & 0 \\ 0 & 0 & \dots & 0 \\ 0 & 0 & 0 & d_n \end{bmatrix}$$

Scaling along the axis (plural)

$$\begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$$

$$\begin{bmatrix} d_1x_1 \\ d_2x_2 \\ \vdots \\ d_nx_n \end{bmatrix}$$

$$\mathsf{A} = \mathsf{arbitrary\ matrix} = \begin{bmatrix} a_{11} & a_{12} & \dots & a_{1n} \\ a_{21} & \dots & \dots & \dots \\ \vdots & \ddots & \ddots & \ddots & \vdots \\ a_{n1} & \dots & \dots & a_{nn} \end{bmatrix}$$

$$\mathsf{DA} = \mathsf{Scaling} \; \mathsf{the} \; \mathsf{rows} = \begin{bmatrix} \; d_1(Row \; 1) \; \\ \\ d_2(Row \; 2) \\ \\ \vdots \\ \\ d_n(Row \; n) \end{bmatrix}$$

AD = Scaling the columns = ...

Spectrum of D =  $\{d_1, d_2, \dots d_n\} / \{0\}$ 

 $E_{d_i} = i^{th}$  axis = In **general**, unless  $d_i = d_j$  for some i, j