



Virtual and Augmented Reality

CS-GY 9223/CUSP-GX 6004

<https://nyu-icl.github.io/courses/2022fall-vr-ar>

Prof. Qi Sun

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Final Project Presentation

2.5min in total (no more) =
cover page +
~.5min on motivation/problem +
~1 min on system showcasing +
~1 min on tech details

Panoramic Imaging and Cinematic VR



Jaunt
VR

Jaunt VR



Lytro



Lytro



Google



Nokia



W: 157,83mm / 6.3"

L: 262,95mm / 10.4"



Facebook



see Brian Cabral's SCIENCE talk @ talks.Stanford.edu



Red

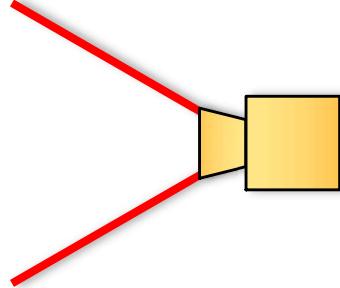


Samsung



Panorama v Stereo Movie v Stereo Panorama

mono & head rotation

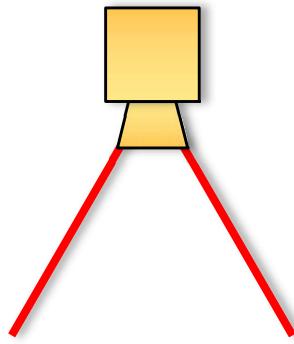


Panorama v Stereo Movie v Stereo

Panorama

Panorama

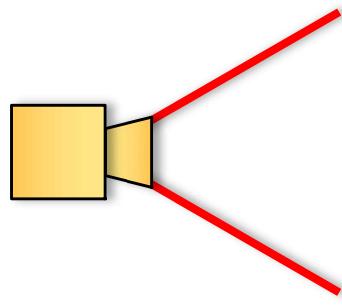
mono & head rotation



Panorama v Stereo Movie v Stereo Panorama

Panorama

mono & head rotation



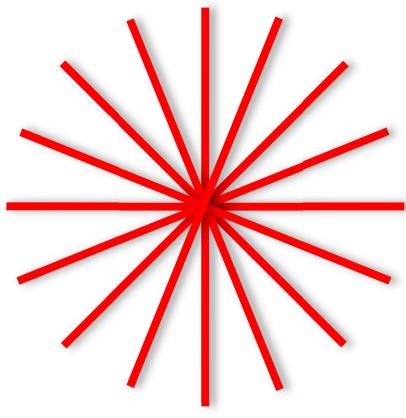
Panorama v Stereo Movie v Stereo Panorama

mono & head rotation



Panorama v Stereo Movie v Stereo Panorama

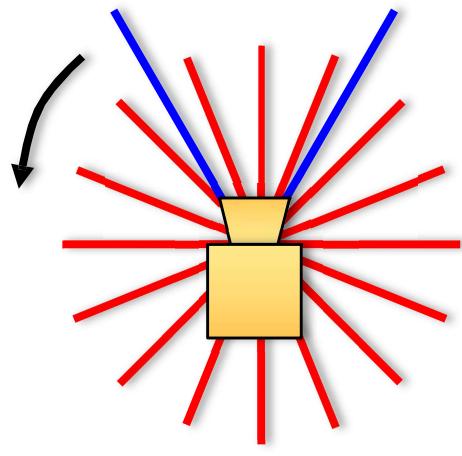
mono & head rotation



1 center of
projection!

Panorama v Stereo Movie v Stereo Panorama

mono & head rotation



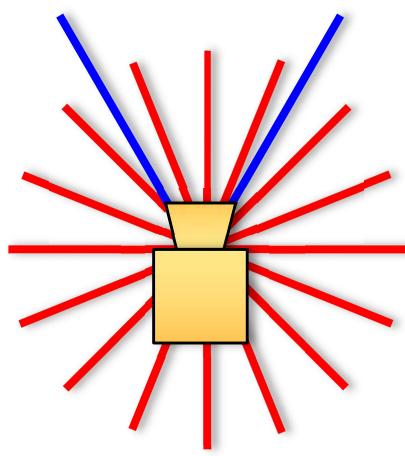
1 center of
projection!

Panorama v Stereo Movie v Stereo

Panorama

center of
projection

mono & head rotation

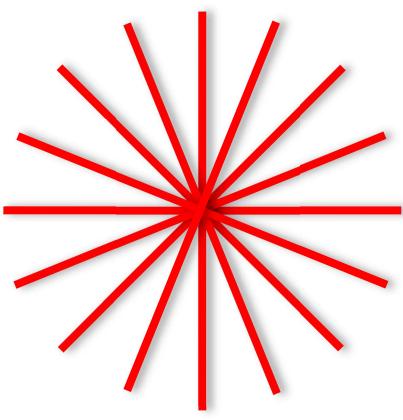


1 center of
projection!

Panorama v Stereo Movie v Stereo Panorama

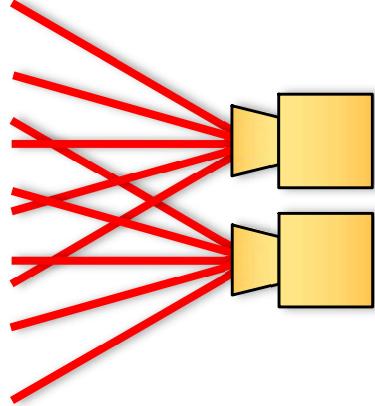
Panorama

mono & head rotation



Stereo

stereo & no head rotation



Stereo Panorama

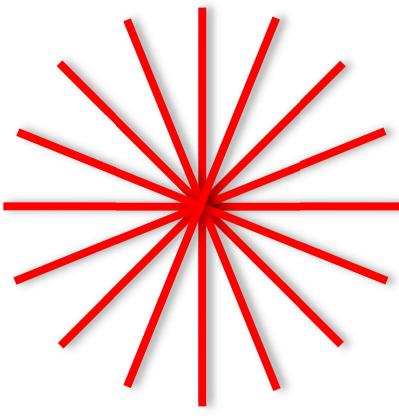
stereo & head rotation

1 center of
projection!

Panorama v Stereo Movie v Stereo Panorama

Panorama

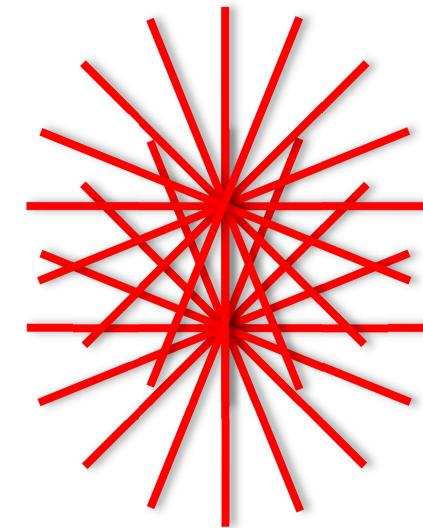
mono & head rotation



1 center of
projection!

Stereo

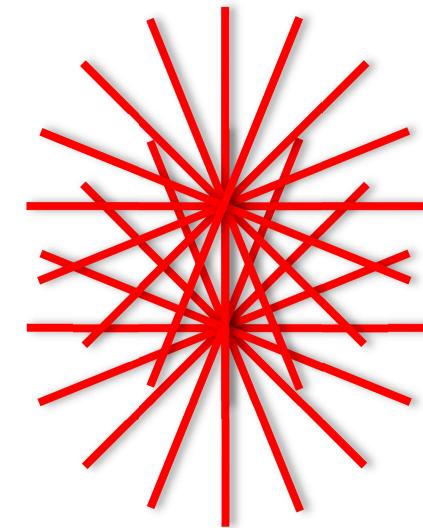
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

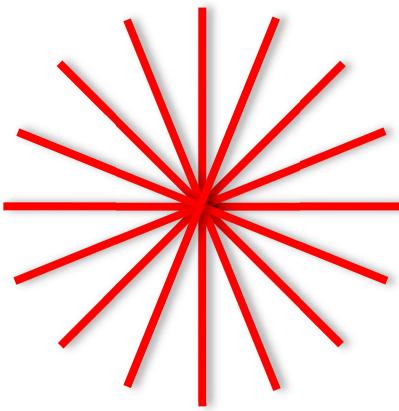
stereo & head rotation



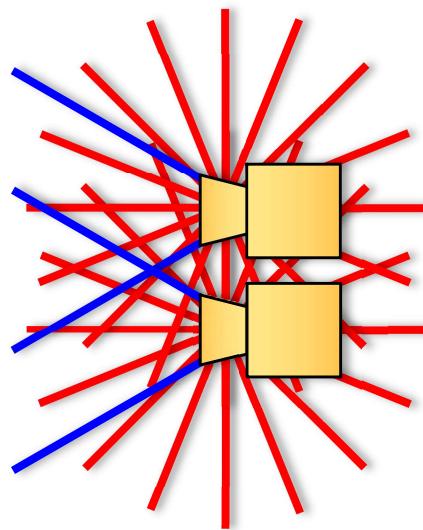
2 centers of
projection!

Panorama v Stereo Movie v Stereo Panorama

Panorama Stereo
mono & head rotation stereo & no head rotation



1 center of
projection!

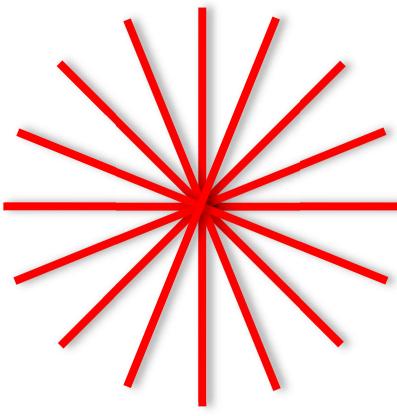


2 centers of
projection!

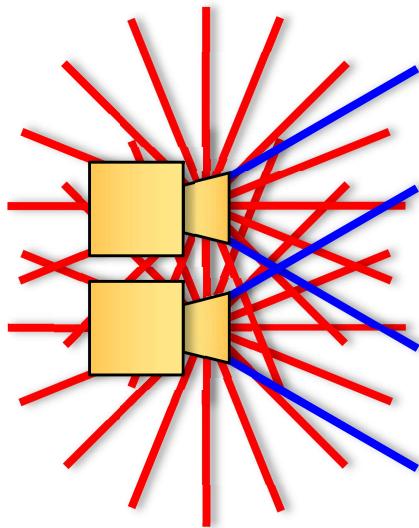
Stereo Panorama
stereo & head rotation

Panorama v Stereo Movie v Stereo Panorama

Panorama Stereo
mono & head rotation stereo & no head rotation



1 center of projection!

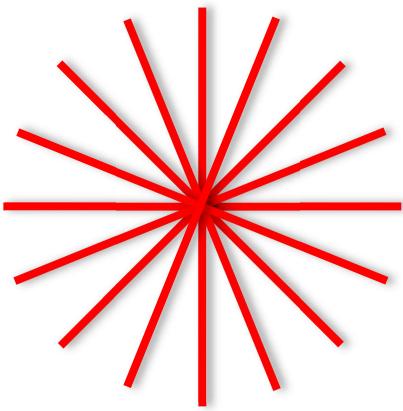


2 centers of projection!

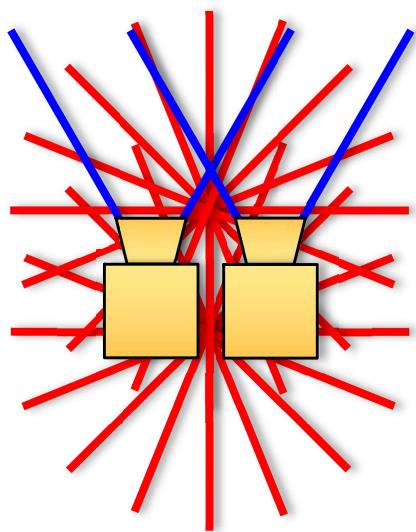
Stereo Panorama
stereo & head rotation

Panorama v Stereo Movie v Stereo Panorama

Panorama Stereo
mono & head rotation stereo & no head rotation



1 center of projection!

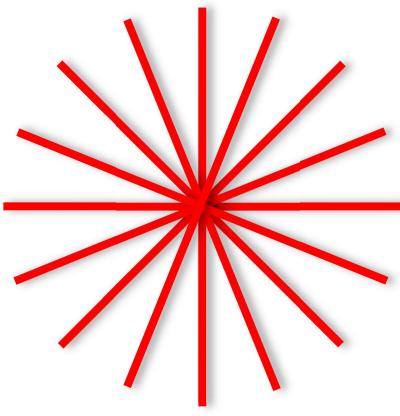


2 centers of projection!

Stereo Panorama
stereo & head rotation

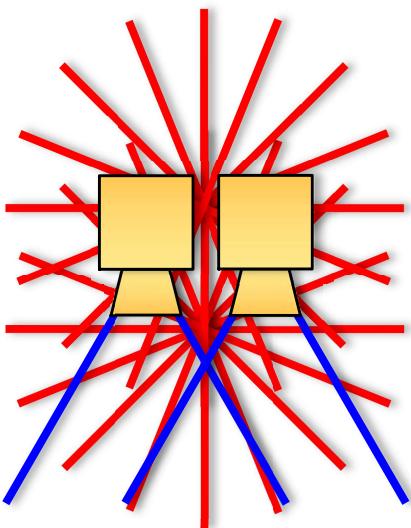
Panorama v Stereo Movie v Stereo Panorama

mono & head rotation



1 center of
projection!

stereo & no head rotation



stereo & head rotation

Stereo Panorama

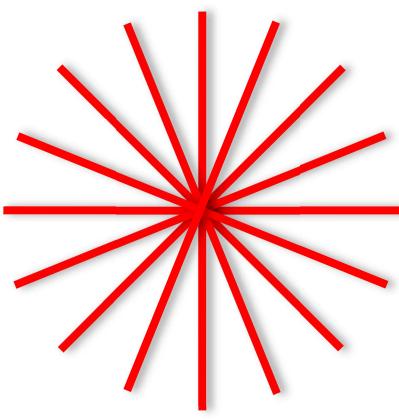
Stereo Panorama

2 centers of
projection!

Panorama v Stereo Movie v Stereo Panorama

Panorama

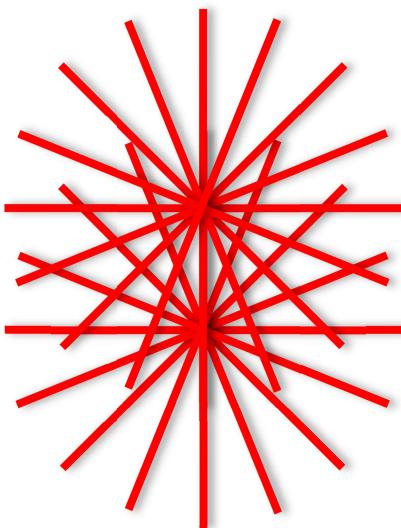
mono & head rotation



1 center of
projection!

Stereo

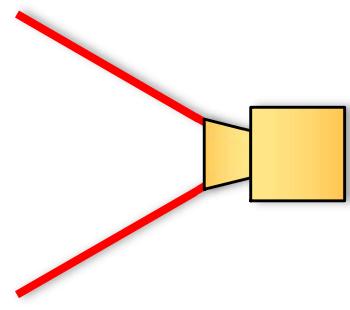
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

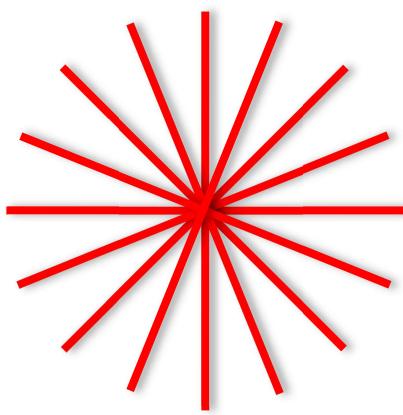
stereo & head rotation



Panorama v Stereo Movie v Stereo Panorama

Panorama

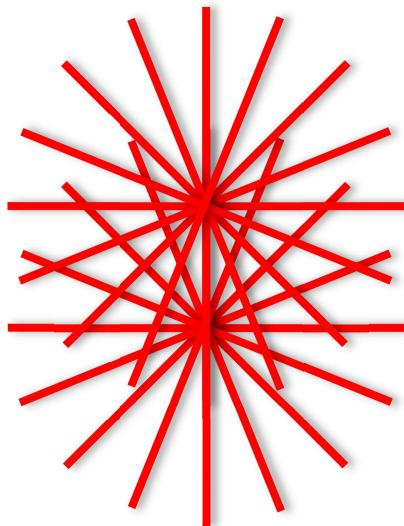
mono & head rotation



1 center of
projection!

Stereo

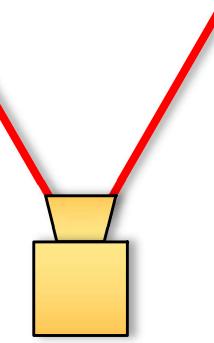
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

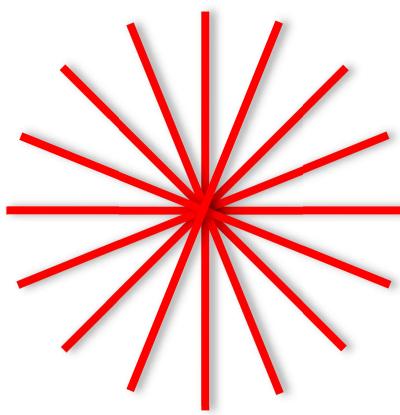
stereo & head rotation



Panorama v Stereo Movie v Stereo Panorama

Panorama

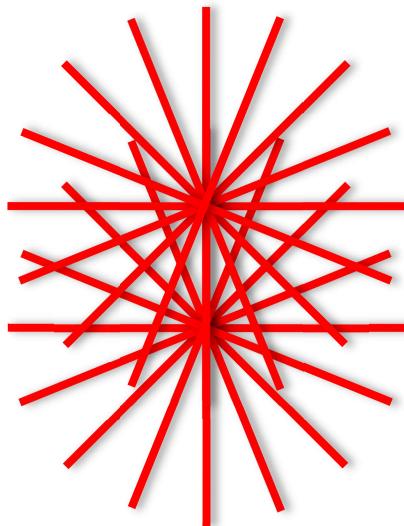
mono & head rotation



1 center of
projection!

Stereo

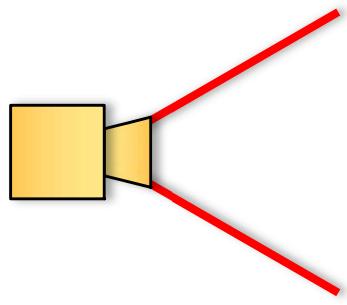
stereo & no head rotation



2 centers of
projection!

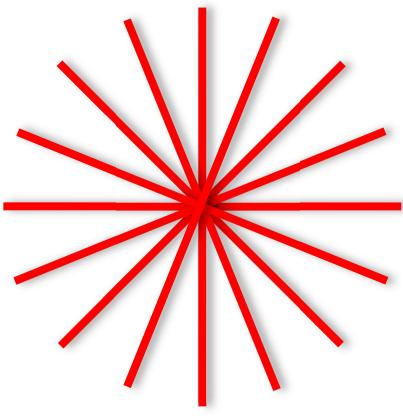
Stereo Panorama

stereo & head rotation



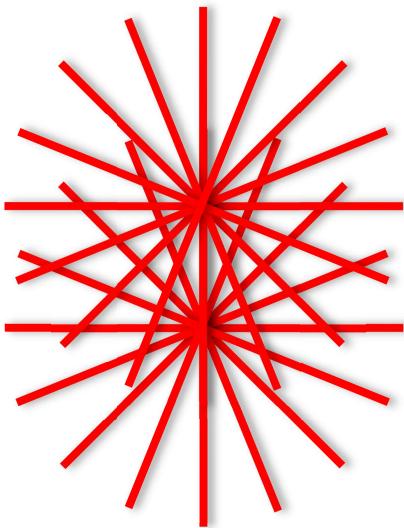
Panorama v Stereo Movie v Stereo Panorama

mono & head rotation



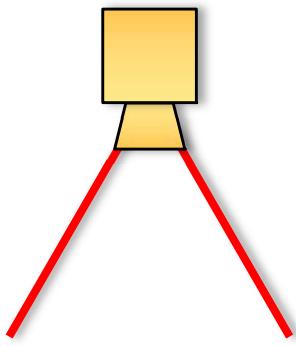
1 center of
projection!

stereo & no head rotation



2 centers of
projection!

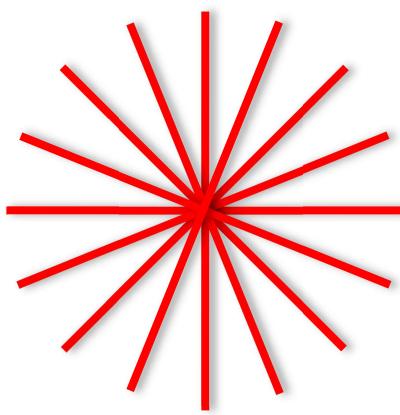
stereo & head rotation



Panorama v Stereo Movie v Stereo Panorama

Panorama

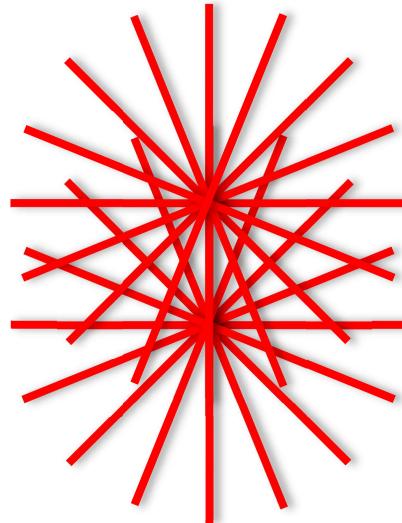
mono & head rotation



1 center of
projection!

Stereo

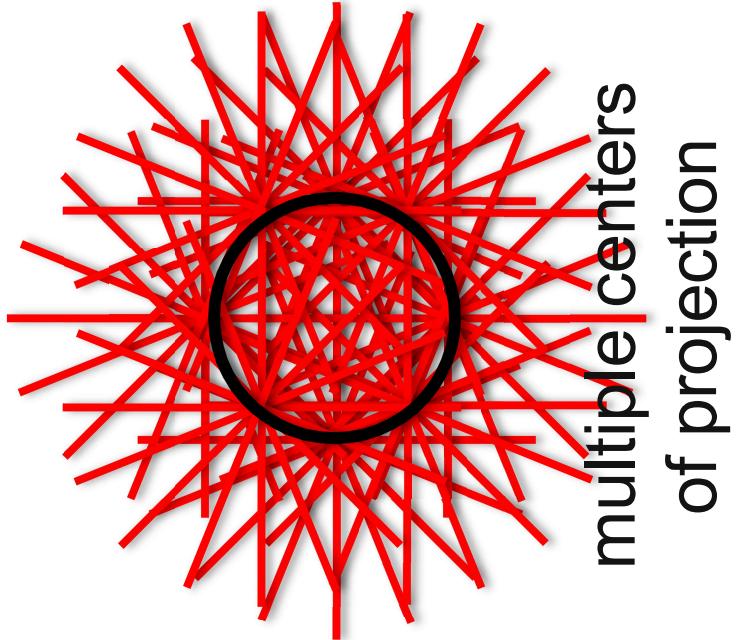
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

stereo & head rotation

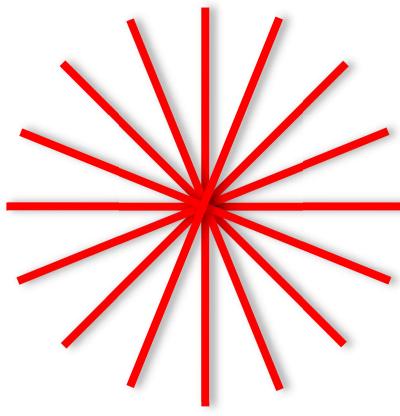


multiple centers
of projection

Panorama v Stereo Movie v Stereo Panorama

Panorama

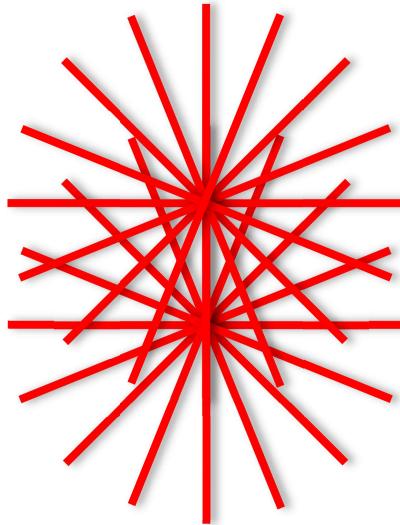
mono & head rotation



1 center of
projection!

Stereo

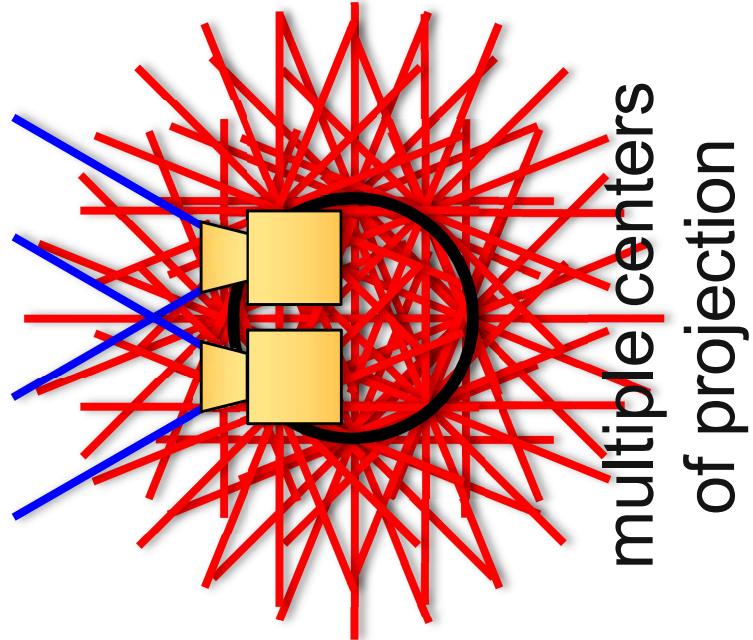
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

stereo & head rotation

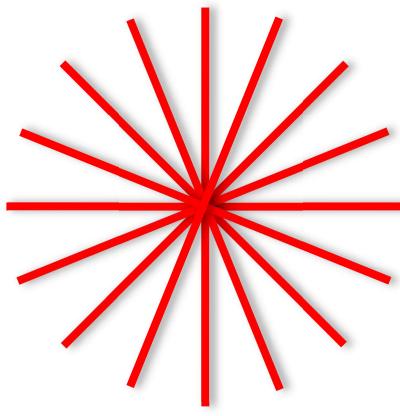


multiple centers
of projection

Panorama v Stereo Movie v Stereo Panorama

Panorama

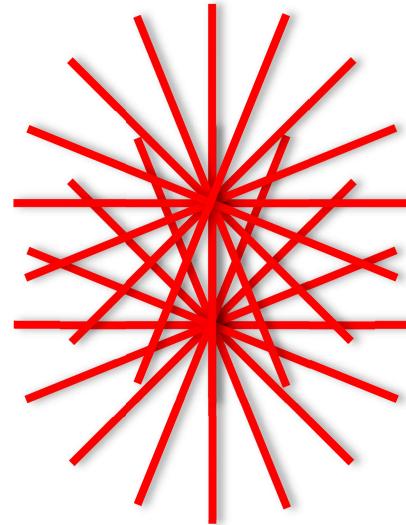
mono & head rotation



1 center of
projection!

Stereo

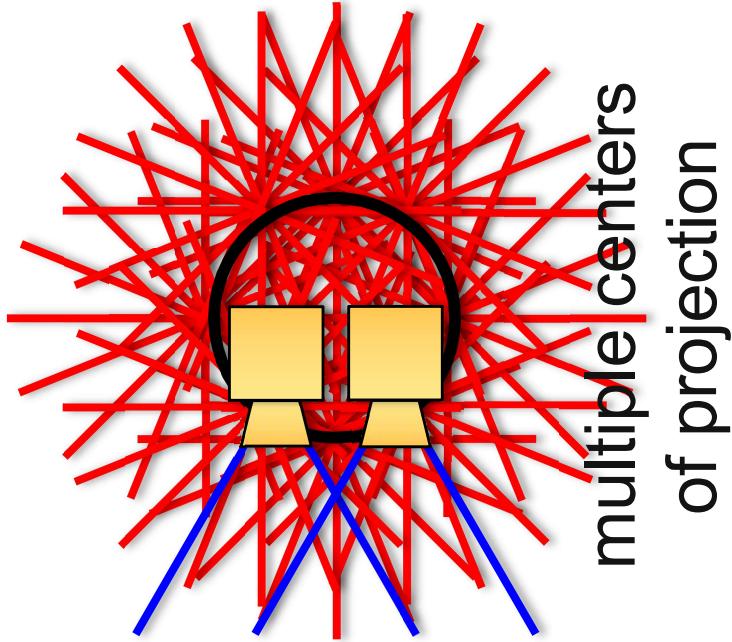
stereo & no head rotation



2 centers of
projection!

Stereo Panorama

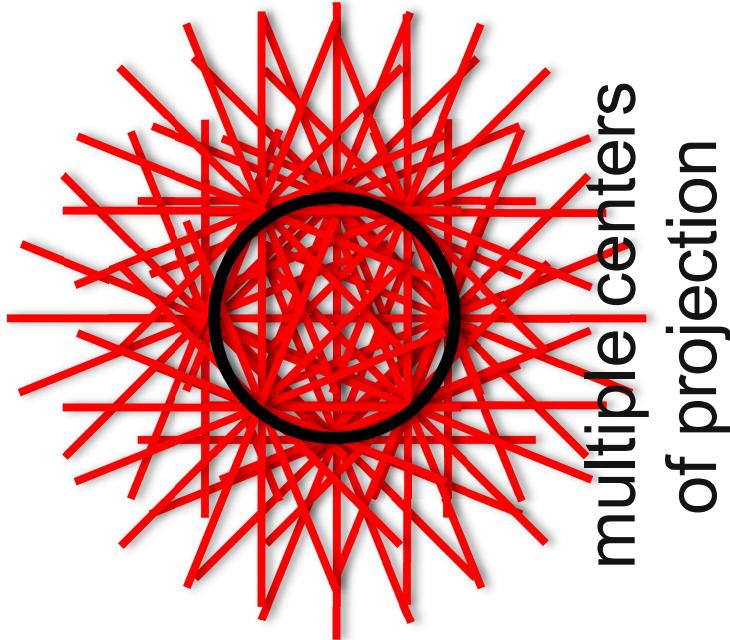
stereo & head rotation



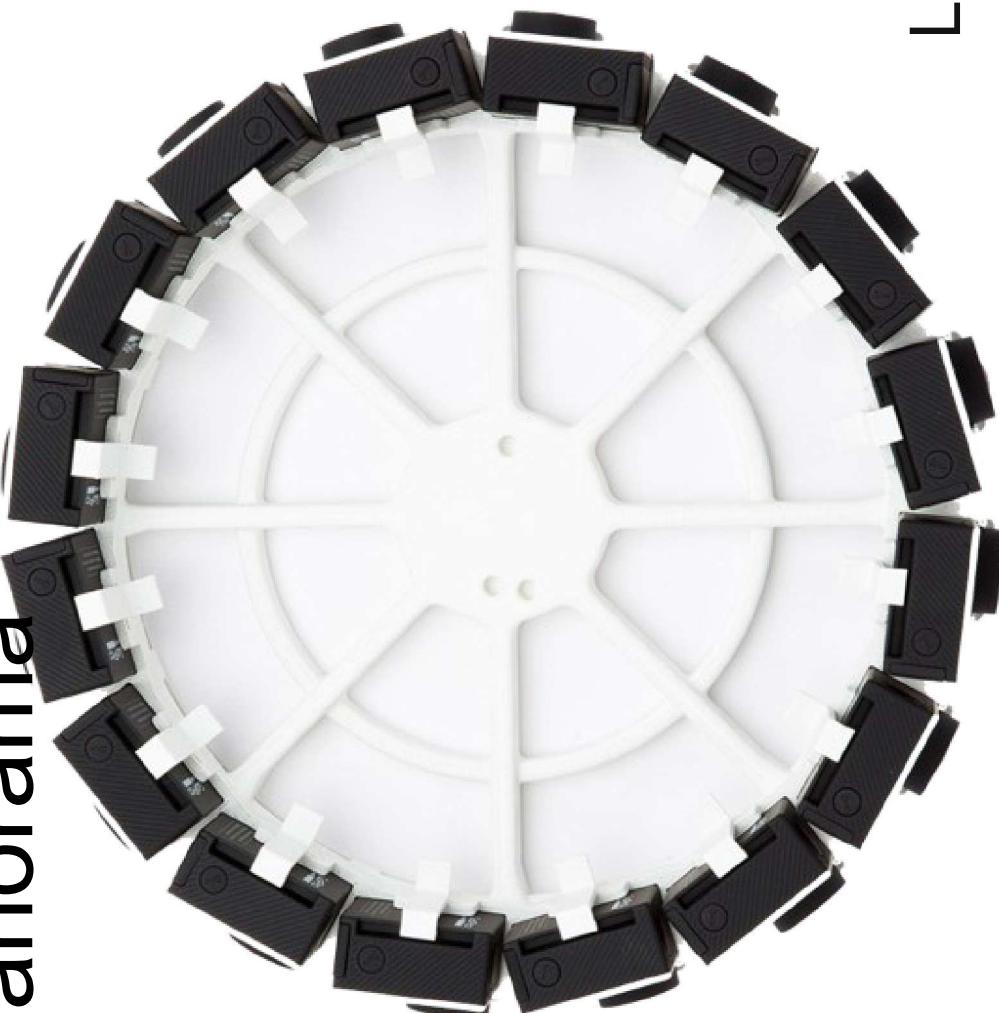
multiple centers
of projection

Panorama v Stereo Movie v Stereo Panorama

Stereo Panorama
stereo & head rotation



Light Field!



Panorama v Stereo Movie v Stereo Panorama

Panorama

mono & head rotation



RICOH Theta

Stereo

stereo & no head rotation



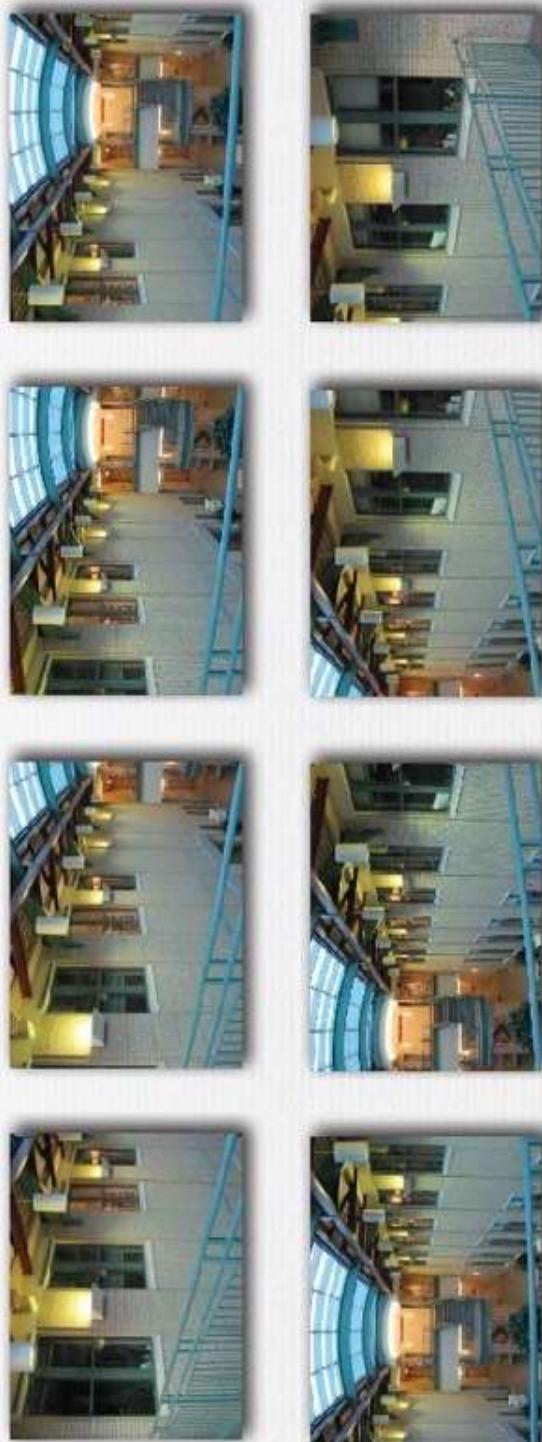
Stereo Panorama

stereo & head rotation



horizontal-only
parallax

Stitching images together to make a mosaic

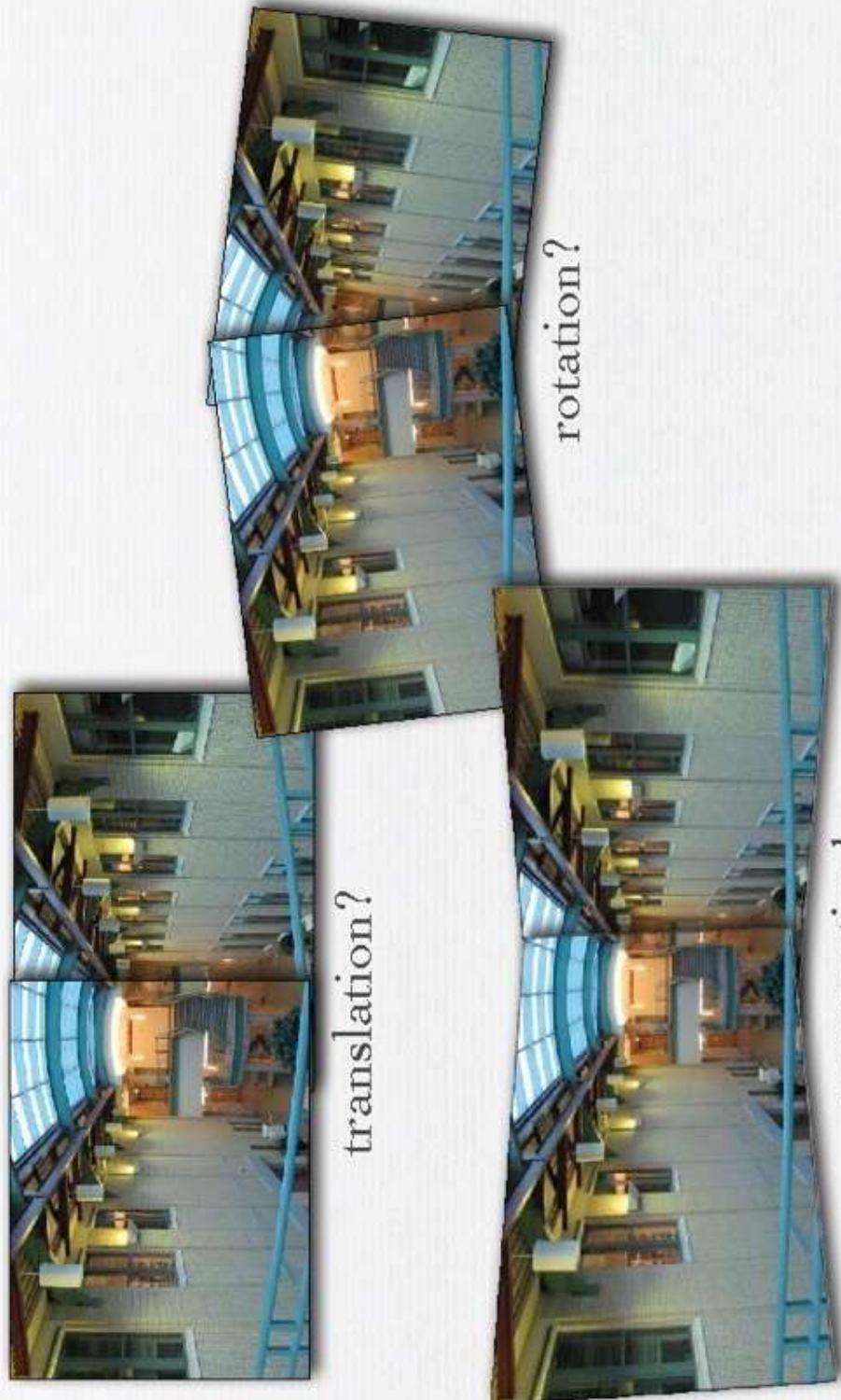


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© Marc Levoy

Slides from Marc Levoy
Panoramas

What kind of transformation do we need?



© Marc Levoy

perspective!

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Slides from Marc Levoy

Panoramas

Stitching images together to make a mosaic



- ♦ step 1: find corresponding features in a pair of image
- ♦ step 2: compute perspective from 2nd to 1st image
- ♦ step 3: warp 2nd image so it overlays 1st image
- ♦ step 4: blend images where they overlap one another
- ♦ repeat for 3rd image and mosaic of first two, etc.

Example: the Matterhorn



common
picture
plane of
mosaic
image

© Marc Levoy

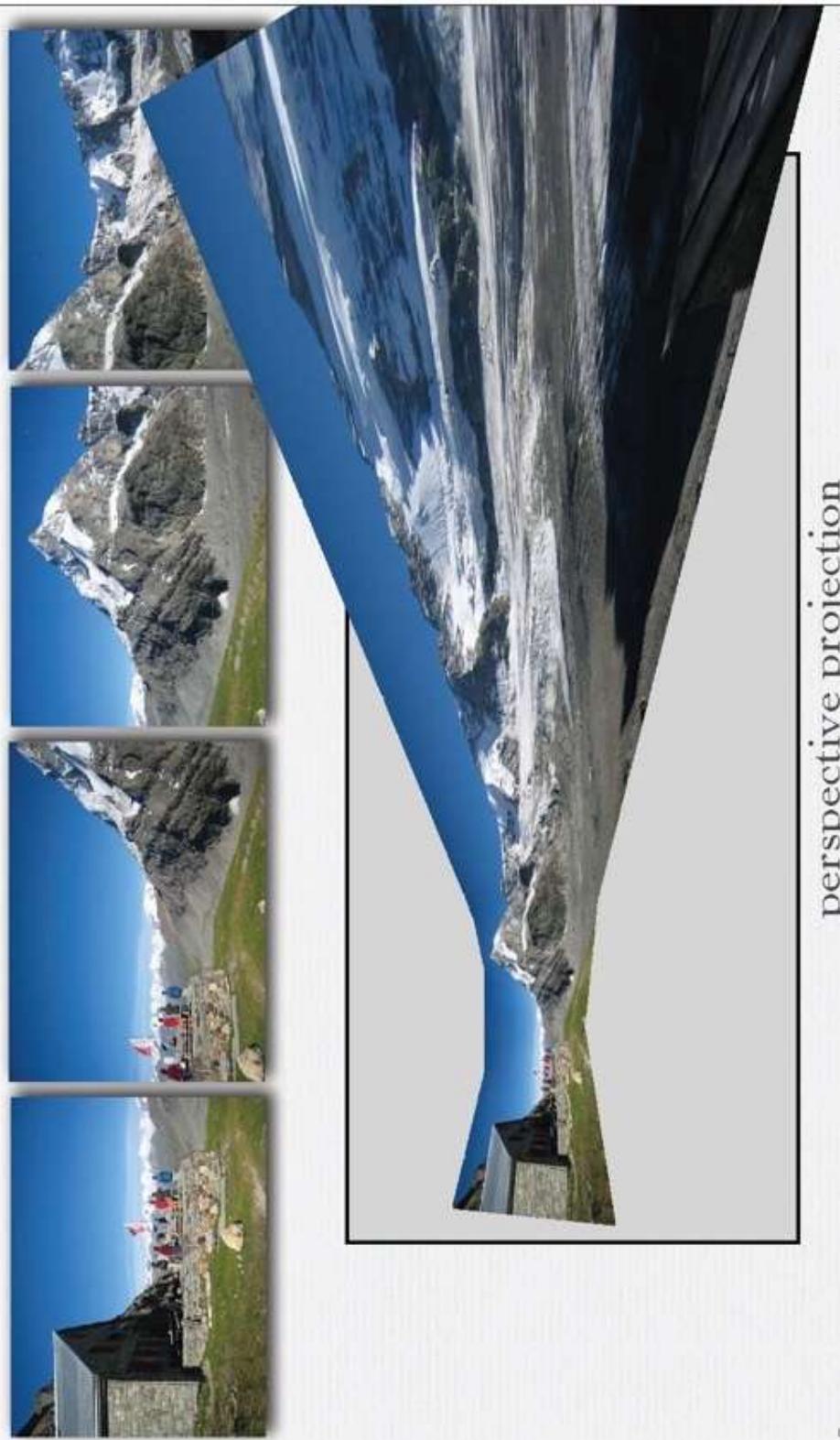
perspective projection

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Slides from Marc Levoy

Panoramas

Using 4 shots instead of 3



27

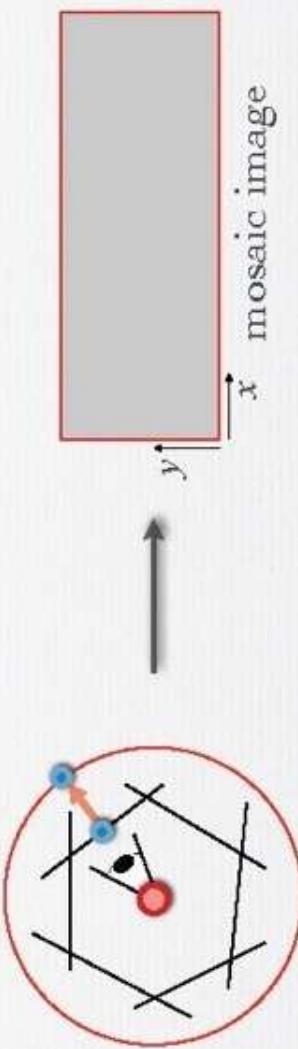
Slides from Marc Levoy

Panoramas

© Marc Levoy

Cylindrical panoramas

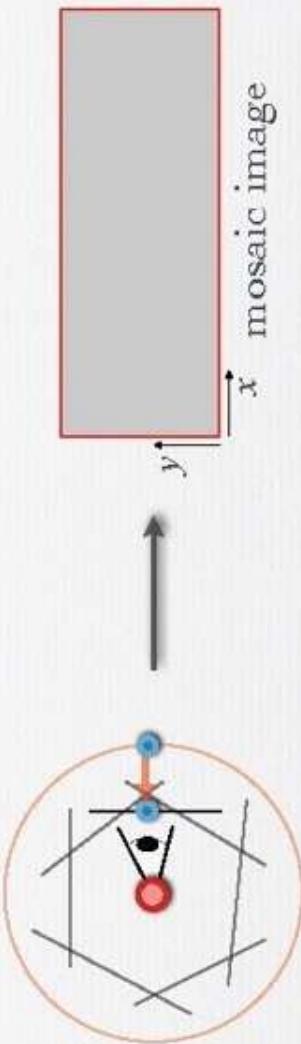
- ♦ even works for 360° panorama



- ♦ project each image onto a cylinder
- ♦ a cylindrical image can be stored as a rectangular image

Cylindrical panoramas

- ♦ even works for 360° panorama



- ♦ project each image onto a cylinder
- ♦ a cylindrical image can be stored as a rectangular image
- ♦ to view without distortion, reproject part of the cylinder onto a picture plane representing the display screen
 - if your FOV is narrow, this view won't be too distorted

(FLASH DEMO)

<http://graphics.stanford.edu/source/se173/applets/projections.html>

Back to the Matterhorn



30

cylindrical projection

© Marc Levoy

Slides from Marc Levoy

Panoramas

Back to the Matterhorn



surface of
cylinder

© Marc Levoy

31

Slides from Marc Levoy

Panoramas

Spherical panoramas



- ◆ projections are to a sphere instead of a cylinder
- ◆ can't store as rectangular image without extreme stretching

© Marc Levoy

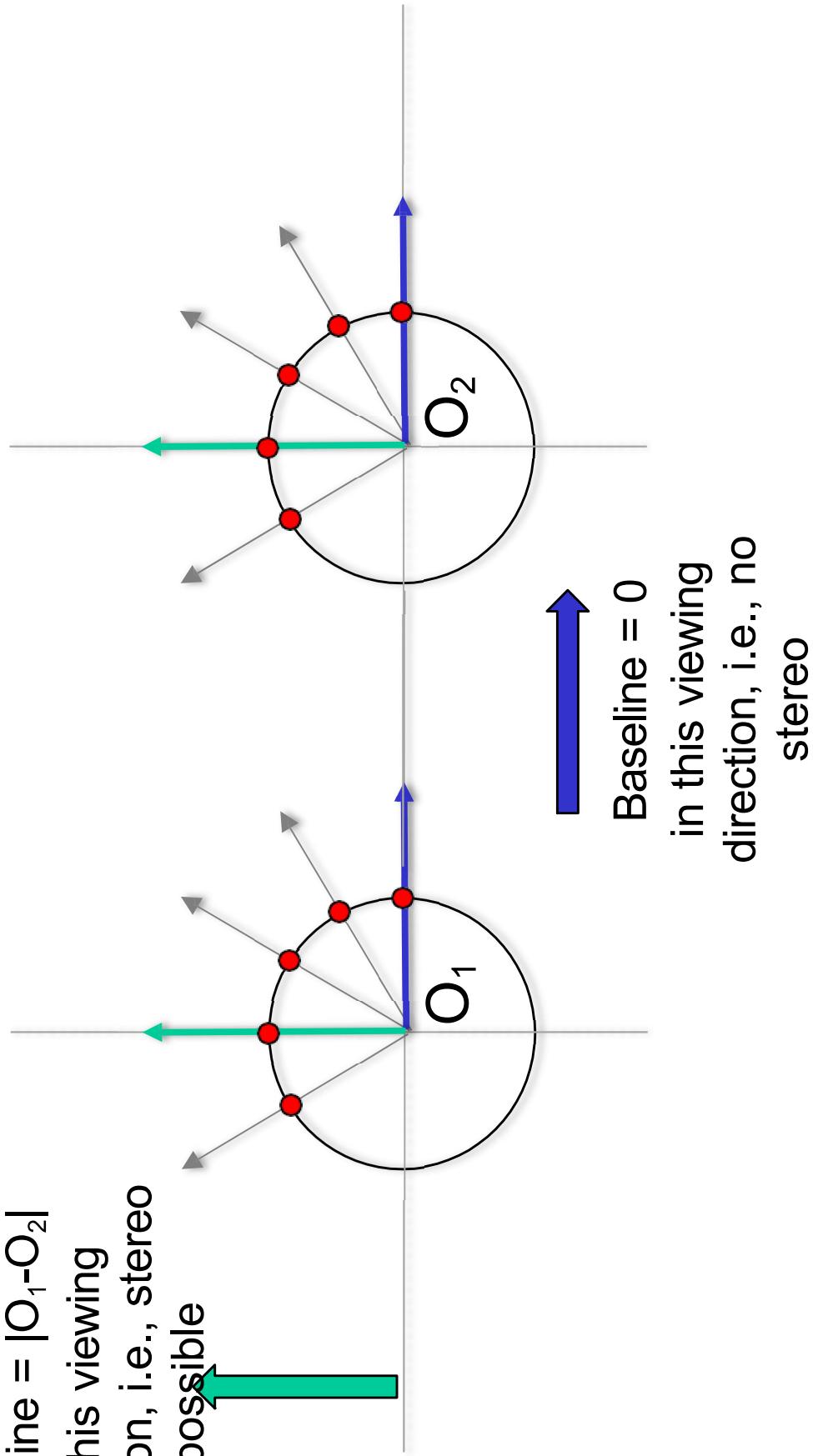
34

Slides from Marc Levoy

Panoramas

A Pair of Mono Panoramas

Baseline = $|O_1 - O_2|$
in this viewing
direction, i.e., stereo
possible



Head Rotation

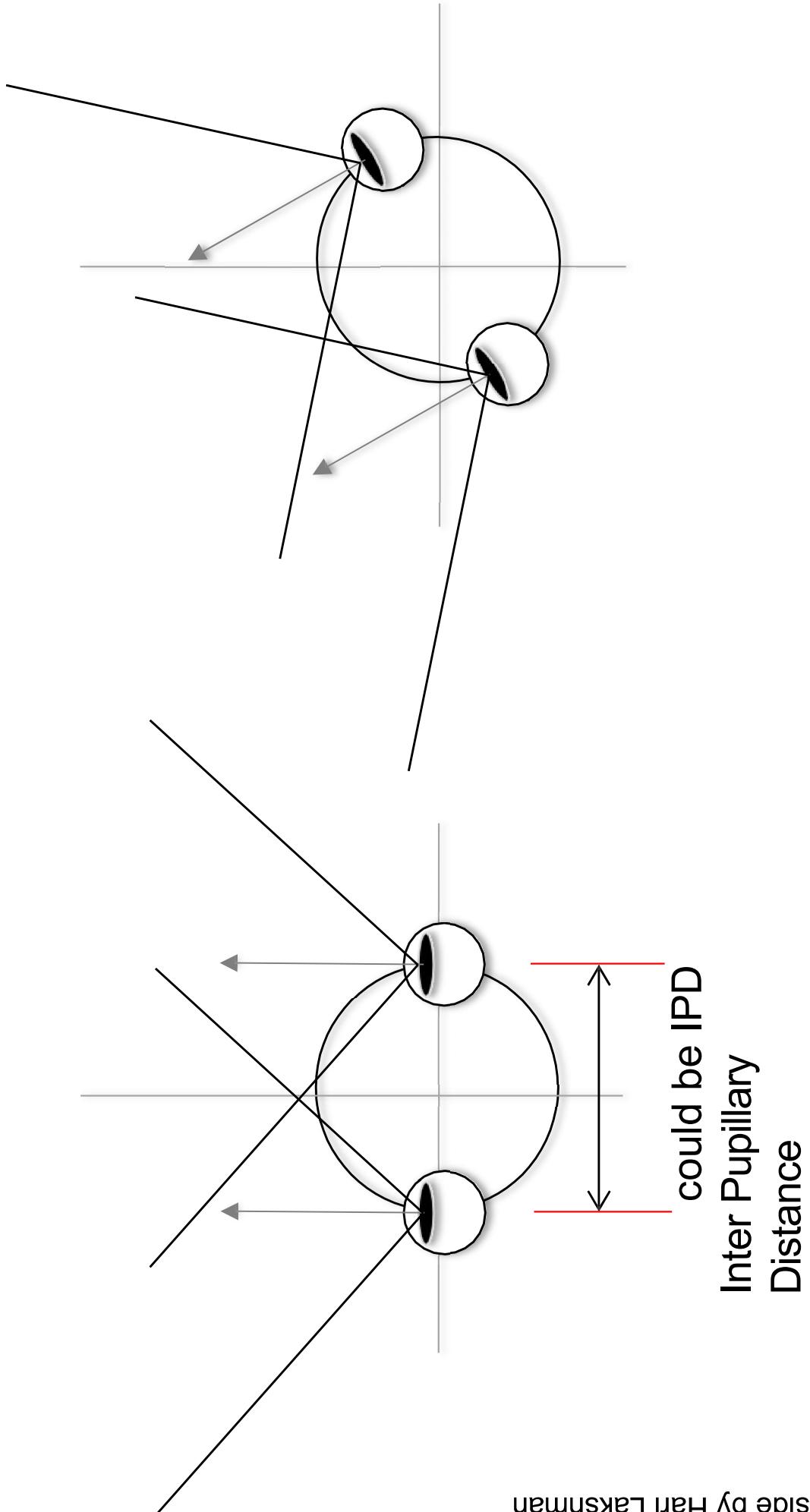
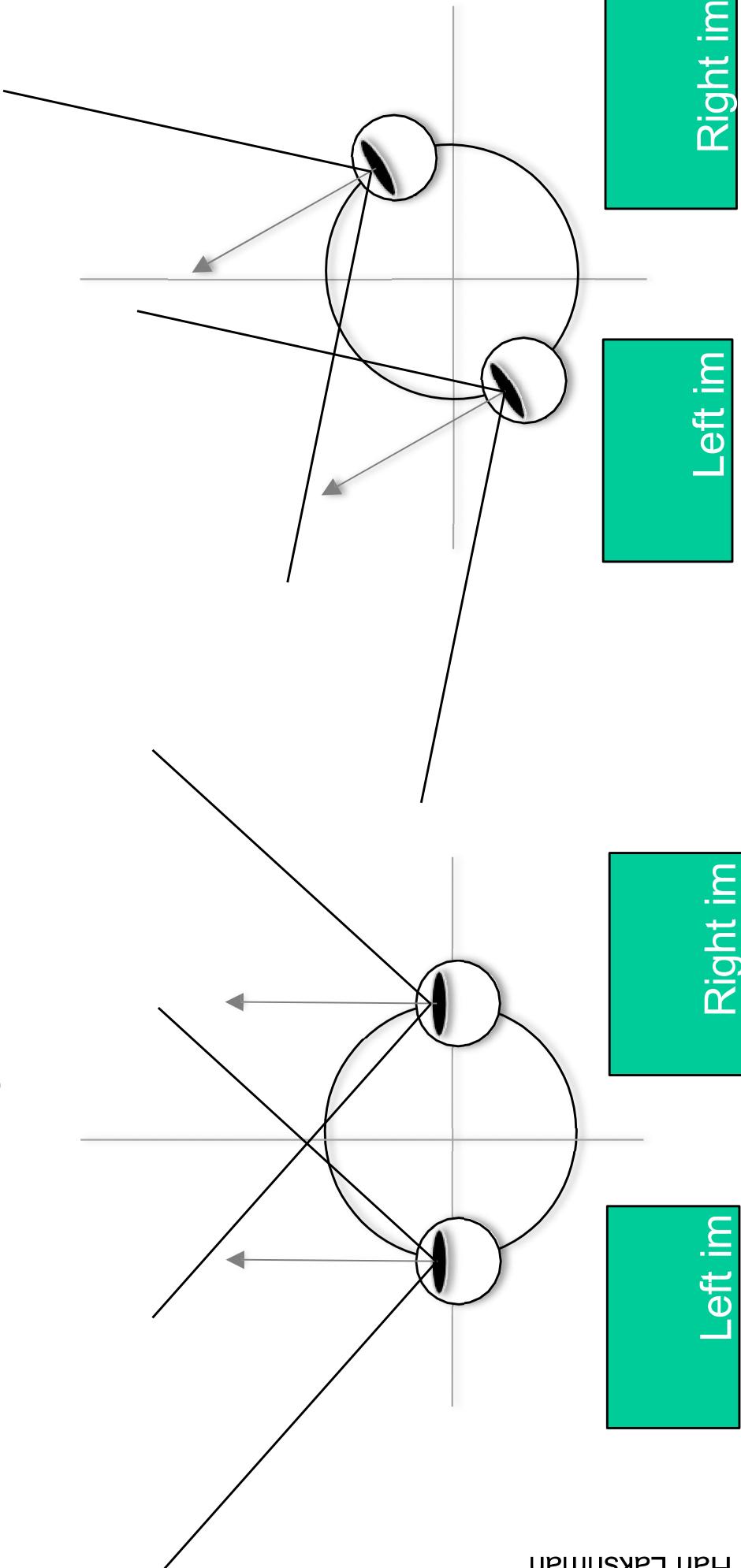


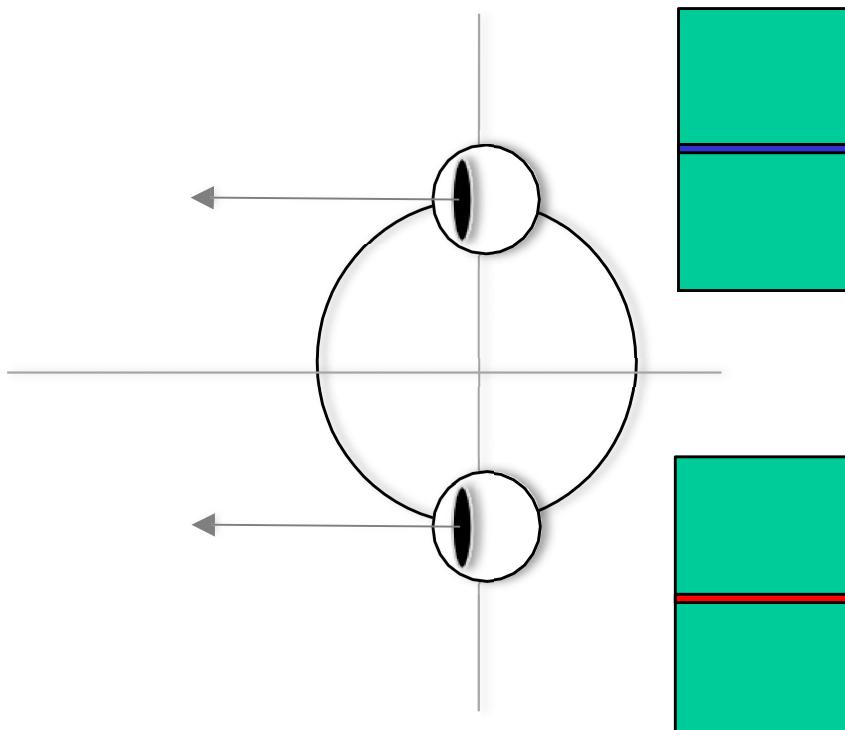
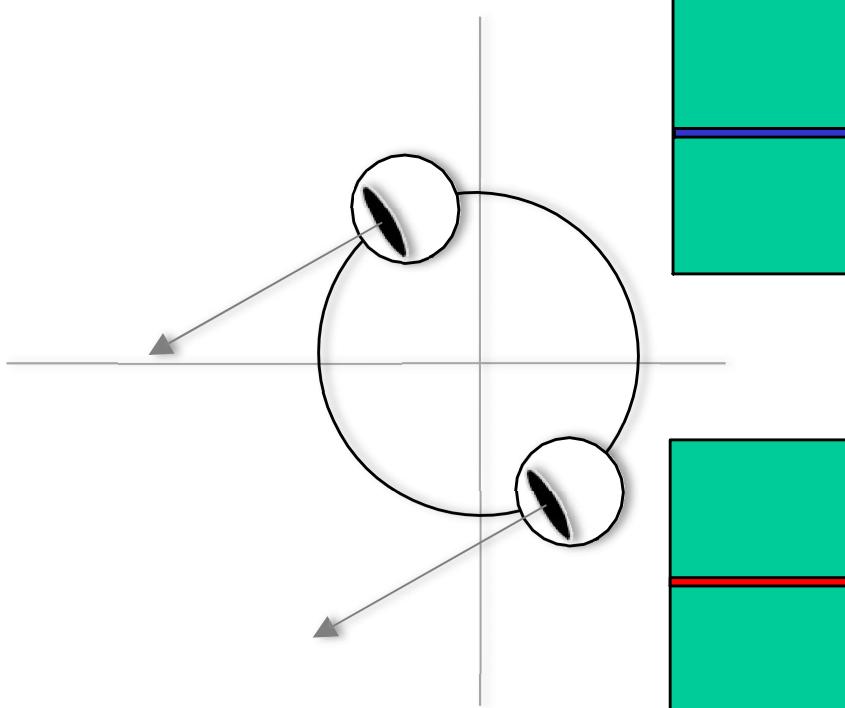
Image Pair for Each Direction



Store image pair for each direction \bowtie Problem: Too much data

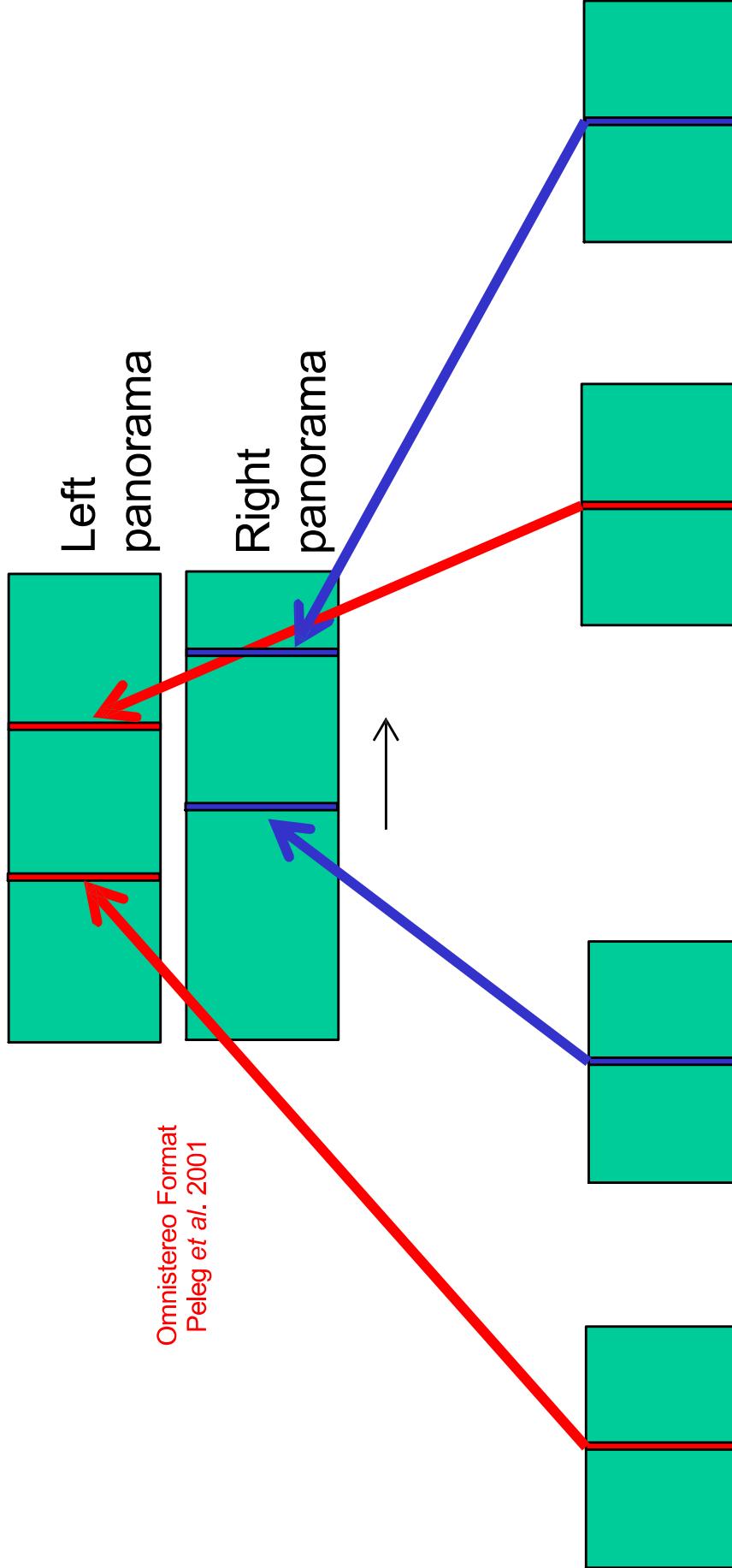
Approximation: Store only Middle Ray

Omnistereo Format
Peleg *et al.* 2001

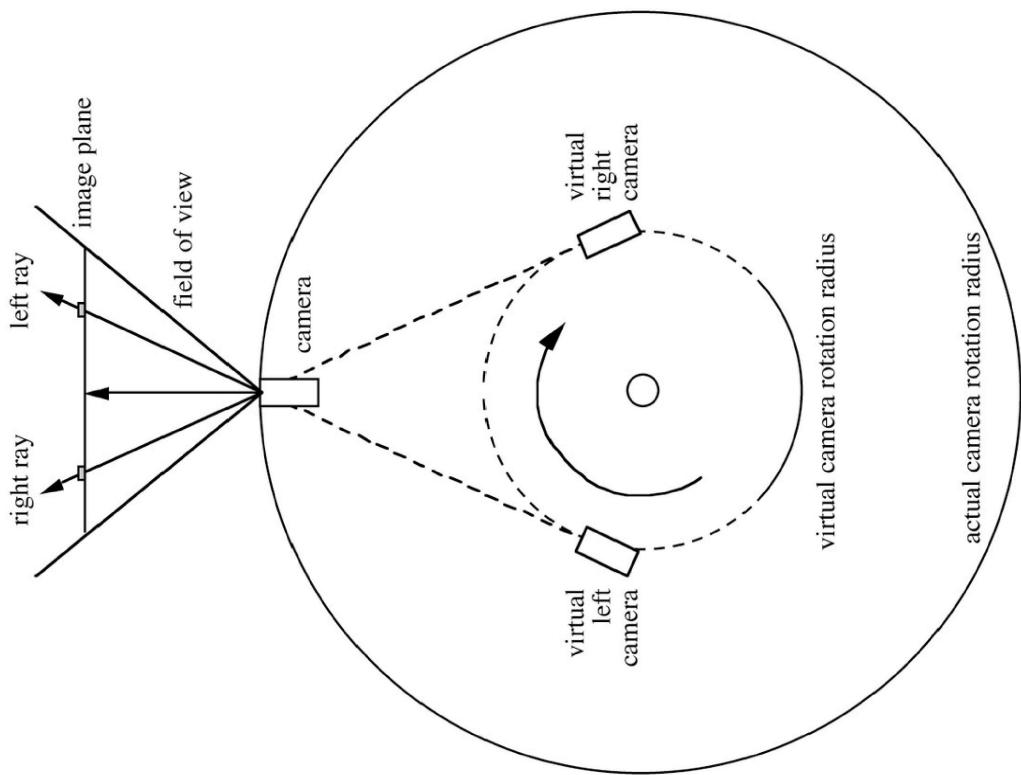


Approximation: store only middle ray for L and R eyes for each direction

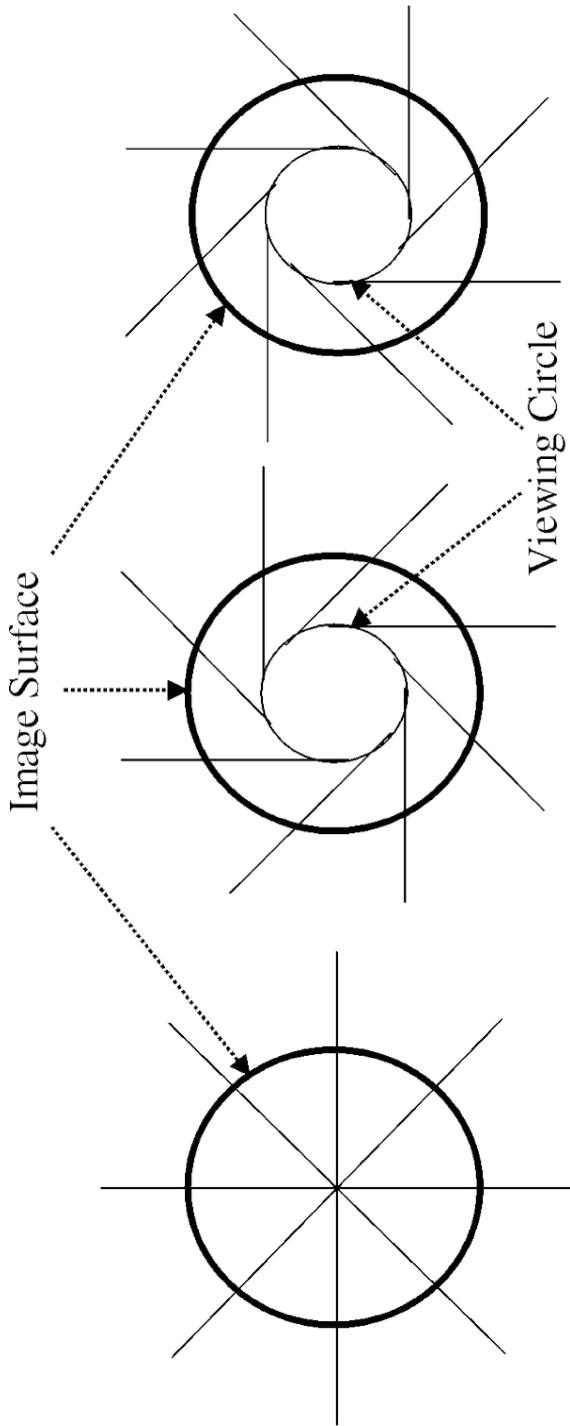
Omnistereo Panoramas



Capture using Single Camera



Comparison: Mono and Stereo Panoramas



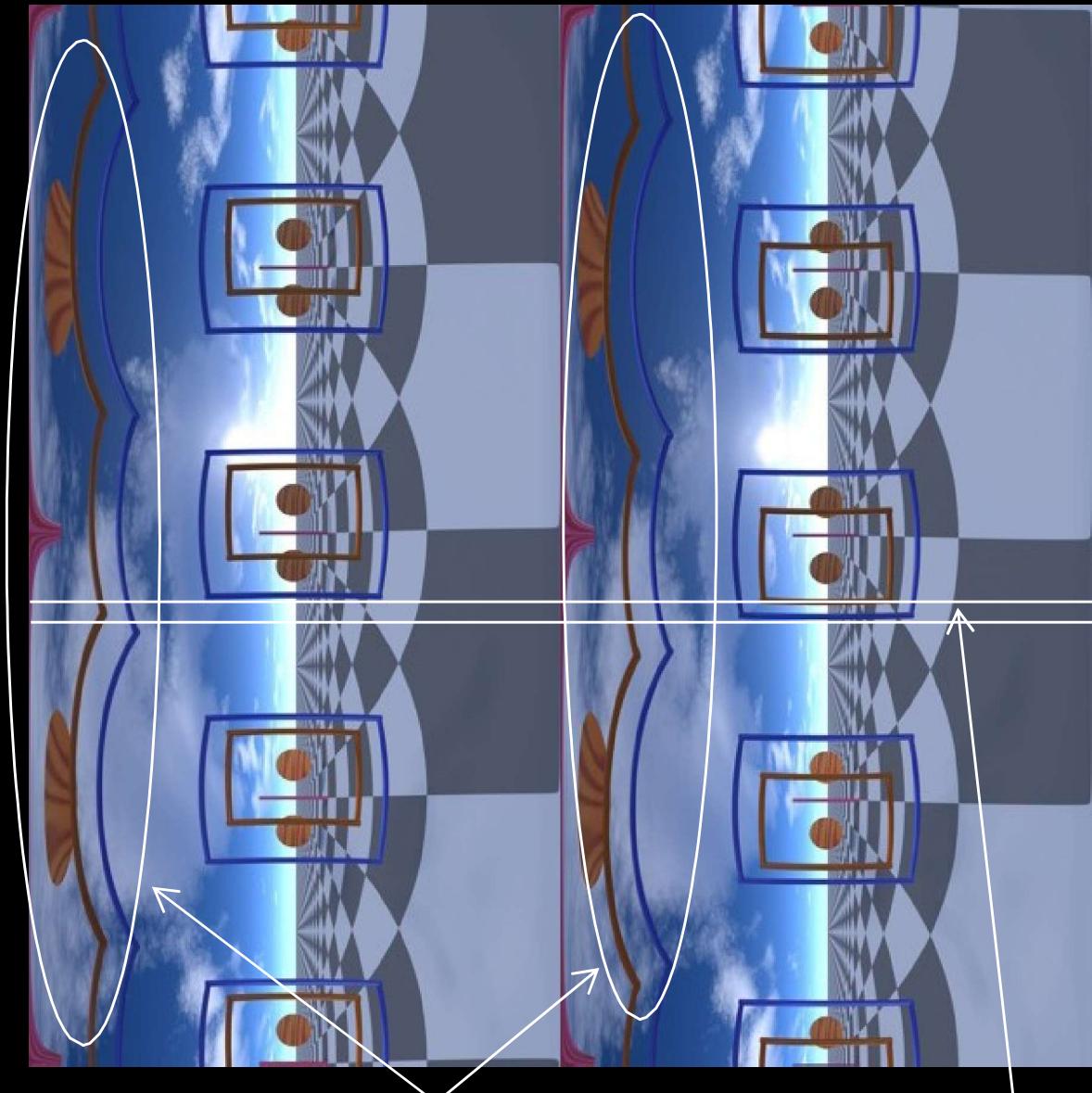
Central,
a.k.a. Mono

Omnistereo,
Multiperspective

Omnistereo
example

Left panorama

Right panorama



Sphere-to-plane
distortions

Disparity

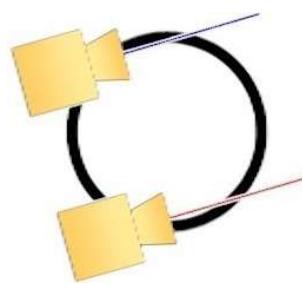
Multiperspective Projection



Omnidirectional Stereo



widely used by YouTube VR, Google Daydream, Facebook, ...



Existing VR Cameras

Recorded Videos ~ 17 Gb/sec



Facebook's Surround 360



RAW Data: 17 Gb/sec

Compute time: days to weeks on conventional computer,
minutes to hours on data center

Facebook's Surround 360



RAW Data: 17 Gb/sec

Compute time: days to weeks on conventional computer,
minutes to hours on data center

Biggest Problem of Panorama – 6DoF Viewing



(b)

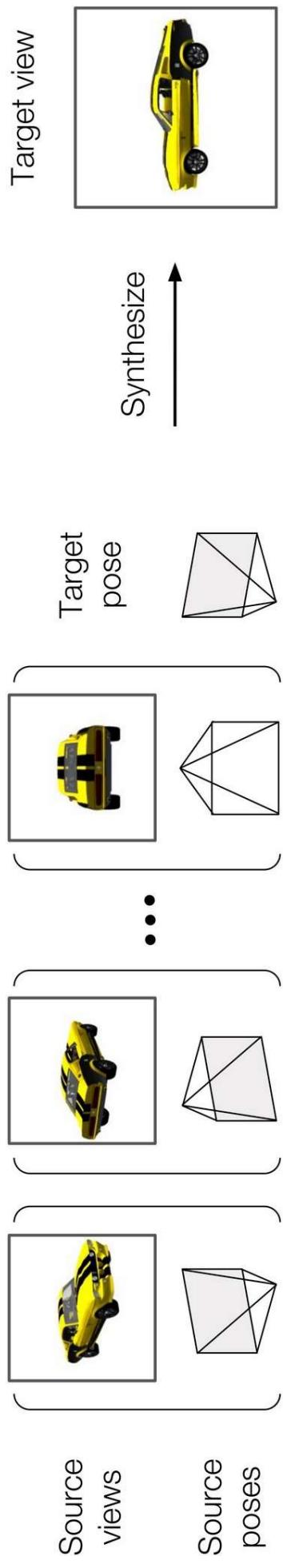


(a)



Problem: Novel View Synthesis

- ❖ The process of using images of a scene and their camera poses to synthesize new images of the scene at arbitrary camera poses.



- ❖ Subset of *Neural Rendering*, “deep image or video generation approaches that enable explicit or implicit control of scene properties”. (Ayush Tewari et. al.)
 - ❖ E.g. illumination, camera parameters, pose, geometry, appearance, and semantic structure

Image: “Multi-view to Novel View: Synthesizing Novel Views with Self-Learned Confidence” (Sun et al., 2018)

Applications in VR



Real-time rendering

Nex: Real-time View Synthesis with Neural Basis Expansion

Related Work

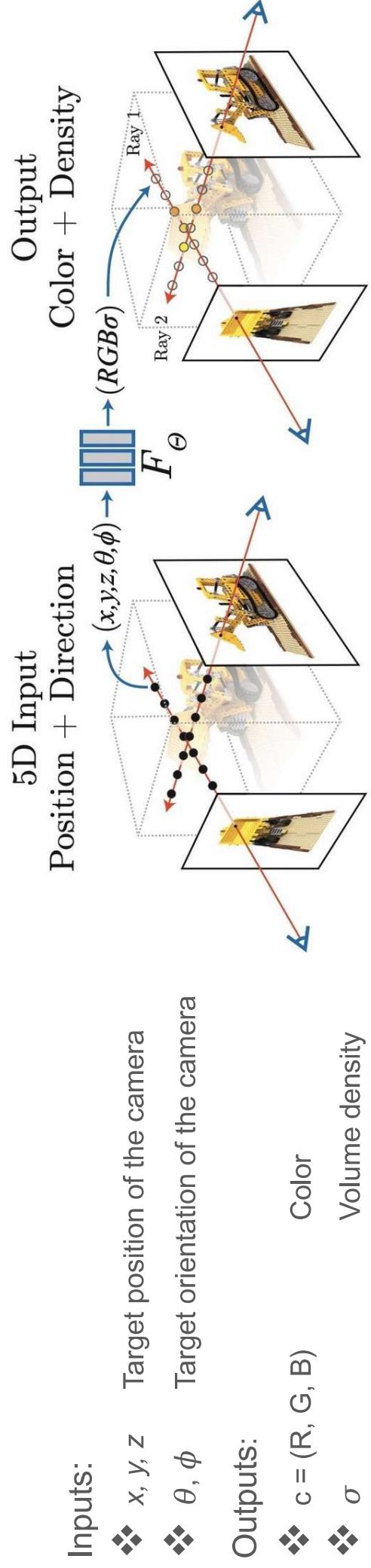
- ❖ Neural Volumes (NV), 2019
 - ❖ Deep 3D convolutional network architecture
 - ❖ Predicts a fixed-size discretized voxel grid
 - ❖ Limitation: discrete voxel grids do not scale well and lose fine detail at high resolutions
 - ❖ Limitation: requires a bounded volume and knowledge of the background
- ❖ Scene Representation Networks (SRN), 2019
 - ❖ Uses a recurrent neural network to model a rendering function
 - ❖ Limited to simple shapes with low geometric complexity
- ❖ Local Light Field Fusion (LLFF), 2019
 - ❖ 3D convolutional network architecture
 - ❖ Predicts multiplane images and fuses them to create new views
 - ❖ Fast to train (<10 minutes) at the cost of large storage requirements (~GB for each scene)

NeRF: Key Insights

- ❖ Represent static scenes in a **continuous space**.
- ❖ Encode a continuous radiance field **within the parameters** of a fully-connected neural network.
- ❖ Regress directly from viewing location and direction to color and **transparency**

Problem Setting

- ❖ Given a dataset containing RGB images of a static scene, their corresponding camera poses, and intrinsic parameters,
- ❖ Predict the color and volume density for every viewing location and direction



NeRF: Inspired by Volume Rendering



Vascular

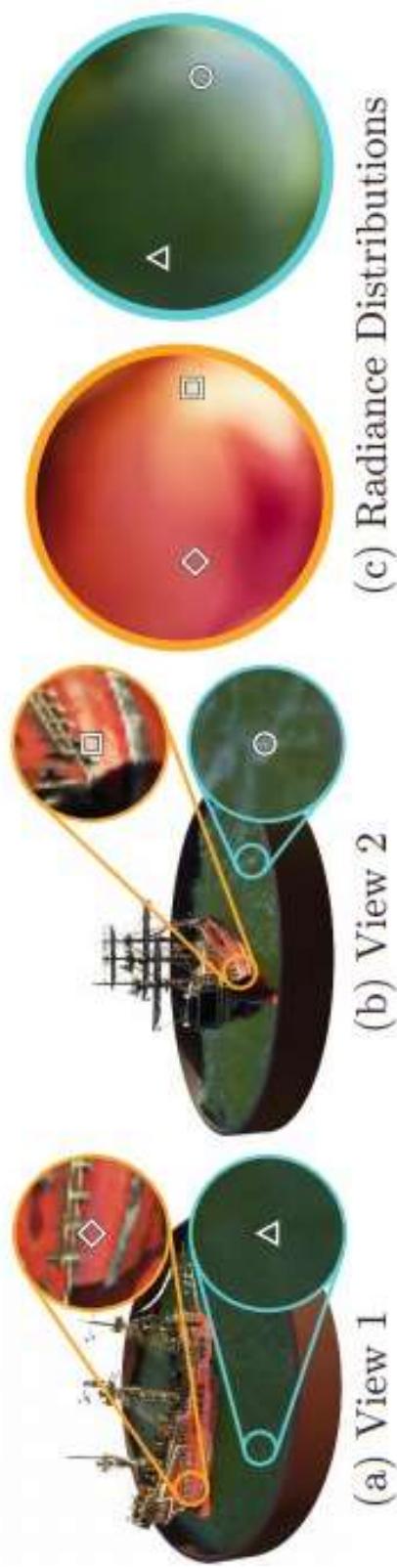
Osseous

Muscular

Cutaneous

Definition of radiance field

- Radiance field is a 5-dimensional function which maps a 3D location $\mathbf{x}, \mathbf{y}, \mathbf{z}$ and a direction \mathbf{d} to a color $(\mathbf{r}, \mathbf{g}, \mathbf{b})$:



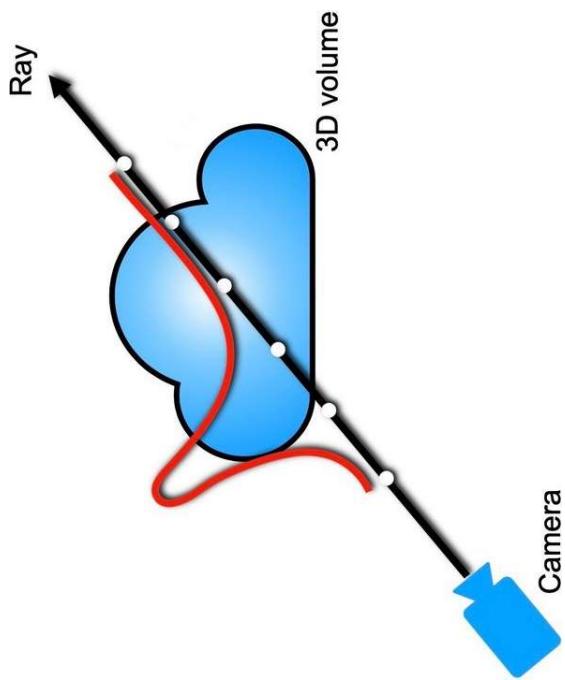
[8]
Mildenhall20

NeRF: Volume Rendering

- ❖ Generating a view from NeRF requires rendering all rays that pass through each pixel of the desired virtual camera
- $$C(\mathbf{r}) = \int_{t_n}^{t_f} T(t) \sigma(\mathbf{r}(t)) \mathbf{c}(\mathbf{r}(t), \mathbf{d}) dt,$$
 where $T(t) = \exp\left(-\int_{t_n}^t \sigma(\mathbf{r}(s)) ds\right)$
 - Expected color of a camera ray
 - Predicted Volume Density
 - Predicted Color
 - Probability that nothing has blocked the ray up to this point
- ❖ Numerically estimated using quadrature and stratified sampling
- $$\hat{C}(\mathbf{r}) = \sum_{i=1}^N T_i (1 - \exp(-\sigma_i \delta_i)) \mathbf{c}_i,$$
 where $T_i = \exp\left(-\sum_{j=1}^{i-1} \sigma_j \delta_j\right)$
 - The relative contribution of this segment
 - Predicted Color
 - Probability that nothing has blocked the ray up to this point
- ❖ Differentiable: allows optimization using gradient descent

NeRF: Hierarchical Sampling

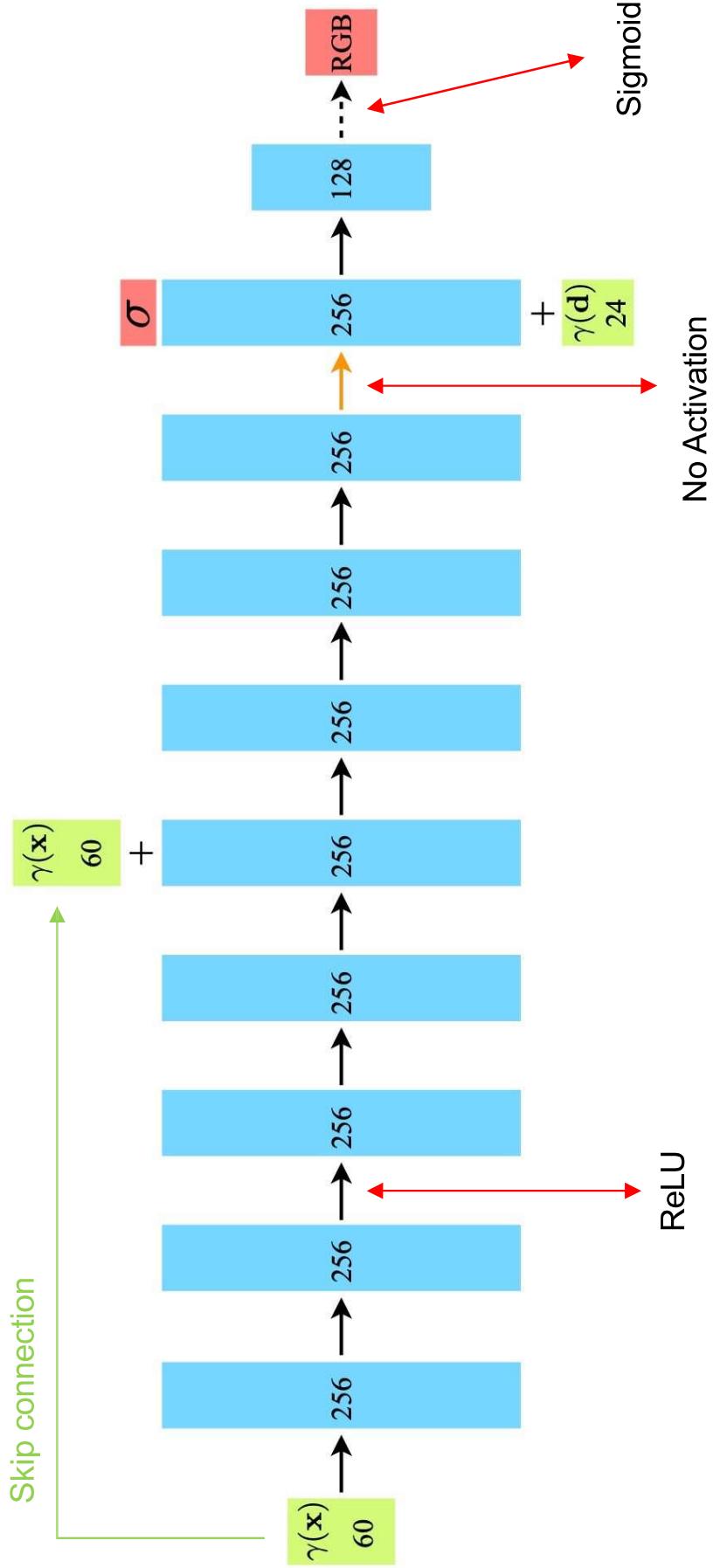
- ❖ Problem: It is inefficient to integrate over empty and occluded spaces in a scene
- ❖ Solution: Allocate samples proportionally to their expected effect on the final rendering.
- ❖ Evaluate a “coarse” network on a set of N_c locations along a ray to produce a PDF along the ray
- ❖ Evaluate a “fine” network on N_c and a second a set of N_f locations sampled from the PDF



NeRF: Positional Encoding

- ❖ Map individual components of position and direction vectors to a higher dimensional space
- $$\gamma(p) = (\sin(2^0 \pi p), \cos(2^0 \pi p), \dots, \sin(2^{L-1} \pi p), \cos(2^{L-1} \pi p))$$
- ❖ Similar concept as positional encoding in Transformer Architectures
- ❖ Empirically improves the preservation of high-frequency geometry and texture
- ❖ Surprising result, explored further in a follow-up work by the same authors
 - ❖ “Fourier Features Let Networks Learn High Frequency Functions in Low Dimensional Domains” (Tancik, Srinivasan, Mildenhall, et al., 2020)

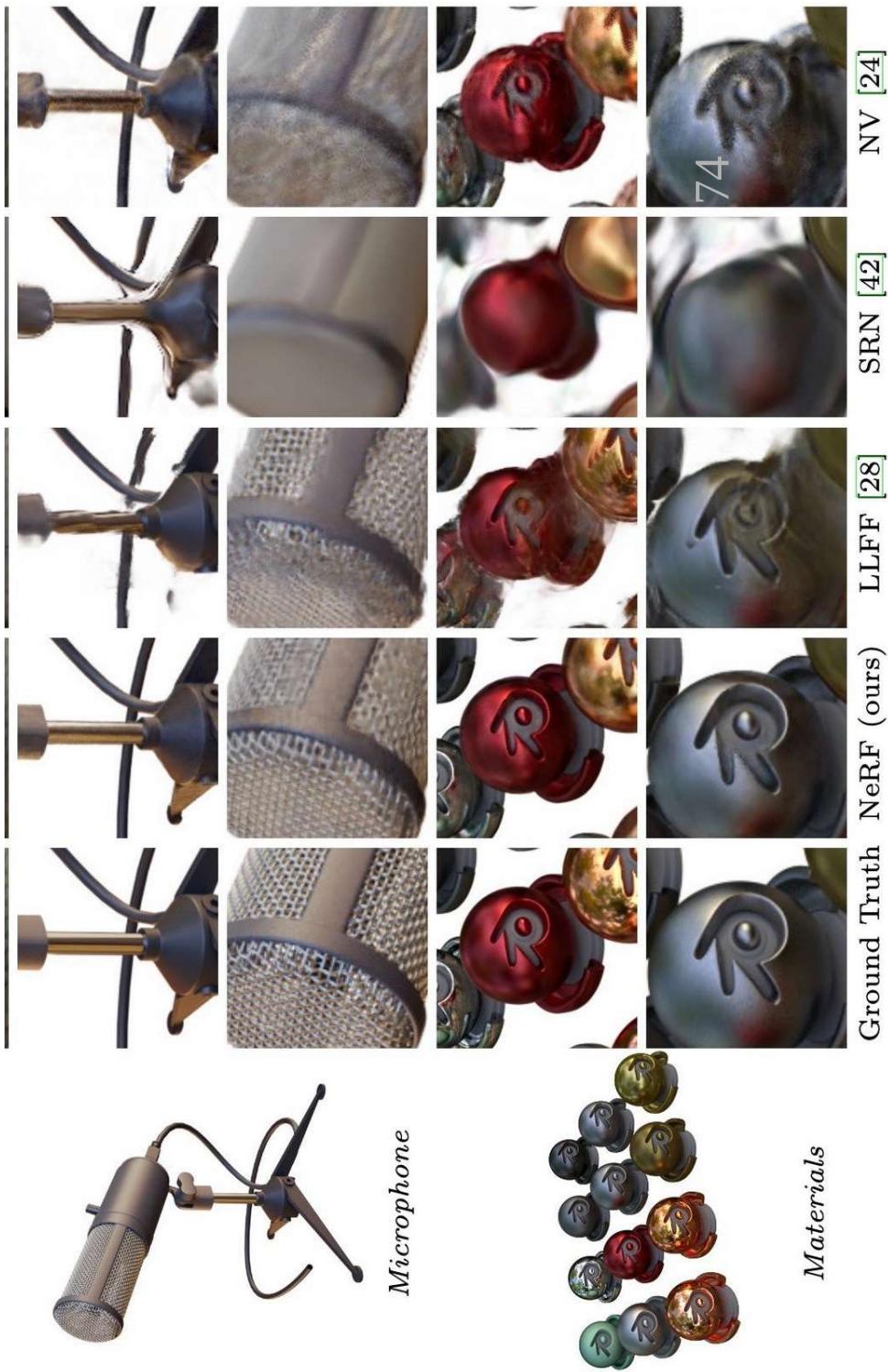
Network Architecture



Training Summary

- ❖ Sample a batch of camera rays from the dataset (bs=4096)
 - ❖ Use hierarchical sampling to query coarse and fine points
 - ❖ Use the volume rendering equation to calculate the color of the ray
 - ❖ Compute the squared error between rendered and true pixel colors
- $$\mathcal{L} = \sum_{\mathbf{r} \in \mathcal{R}} \left[\left\| \hat{C}_c(\mathbf{r}) - C(\mathbf{r}) \right\|_2^2 + \left\| \hat{C}_f(\mathbf{r}) - C(\mathbf{r}) \right\|_2^2 \right]$$
- ❖ Optimize network parameters using Adam

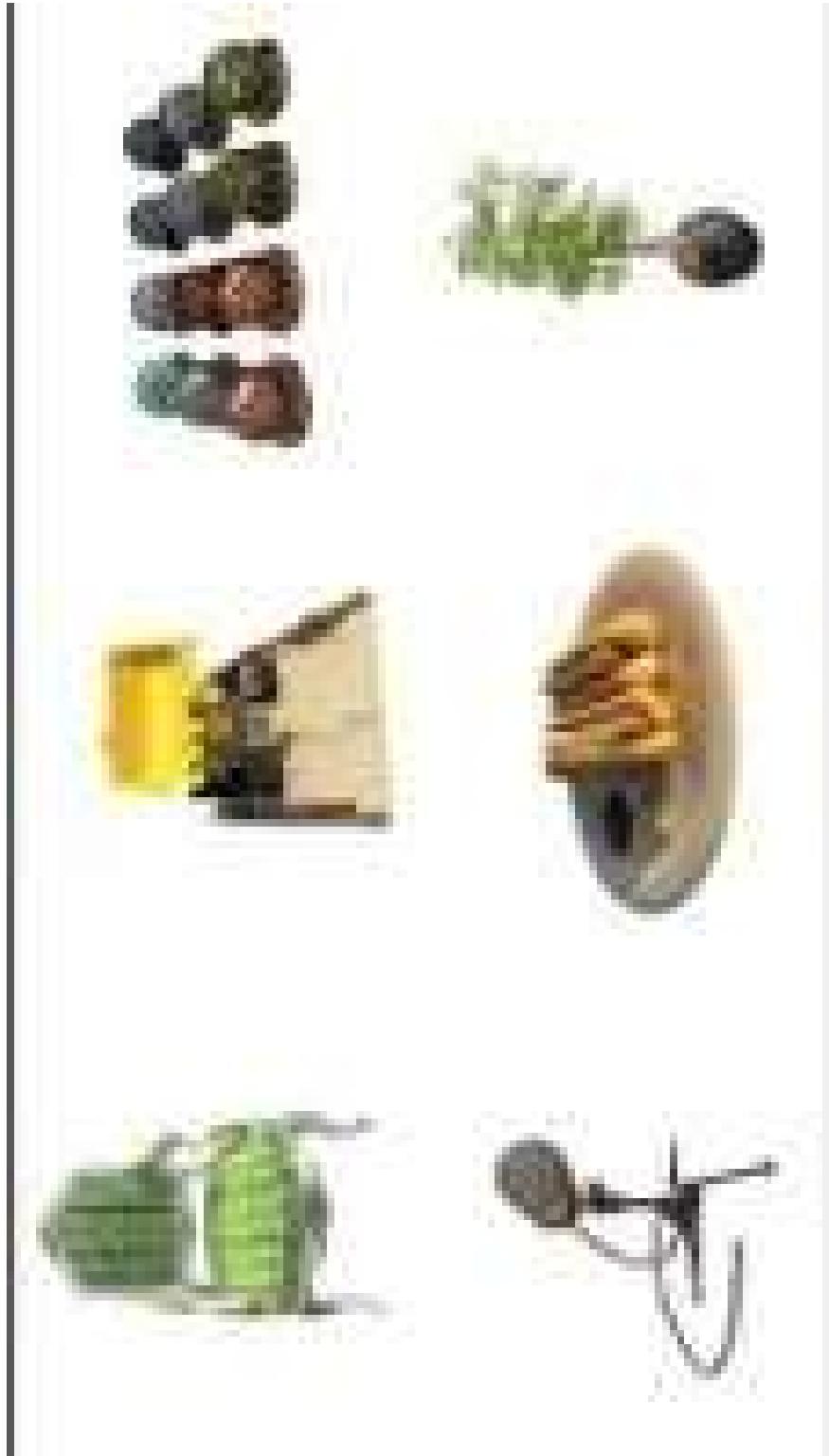
Qualitative Results: Realistic Synthetic Objects



Qualitative Results: Real-world scenes



Animated Results



Video: <https://www.matthewtancik.com/heif>

Instant Neural Graphics Primitives



<https://github.com/NVlabs/instant-ngp>

Limitations

- ❖ NeRF only works with static scenes
- ❖ A trained NeRF model does not generalize to more than one scene
- ❖ Computationally expensive: 1-2 days to train each individual scene on a modern GPU
- ❖ Inference is slow: each pixel in a synthesized image requires volume rendering

Summary

- ❖ Novel view synthesis generates images of scenes at previously unseen viewpoints.
- ❖ Prior works are limited to simple shapes and do not scale well to high-resolution images
- ❖ NeRF encodes a static scene within the parameters of a feedforward neural network.
- ❖ The authors show very impressive qualitative results and show state-of-the-art performance with quantitative metrics and different scene types.

D-NeRF: Neural Radiance Fields for Dynamic Scenes

| NERF | D-NeRF |
|---|---|
| - Only applicable to rigid scenes | + Applicable for rigid and non-rigid scenes |
| - 5D continuous function | + 6D continuous function by considering time-component as an additional input |
| - Requiring multiple views of a rigid scene | + Requiring a single view per time instant for non-rigid scenes. |



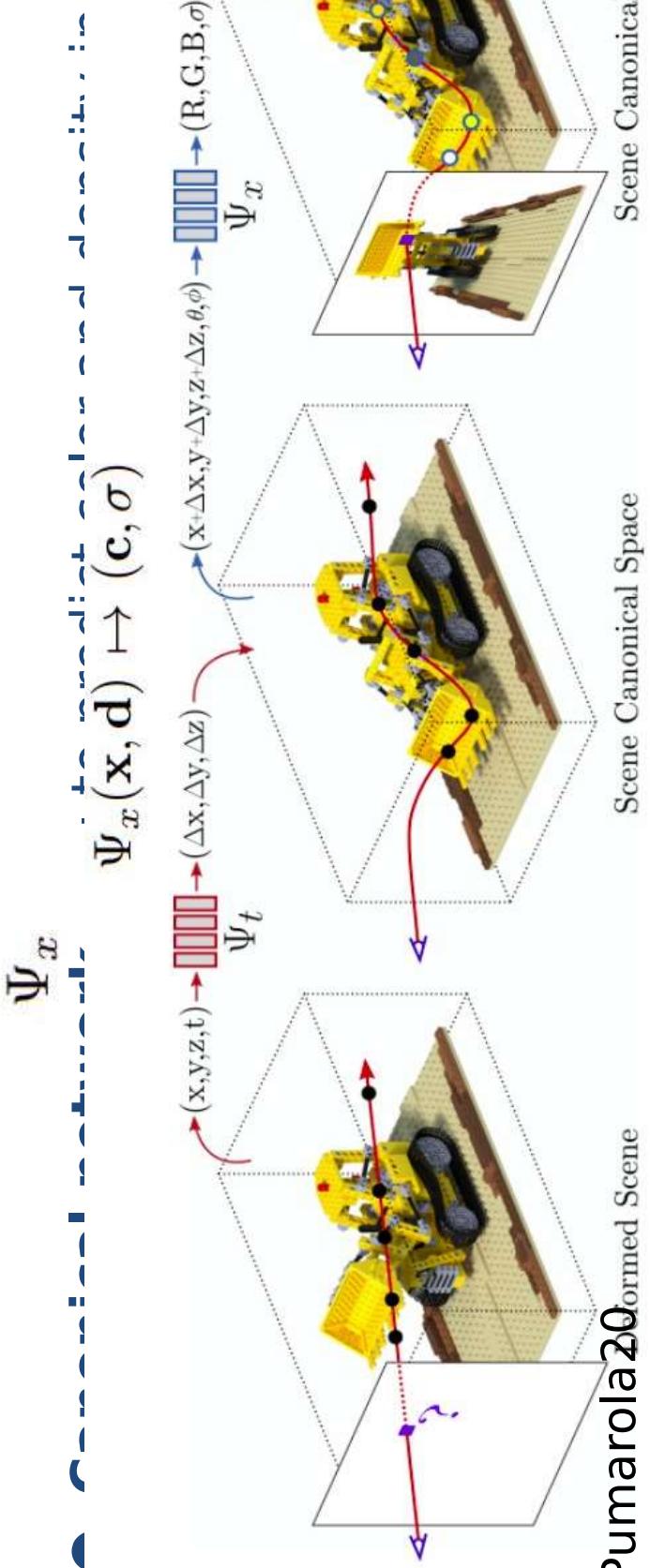
Michaël Ramamonjisoa, Van Nguyen Nguyen, Imagine Point of View & Time

[12] Pumarola20

D-Nerf: Neural Radiance Fields for

Dynamical Scenes Ψ_t : to predict deformation field between the scene at time instant t and the scene in canonical space (t=0)

$$\Psi_t(\mathbf{x}, t) = \begin{cases} \Delta \mathbf{x}, & \text{if } t \neq 0 \\ 0, & \text{if } t = 0 \end{cases}$$



[12] Pumarola et al. 2019

Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

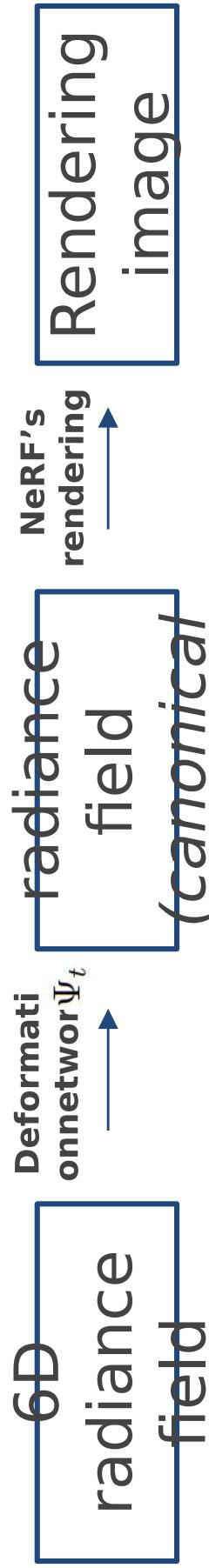
Scene Canonical Space

Scene Canonical Space

Scene Canonical Space

D-Nerf: Neural Radiance Fields for Dynamic Scenes

Volumetric rendering is the same as NeRF in **canonical space**:



Opacity colors

$$C(p, t) = \int_{h_n}^{h_f} \mathcal{T}(h, t) \sigma(\mathbf{p}(h, t)) \mathbf{c}(\mathbf{p}(h, t), \mathbf{d}) dh$$

where $\mathbf{p}(h, t) = \mathbf{x}(h) + \Psi_t(\mathbf{x}(h), t)$,

$$[\mathbf{c}(\mathbf{p}(h, t), \mathbf{d}), \sigma(\mathbf{p}(h, t))] = \Psi_x(\mathbf{p}(h, t), \mathbf{d}),$$
$$\text{and } \mathcal{T}(h, t) = \exp\left(-\int_{h_n}^h \sigma(\mathbf{p}(s, t)) ds\right).$$

[12] Pumarola20
Volume density

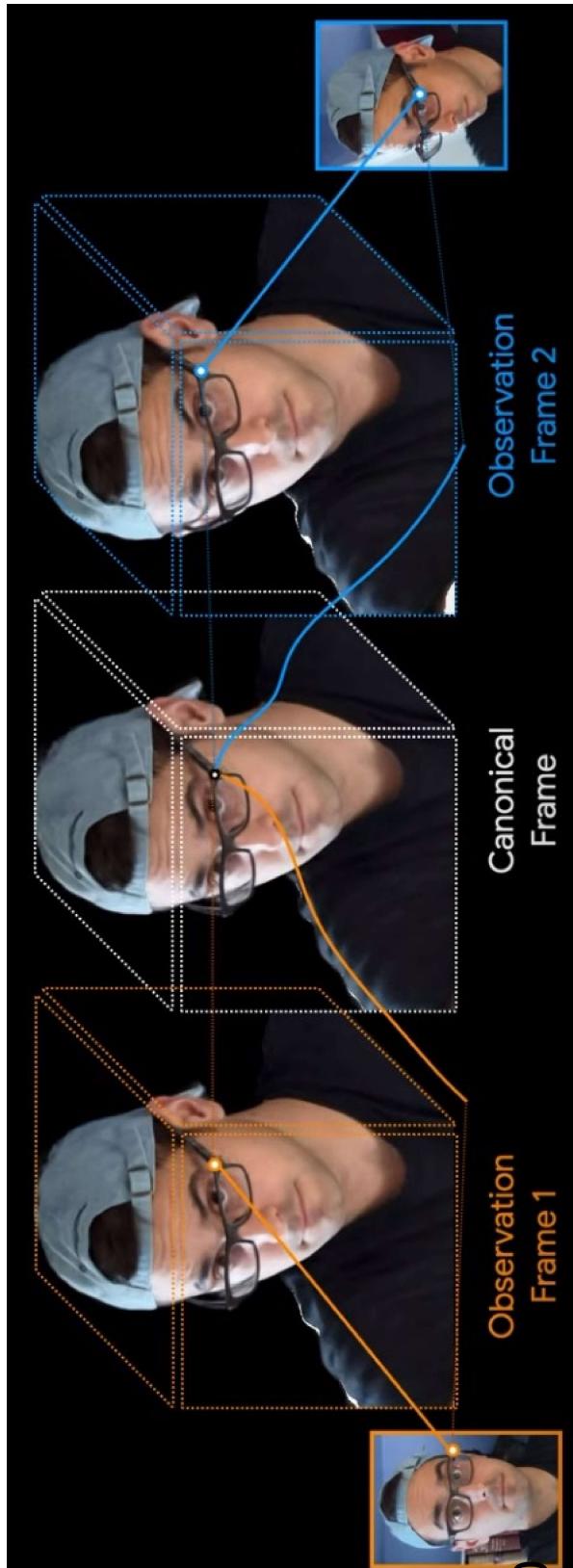
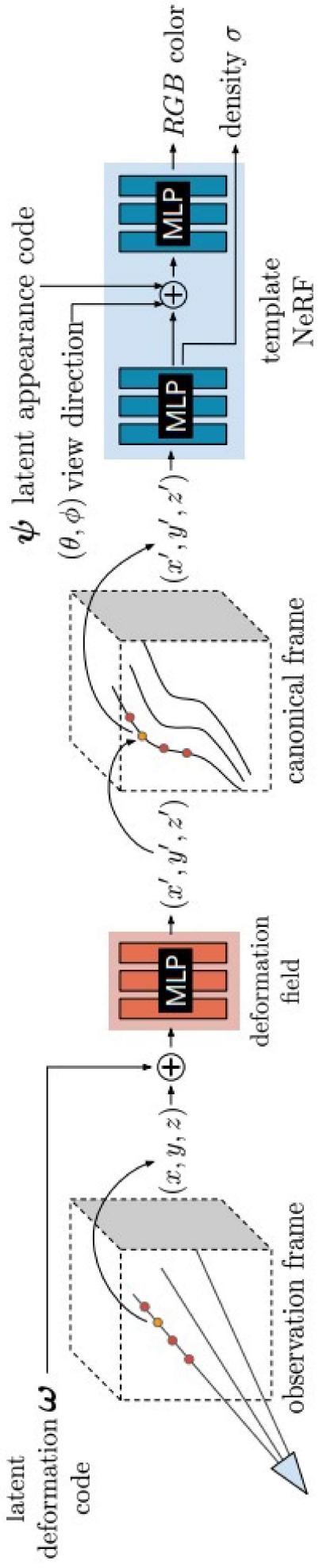
D-NeRF: Neural Radiance Fields for Dynamic Scenes



[12] Pumarola20

Michaël Ramamonjisoa, Van Nguyen Nguyen, Imagine -

Deformable Neural Radiance Fields



Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

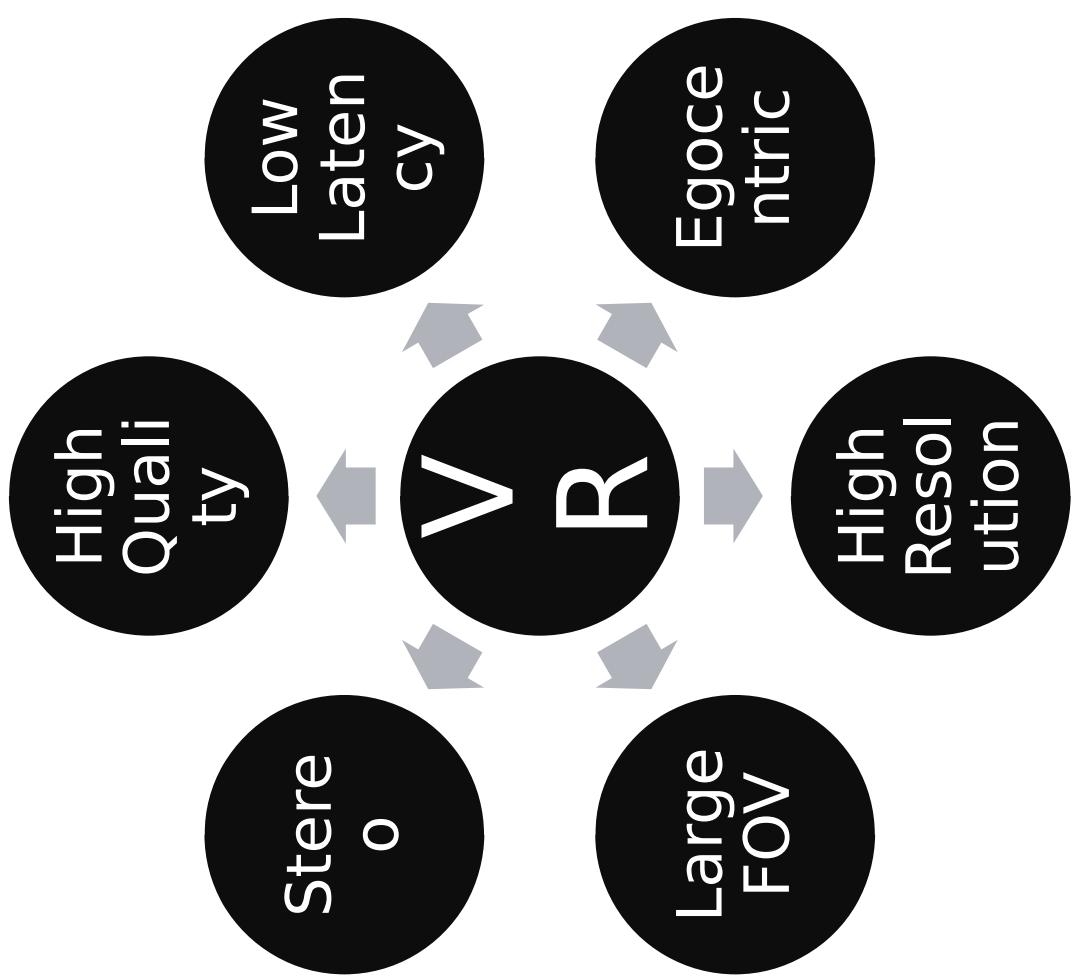
[13] Park20

Deformable Neural Radiance Fields



[13] Park20

Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

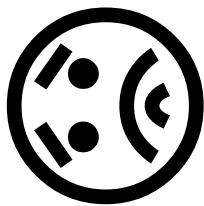


NeRF

x90 Speed

High Latency

Low Quality



VR

High Resolution

Stereo

Egocentric

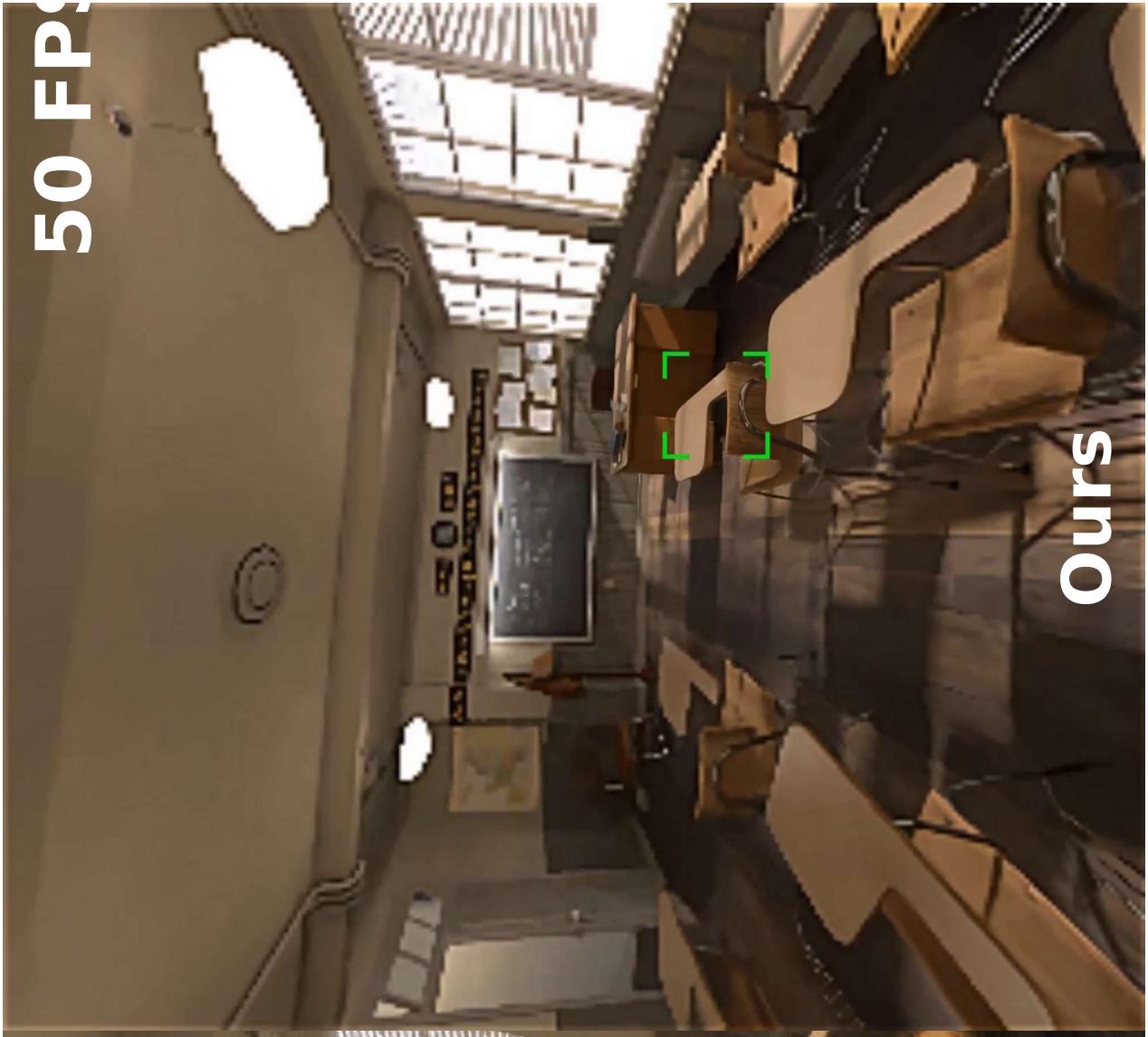


Gaze-Contingent Neural Rendering for VR



x90 Speed

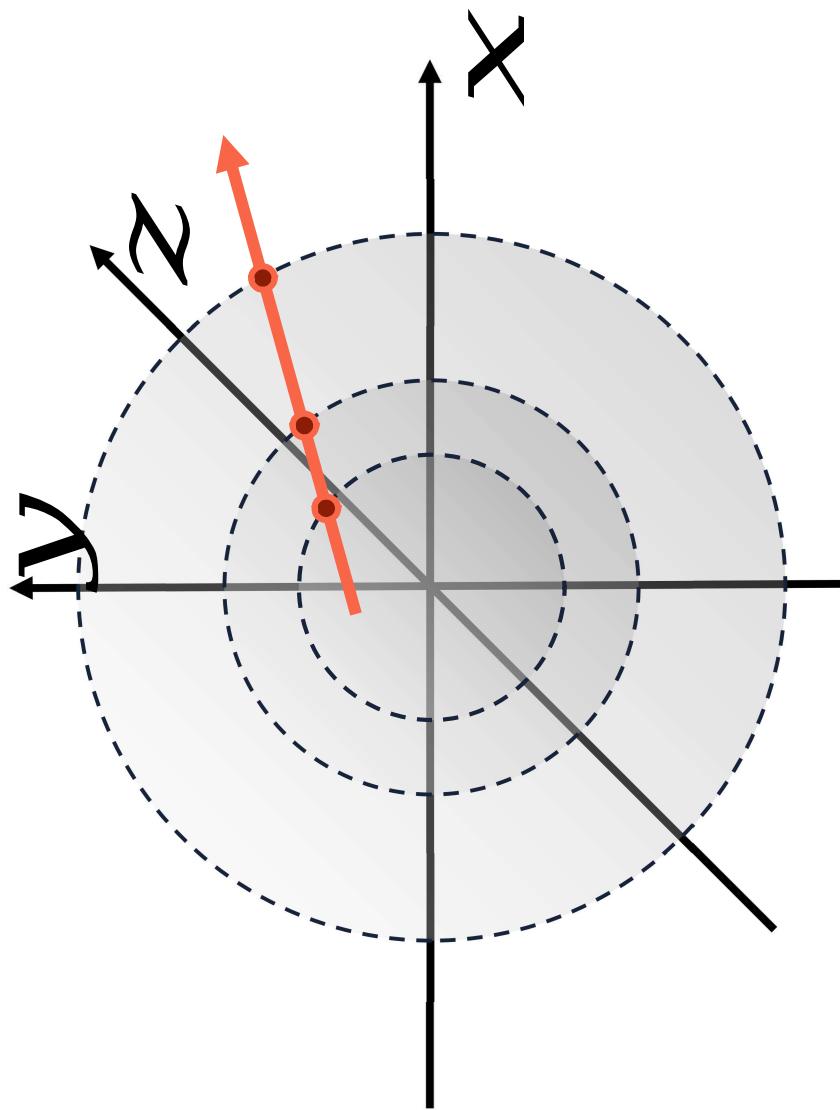
50 FPS



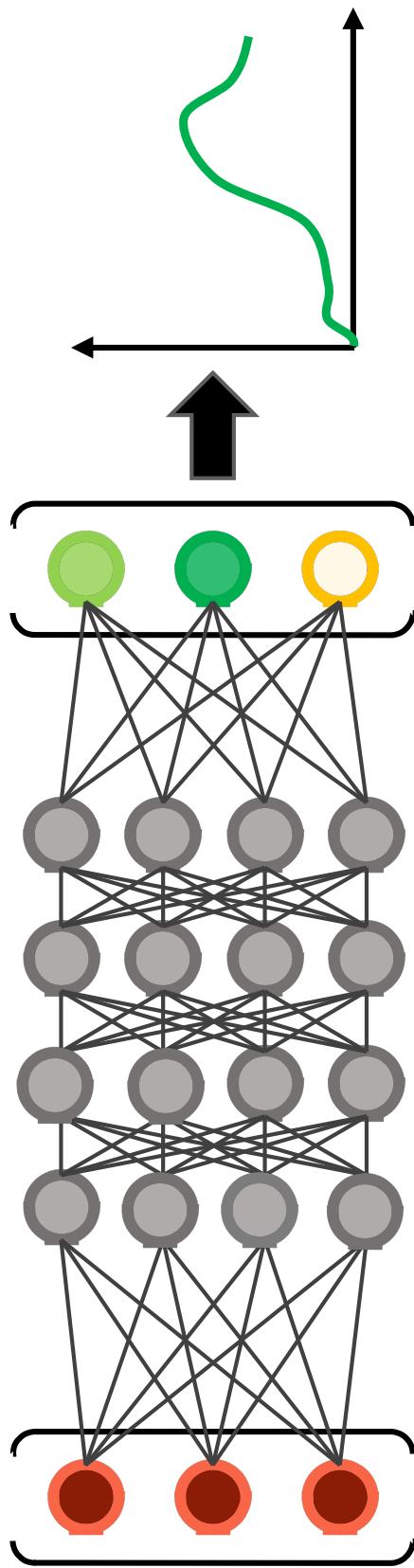
NeRF



#1 Egocentric Neural Representation



#1 Egocentric Neural Representation

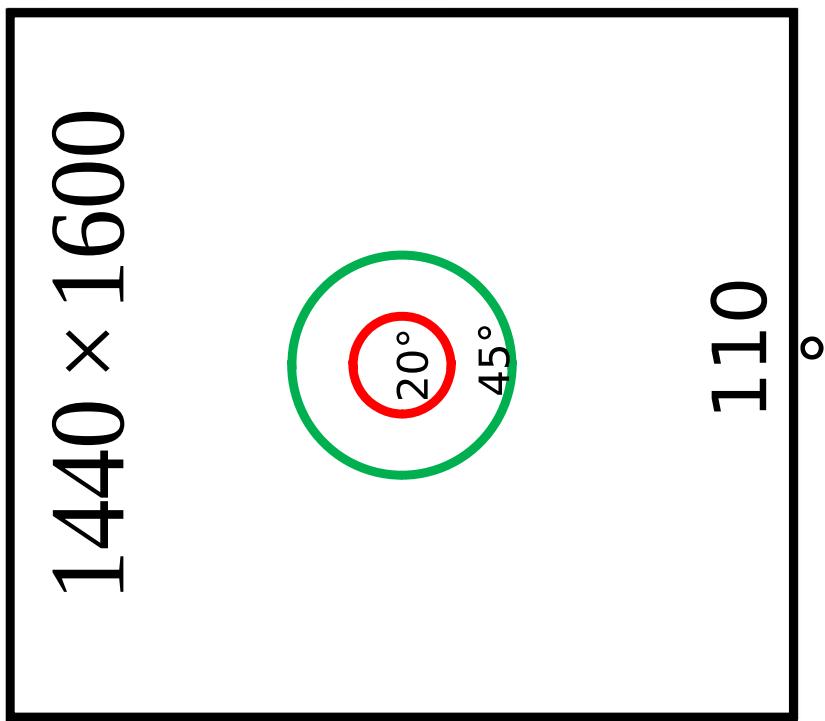


Higher quality
Faster

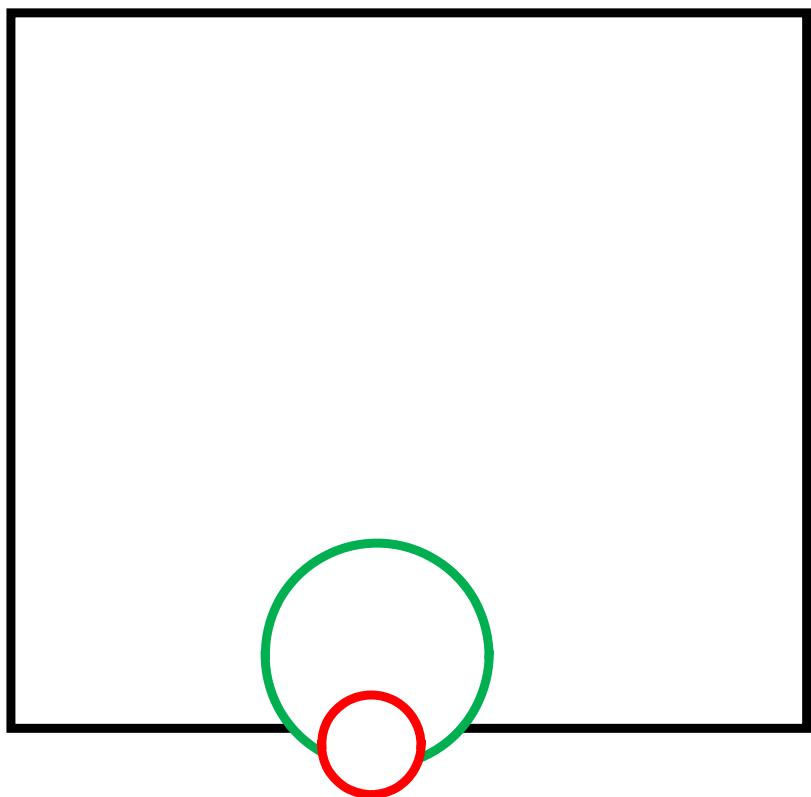
#2. Adaptive Visual Acuity



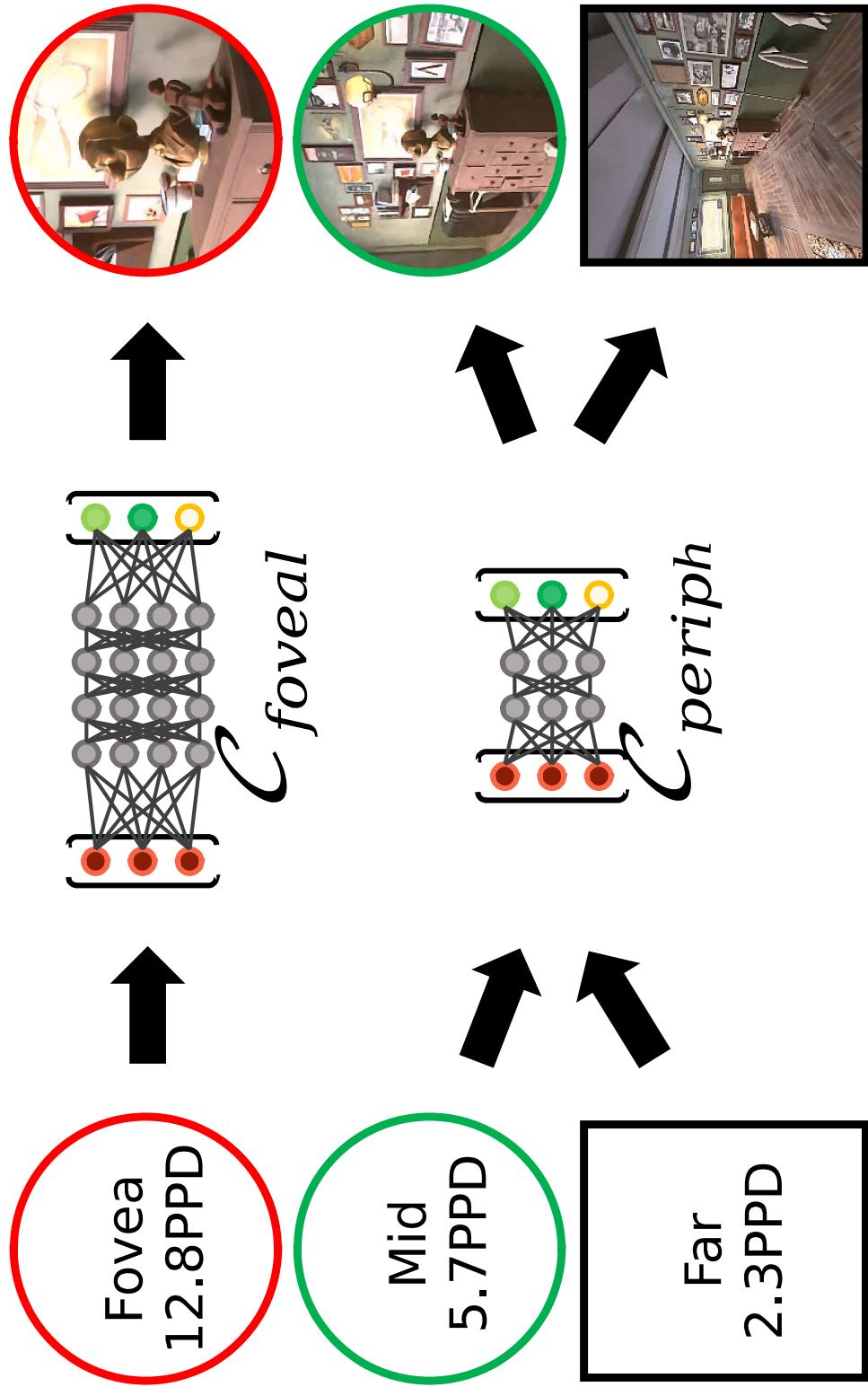
#2. Adaptive Visual Acuity



#2 Adaptive Visual Acuity



#2 Adaptive Visual Acuity



#2 Adaptive Visual Acuity

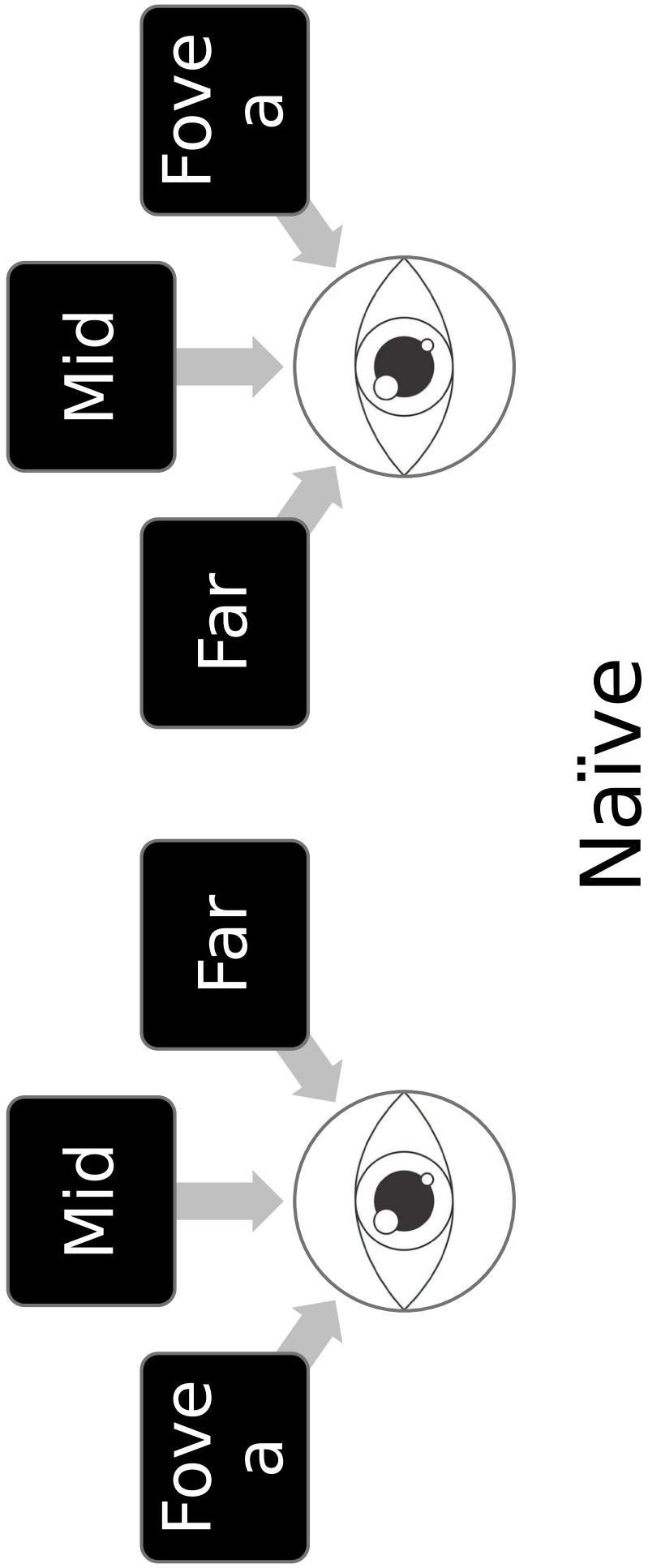


Save

~98

9% computational cost

#3 Adaptive Stereoscopic Acuity



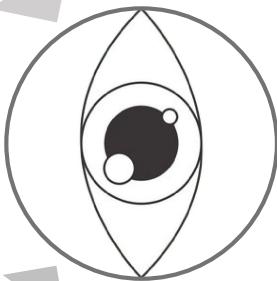
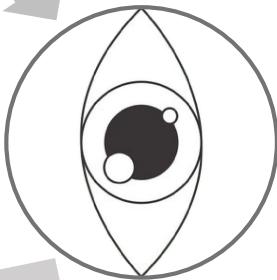
#3 Adaptive Stereoscopic Acuity

25% faster

Mid & Far

Fove
a

Fove
a



Adaptive

#4 Latency-Quality Joint Optimization

Hyper parameters:

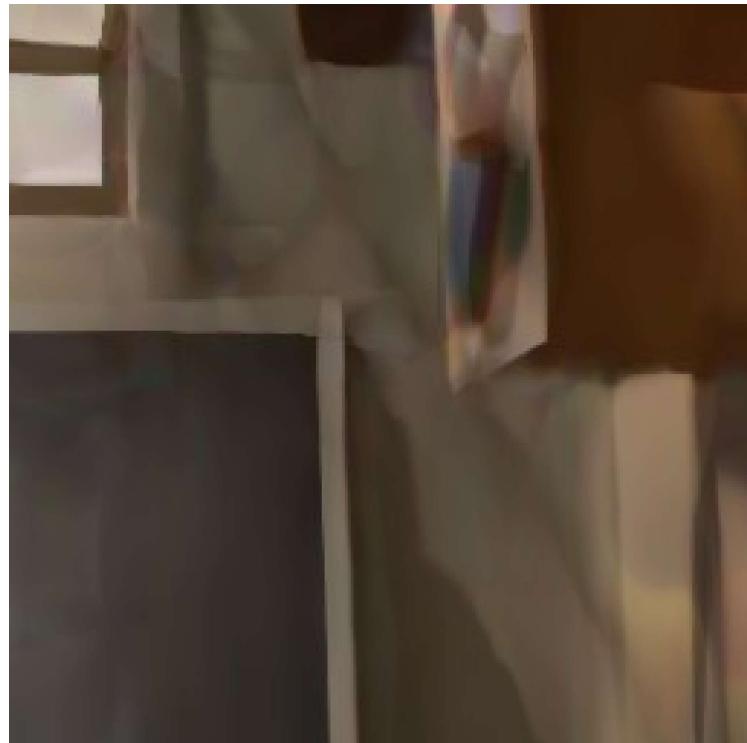
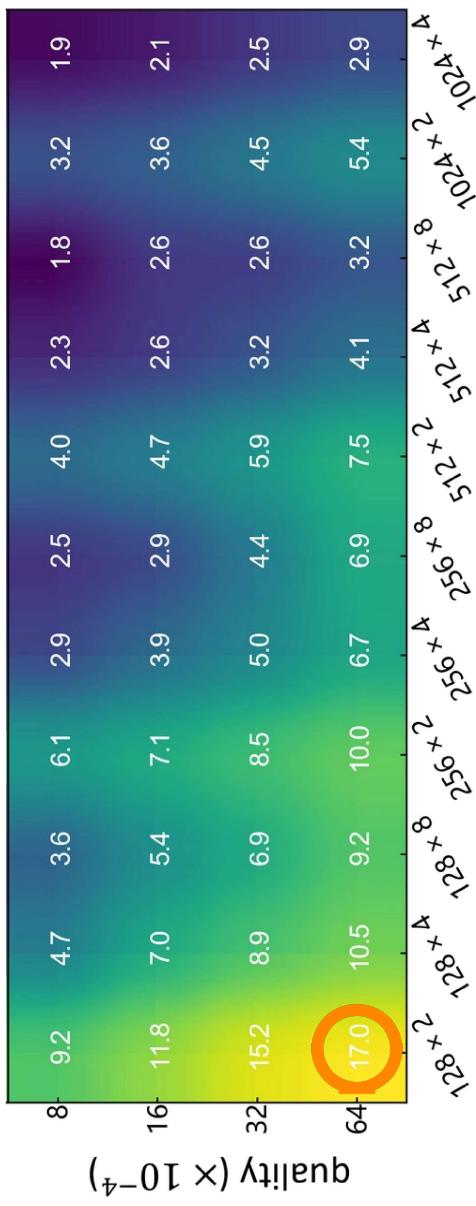
- : # of networks
- : # of layers per network
- : # of channels per layer

Spatial-temporal modeling:

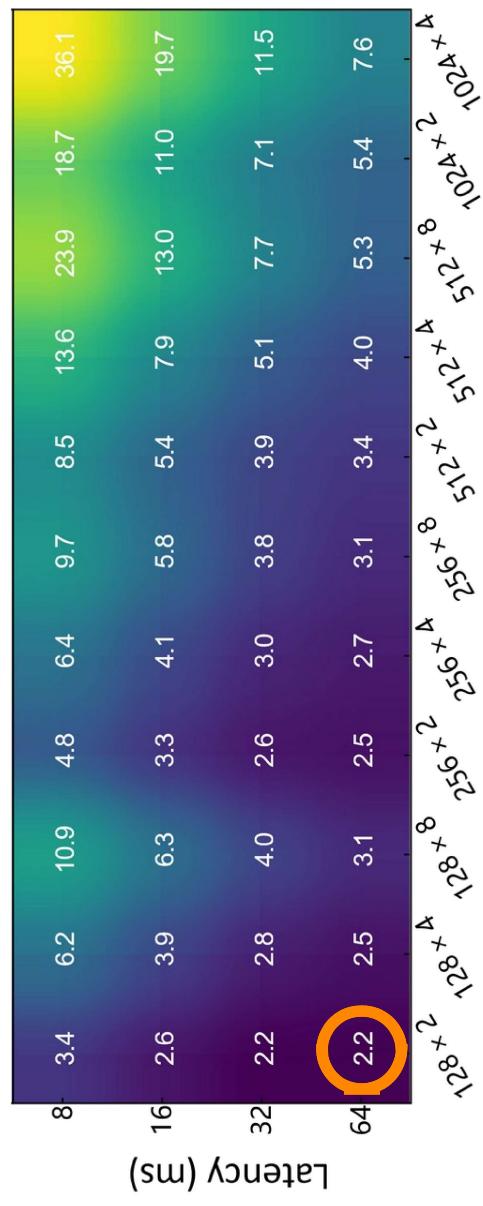
Objective function:

$$\underset{N, N_m, N_c}{\operatorname{argmin}} E(N, N_m, N_c), \text{s.t. } l(N, r) < L_0$$

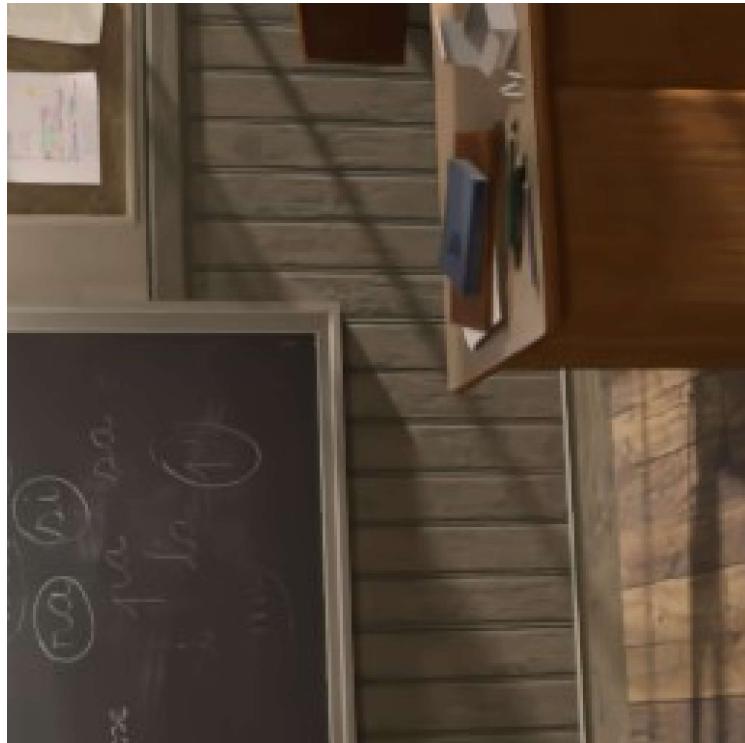
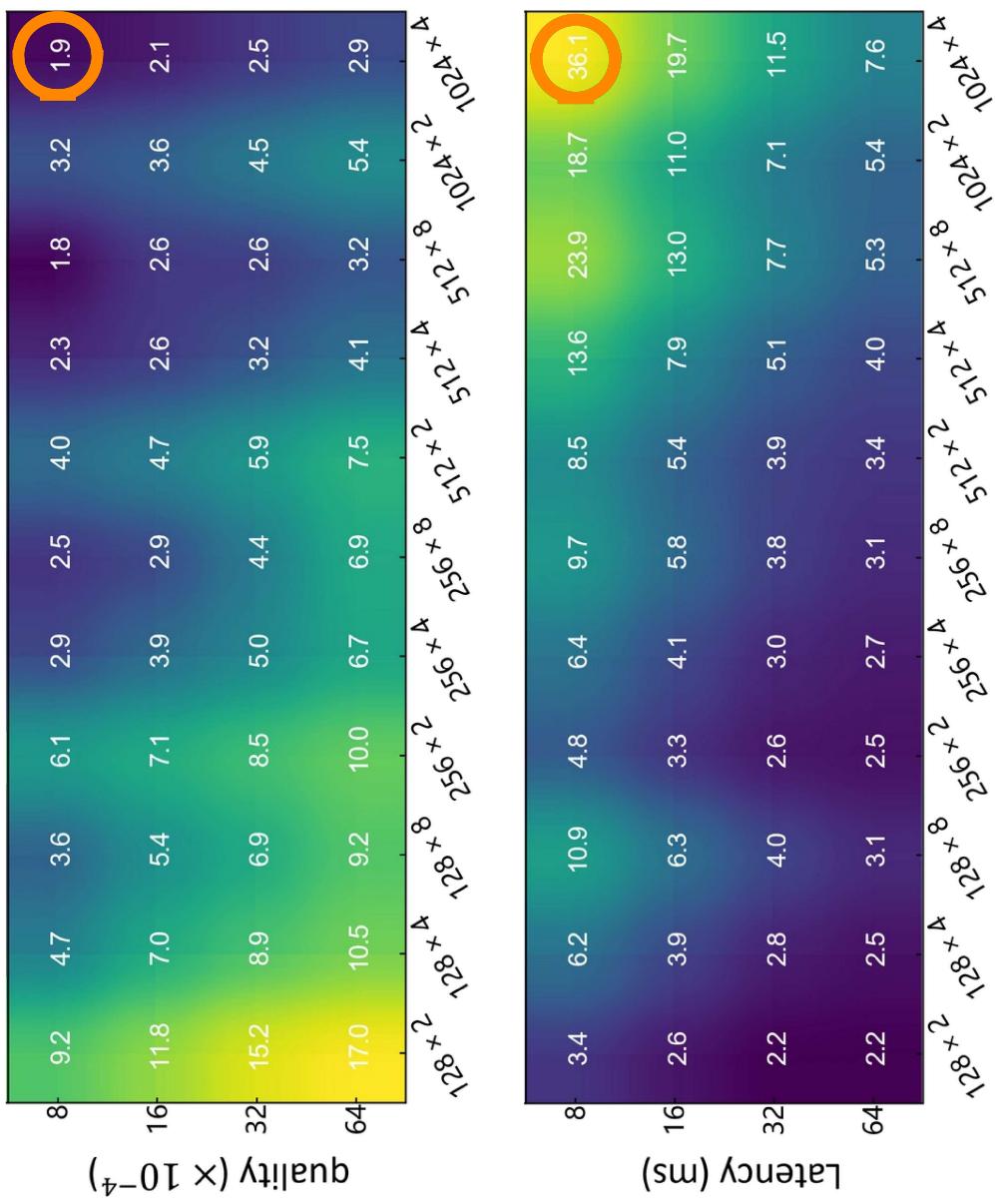
#4 Latency-Quality Joint Optimization



Best Performance

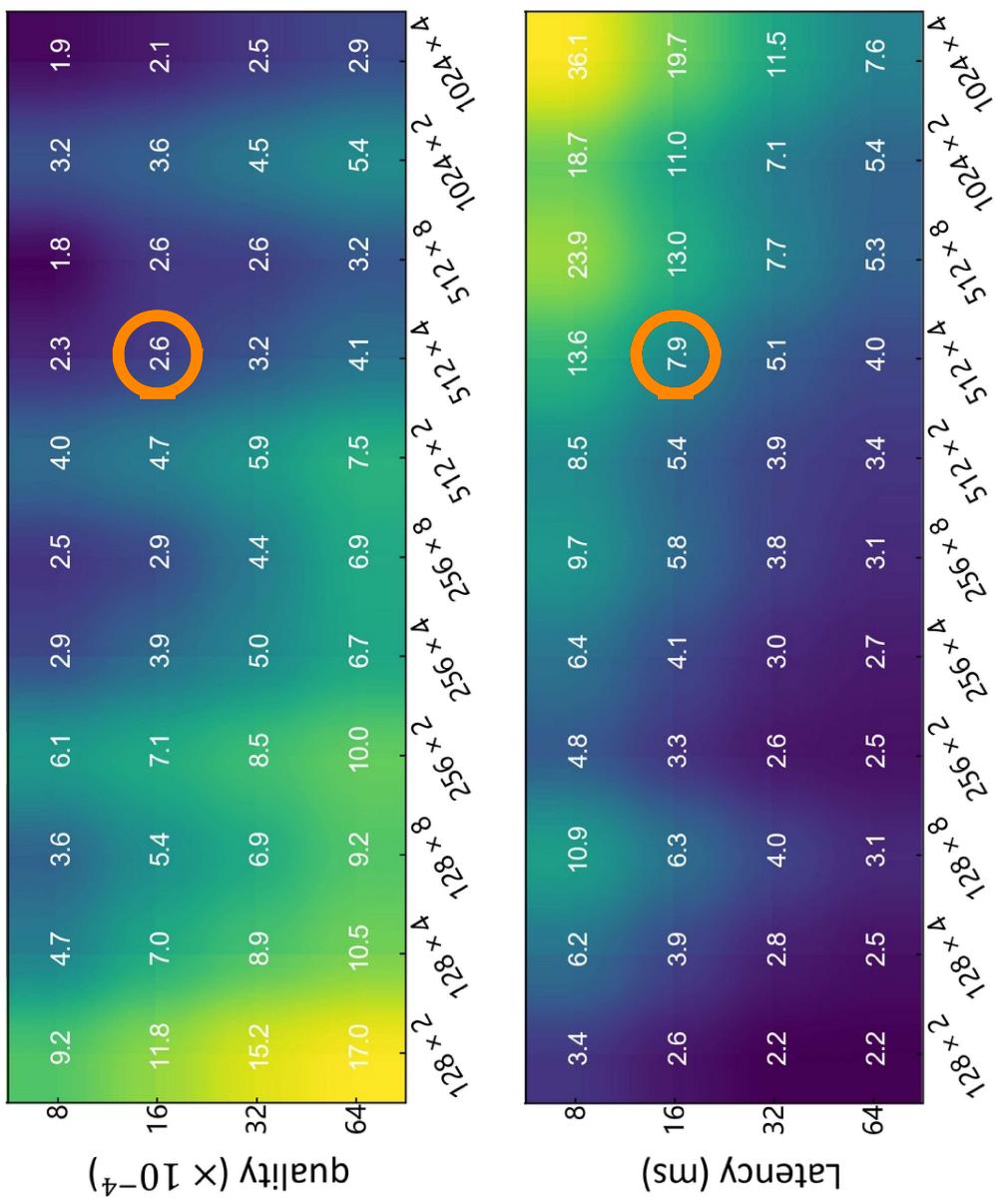


#4 Latency-Quality Joint Optimization



Best Quality

#4 Latency-Quality Joint Optimization



Ours

Comparison with Panorama-Based View Synthesis Method

Up to 1m
translation



Ours
[Lin et al. 2020]
visible artifact with dis-
robust to dis-

Explicit vs Implicit Representation (2D)

Explicit

$$\mathbf{f}(\alpha) = (r \cos(\alpha), r \sin(\alpha))^T$$

Domain: $[0, 2\pi]$

Implicit: $F(x, y)$

$$f([0, 2\pi])$$

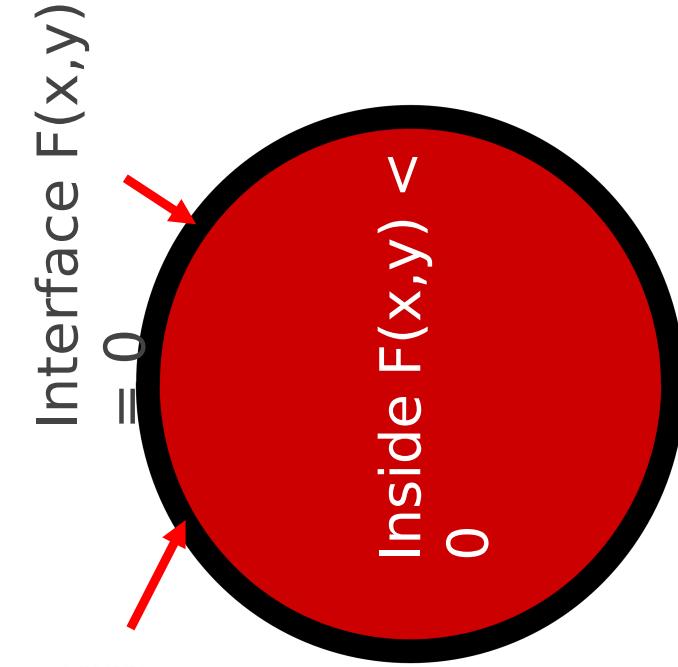
Domain: \mathbb{R}^2

Implicit:

$$F(x, y) = \sqrt{x^2 + y^2} - r$$

Domain: $(x, y) \in \mathbb{R}^2$

\Rightarrow Circle is implicitly defined by $\{(x, y) | F(x, y) = 0\}$



$\mathbf{f}(\alpha)$ defines the interface
 $F(x, y)$ defines the **Signed Distance Function** of the circle

Explicit vs Implicit Representation (3D)

Explicit

$$\mathbf{f}(\alpha, \beta) = (r \sin(\alpha) \cos(\beta), -r \cos(\alpha) \cos(\beta), r \sin(\alpha) \sin(\beta))$$

Domain: $\alpha \in [0; 2\pi], \beta \in [0; \pi]$

Implicit

$$F(x, y, z) = \sqrt{x^2 + y^2 + z^2} - r$$

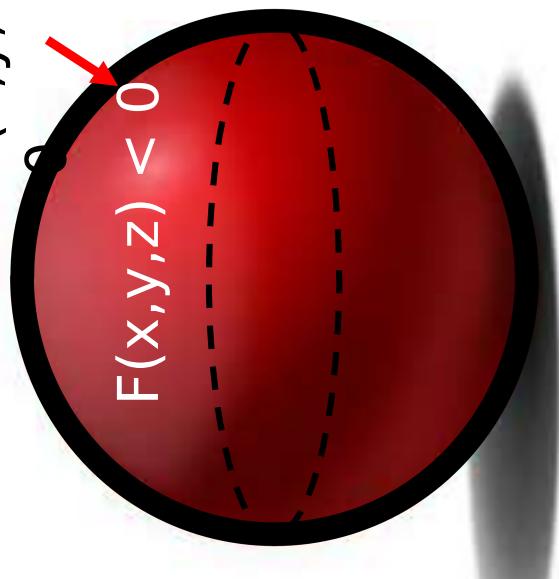
Domain: $(x, y, z) \in \mathbb{R}^3$

\Rightarrow Sphere is implicitly defined by $\{(x, y, z) | F(x, y, z) = 0\}$

$\mathbf{f}(\alpha, \beta)$ defines the 3D surface

$F(x, y, z)$ defines the **Signed Distance Function** of the sphere

$$F(x, y, z) > 0$$

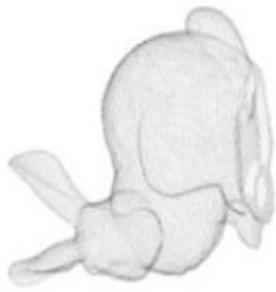


Representing 3D surfaces

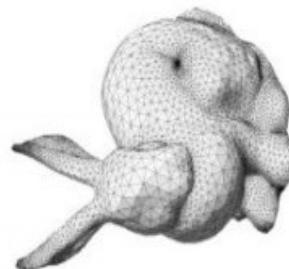
Explicit:



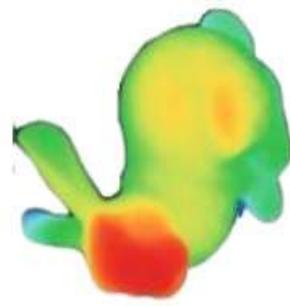
Voxels



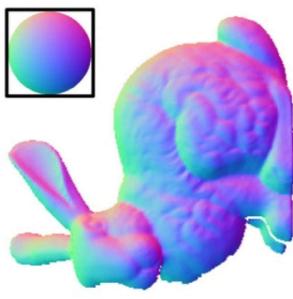
Point clouds



Mes h

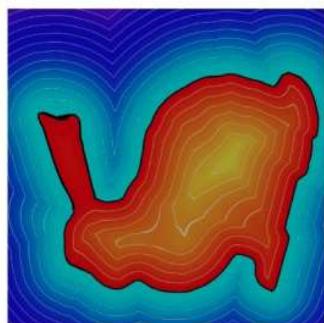


Dept



Surface Normals

Implicit:



Signed distance field

Mixture of primitives
(e.g gaussian mixtures)

Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

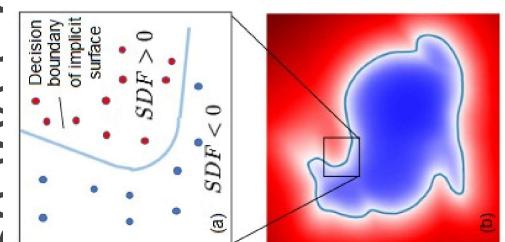
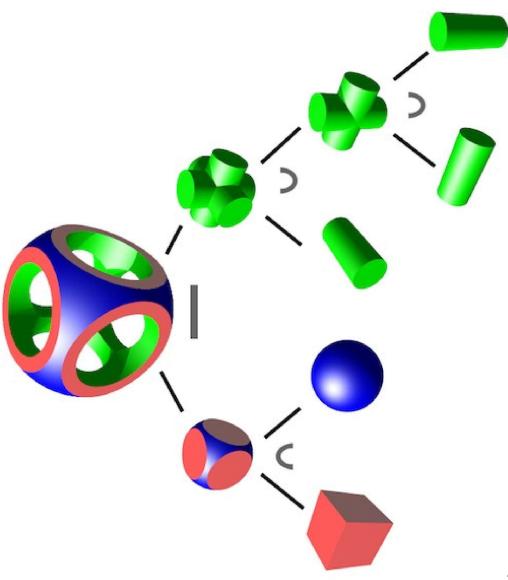
Signed Distance Field (SDF)

- Maps each 3D points p to its signed distance to the object surface S . The sign is positive if the p is inside the object, and negative otherwise
- $$SDF(p) = \text{sign}(p) \cdot \min_{q \in S} \|p - q\|$$

- Sign indicates whether the point p is inside (-) or outside (+) of the shape

Channo's hand, on the zero-level-set (---)

d Geometry (

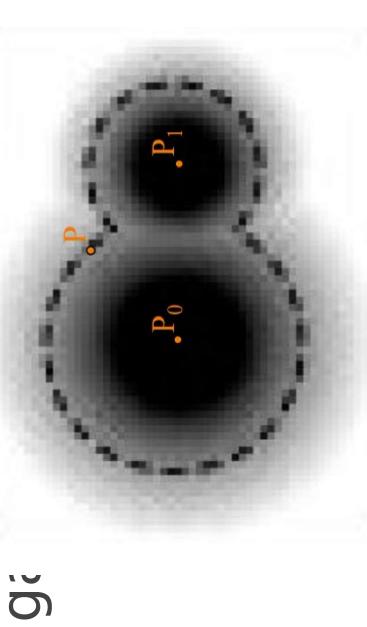


(c)

Michaël Ramamorjisoa, Van Nguyen Nguyen, Imagine -

Mixture of Gaussians

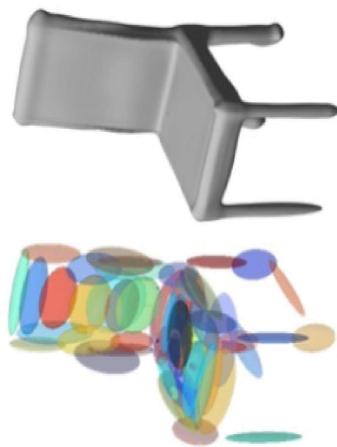
- Represents a shape as a mixture of local implicit functions (3D)



g_i

$$F(\mathbf{x}, \Theta) = \sum_{i \in [N]} f_i(\mathbf{x}, \theta_i)$$
$$f_i(\mathbf{x}, \theta_i) = c_i \exp \left(\sum_{d \in \{x, y, z\}} \frac{-(\mathbf{p}_{i,d} - \mathbf{x}_d)^2}{2\mathbf{r}_{i,d}^2} \right)$$

- Shape's boundary is defined as an iso-level of the **global** implicit function



- [1] Genova19
[2] Genova20

Representing 3D surfaces with implicit functions

Pros:

- Compared to **point clouds**: clearly defines the (*iso-*)**surface**
- Compared to **meshes**: can continuously **adapt to arbitrary topology**
- Compared to **voxels**: can be represented with **few parameters** (e.g. mixture of simple implicit functions)
 - They are **continuous** in 3D
 - Can give analytic normals, can be applied with boolean operations, etc

Representing 3D surfaces with Implicit Functions

Pros:

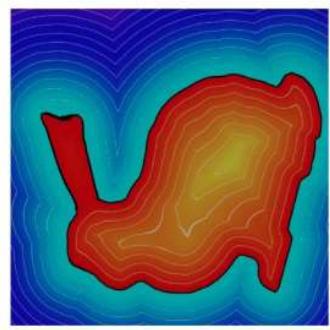
- Compared to **point clouds**: clearly defines the (iso-)surface
- Compared to **meshes**: can continuously adapt to arbitrary **topology**
- Compared to **voxels**: can be represented with **few parameters** (e.g. mixture of simple implicit functions)
 - They are **continuous** in 3D
 - Can give analytic normals, can be applied with boolean operations, etc

Cons:

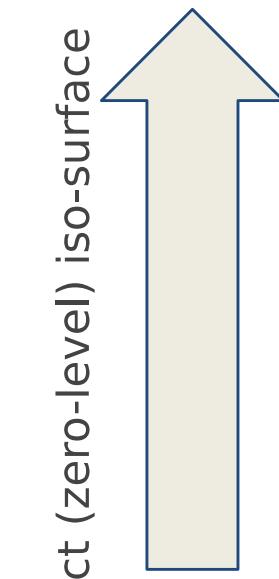
- SDF is well-defined for only watertight meshes (there is an interior and an exterior)

Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

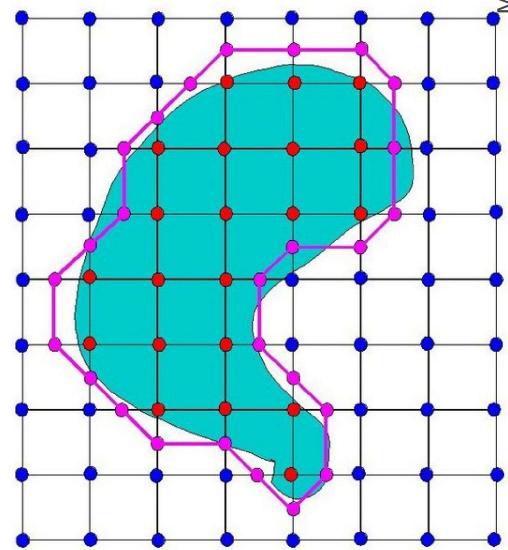
Converting Implicit Surfaces to meshes



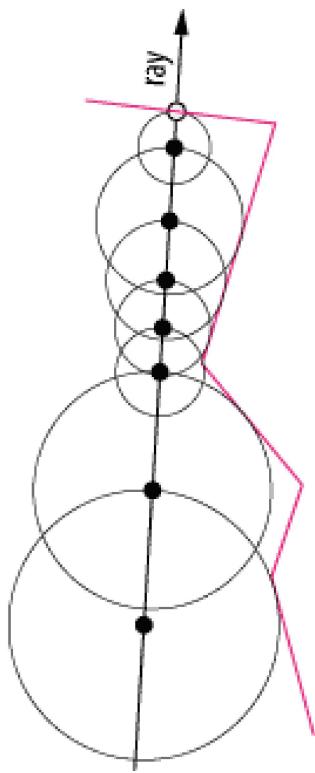
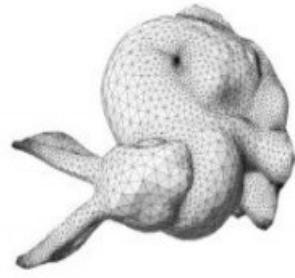
Extract (zero-level) iso-surface



Implicit
Marching Cubes



Mes
Ray marching



Michaël Ramamrissa, Van Nguyen Nguyen, Imagine -

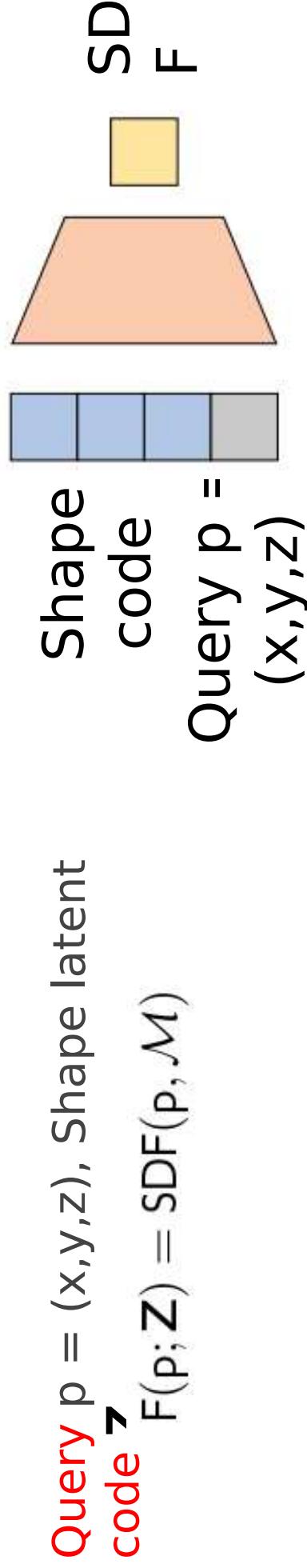
Representing 3D surfaces with implicit functions

- Compared to **point clouds**: **clearly defines the (iso-)surface**
 - Compared to **meshes**: can continuously **adapt to arbitrary topology**
 - Compared to **voxels**: can be represented with few parameters (e.g. mixture of simple implicit functions
 - They are **continuous** in 3D
 - Can give analytic normals, can be applied with boolean operations, etc
- Cons:**
- Implicit functions is well-defined for only watertight meshes (there is an interior and an exterior)
 - **Need extra steps to visualize**
 - **Not all complex shapes can be efficiently / accurately represented with simple primitives**

Representing 3D surfaces

DeepSDF: Efficiently representing complex shapes by learning their SDF

Idea: Learn a **continuous** representation of 3D implicit surfaces

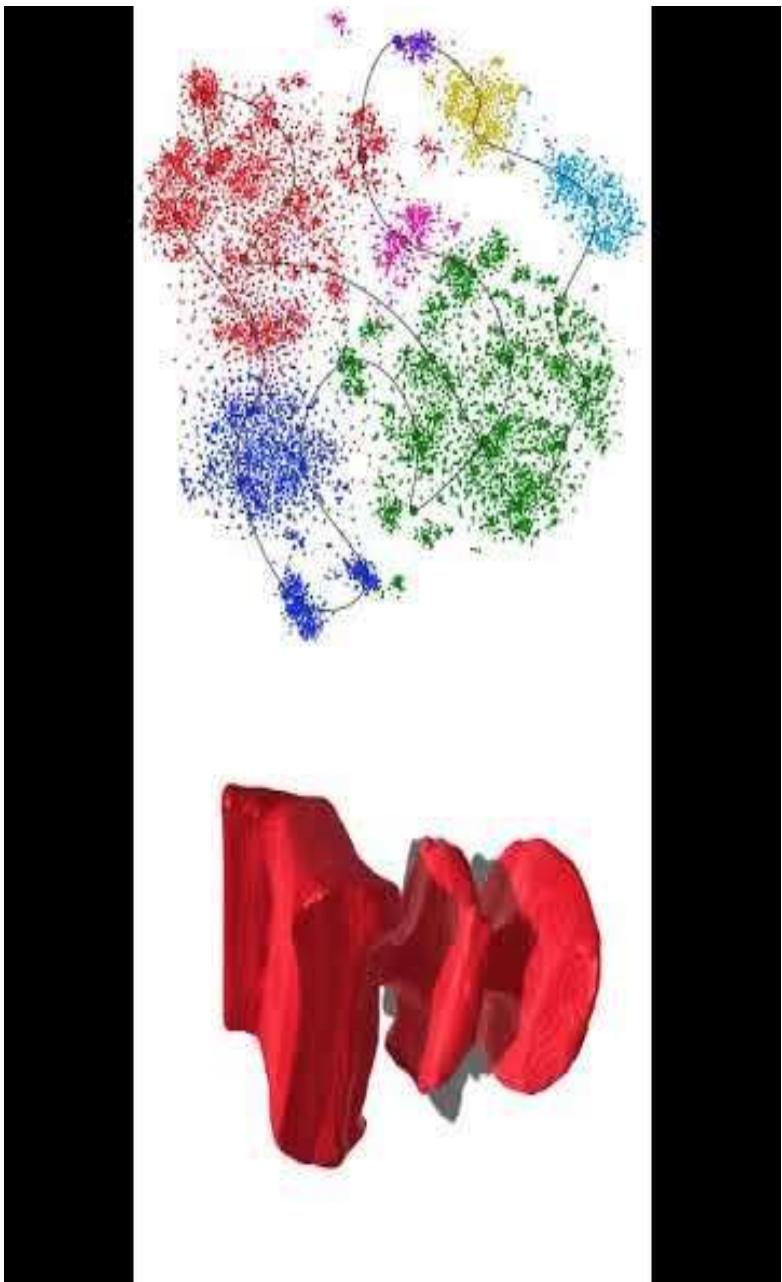


=> **Continuity** in 3D space **AND** shapes space

[3]
Park19

Representing 3D surfaces

DeepSDF: Representing complex shapes by learning their SDF



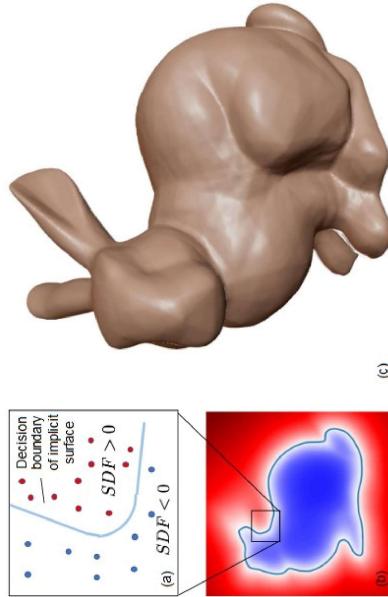
[3]
Park19

Take home message on Implicit Functions

Representation of a continuous field

Learned implicit functions:

- Can represent complex shapes
- Are **continuous mappings** because they use N-D data: 2D images, 3D radiance fields

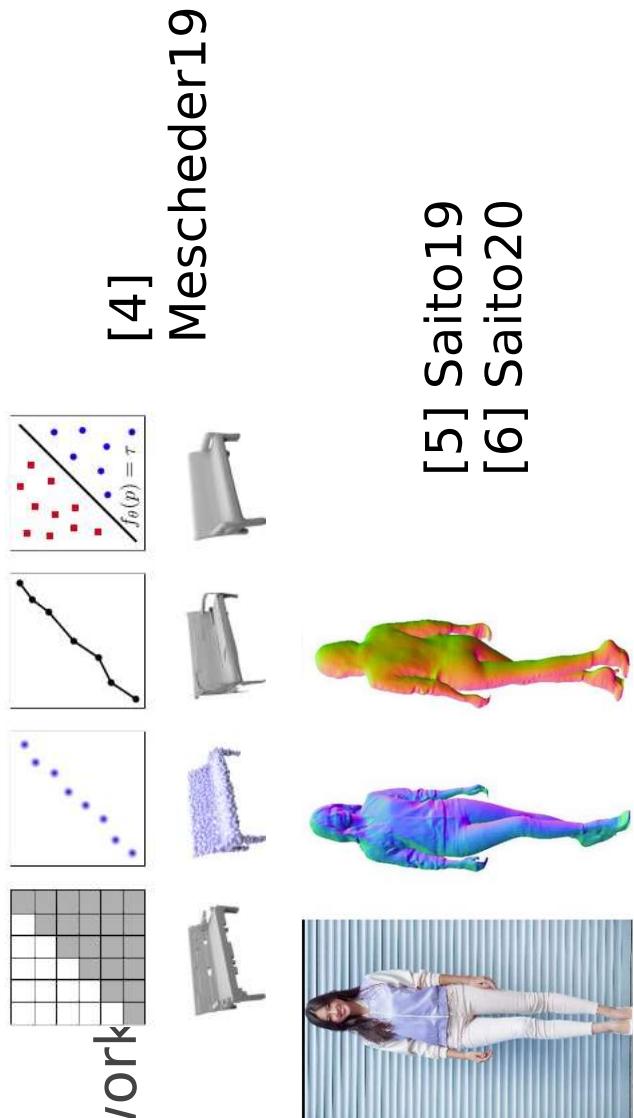


Visualization of implicit functions is done by extracting iso-surfaces:

1. Running inference for multiple queries in input space
2. Rendering the result by combining the queries

More works on Implicit Functions for 3D shape

- Occupancy Network



- PiFu and PiFuHD

References

- [1] Genova et al., [Learning Shape Templates with Structured Implicit Functions](#), ICCV 2019
- [2] Genova et al., [Local Deep Implicit Functions for 3D Shape](#), CVPR 2020
- [3] Park et al.,
[DeepSDF: Learning Continuous Signed Distance Functions for Shape Representation](#), CVPR 2019
- [4] Mescheder et al., [Occupancy Networks: Learning 3D Reconstruction in Function Space](#), CVPR 2019
- [5] Saito, Huang, Natsume et al., PIFU:
[Pixel-Aligned Implicit Function for High-Resolution Clothed Human Digitization](#), ICCV 2019
- [6] Saito et al.,
[PIFuHD: Multi-Level Pixel-Aligned Implicit Function for High-Resolution 3D Human Digitization](#)
[Lectures 2026](#)
Implicit geometry
Lecture on Implicit surface
Lecture on Explicit & Implicit Surfaces

Courses and Seminars

Thomas Funkhouser's talk at 3DGV seminar

Princeton COS 426, Spring 2014 on [Implicit Surfaces & Solid Representations](#)