



Virtual and Augmented Reality

CS-GY 9223/CUSP-GX 6004

<https://nyu-icl.github.io/courses/2022fall-vr-ar>

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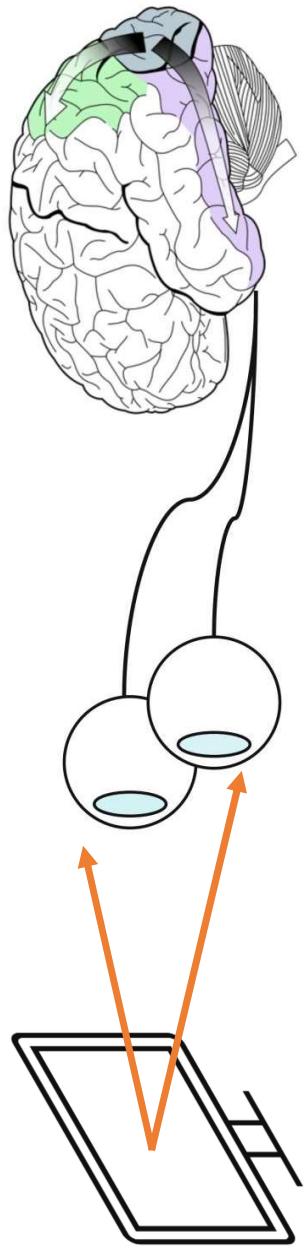
Logistics

- Everyone gets a Google Cardboard
- Tutorial/workshop today
- Assignment 1 recap



The Human Visual System

- **visual field:** ~200°monocular, ~120°binocular, ~135°vertical
- **visual acuity:** 20/20 is ~1 arc min; varies over retina
- **depth cues in 3D displays:** disparity, vergence, accommodation, blur, ...
 - **accommodation range:** ~8cm to ∞ , degrades with age
- **temporal resolution:** ~60 Hz (depends on contrast, luminance)
- **temporal behaviors:** saccade, pursuit, etc



generation sensing processing

Anatomy

The Human visual System

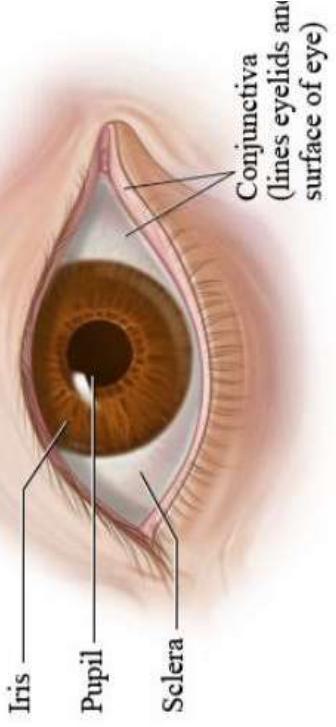
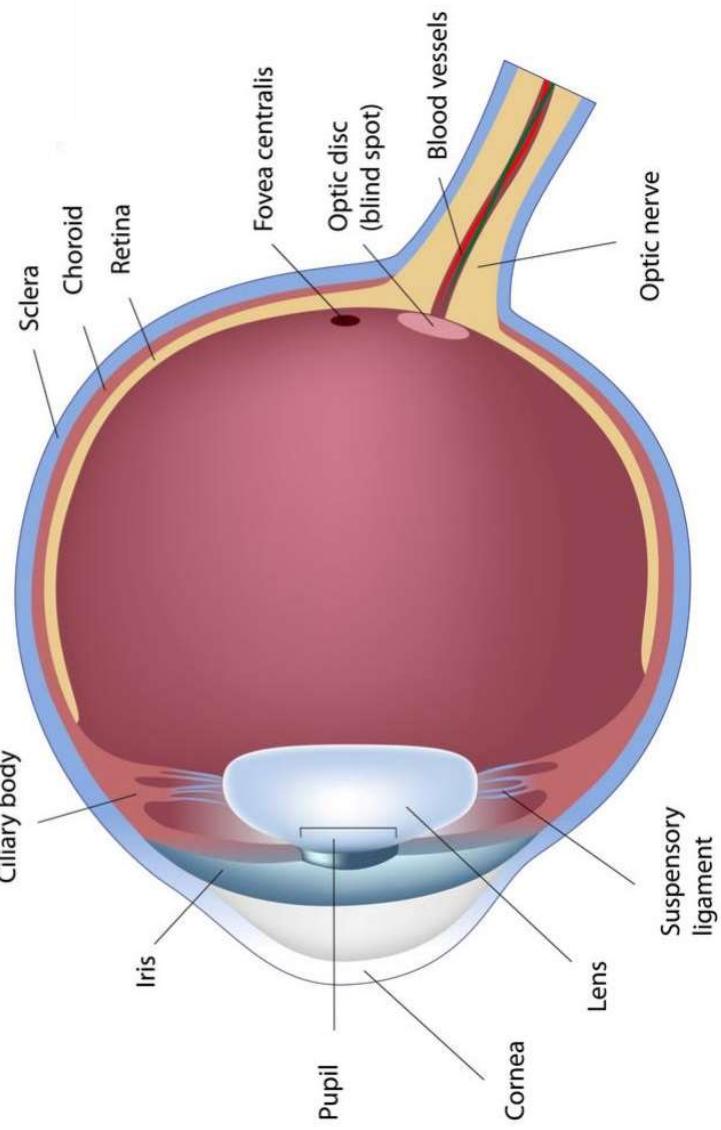
Human Eye Anatomy

Control the focal length of the lens

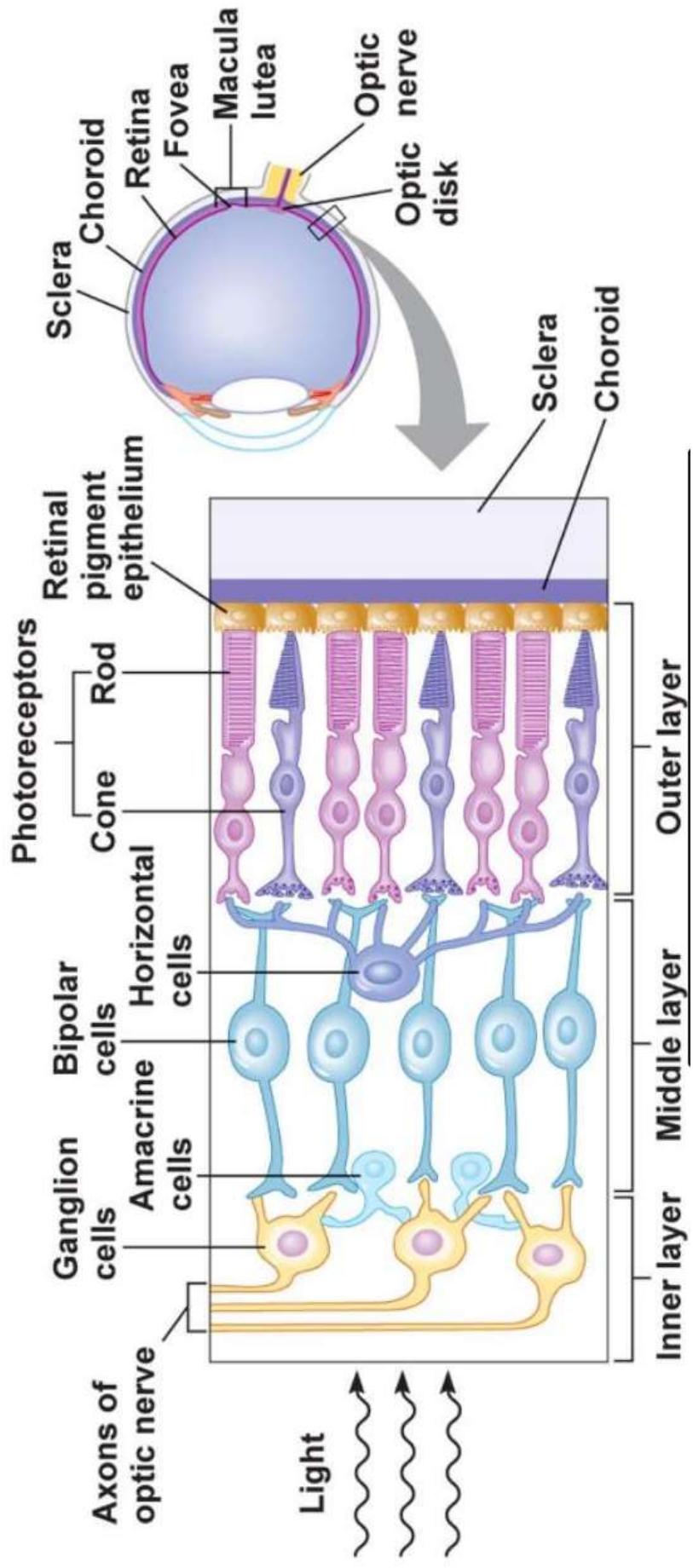
Control the pupil size

Where the light enters

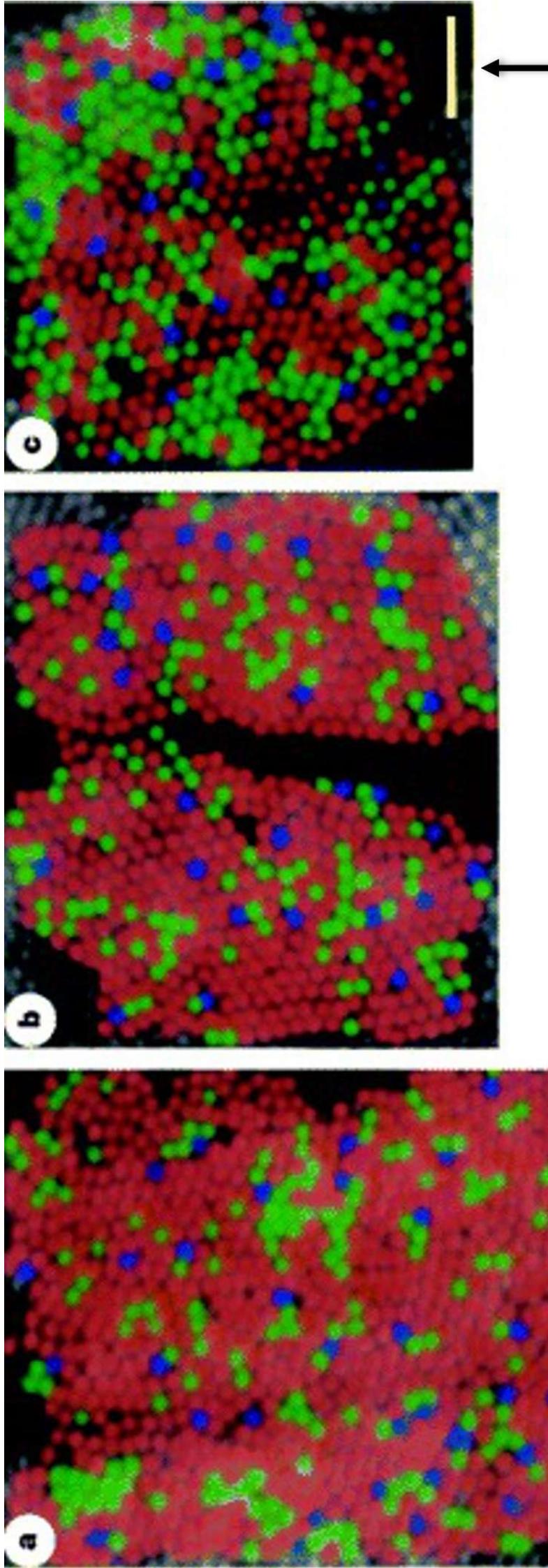
Focus the light



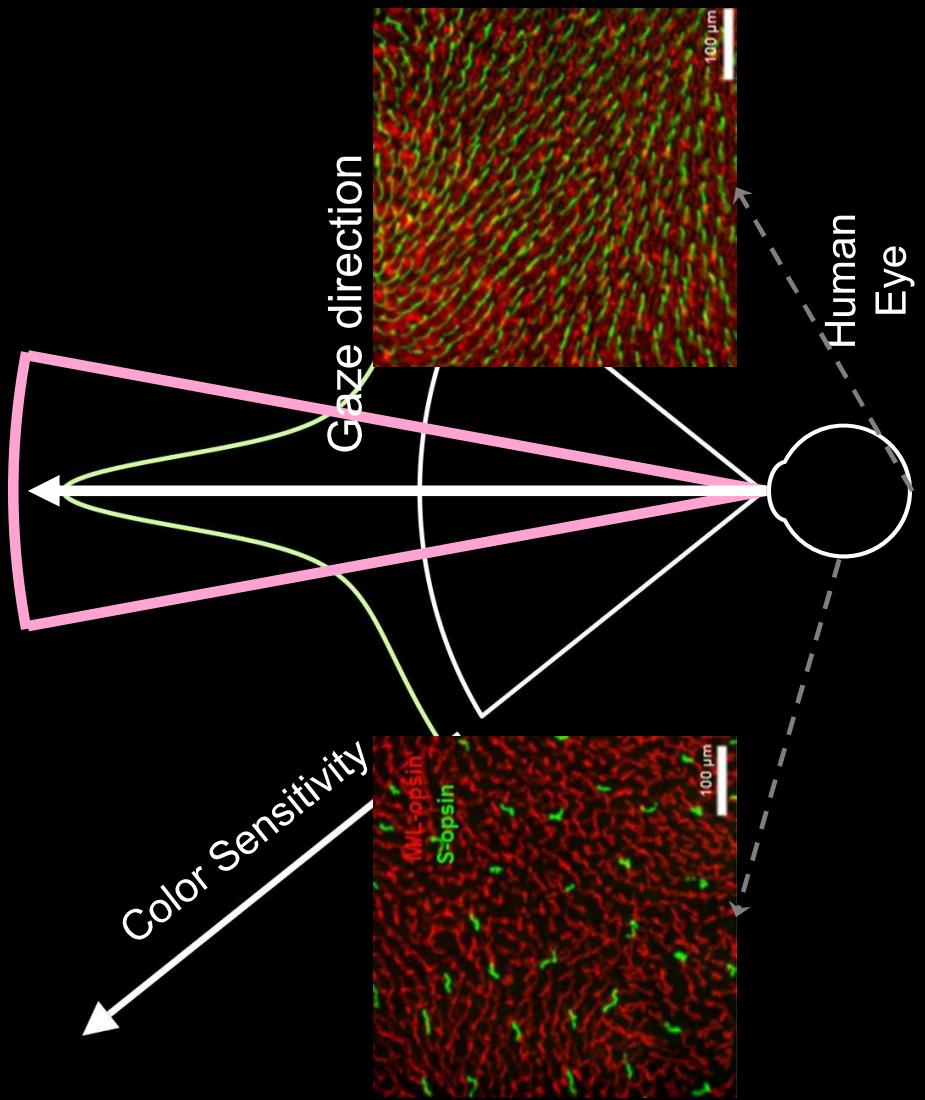
The Human Visual System



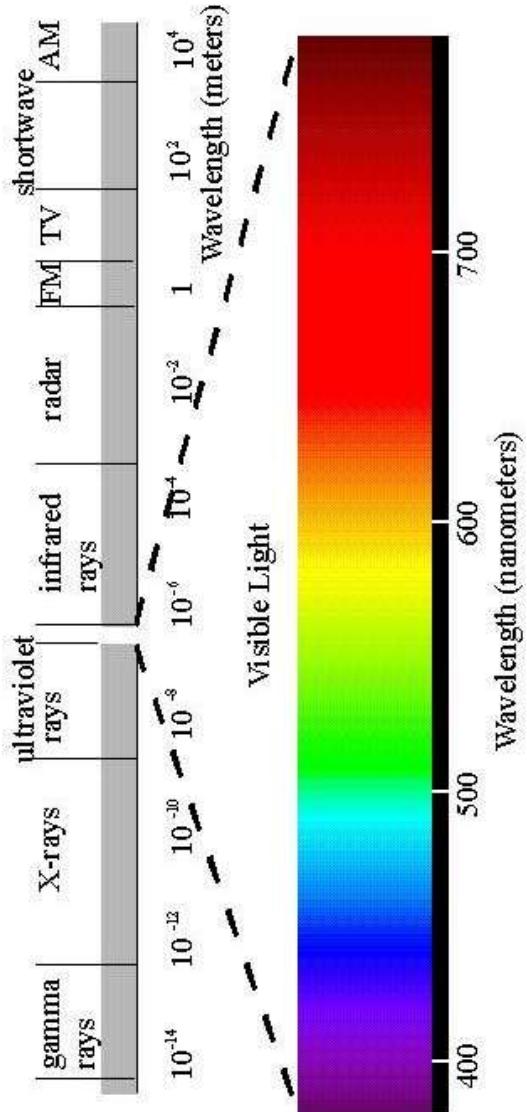
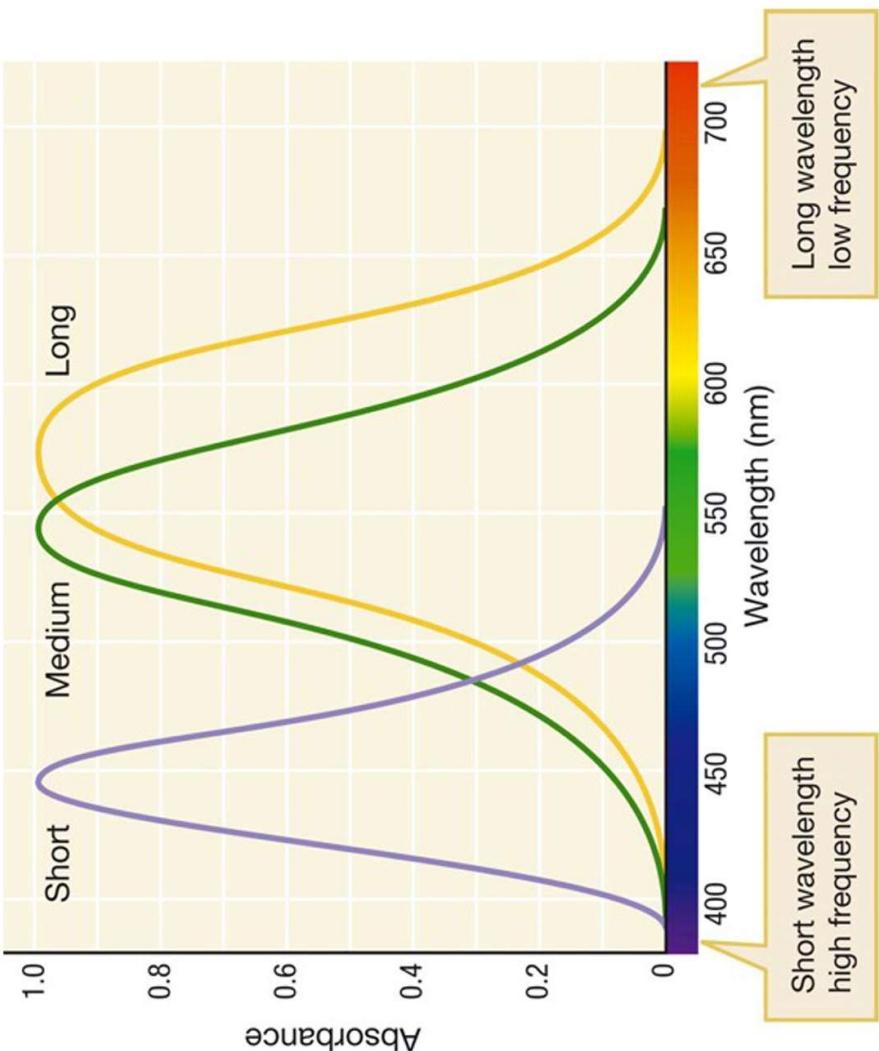
The Human visual System



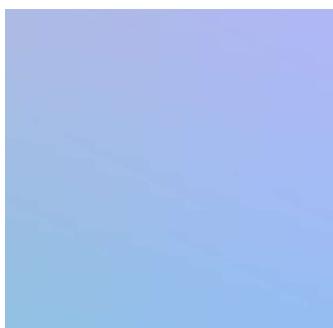
5 arcmin visual angle



The Human Visual System

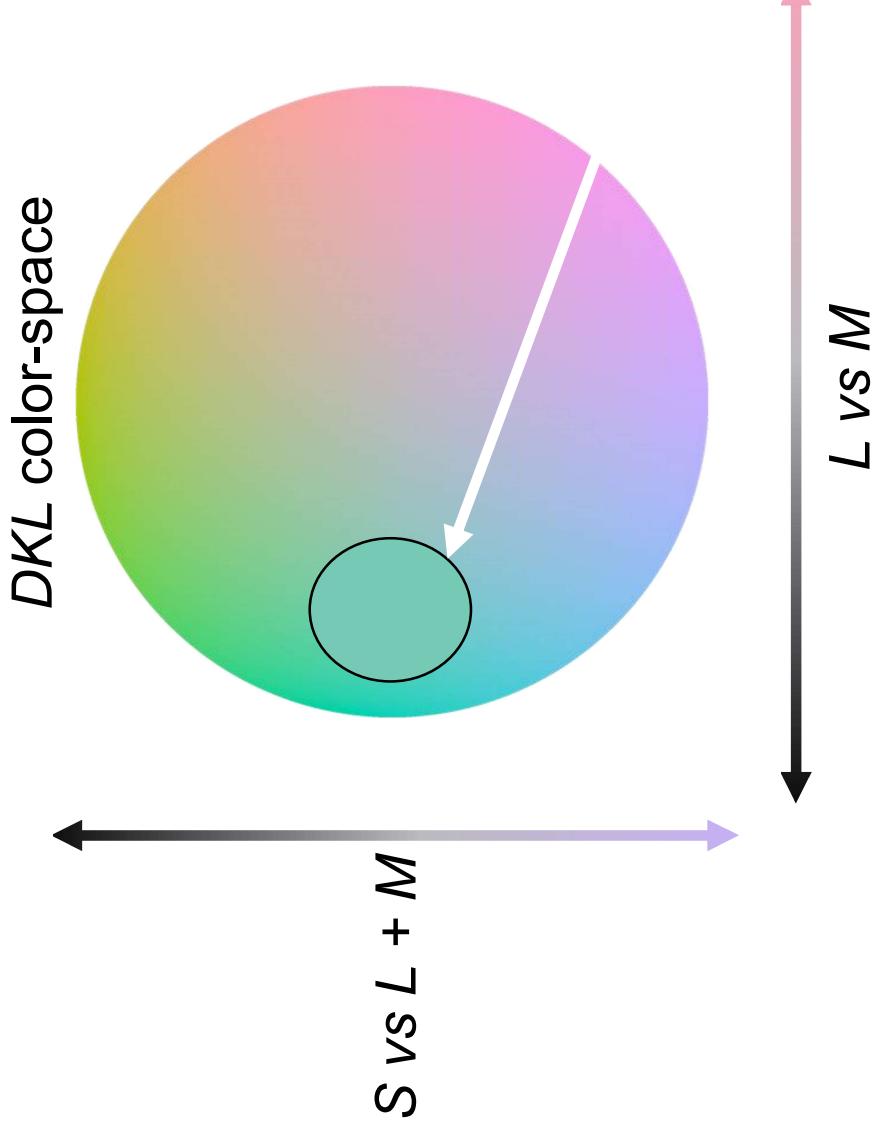


Perceptual Color Space



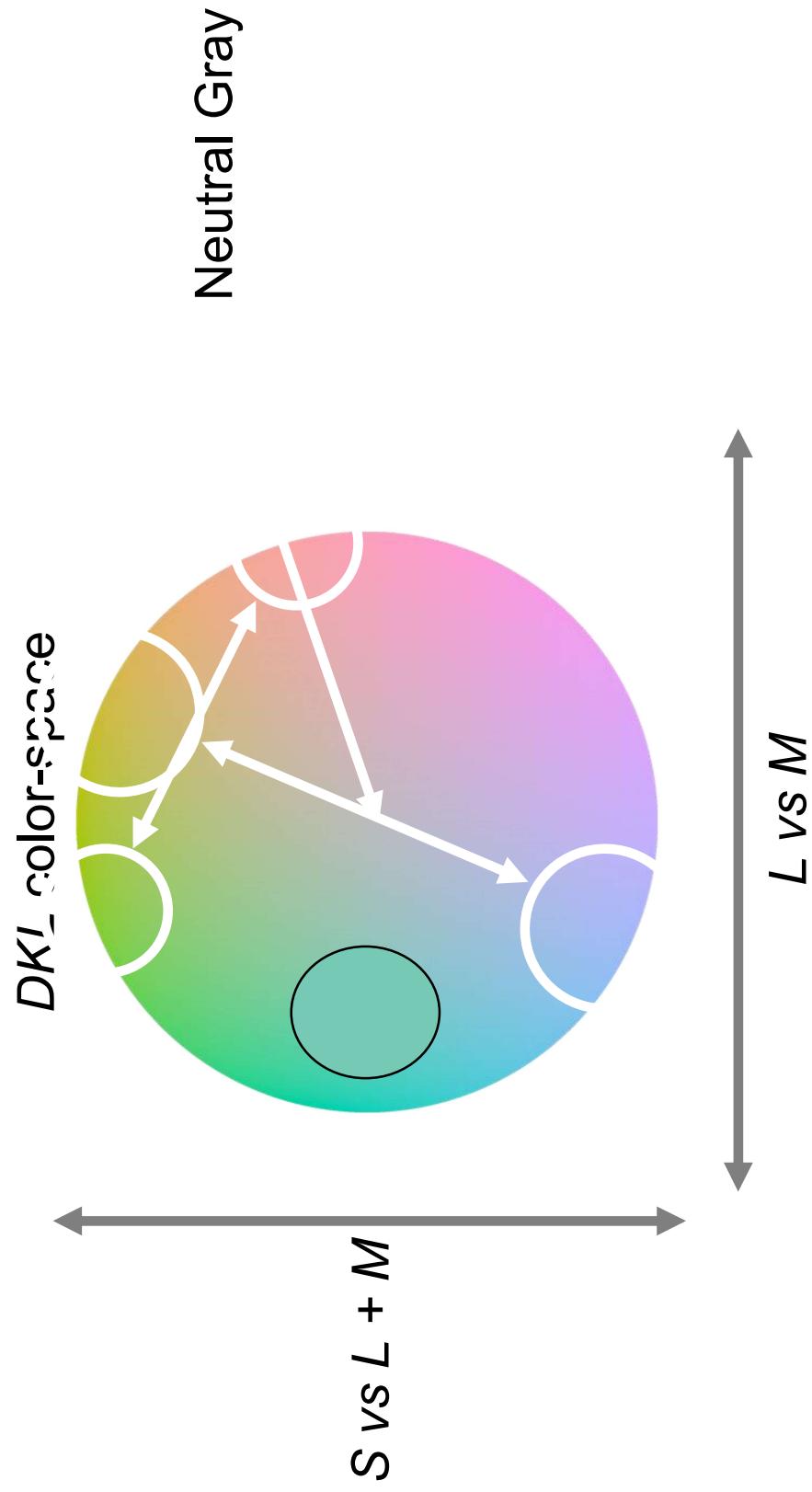
Color-Perception-Guided Display Power Reduction for Virtual Reality
Budmonde Duinkhajav et al., ACM ToG (SIGGRAPH Asia 2022)

Perceptual Color Space – Opponency Theory

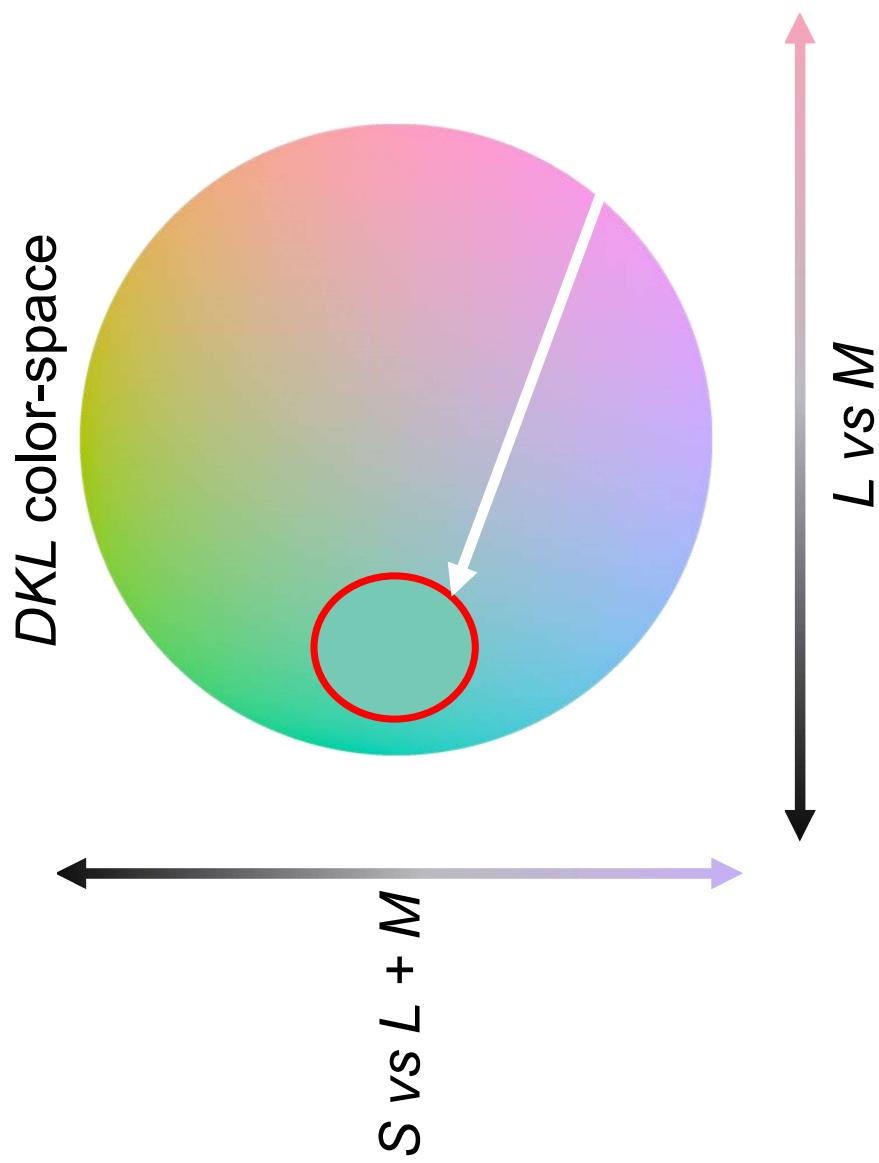


Color-Perception-Guided Display Power Reduction for Virtual Reality
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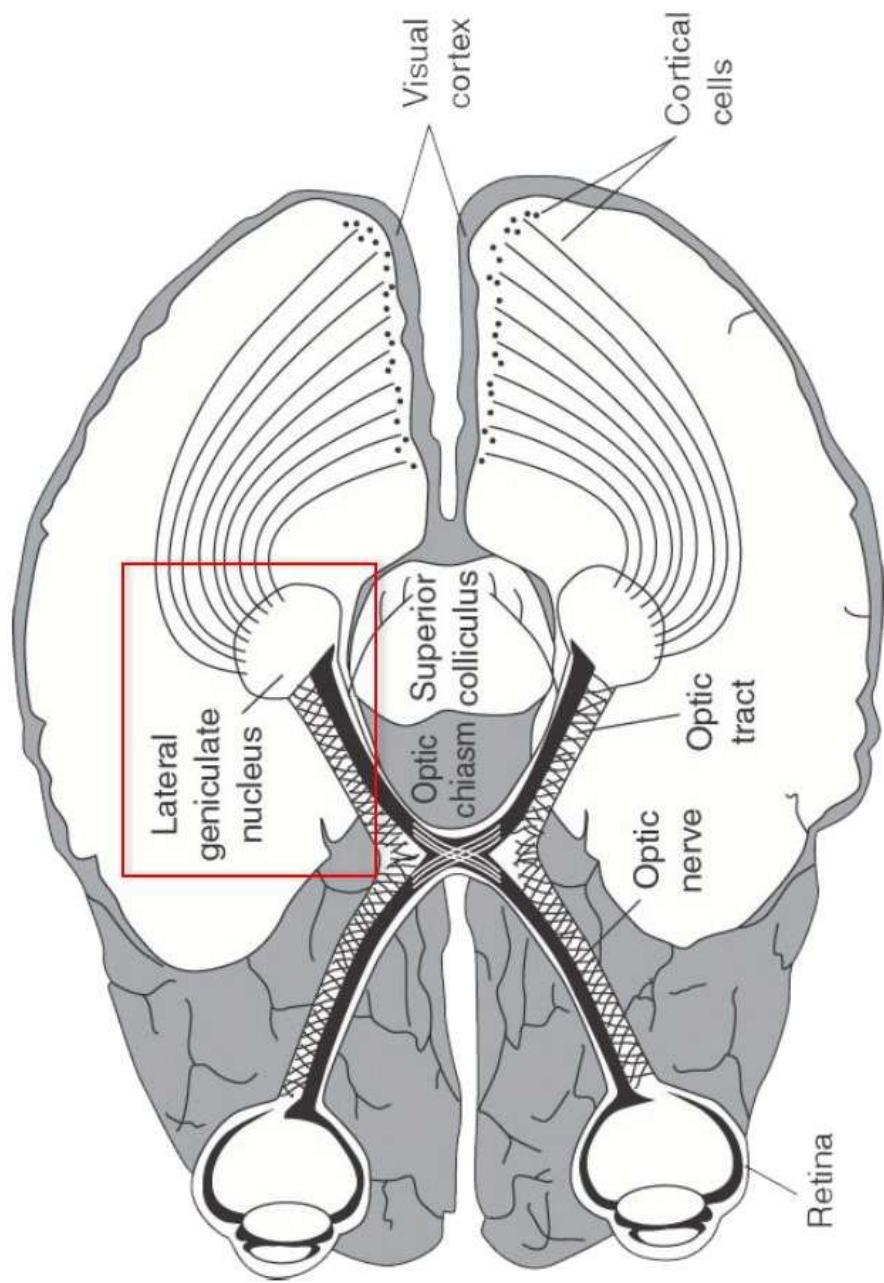
Perceptual Color Space – Opponency Theory



Perceptual Color Space – Opponency Theory

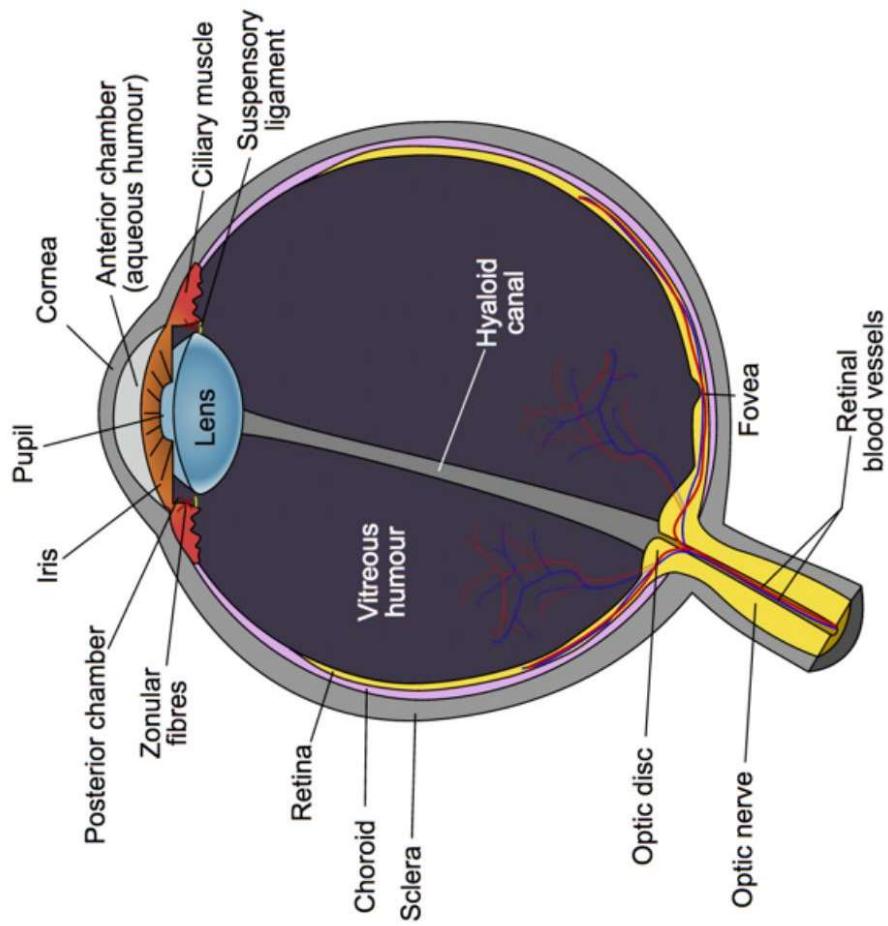


The Brain



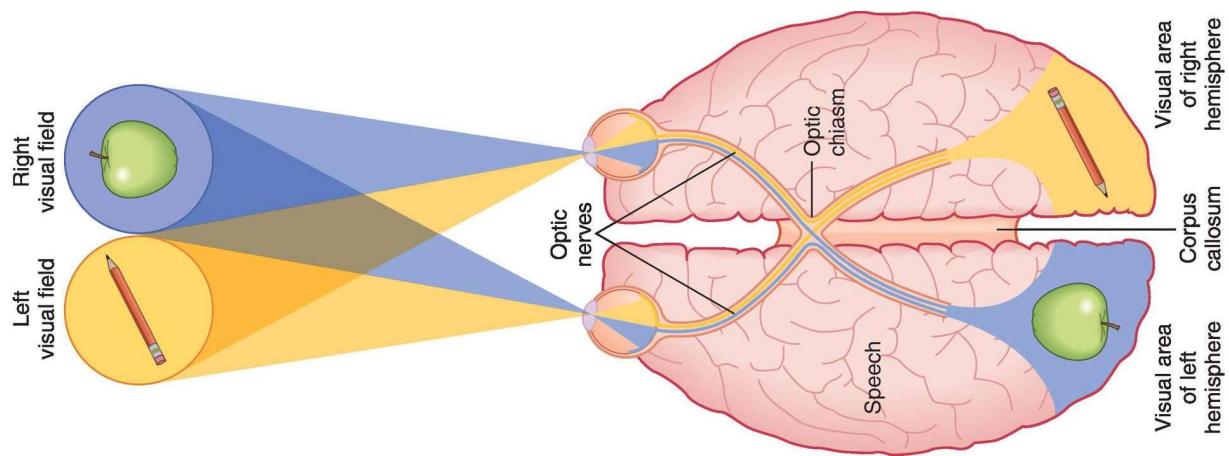
Overview

- Visual field
- Visual acuity
- Depth cue
- Temporal behaviors/perception

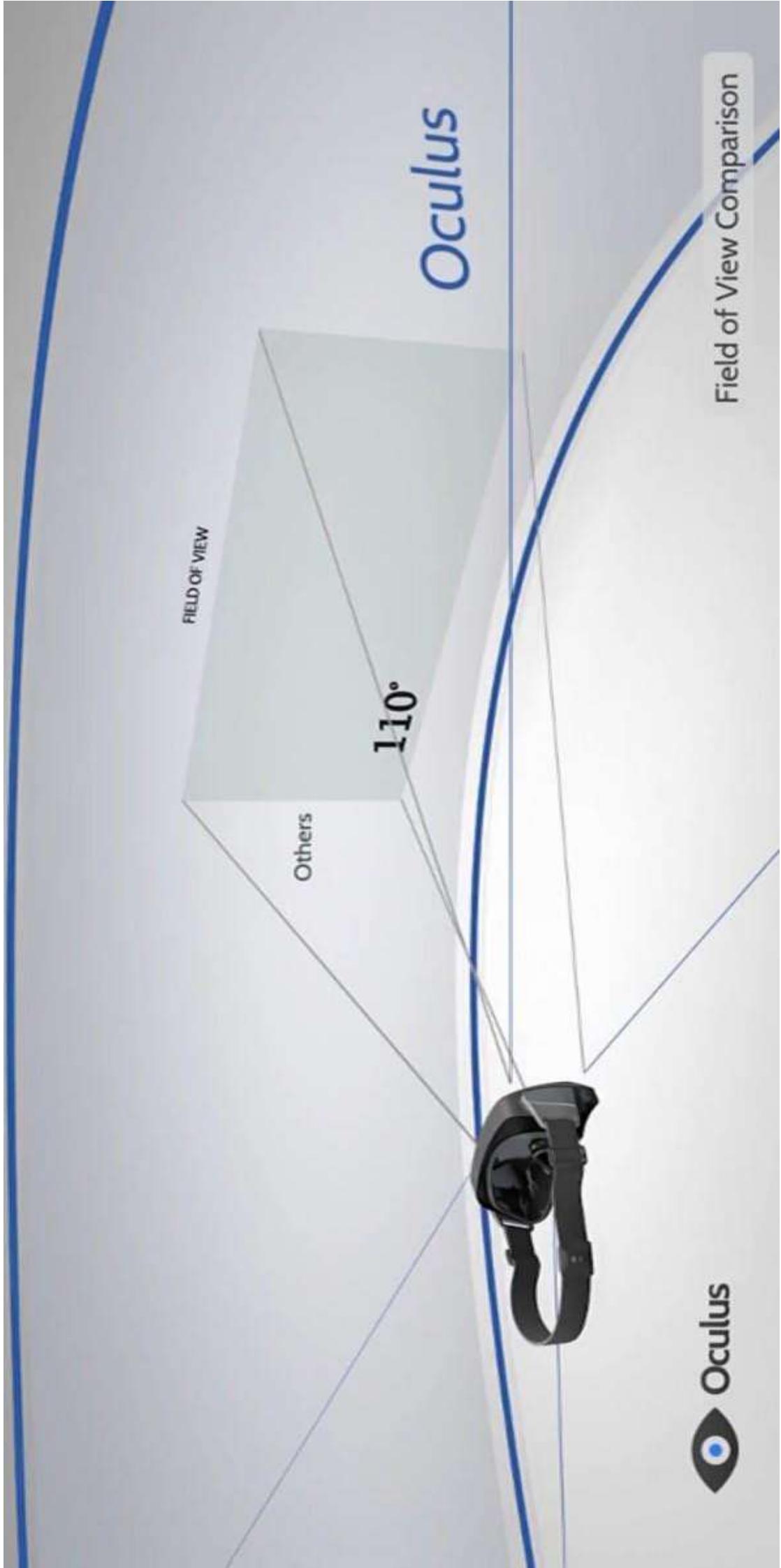


Visual Field

Field of View (FoV)



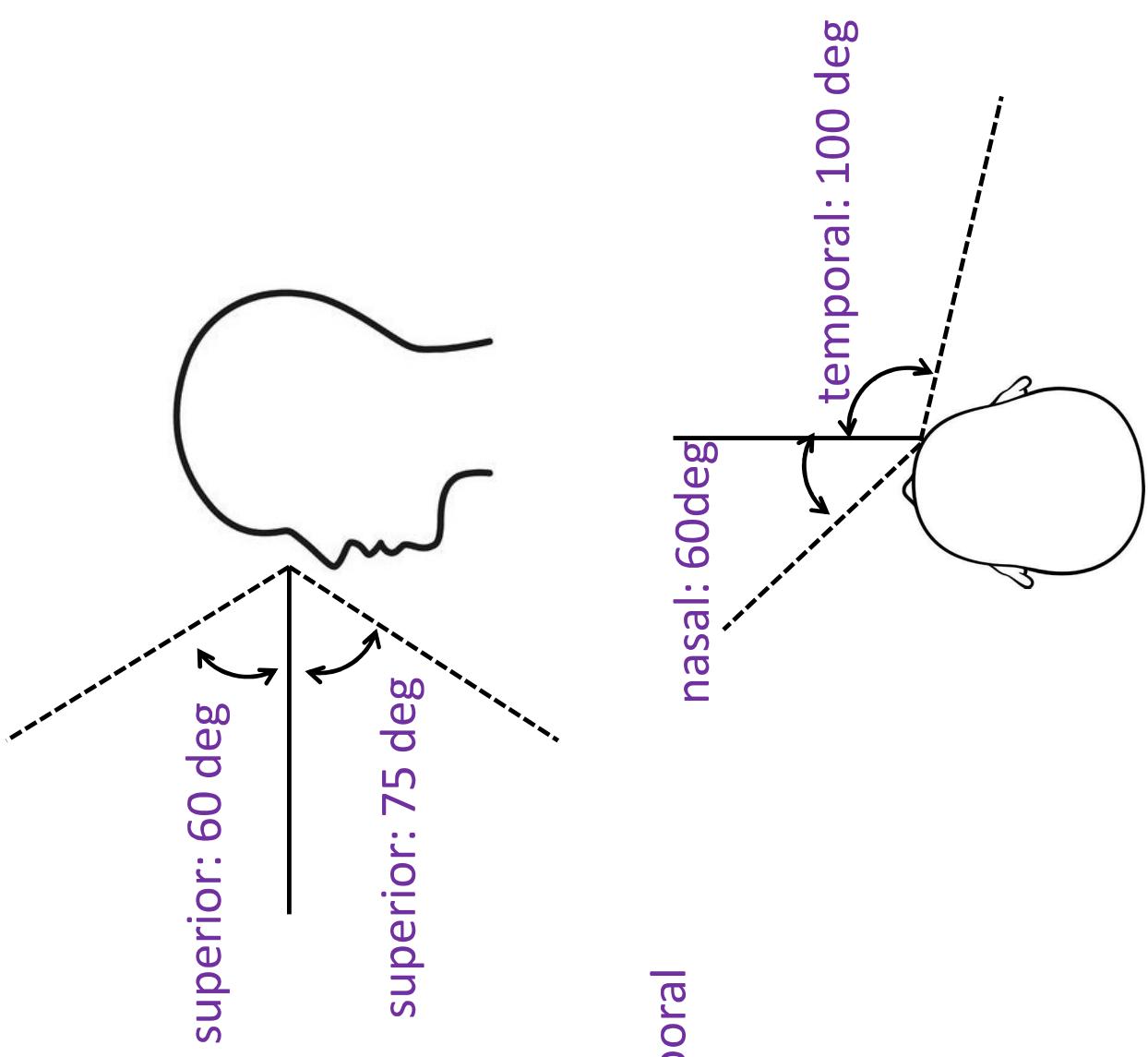
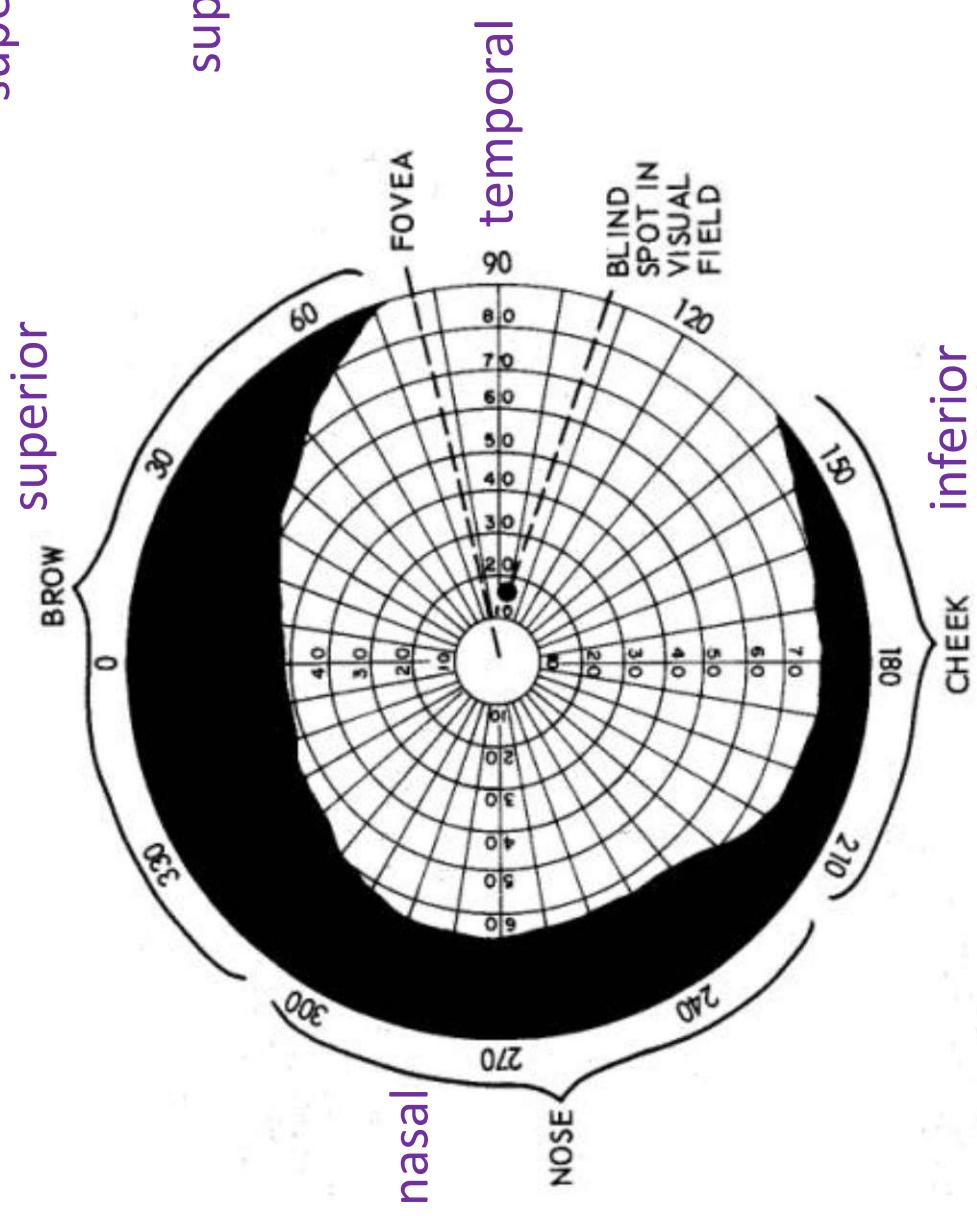
Immersive VR – How important is the FOV?



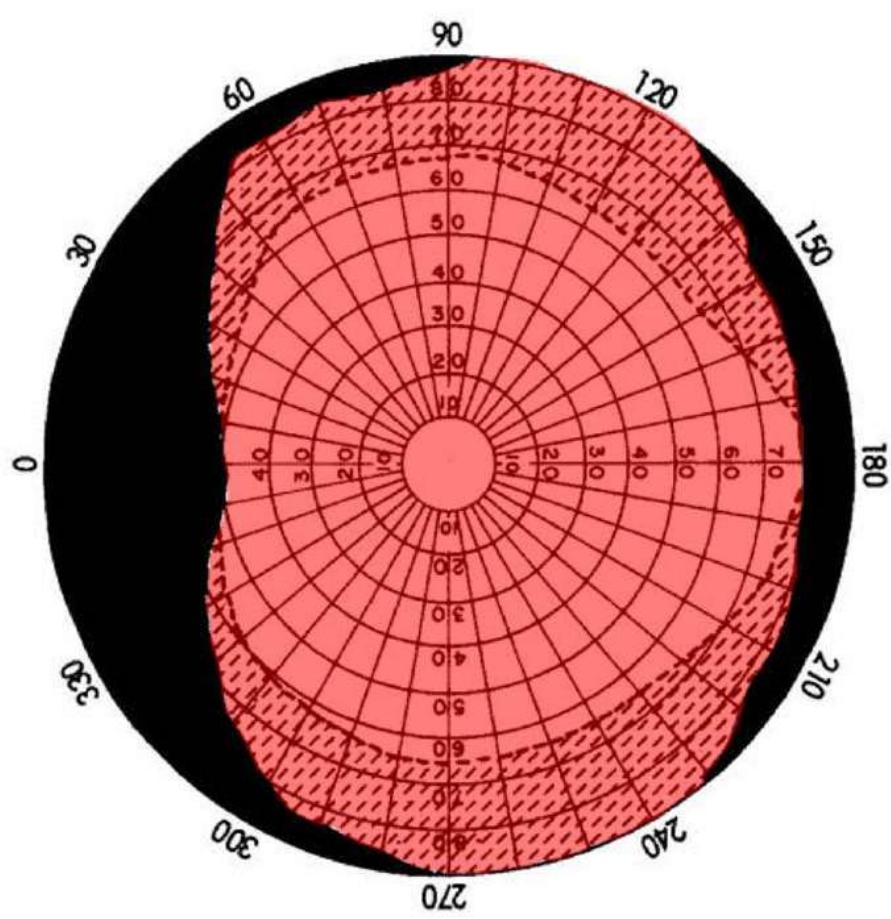
Visual Field - Terminology

- monocular visual field: visual field of either only the left or right eye
- binocular visual field or region of binocular overlap: intersection of monocular visual fields, i.e. only the overlapping part of both eyes – this is where we see stereo!
- total visual field: union of monocular visual fields, i.e. visual fields of both eyes combined – not all of this is stereo, temporal peripheries are mono!

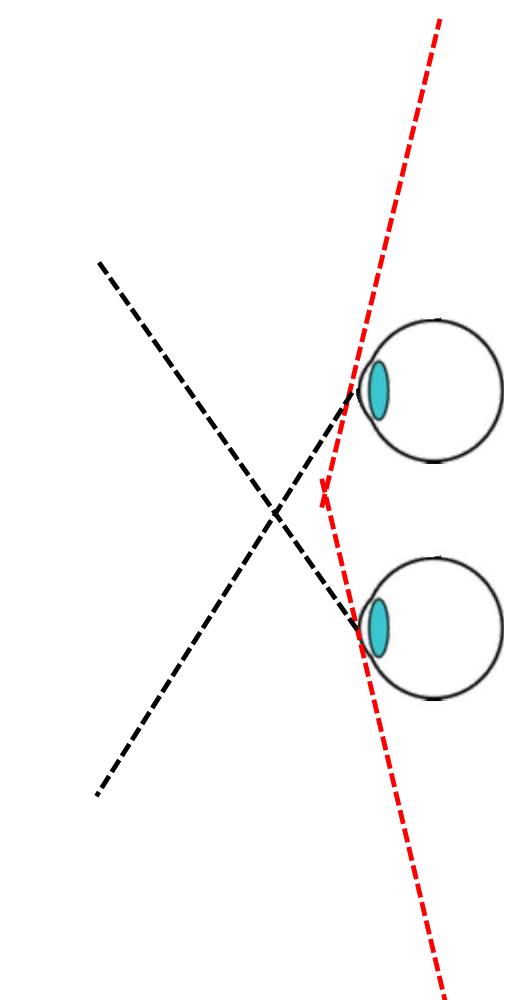
Visual Field



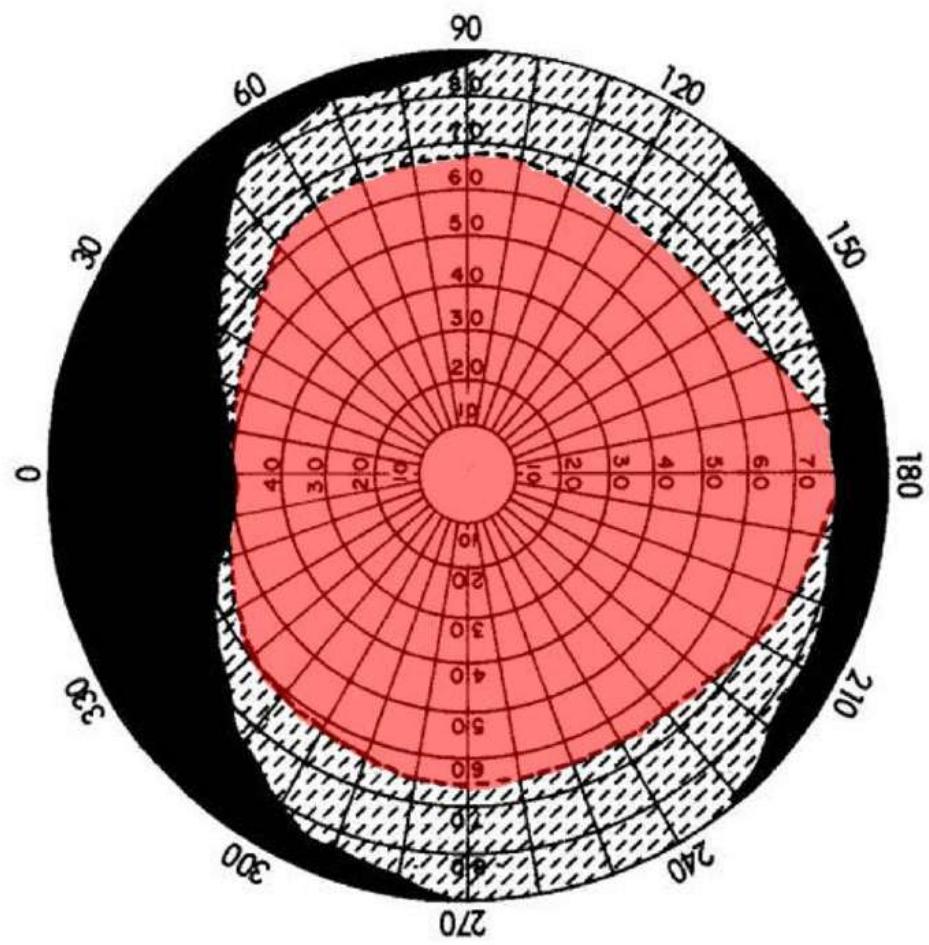
Visual Field



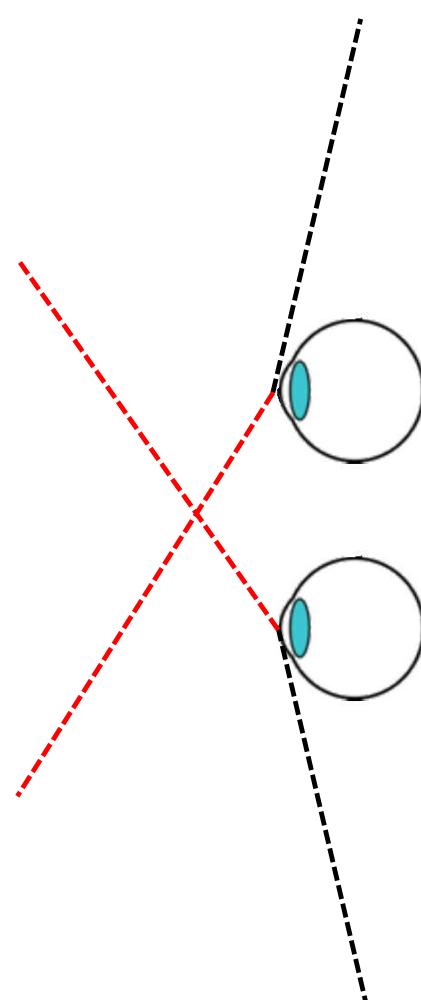
~200 deg



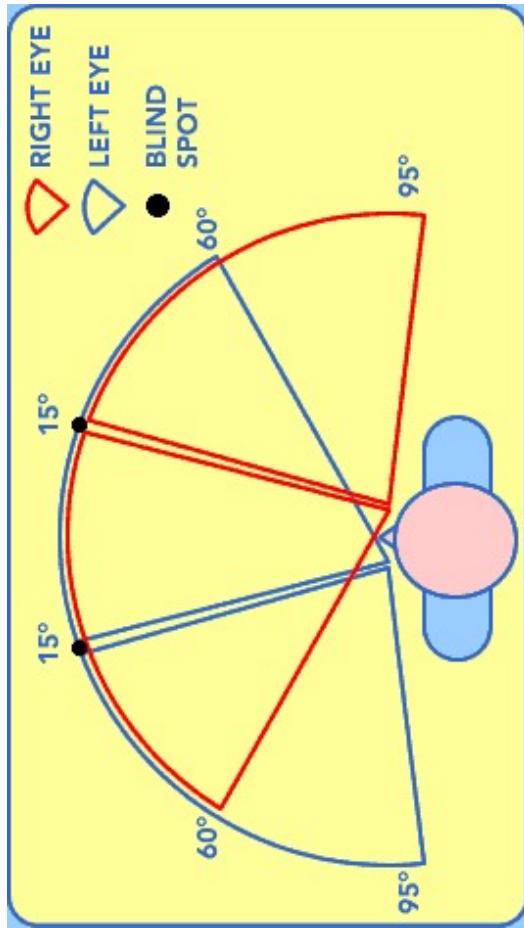
Visual Field



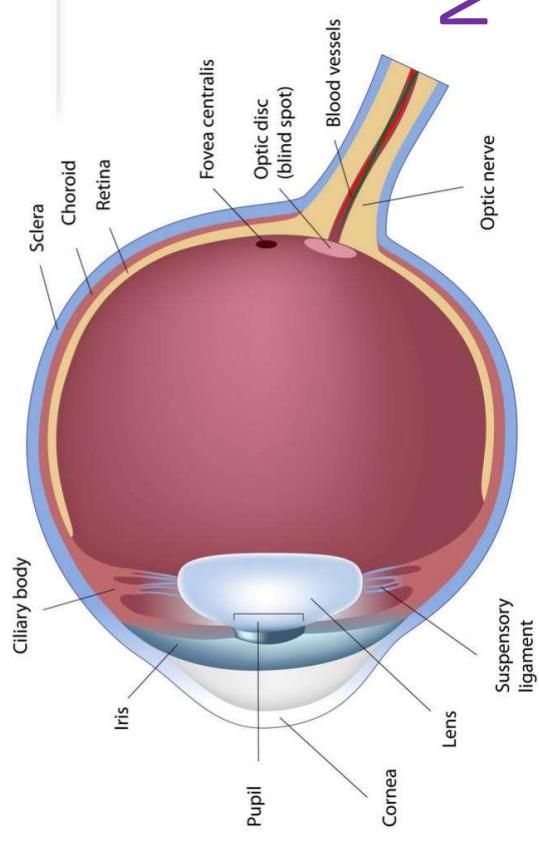
~120 deg



Visual Field



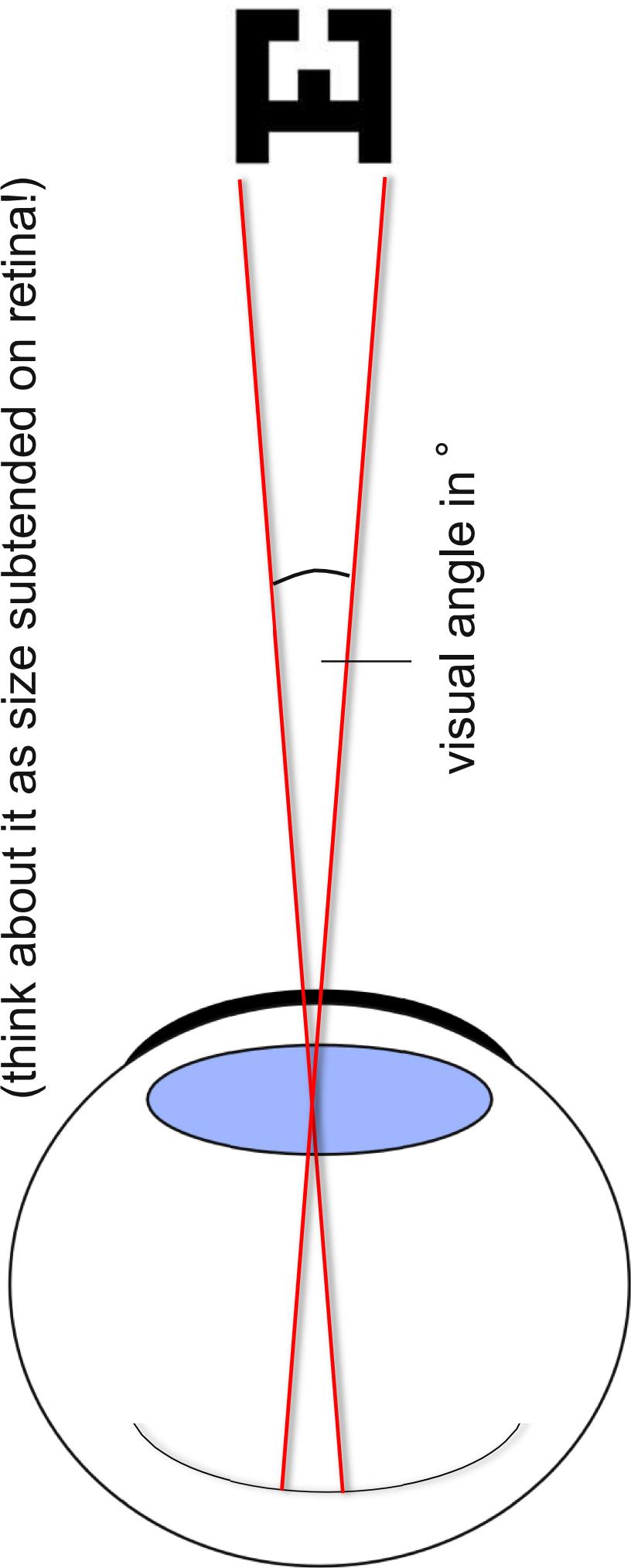
Human Eye Anatomy



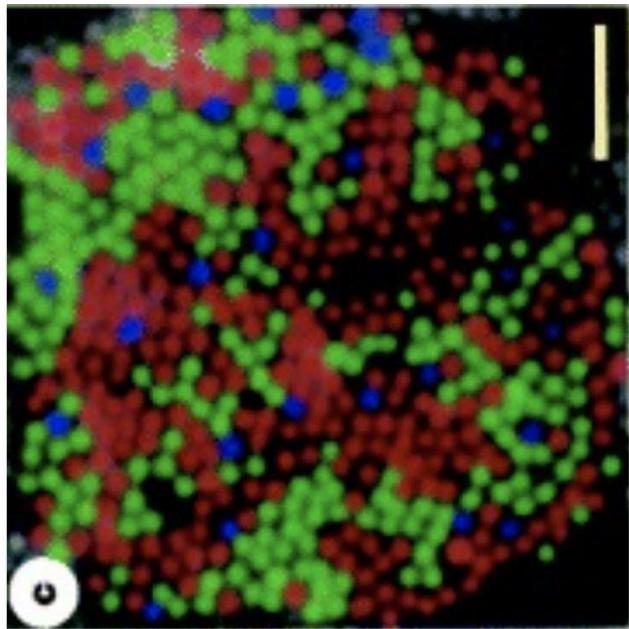
NO photoreceptor exists

Visual Angle

- vision scientists often measure size in visual angle
- visual angle \approx object size / object distance in degree
(think about it as size subtended on retina!)



Visual Acuity



5 arcmin visual angle

each photoreceptor
 $\sim \frac{1 \text{ arc min}}{\text{of visual angle}}$ (1/60 of a degree)

E P 1 20/200
T O Z 2 20/100
L P E D 3 20/70
P E C F D 4 20/50
E D F C Z T 5 20/40
F E L O P Z D 6 20/30
D E F P O T E C 7 20/25
L E F O D P C T 8 20/20
F D P L T C E O 9
F E Z O T O D T 10
11

characters are 5 arc min of visual angle, need to resolve 1 arc min to read

Retina VR Display – What does it Take?

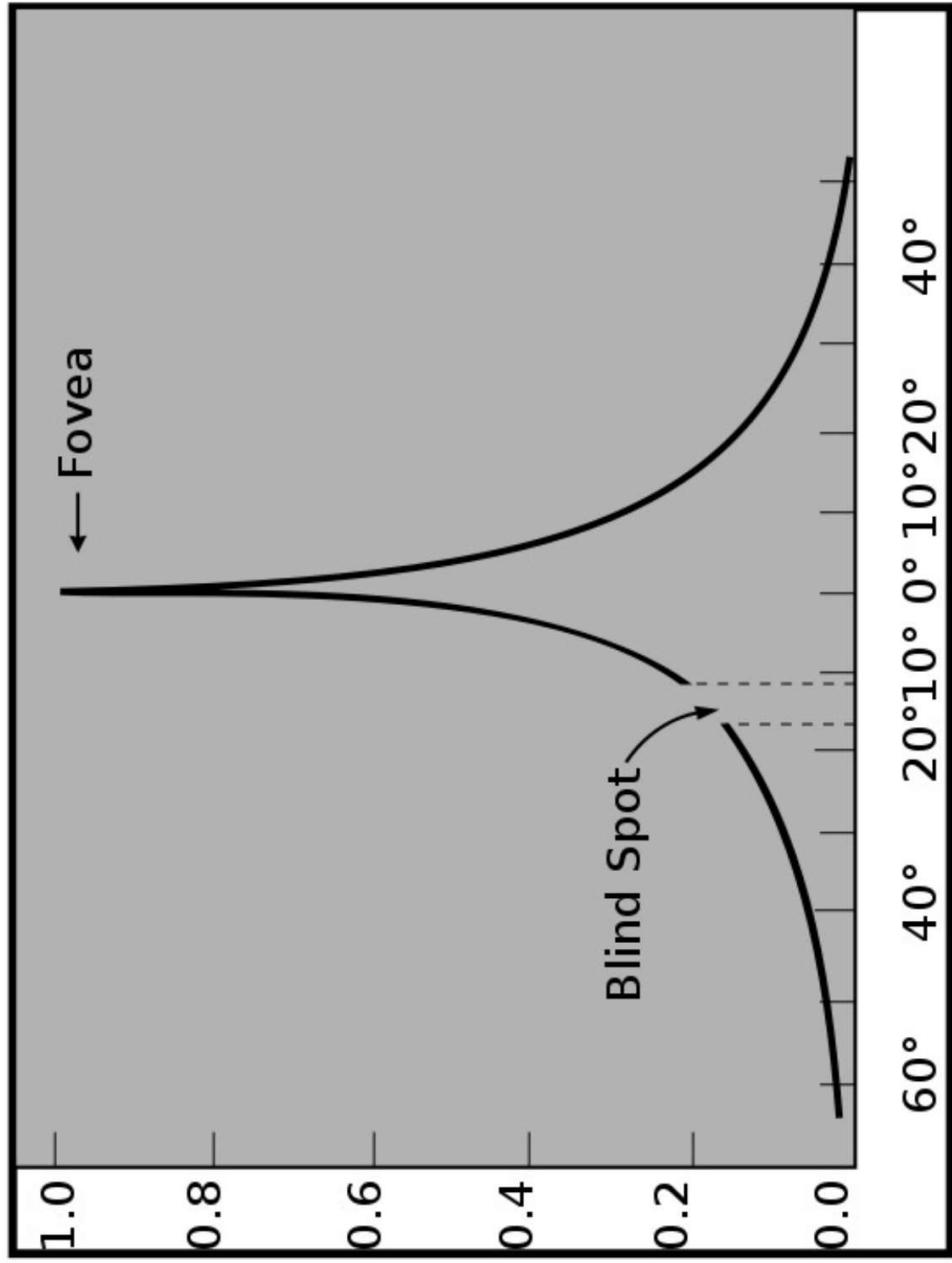
need per eye:

$$\begin{aligned} & 150^\circ \times 135^\circ \text{ with pixels covering } 1 \text{ arc min of visual angle} \\ & = 9000 \times 8100 \text{ pixels (probably 2-3x of that in practice)} \end{aligned}$$

biggest challenge: bandwidth

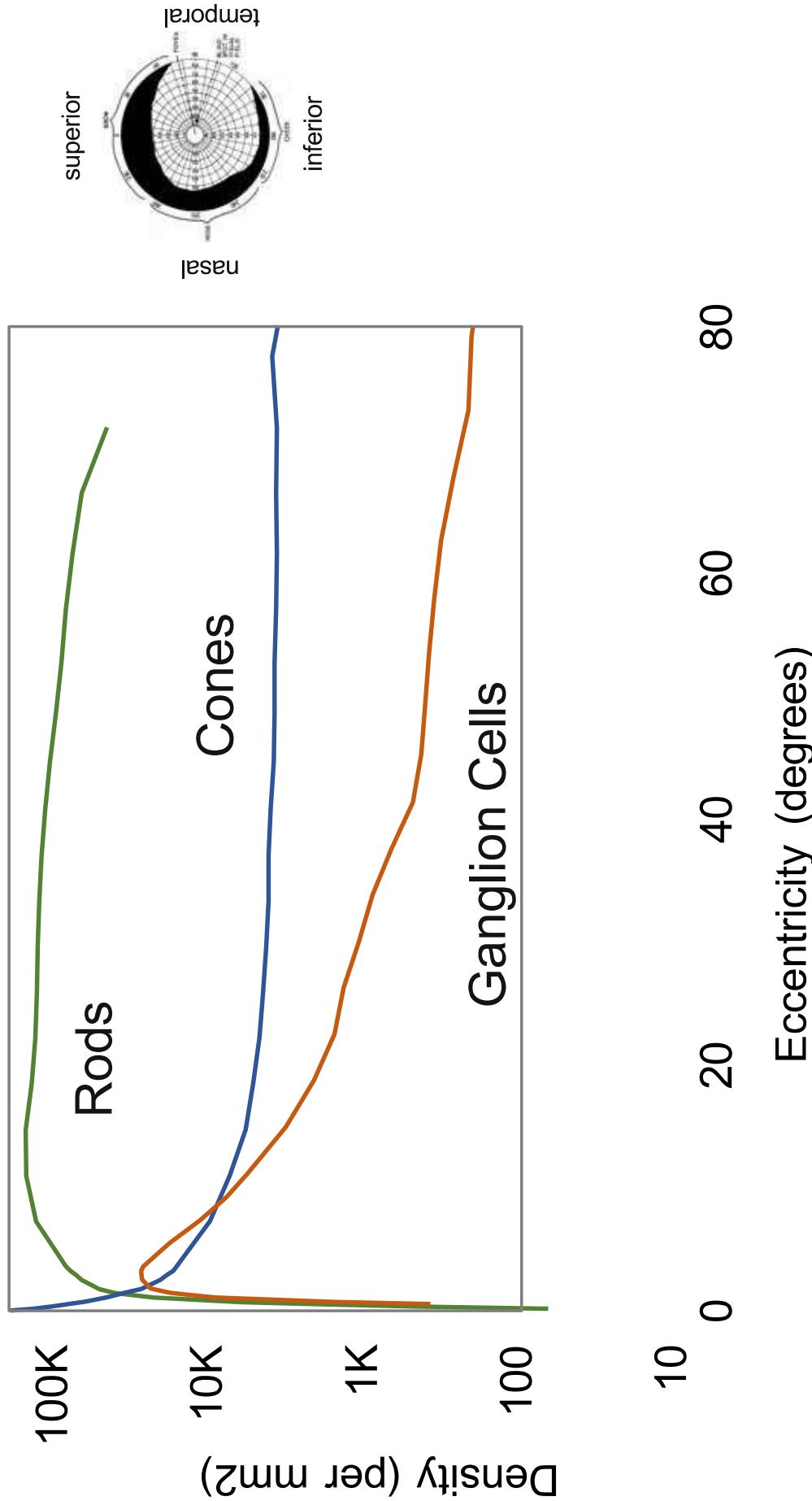
- capture or render stereo panoramas or images at that resolution
- compress and transmit huge amount of data
- drive and operate display pixels

Relative Acuity Over Retina

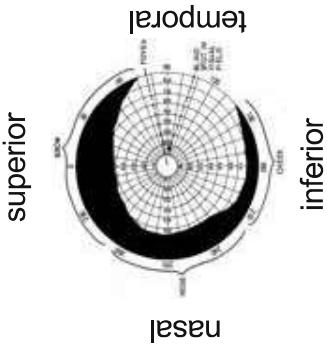
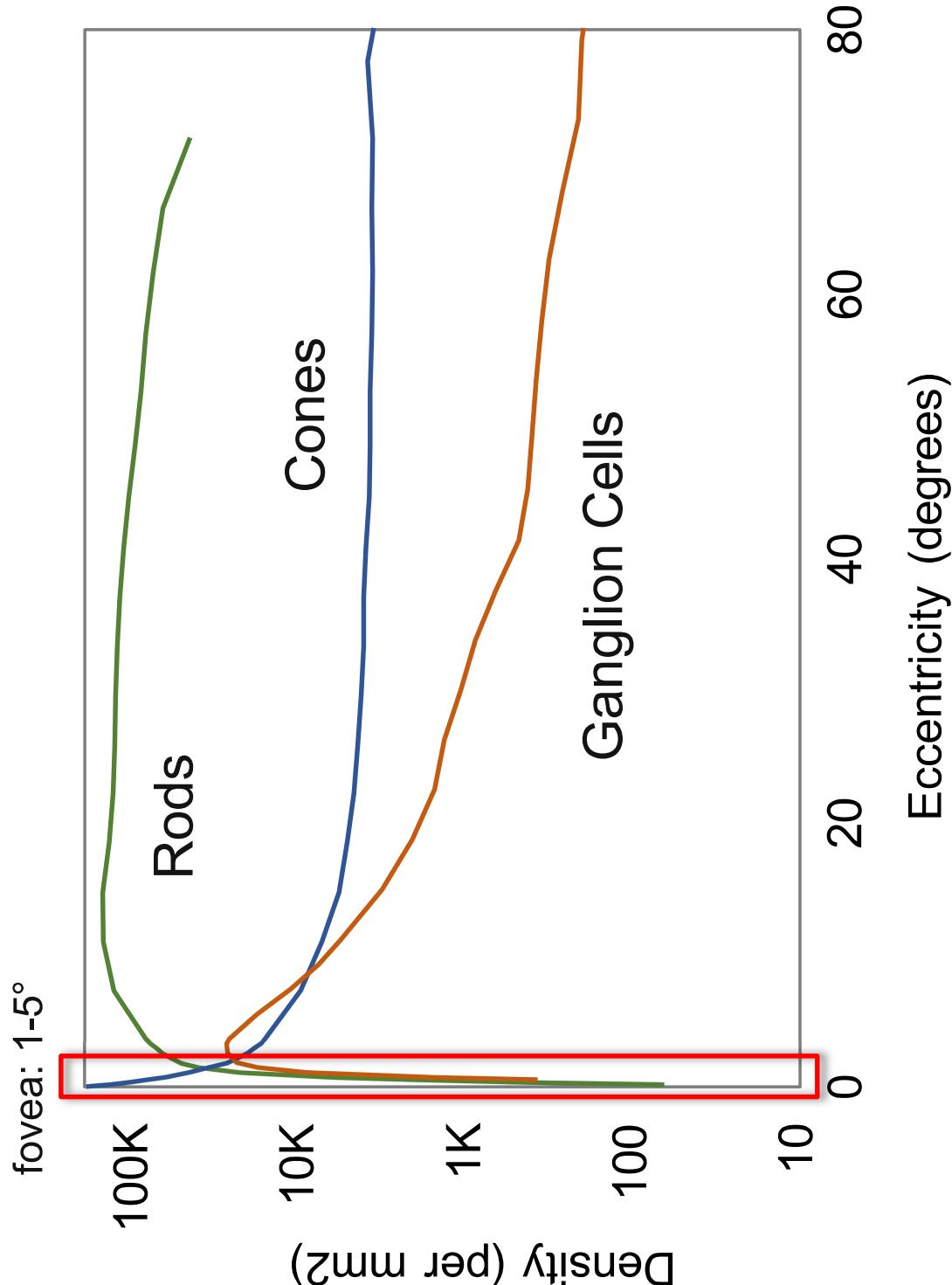


Eccentricity (i.e., distance to fovea in degrees of visual angle)

Density of Photoreceptors on Retina



Density of Photoreceptors on Retina



Acuity Over Retina / MAR

acuity falls off due to:

- reduced receptor and ganglion cell density
- reduced optical nerve “bandwidth”
- reduced “processing” devoted to periphery in the visual cortex

Acuity Over Retina / MAR

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- reduced receptor and ganglion cell density
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MAR: minimum angle of resolution in deg/cycle

$$\omega_0 = (1 / 48)^\circ \quad \text{somewhere between 20/20 (30 cycles per degree) and 20/10 (60 cycles per degree)}$$

slope

$$m = 0.022 - 0.034^\circ \quad \begin{array}{l} \text{range of acceptable -} \\ \text{equivalent for observed image} \\ \text{quality} \end{array}$$

$$\omega = me + \omega_0$$

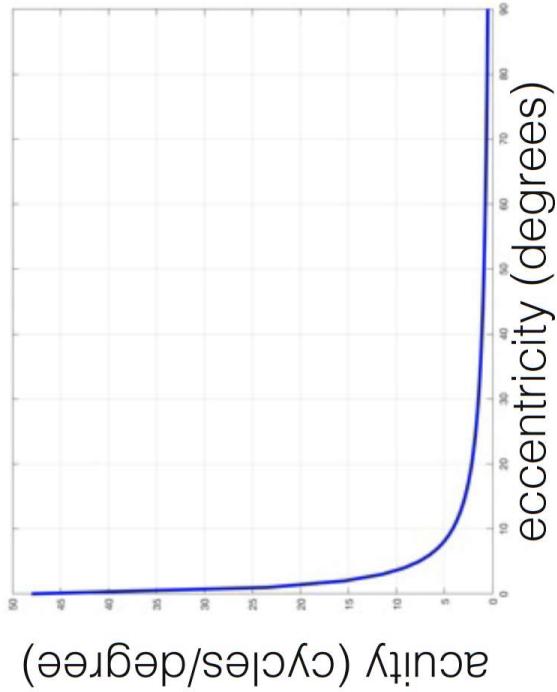
$\downarrow \qquad \downarrow$

eccentricity in degrees

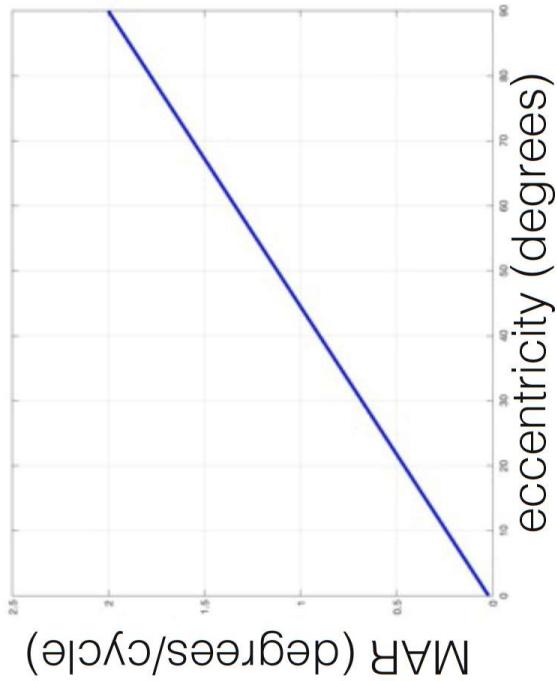
smallest resolvable angle at fovea in deg/cycle

Acuity Over Retina / MAR

MAR
Acuity ($= 1/\text{MAR}$)



MAR



MAR slope

$$\omega = me + \omega_0$$

$\downarrow \quad \uparrow$

eccentricity in degrees

smallest resolvable angle at fovea in deg/cycle





Reading/final project options

[1] **Foveated 3D graphics**

Guenther et al. 2012

<https://dl.acm.org/doi/10.1145/2366145.2366183>

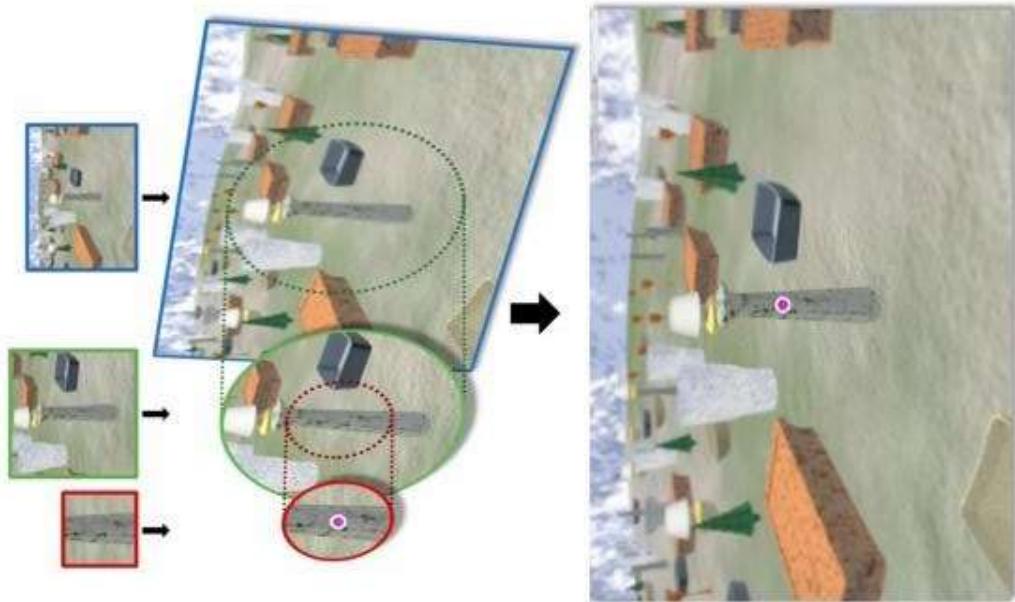
[2] **Towards foveated rendering for gaze-tracked virtual reality**

Patney et al. ACM Trans. Graph 2016

<https://dl.acm.org/doi/abs/10.1145/2980179.2980246>

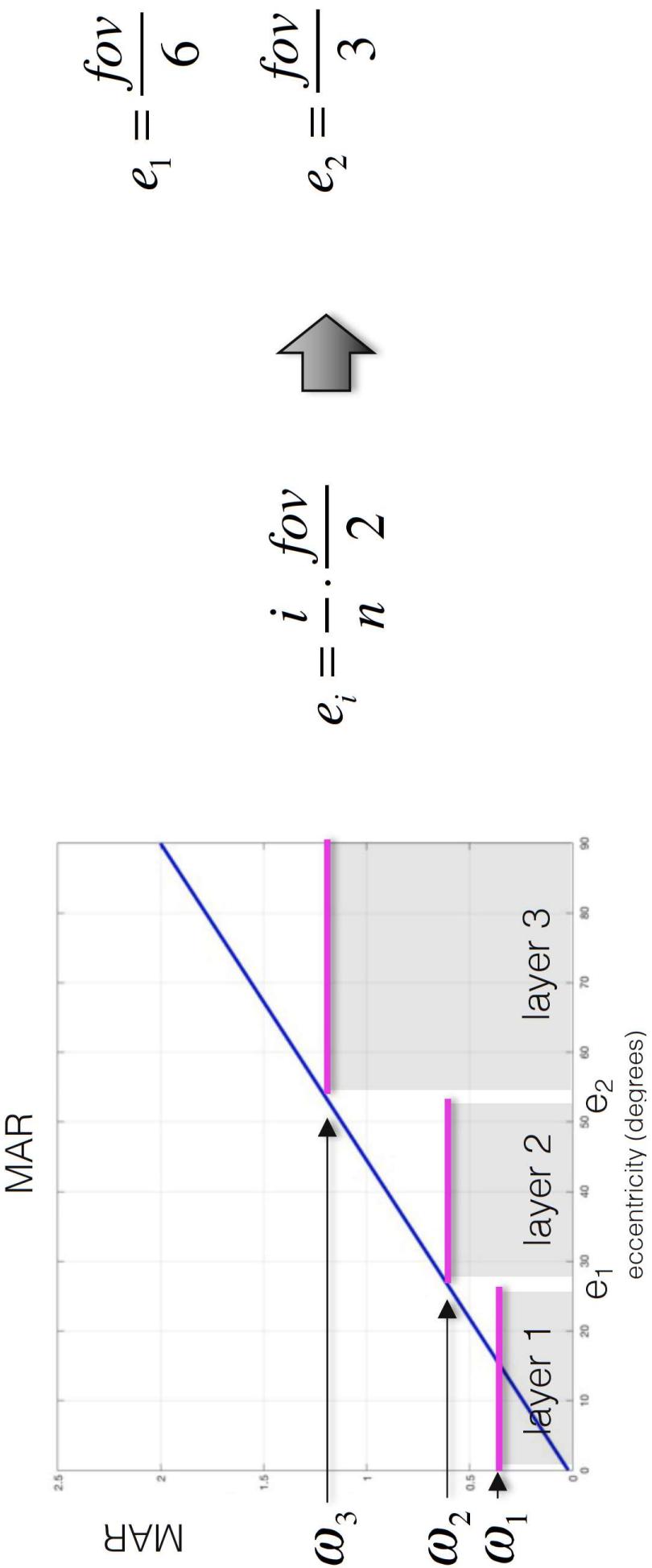
Foveated Rendering

- Guenter et al. 2012: split image into n layers,
e.g. inner (foveal, 1), middle (2), outer (3)
- render image in each zone with progressively
lower resolution
- goals: save computation & bandwidth!



Foveated Rendering

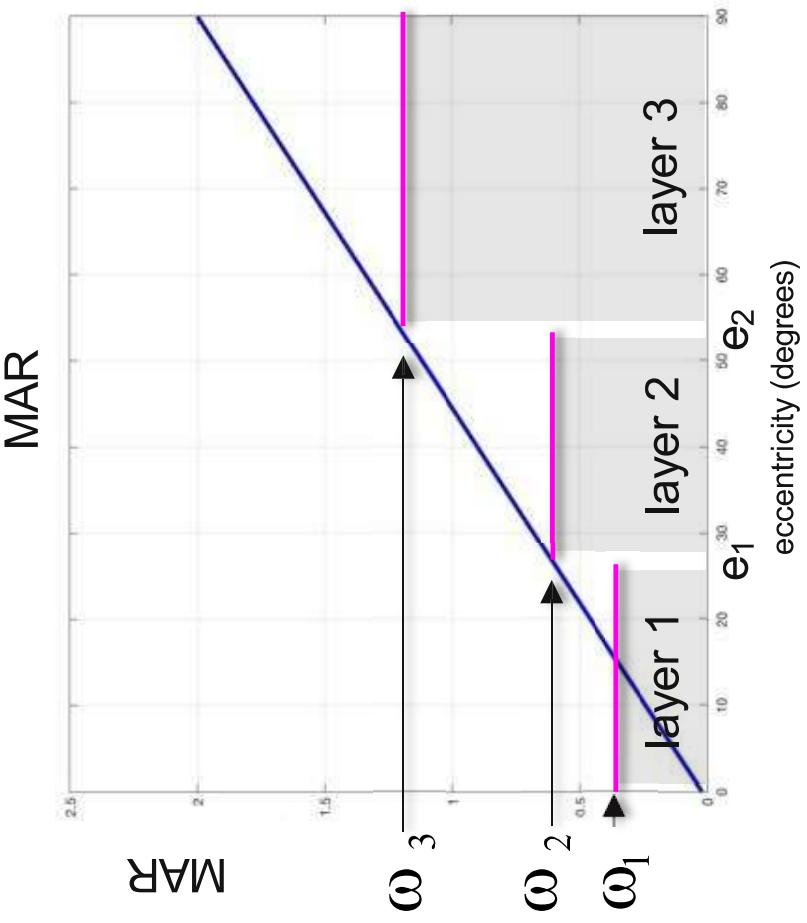
- Guenter et al. 2012: split image into n layers,
e.g. inner (foveal, 1), middle (2), outer (3)



Foveated Rendering

ω_1 is best the display can do!

$$\text{unit of } \omega_1: \frac{\text{degrees}}{\text{cycle}} = \frac{\text{degrees}}{2 \cdot \text{pixel_size}}$$

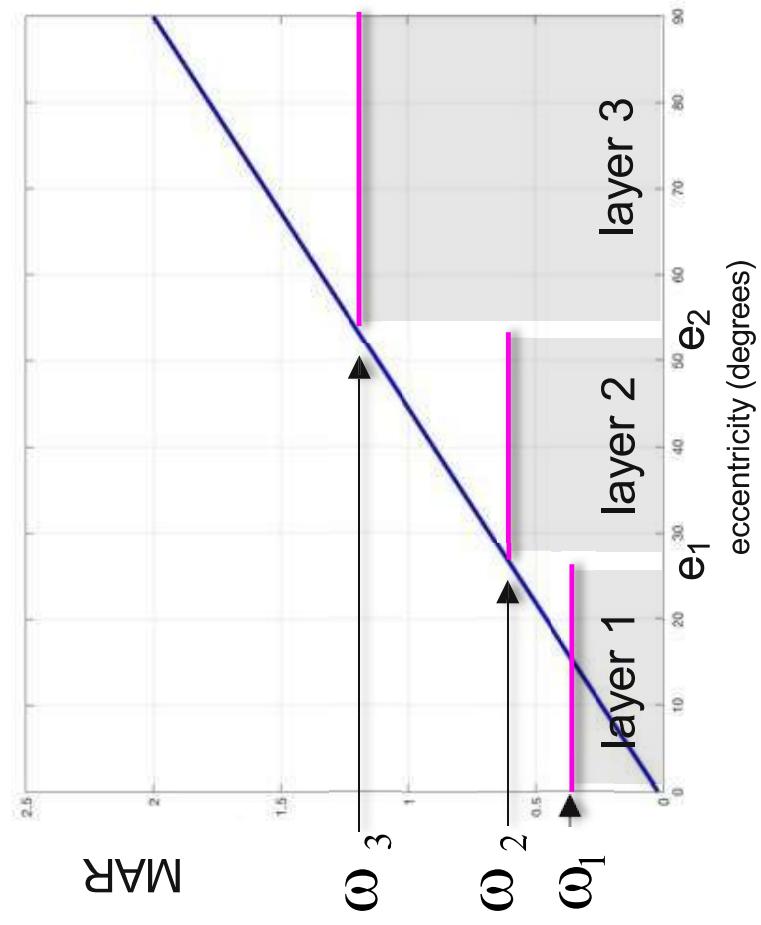
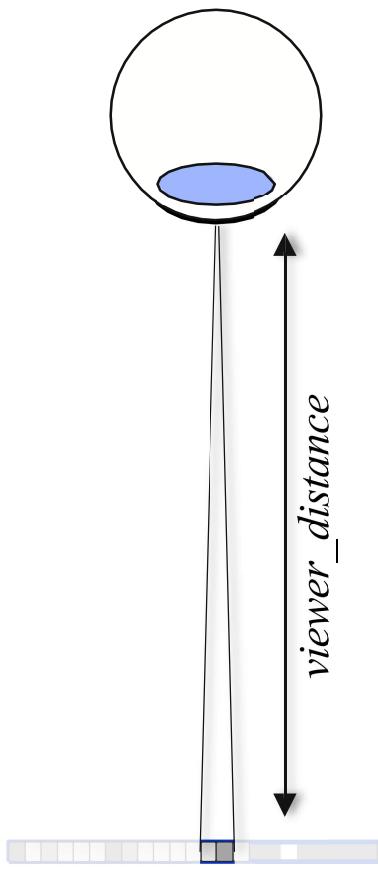


Foveated Rendering

ω_1 is best the display can do!

$$\text{unit of } \omega_1: \frac{\text{degrees}}{\text{cycle}} = \frac{\text{degrees}}{2 \cdot \text{pixel_size}}$$

$$\omega_1 = 2 \pi^{-1} \left(\frac{\text{screen_size}}{\text{screen_resolution} \cdot \text{viewer_distance}} \right) \frac{360}{2\pi}$$



Foveated Rendering

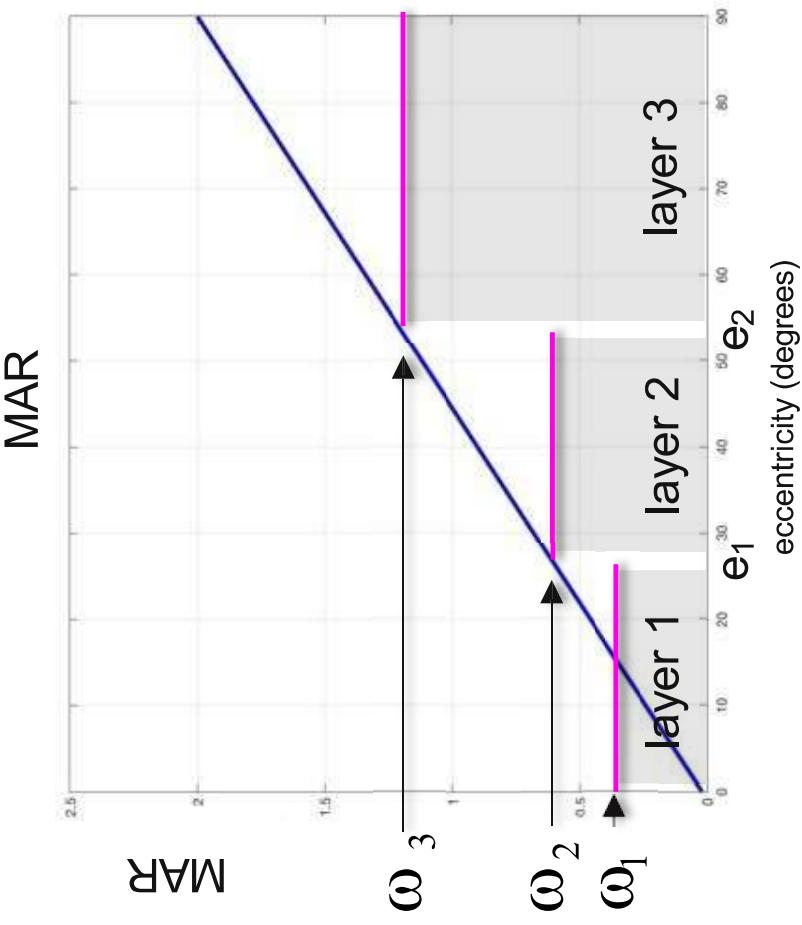
ω_1 is best the display can do!

$$\text{unit of } \omega_1: \frac{\text{degrees}}{\text{cycle}} = \frac{\text{degrees}}{2 \cdot \text{pixel_size}}$$

$$\omega_1 = 2 \text{ m}^{-1} \left(\frac{\text{screen_size}}{\text{screen_resolution} \cdot \text{viewer_distance}} \right) \frac{360}{2\pi}$$

screen_size is either screen width or height (same units as viewer_distance)

screen_resolution is either number of horizontal pixels or vertical pixels of the screen (same dimension as screen_size)

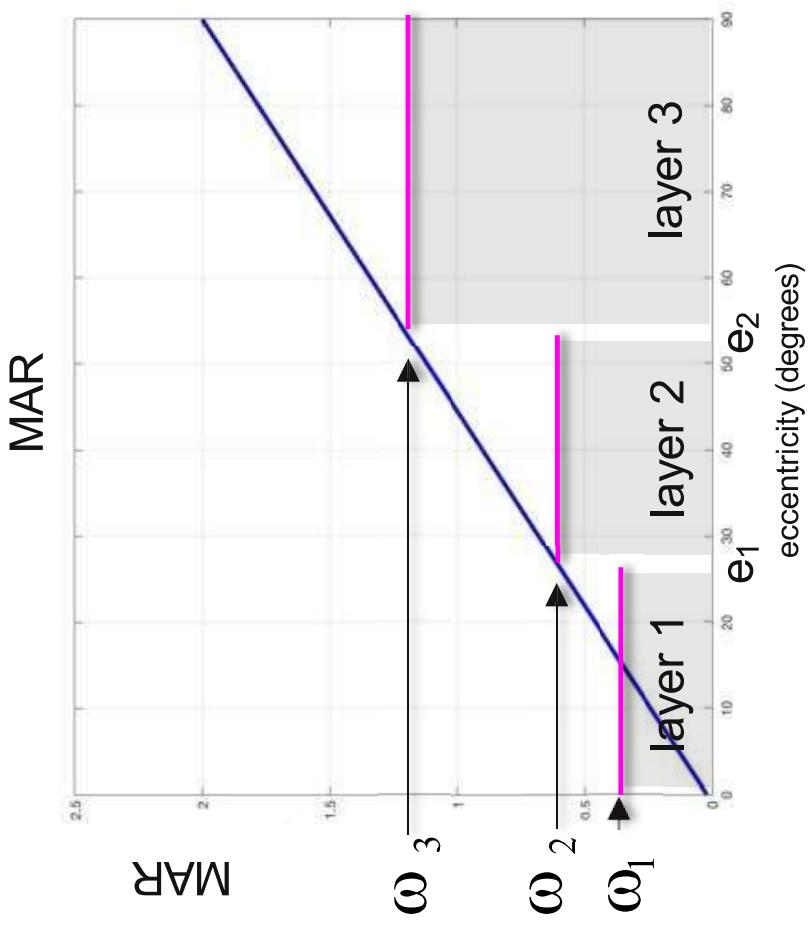


Foveated Rendering

$$\omega_1 = 2 \text{ m}^{-1} \left(\frac{\text{screen_size}}{\text{screen_resolution} \cdot \text{viewer_distance}} \right) \cdot \frac{360}{2\pi}$$

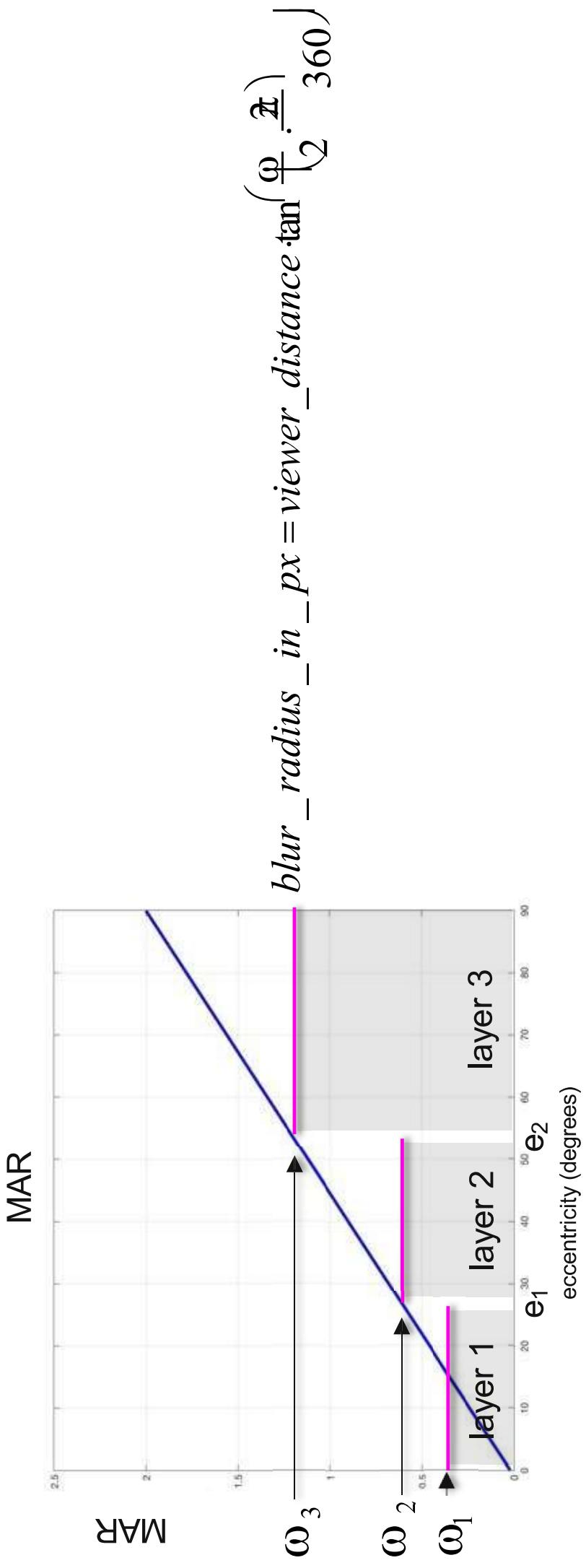
$$\omega_2 = me_2 + \varphi$$

$$\omega_3 = me_3 + \varphi$$



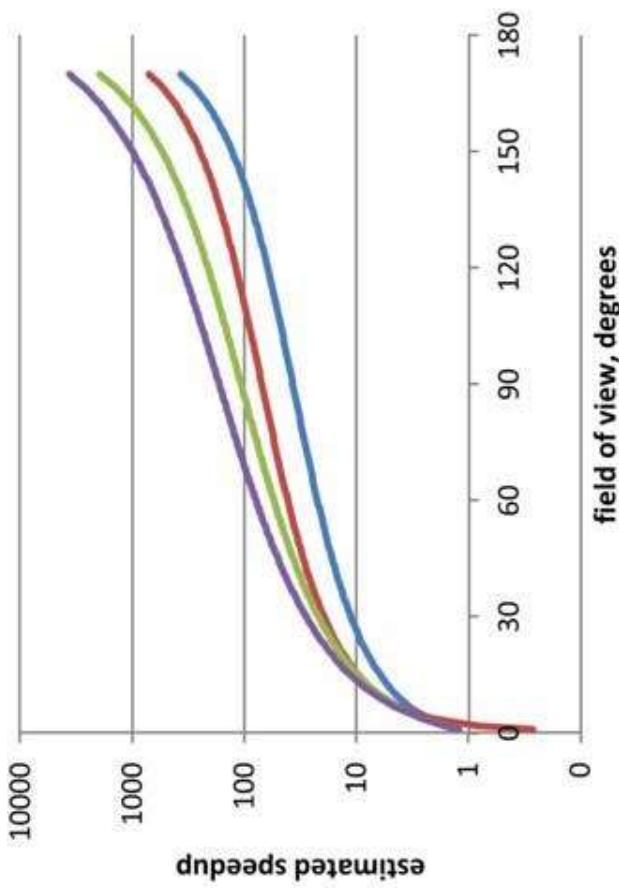
Foveated Rendering

- convert MAR (in degrees/cycle) to pixels

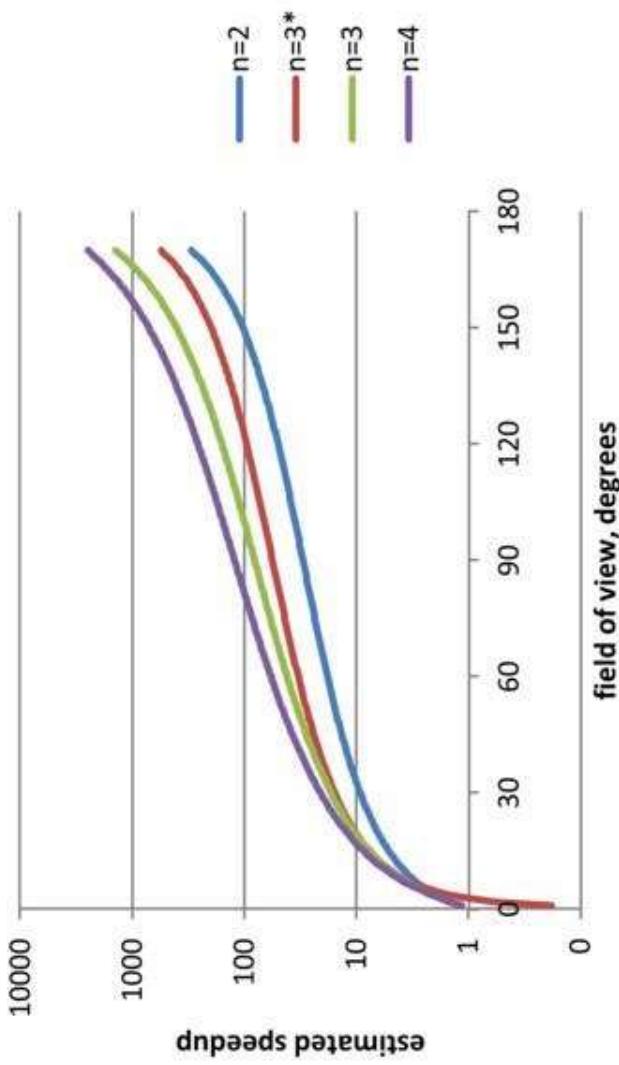


Foveated Rendering – Performance Gain

$$m = 0.028$$



$$m = 0.022$$

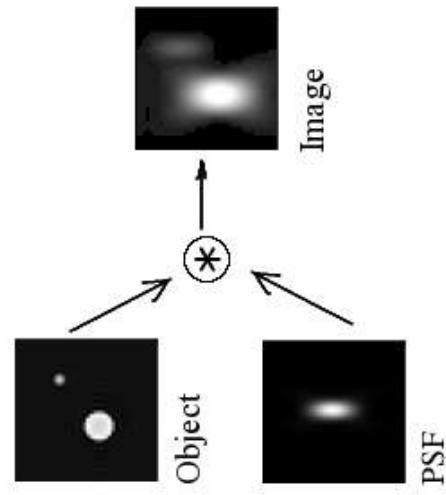
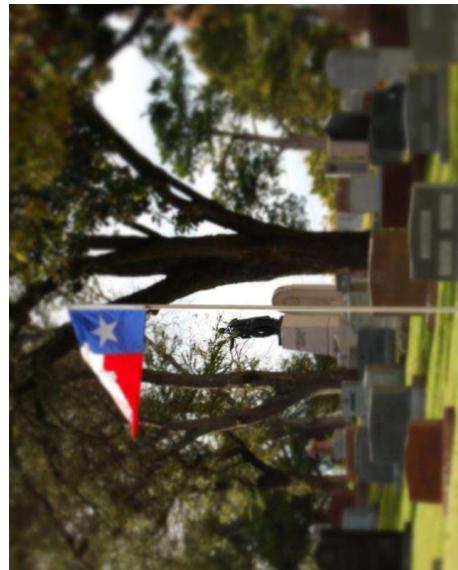


n is number of layers

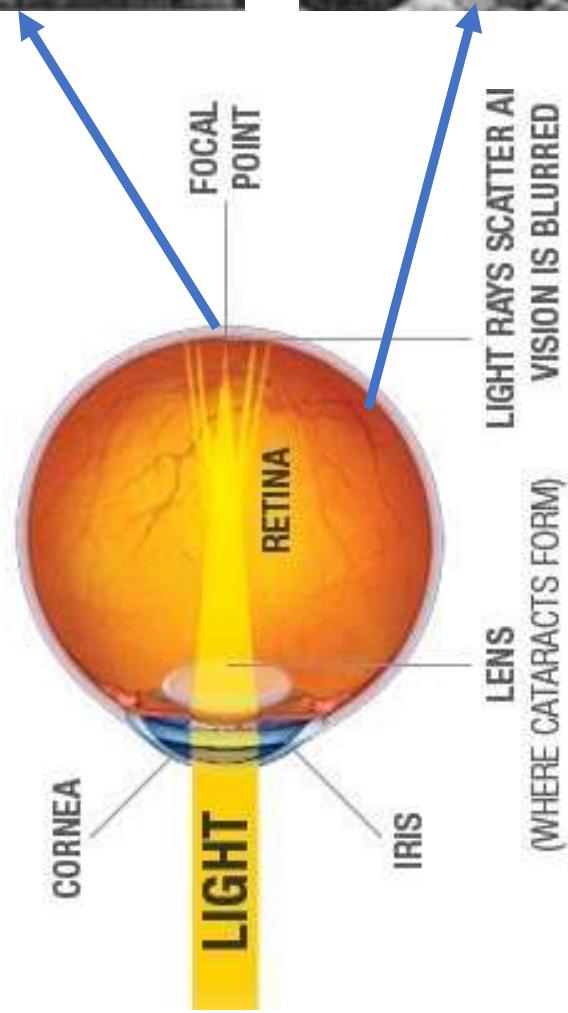
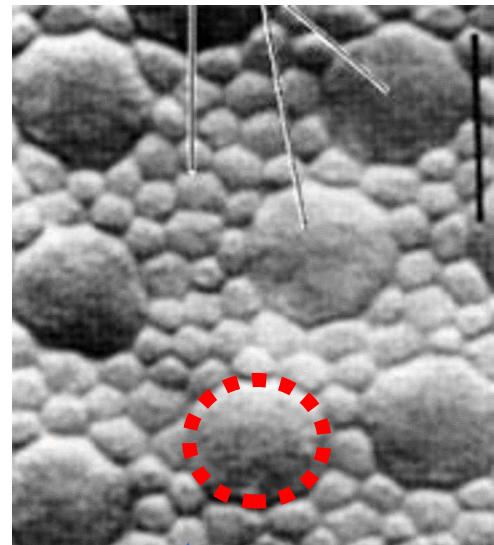
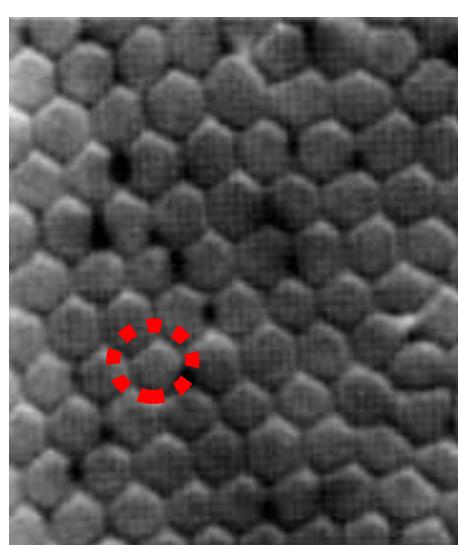
speedup is total number of display pixels / number of pixels in all layers combined

conclusion: for large fov & high-res displays, we need to shade much fewer pixels!

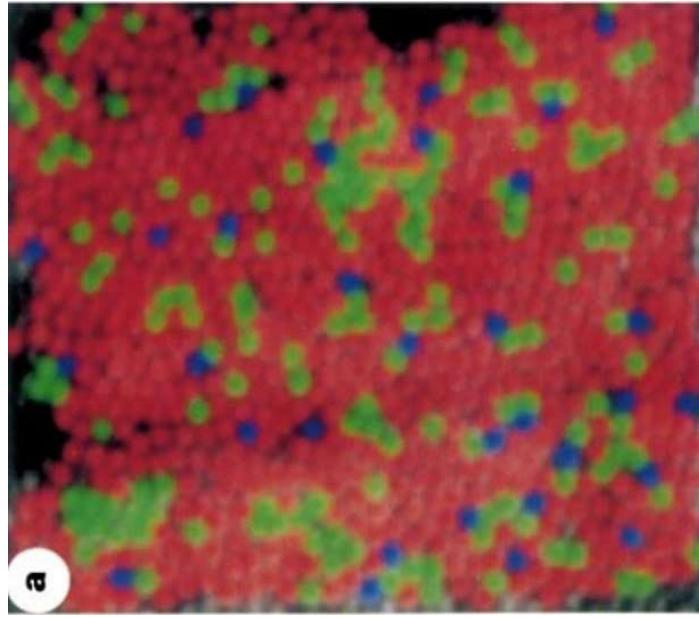
Visual Acuity



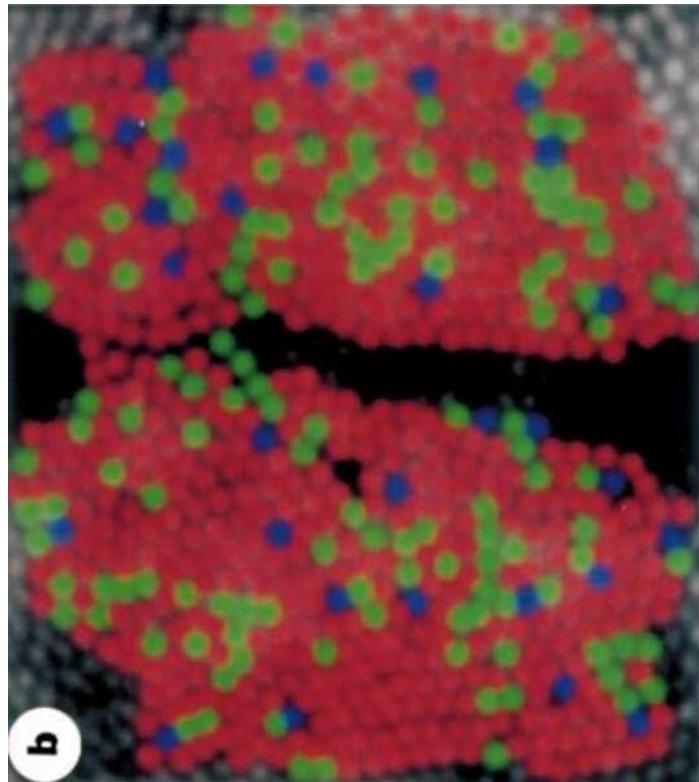
Source: Mango Optics



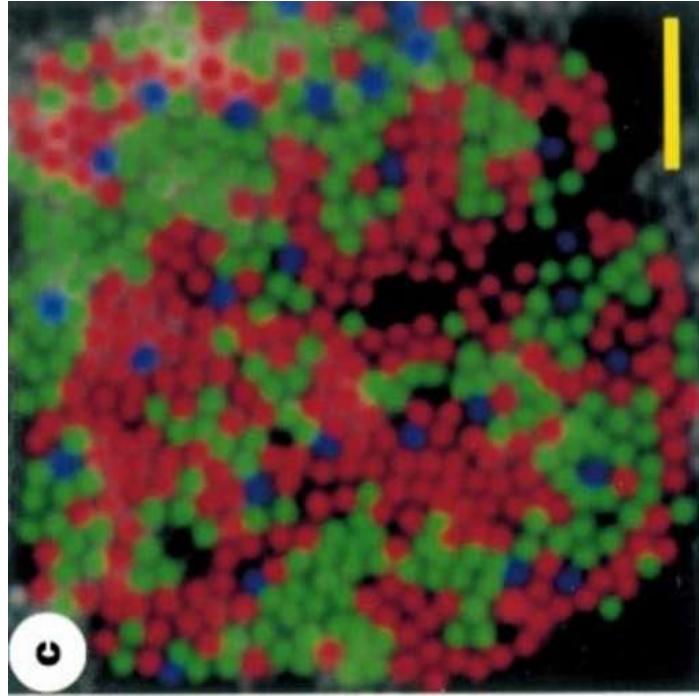
Visual Acuity



a



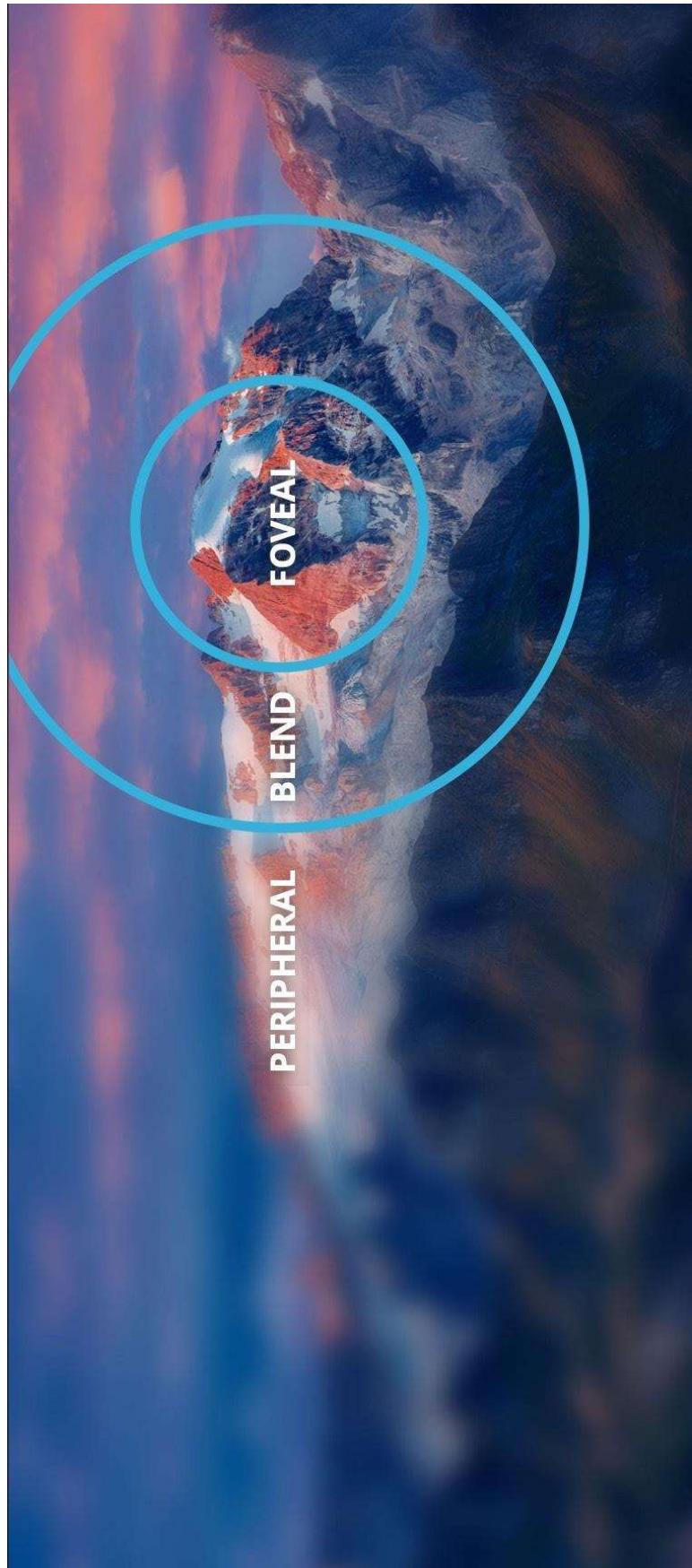
b



c

The arrangement of the three cone classes in the living human eye,
Roorda and Williams, Nature 1999

Visual Acuity



Visual Field – Find Your Own Blind Spot!

shorturl.at/fgix5

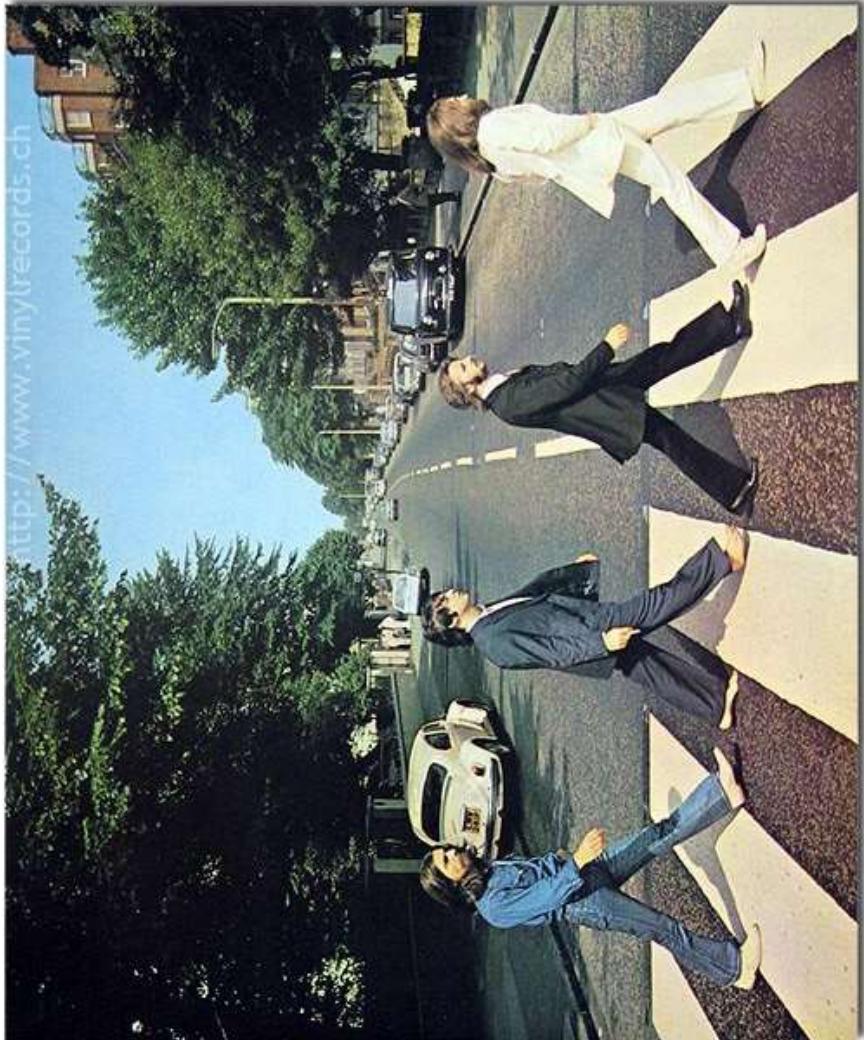
+



Depth Cues

3D Depth Cues

- Monocular vision
- Binocular vision

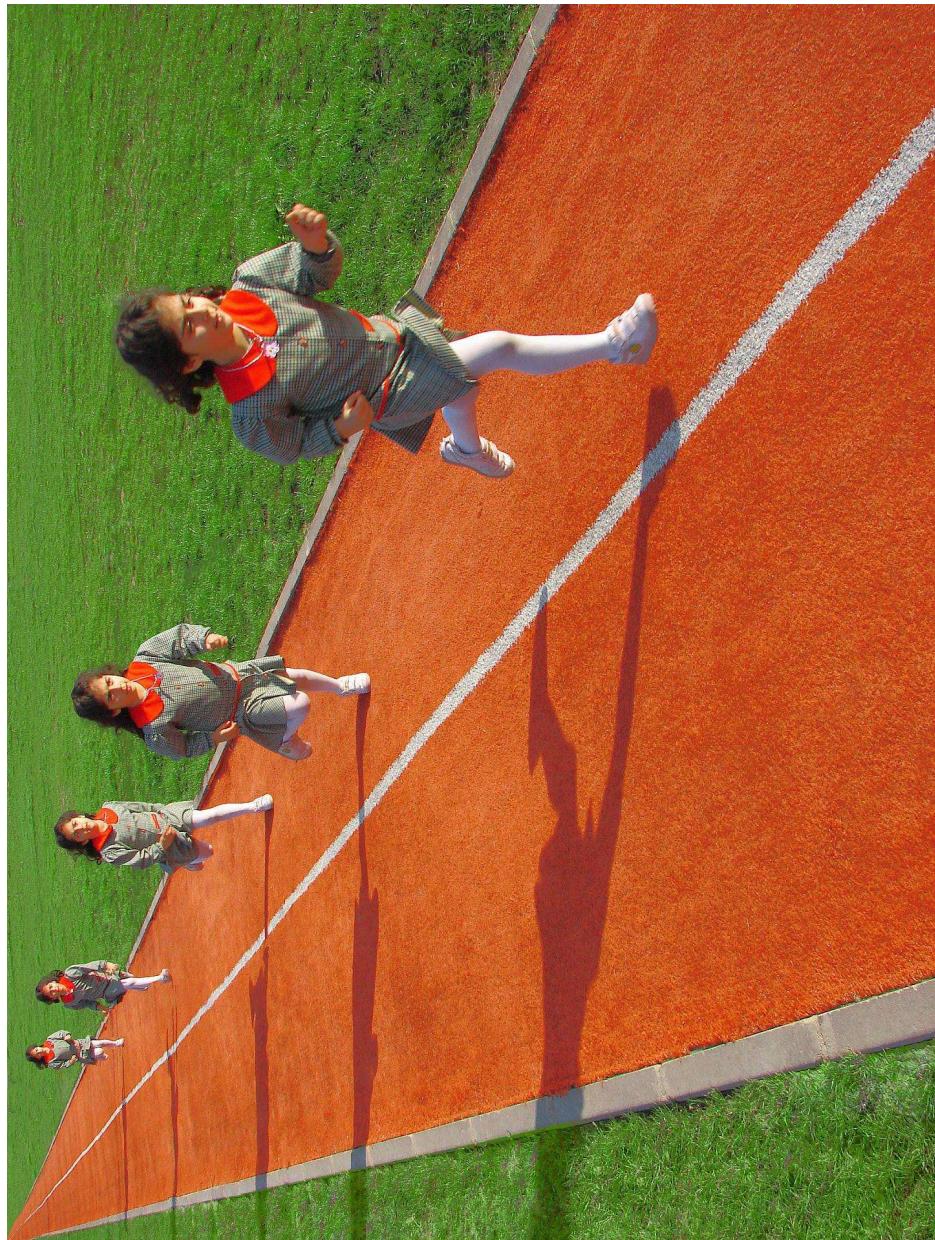


[The Beatles, Abbey Road]

Monocular Cues – Motion Parallax

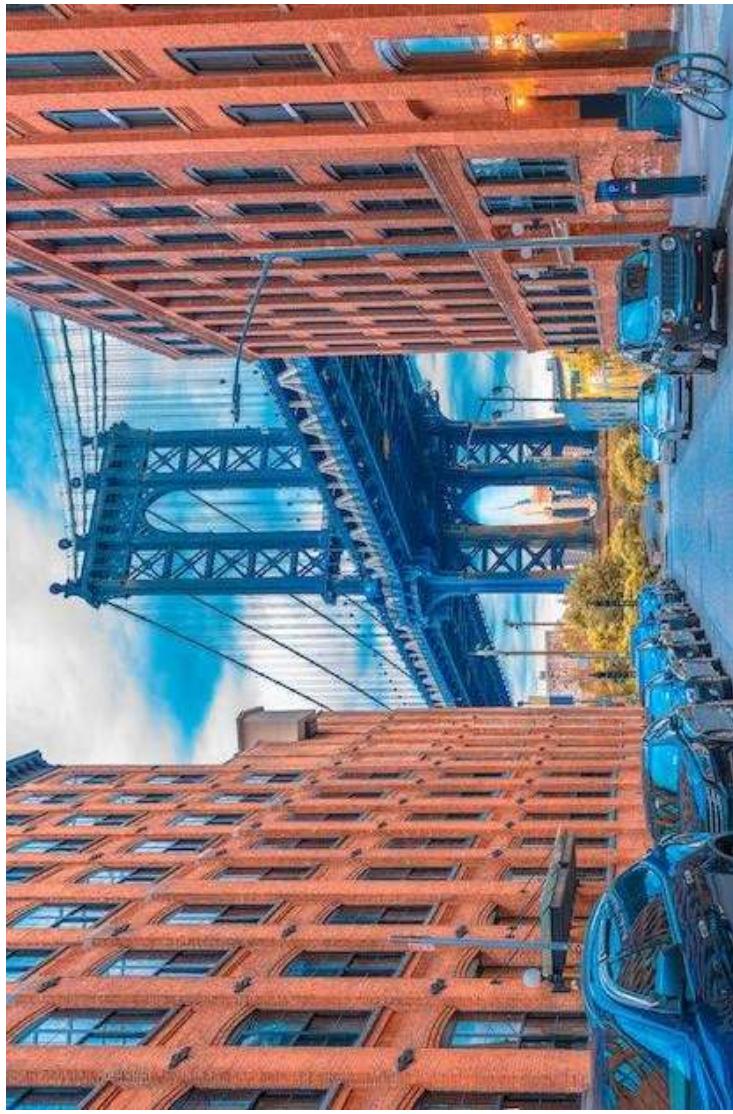


Monocular Cues – Perspective Projection

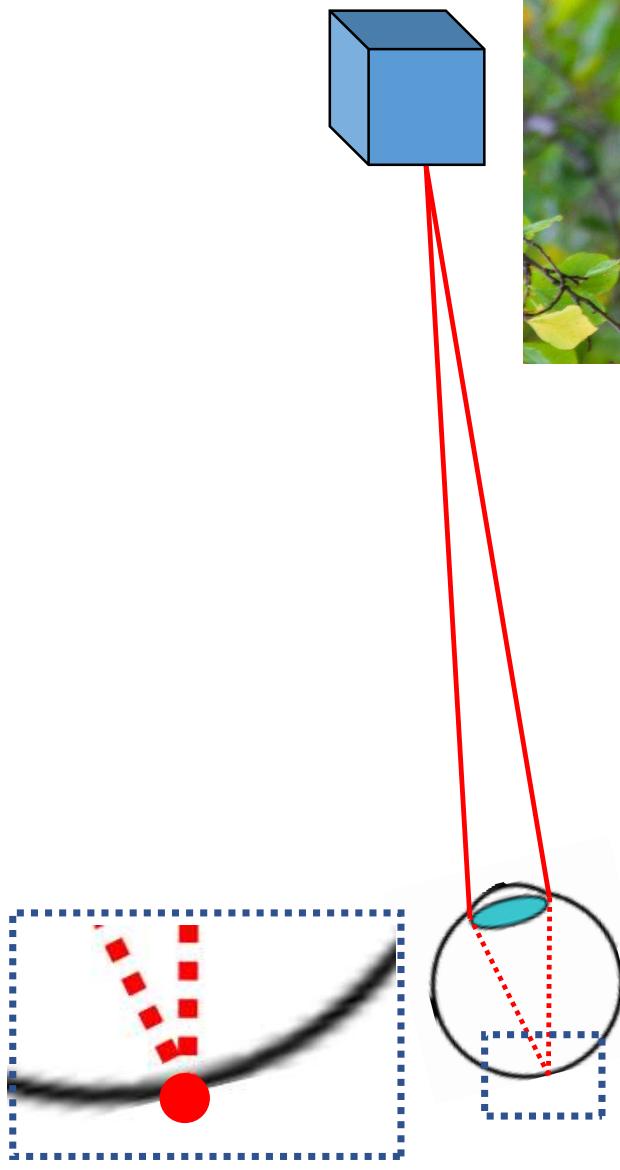


https://en.wikipedia.org/wiki/Depth_perception#/media/File:08913-Perspective_Run.jpg

Monocular Cues – Occlusion

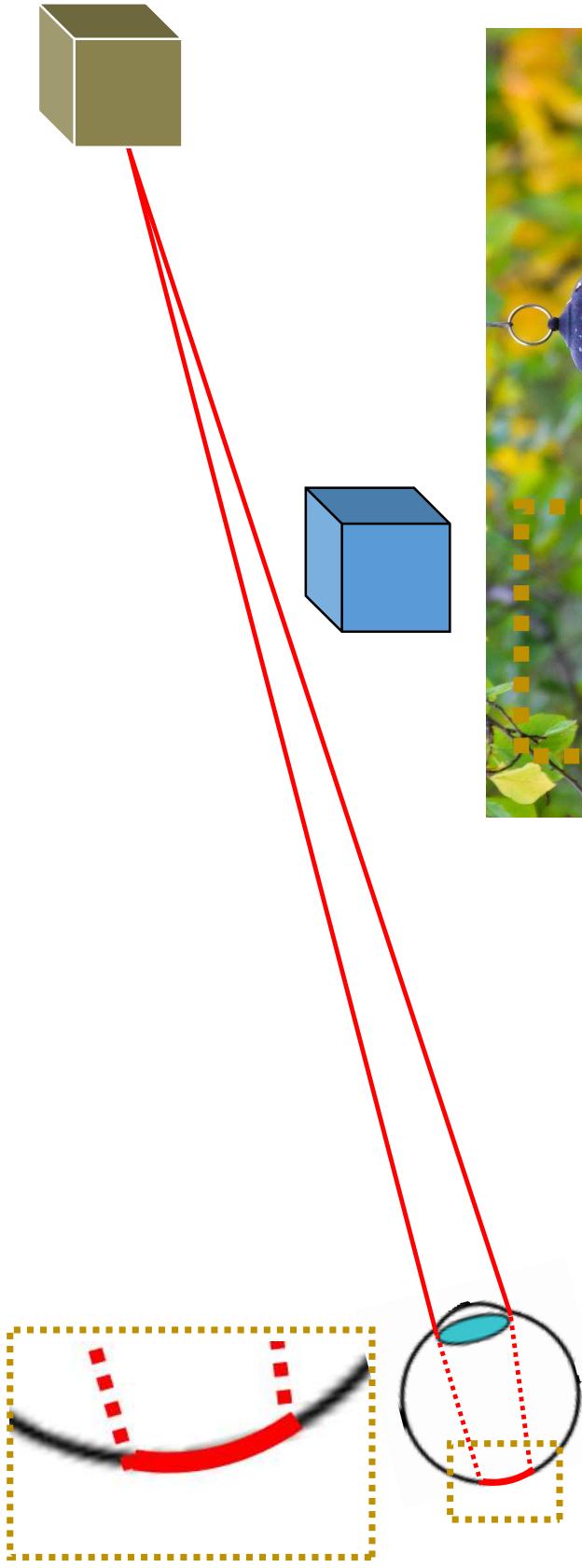


Monocular Cues – Accommodation



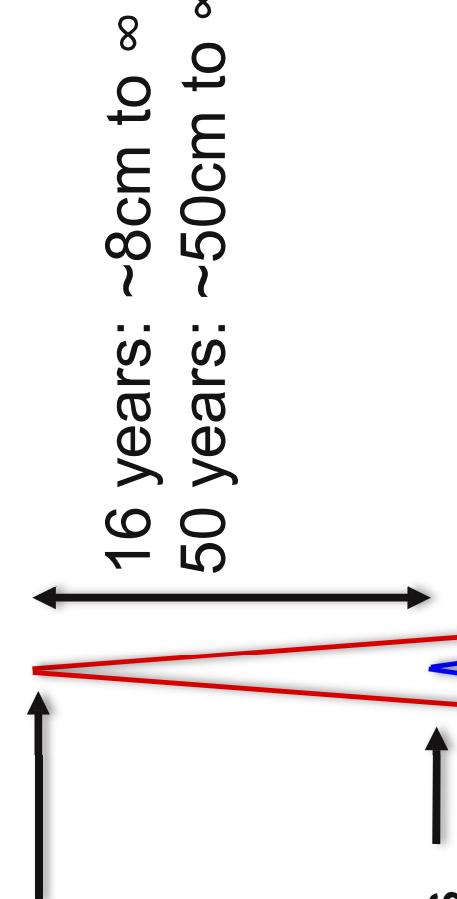
<https://www.housebeautiful.com/lifestyle/gardening/g30613155/squirrel-proof-bird-feeder/>

Monocular Cues – Accommodation



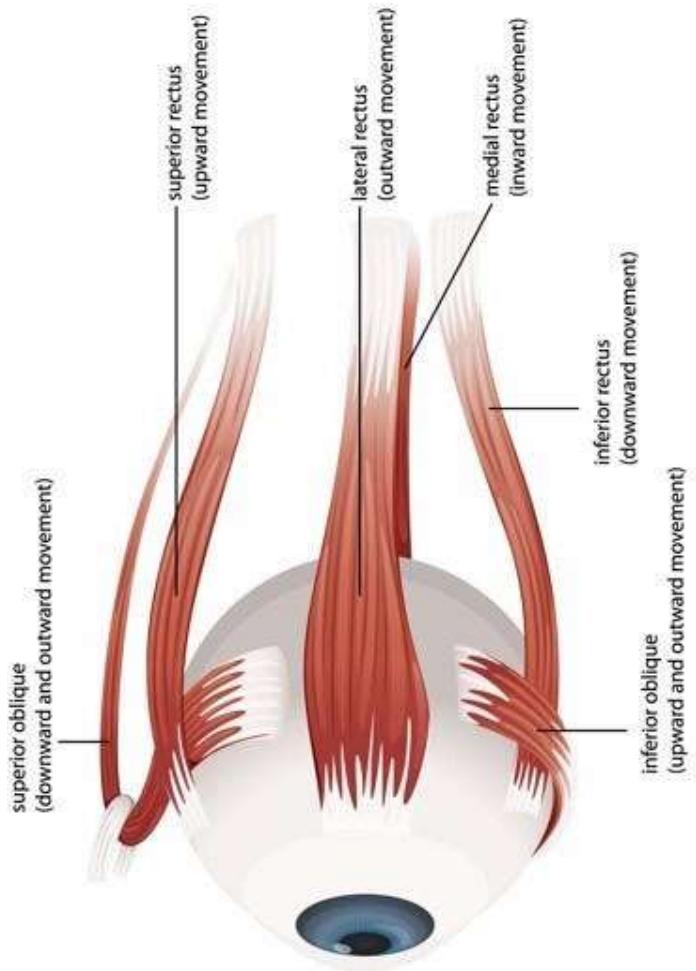
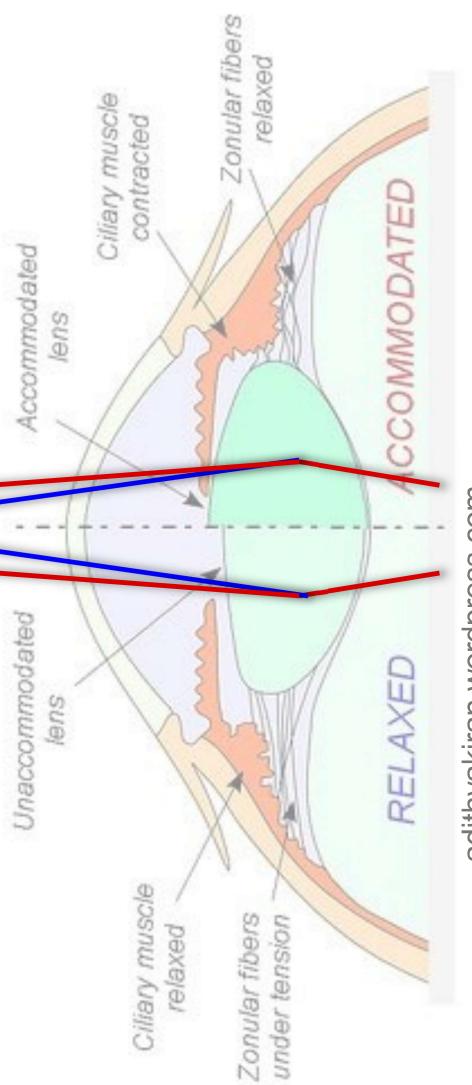
Oculomotor Processes

far focus



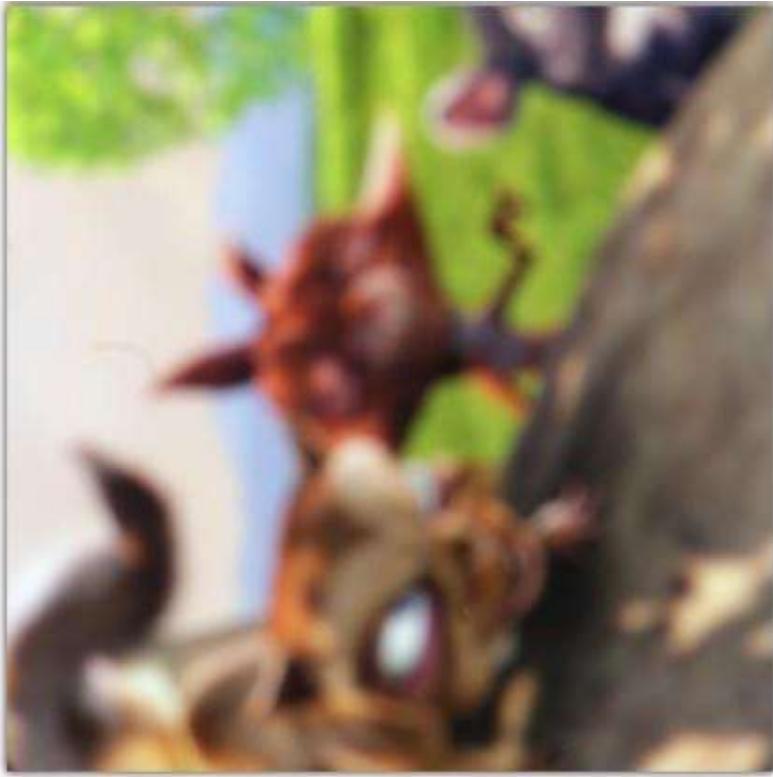
16 years: ~8cm to ∞
50 years: ~50cm to ∞ (mostly irrelevant)

near focus



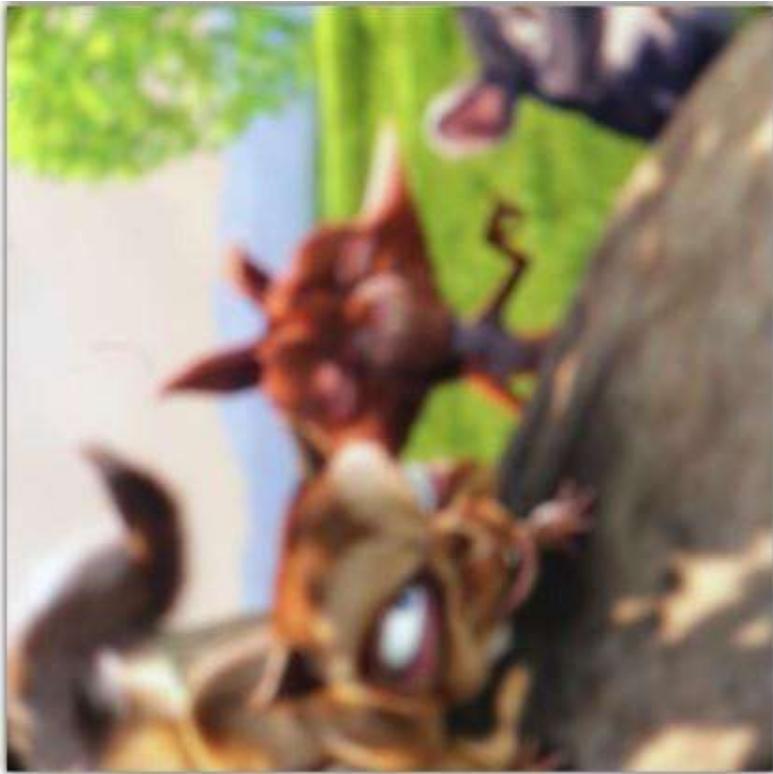
Accommodation and Retinal Blur

Conventional Display



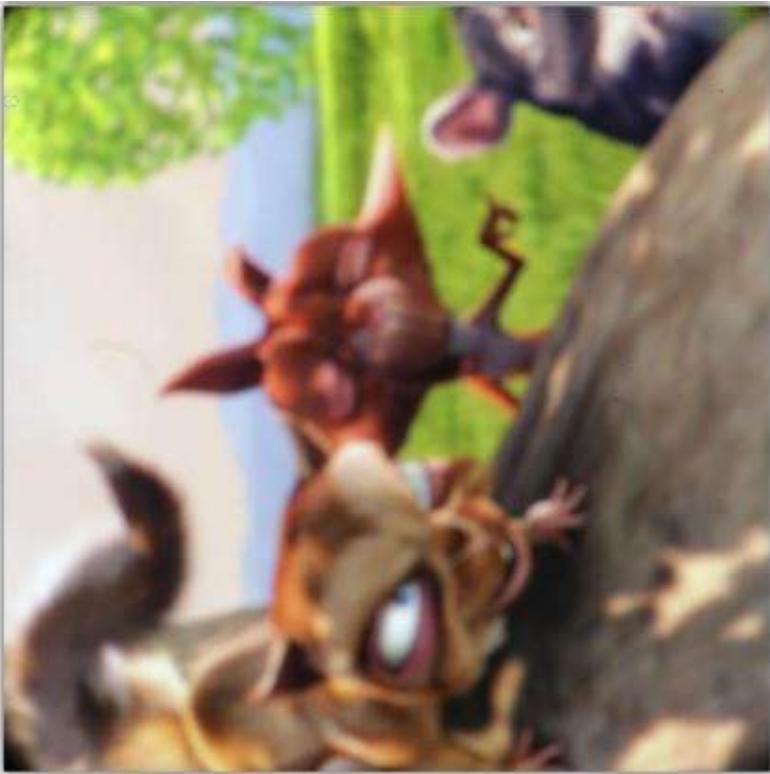
Accommodation and Retinal Blur

Conventional Display



Accommodation and Retinal Blur

Conventional Display



∞ (0D)

2m (0.5D)

0.7m (1.43D)

0.5m (2D)

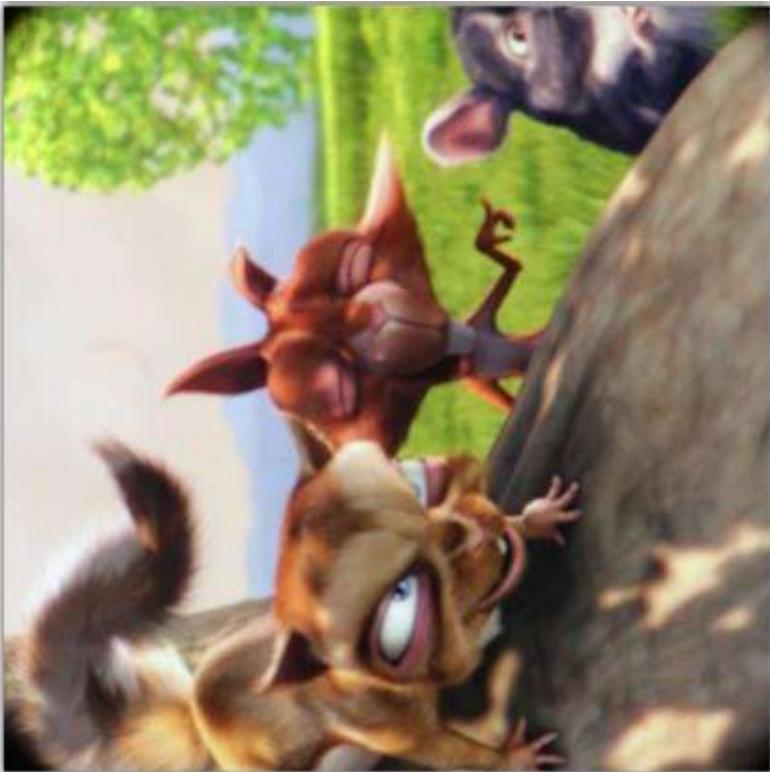
0.25m (4D) 0.3m (3.33D) 0.35m (2.86D)

virtual image of screen

1 m

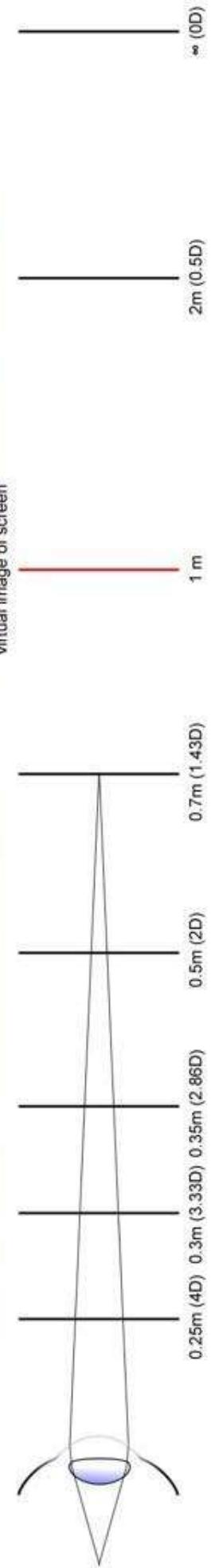
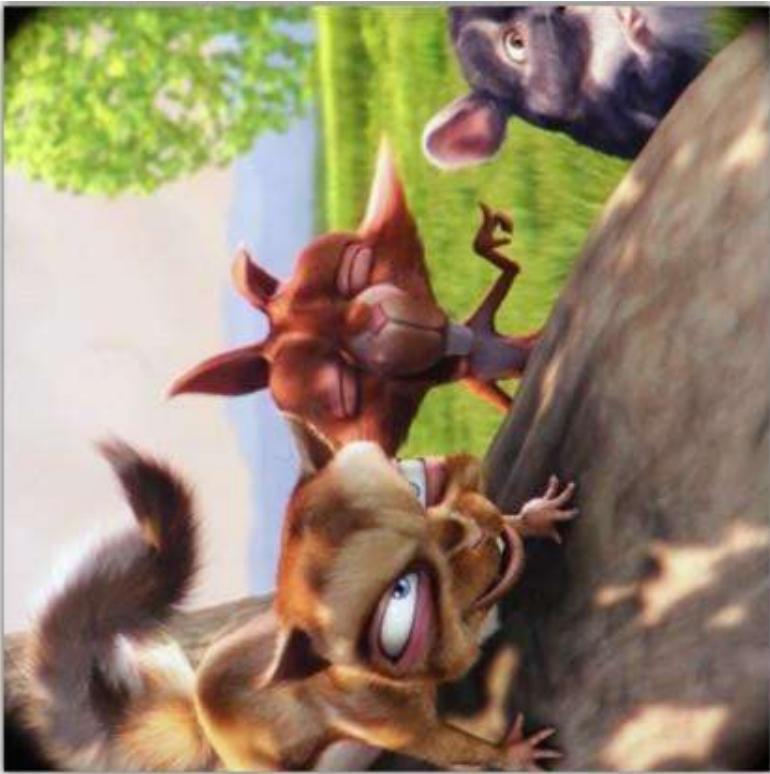
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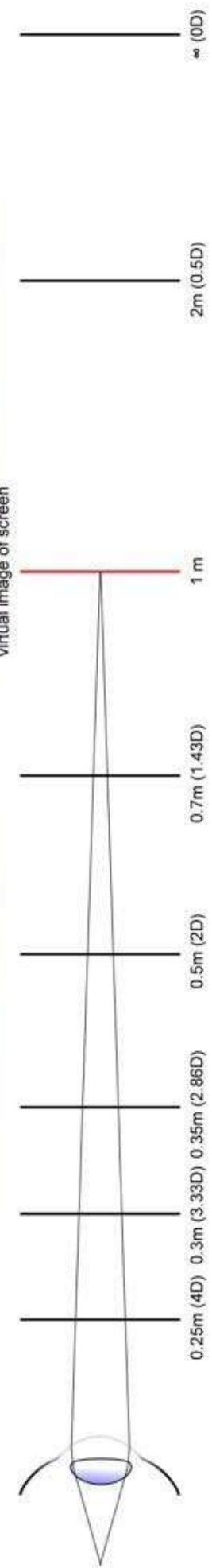
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Accommodation and Retinal Blur

Conventional Display

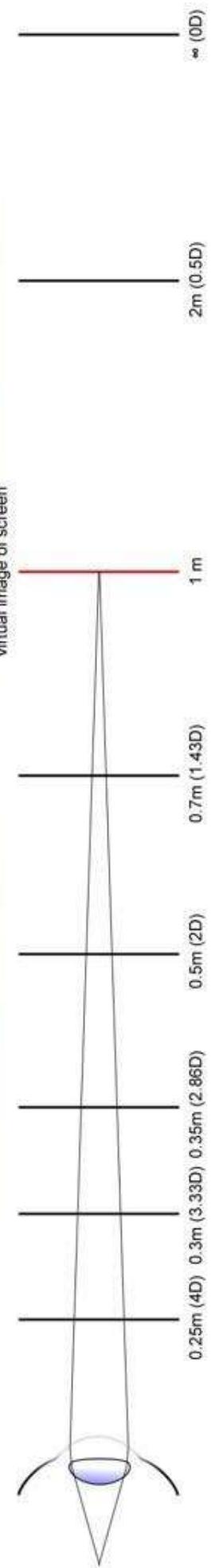


Accommodation and Retinal Blur

Conventional Display



Accommodation-dependent Point Spread Functions



Focusing Ability Degrades With Age - Presbyopia

0D (∞ cm)

4D (25cm)

8D (12.5cm)

12D (8cm)

16D (6cm)

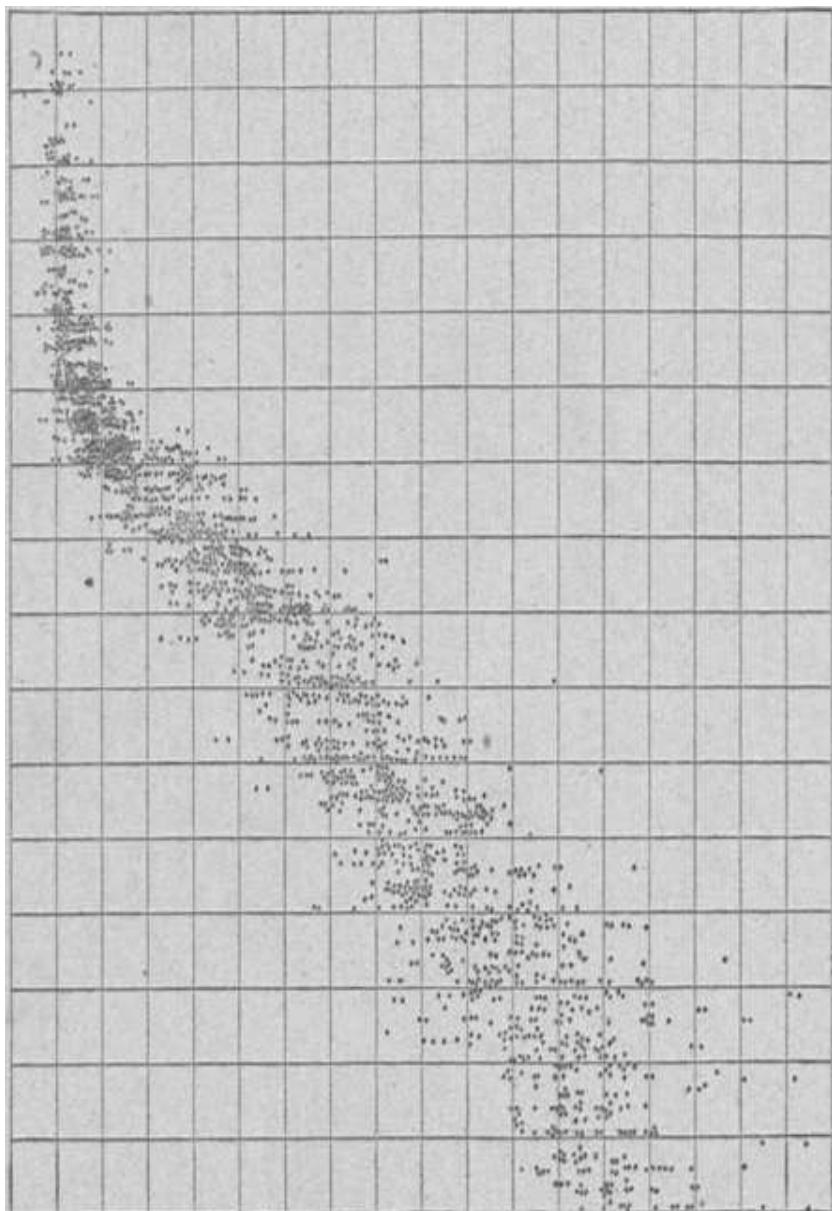
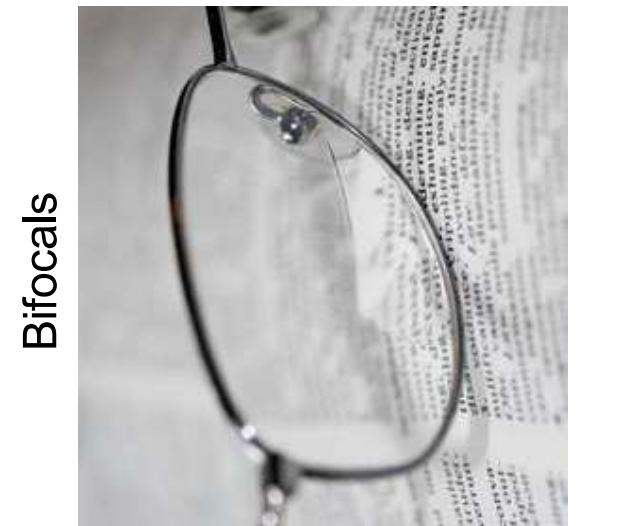
Nearset focus distance

8 16 24 32 40 48 56 64 72

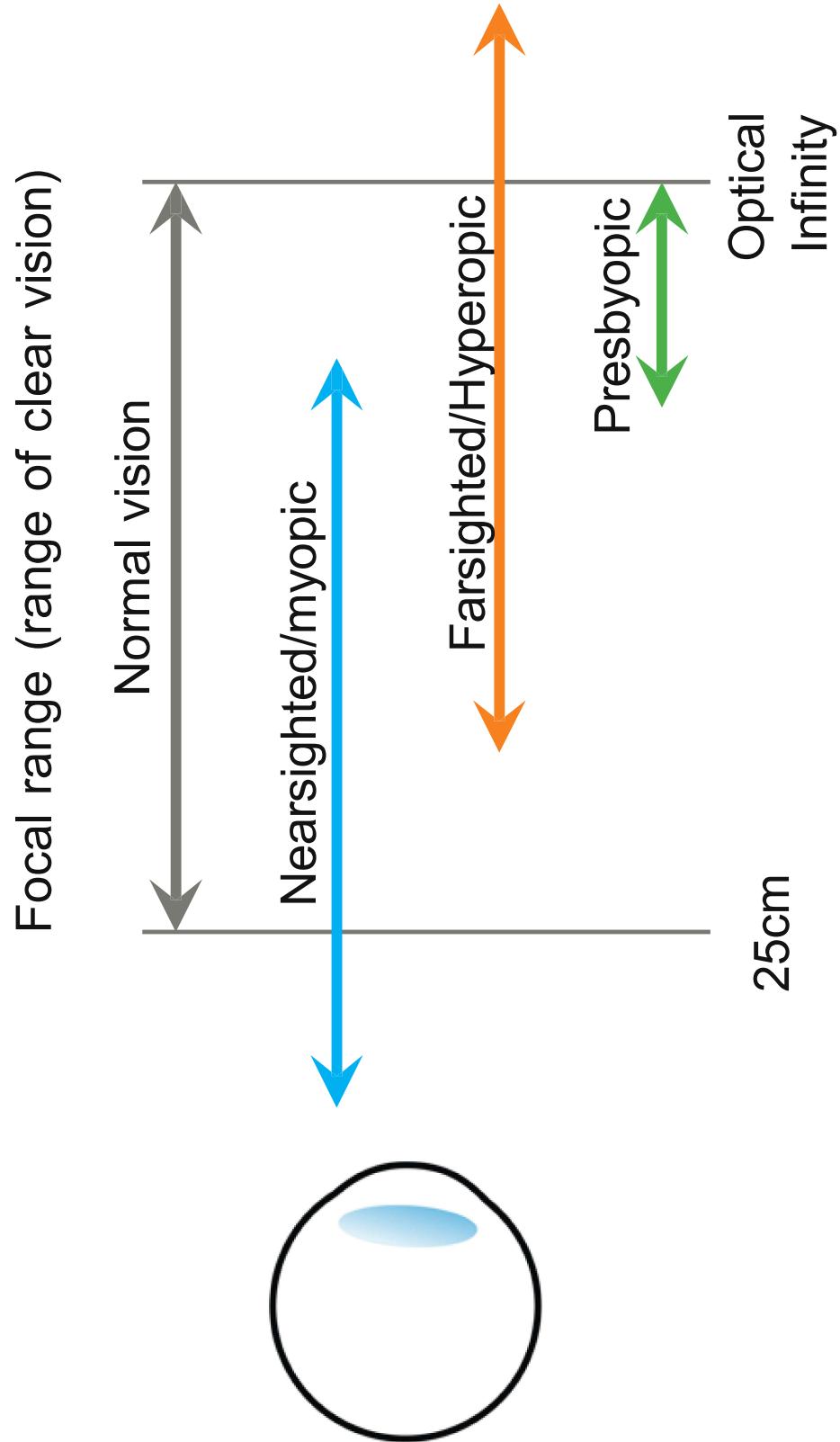
Age (years)

Duane, 1912

Bifocals



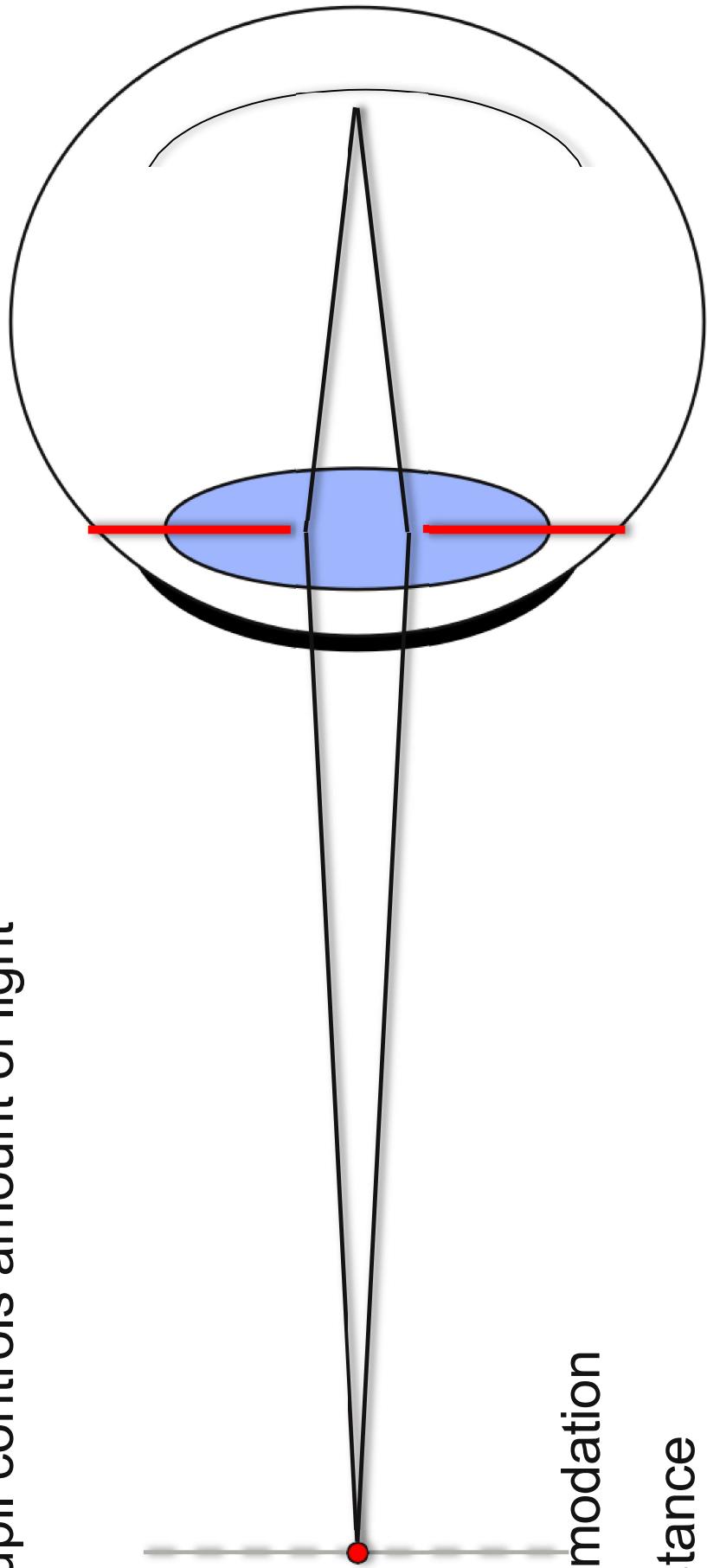
Myopia, Hyperopia, Presbyopia



Modified from Pamplona et al. SIGGRAPH 2010

Retinal Blur

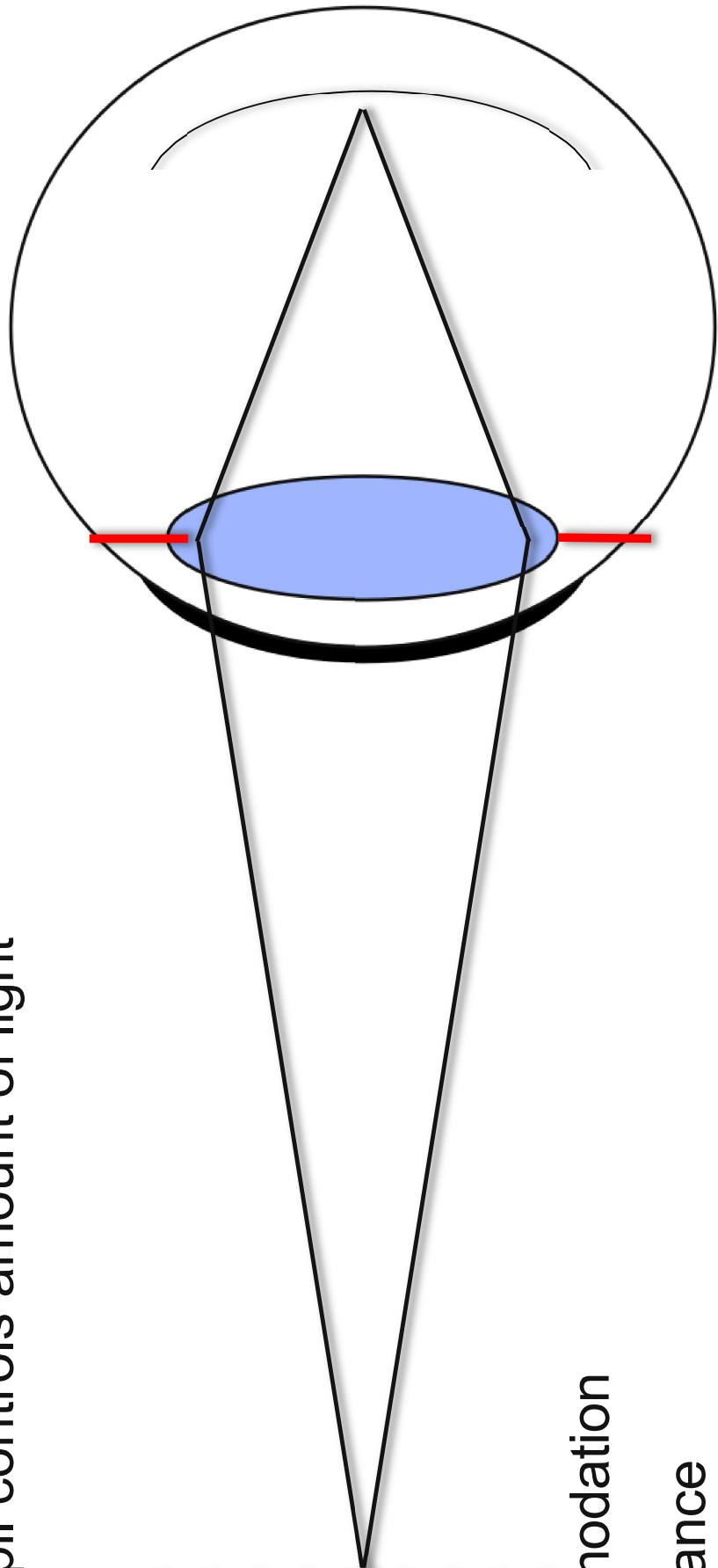
- pupil controls amount of light



accommodation
distance

Retinal Blur

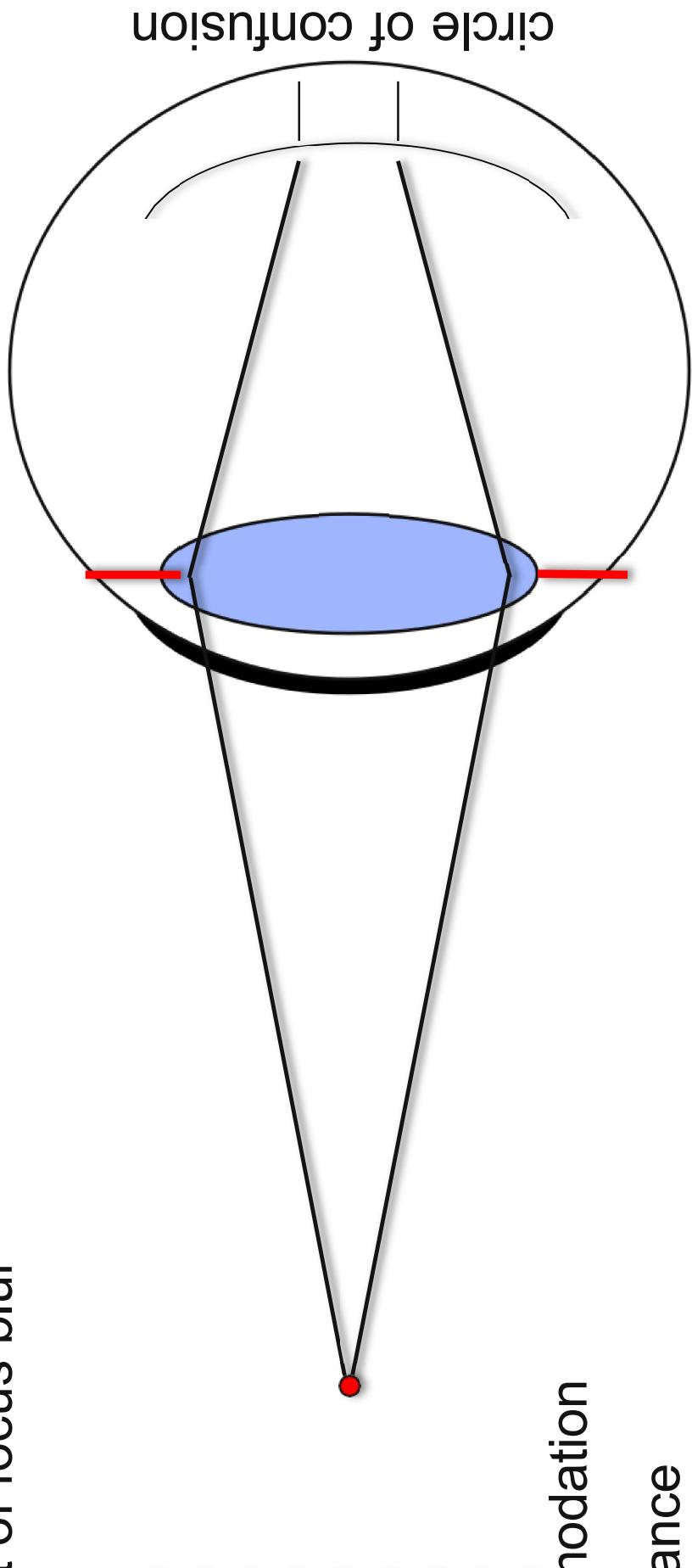
- pupil controls amount of light



accommodation
distance

Retinal Blur

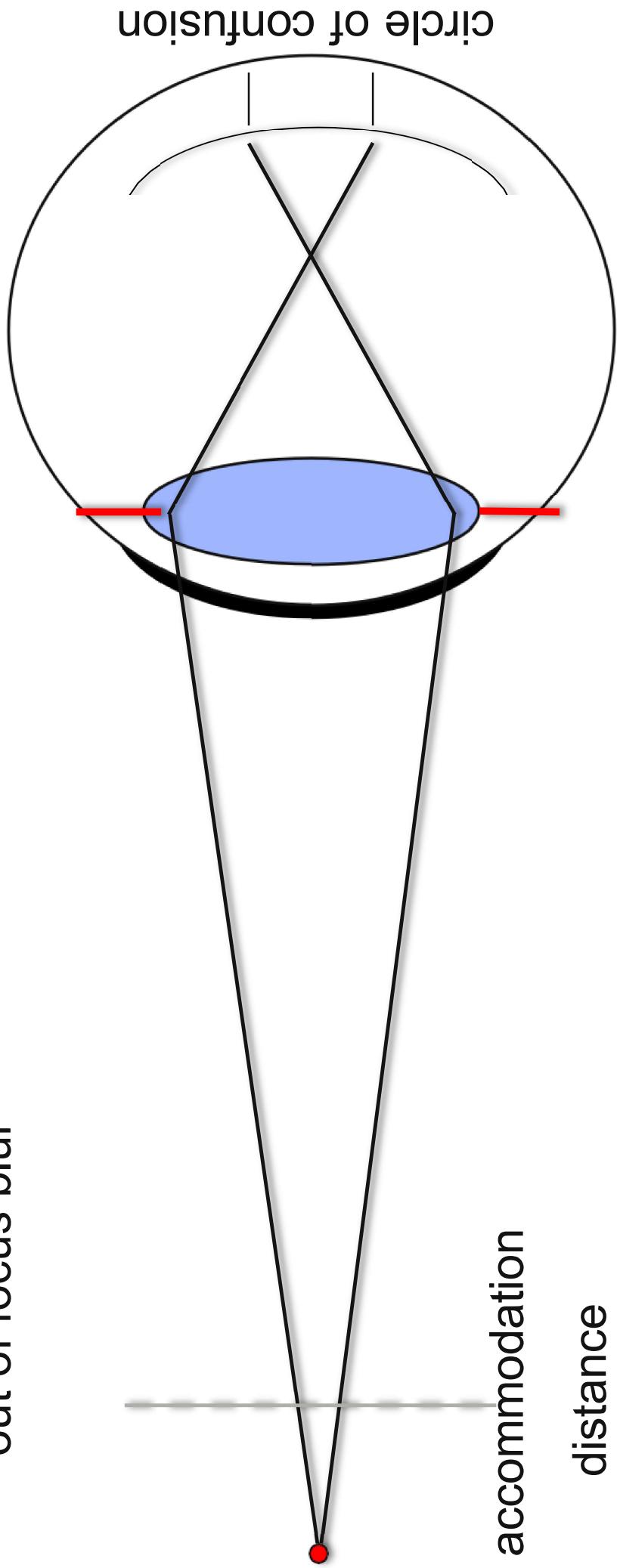
- Out of focus blur



accommodation
distance

Retinal Blur

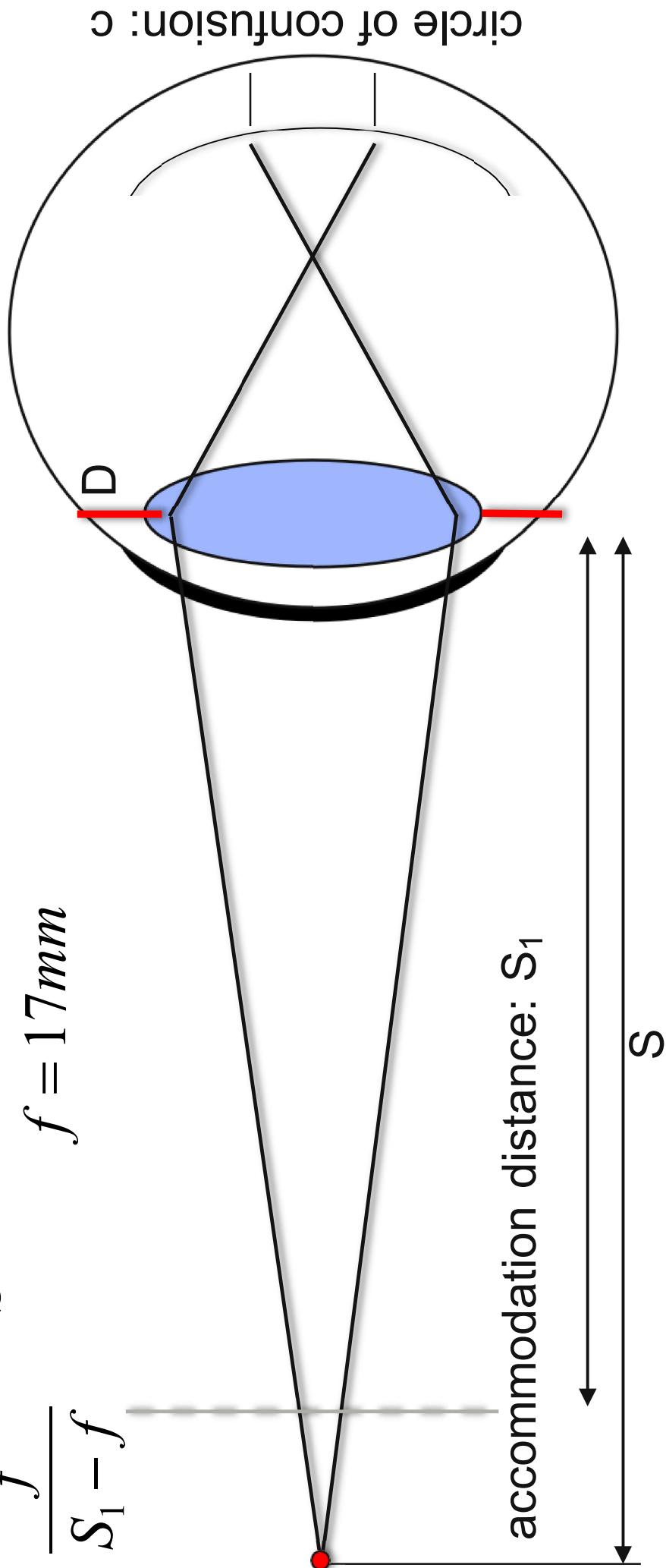
- Out of focus blur



accommodation
distance

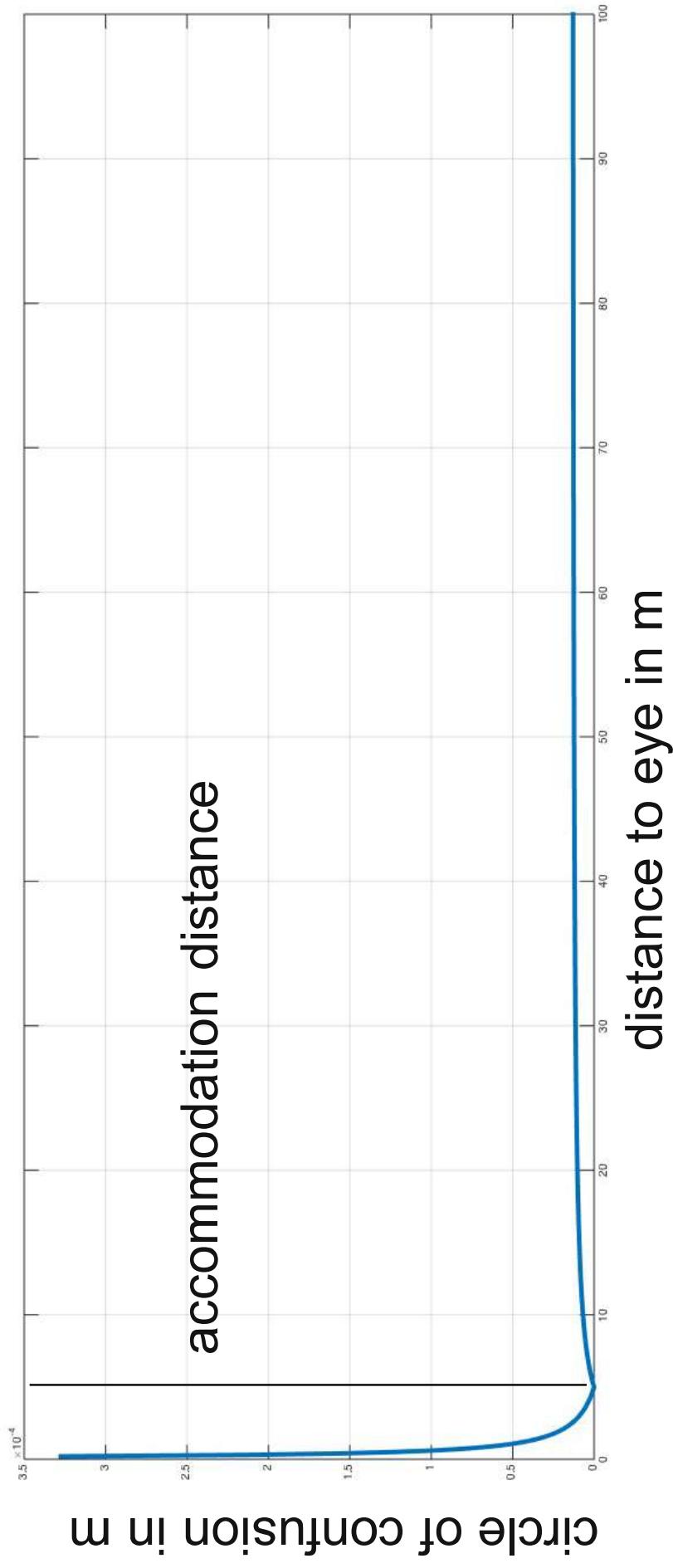
Retinal Blur / Depth of Field Rendering

$$M = \frac{f}{S_1 - f}$$
$$c = M \cdot D \cdot \frac{|S - S_1|}{S}$$
$$f = 17\text{mm}$$

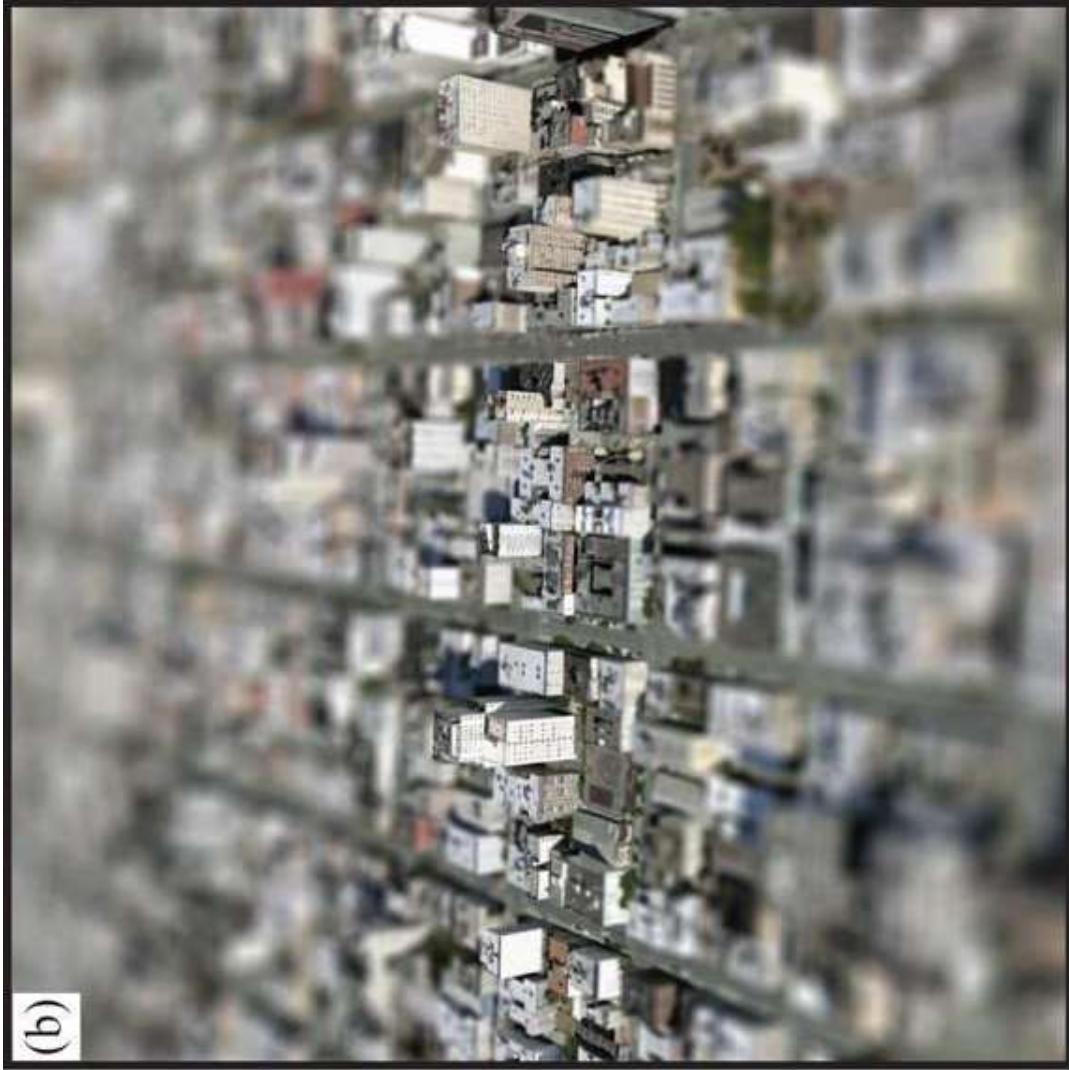
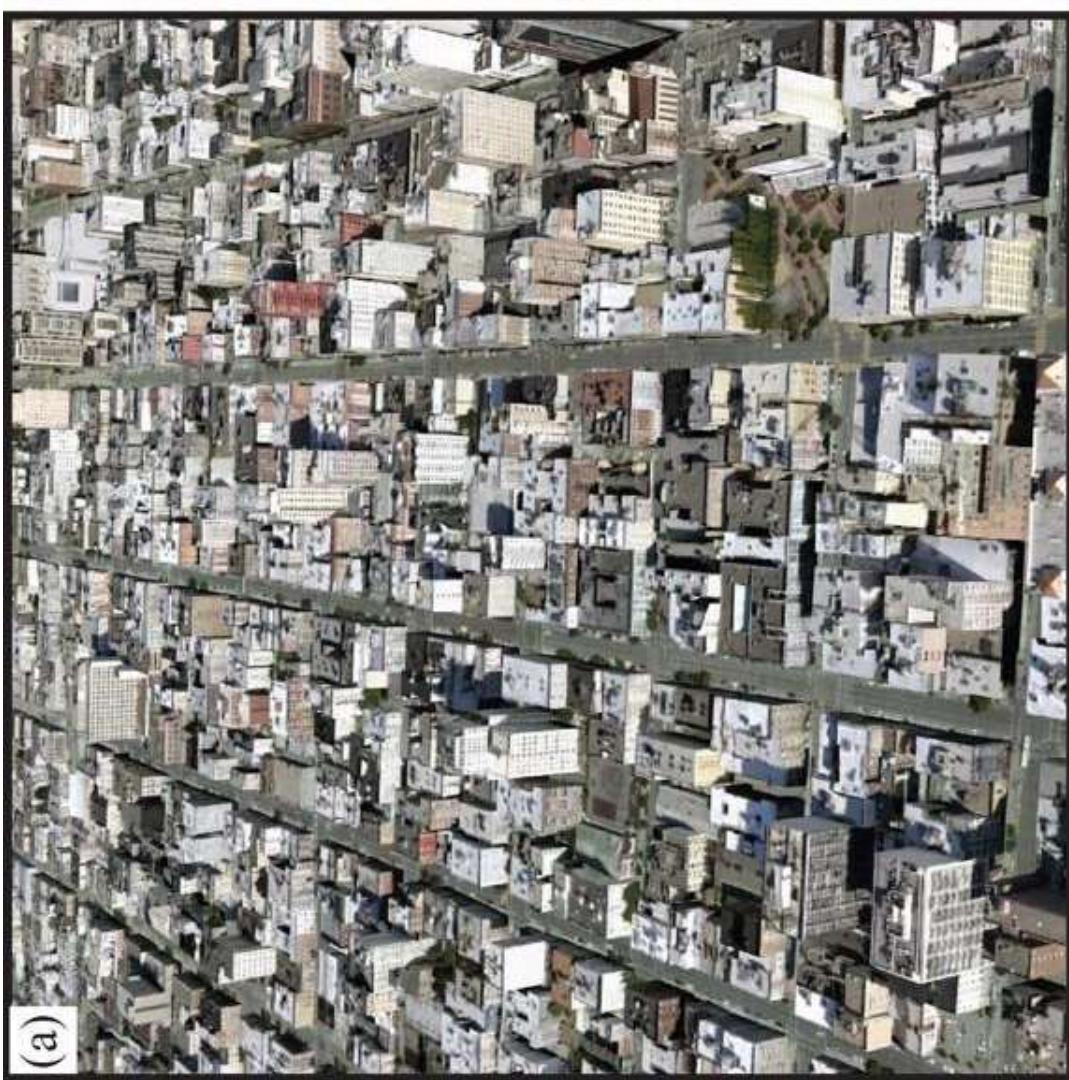


Circle of Confusion

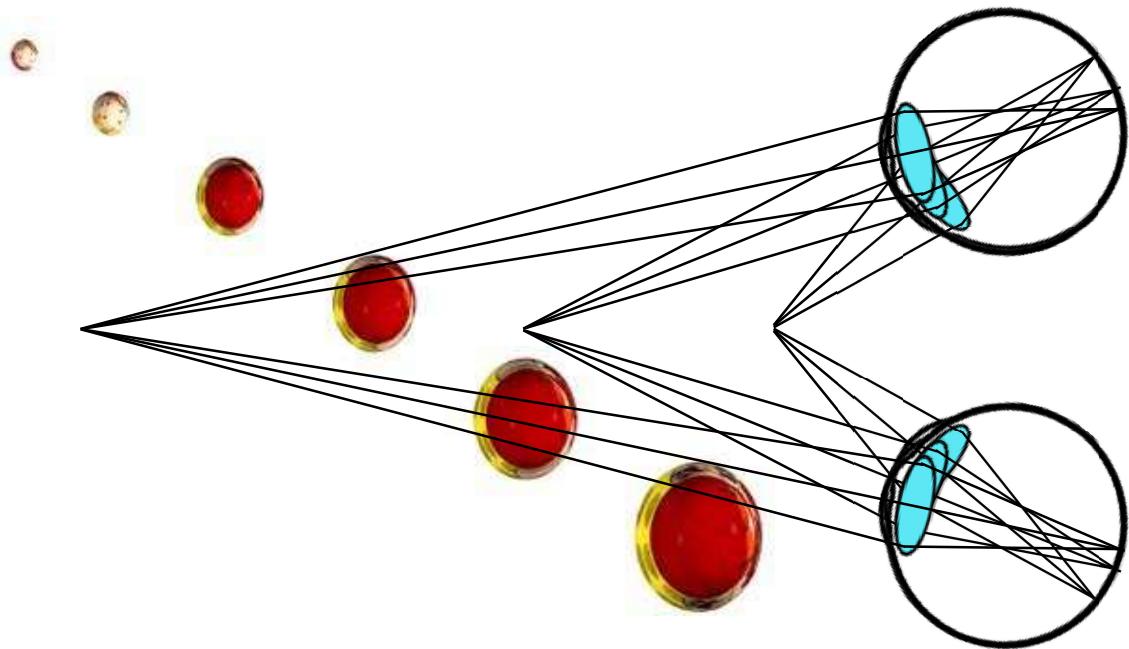
$$c = M \cdot D \cdot \frac{|S - S_1|}{S}$$



Blur Affects Relative Object Size!

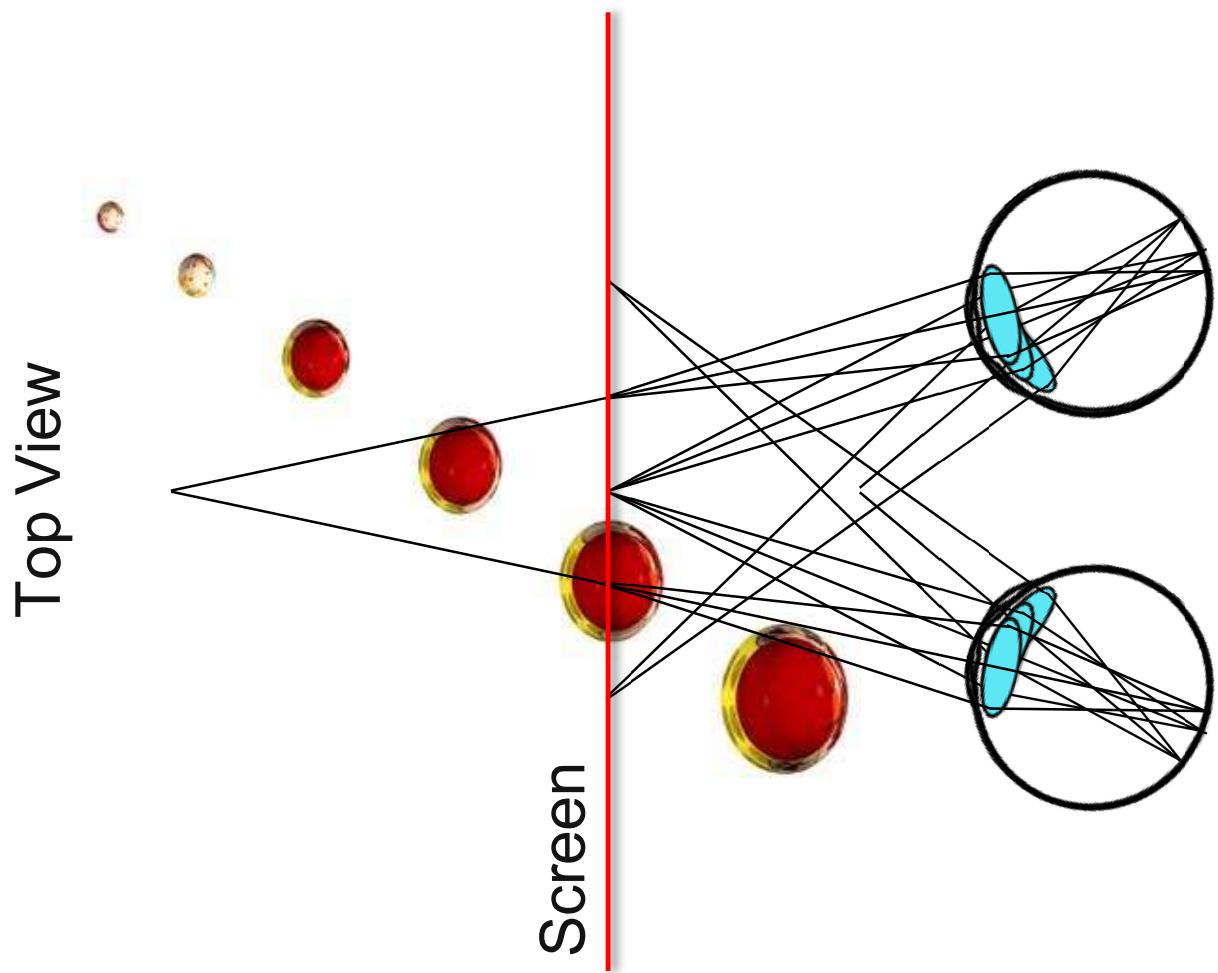


Top View



Real World:

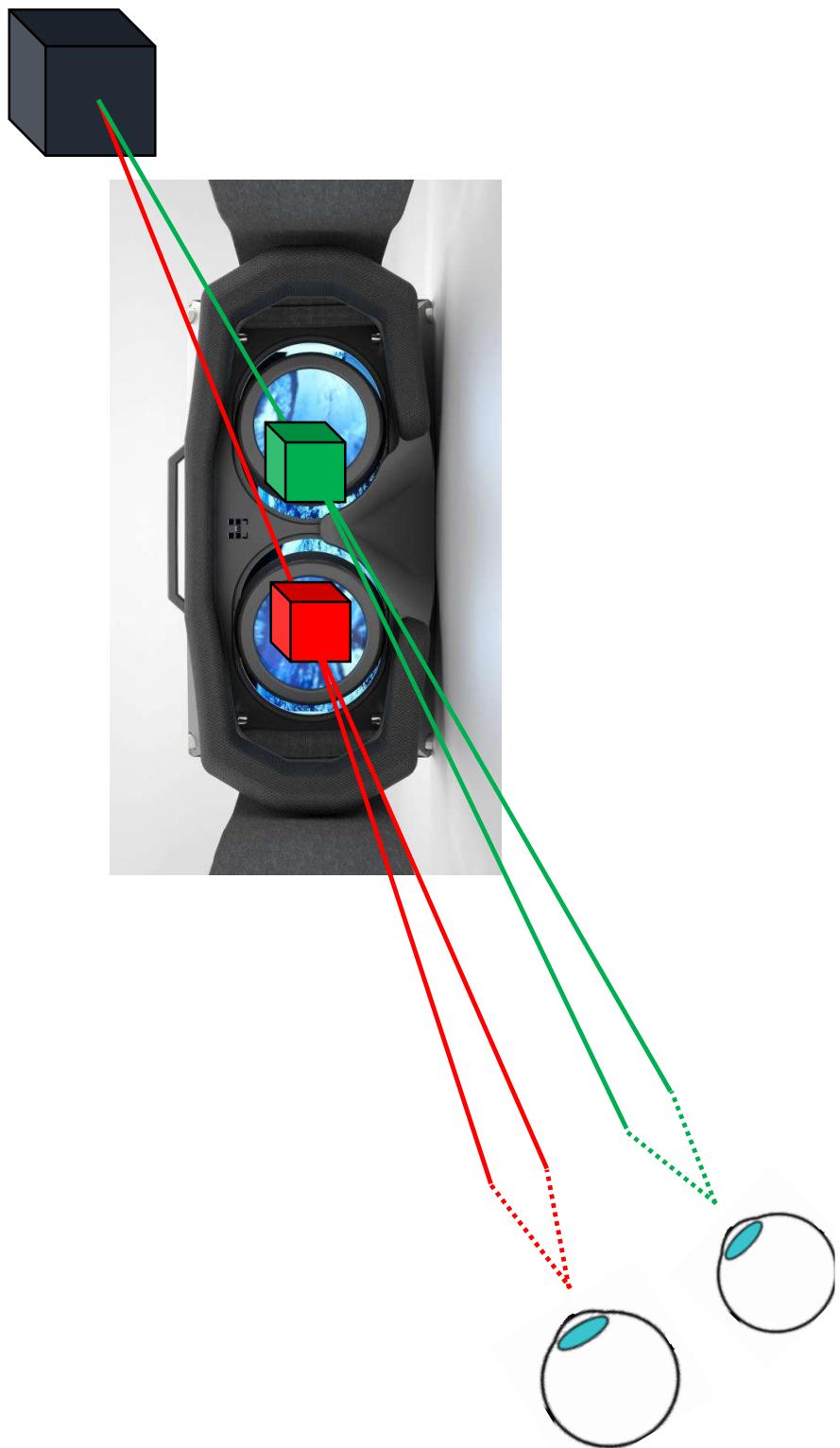
Vergence & Accommodation **Match!**



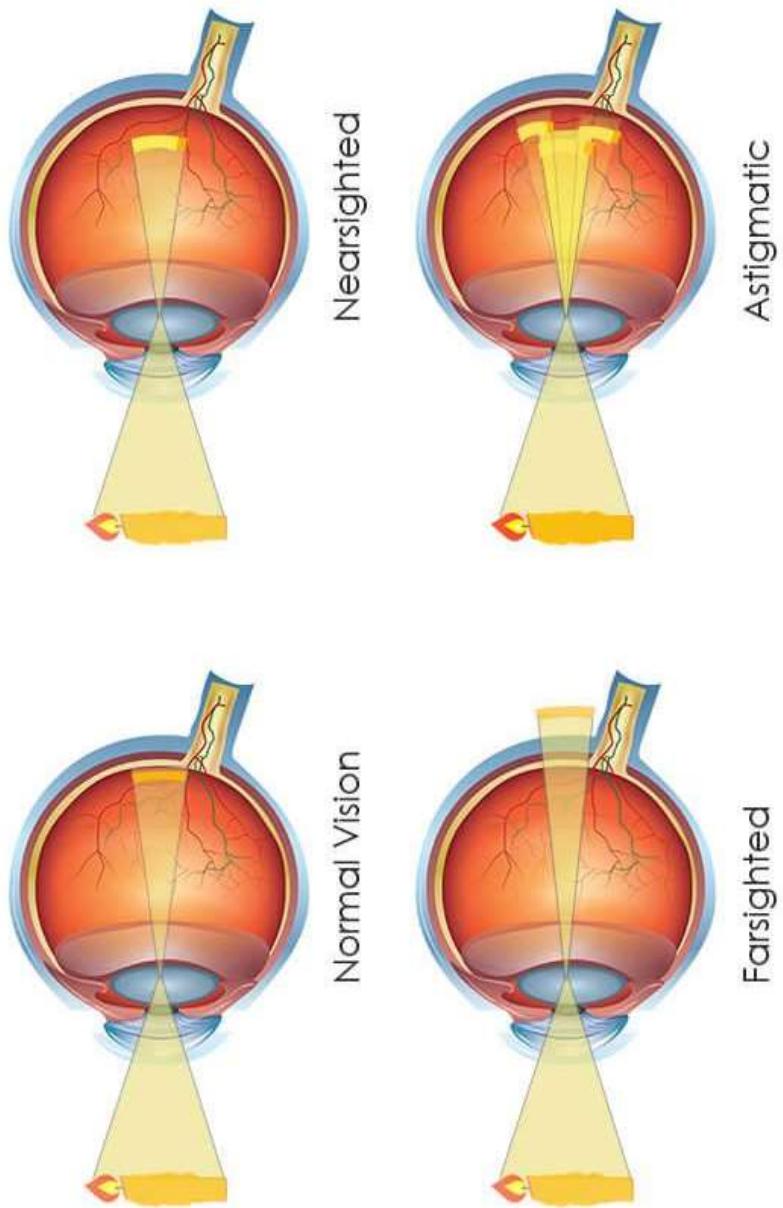
Stereo Displays Today:
Vergence-Accommodation **Mismatch!**

Vergence-Accommodation Conflict

What visual/displays suffice for Vergence? Accommodation?

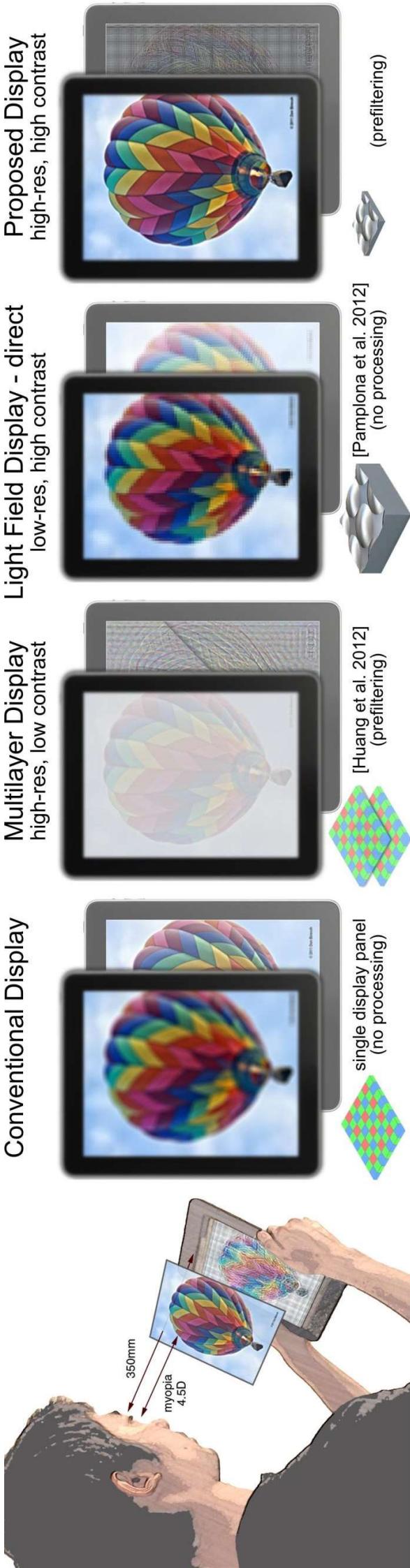


Myopia/near-sighted vs. hyperopia/far-sighted

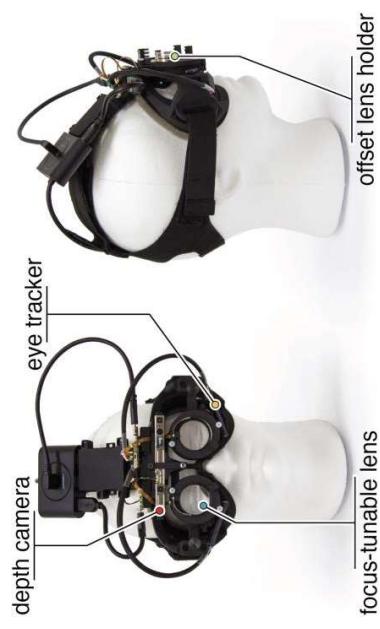


https://en.wikipedia.org/wiki/Depth_perception#/media/File:08913-Perspective_Run.jpg

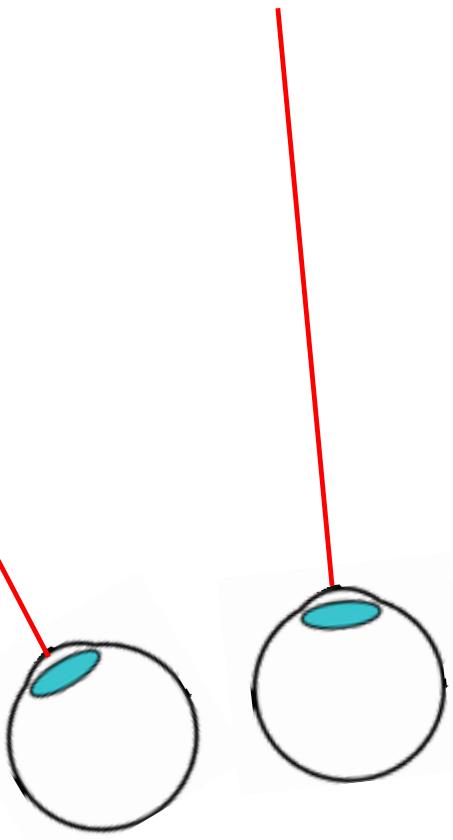
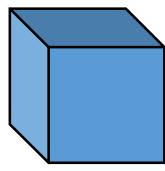
Myopia/near-sighted vs. hyperopia/far-sighted



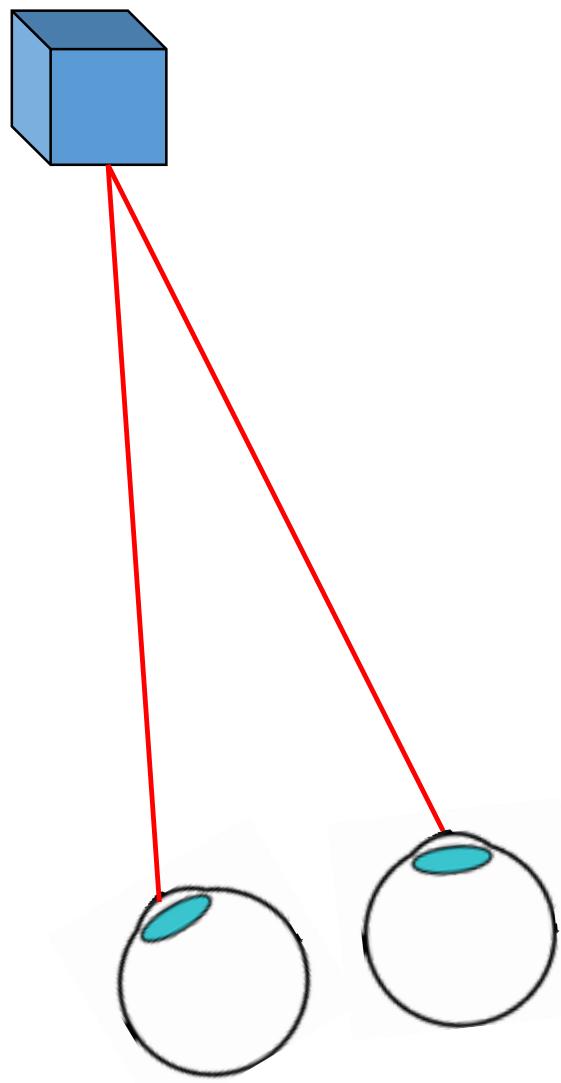
Myopia/near-sighted vs. hyperopia/far-sighted

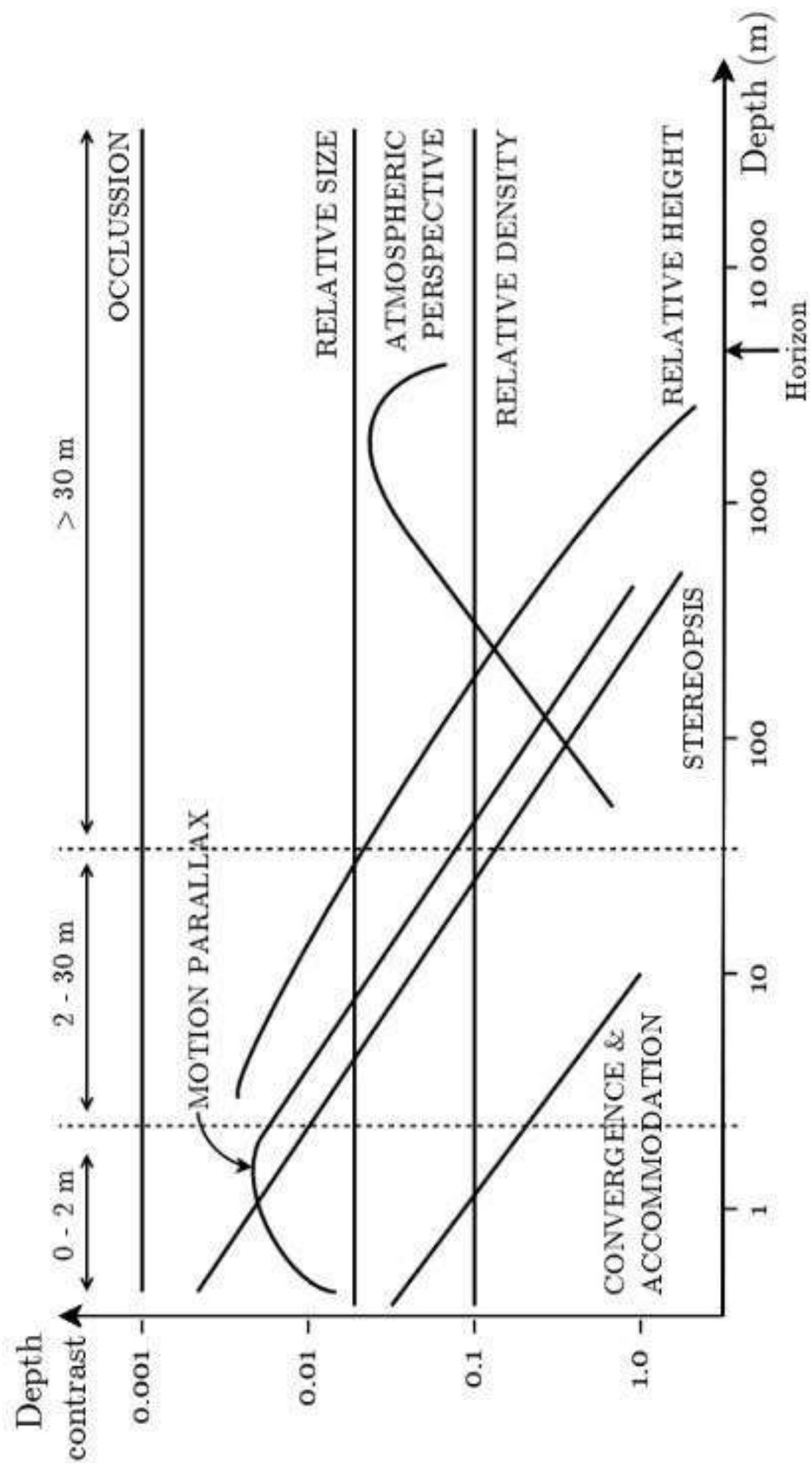


Binocular Cues – Vergence



Binocular Cues – Vergence



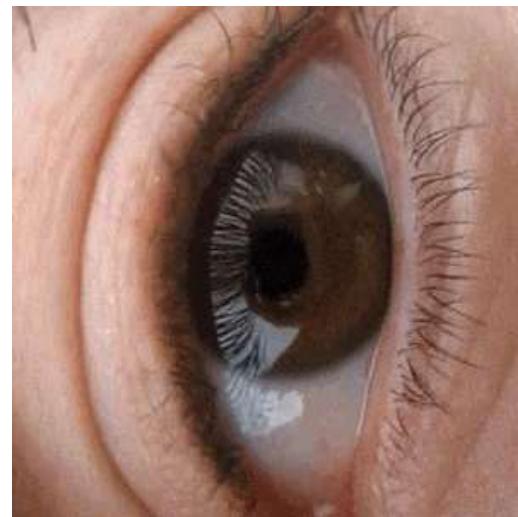


Temporal Behaviors

Temporal Behaviors



vergence



saccade



vestibulo-ocular reflex

Temporal Behaviors – Saccade (fast movement)

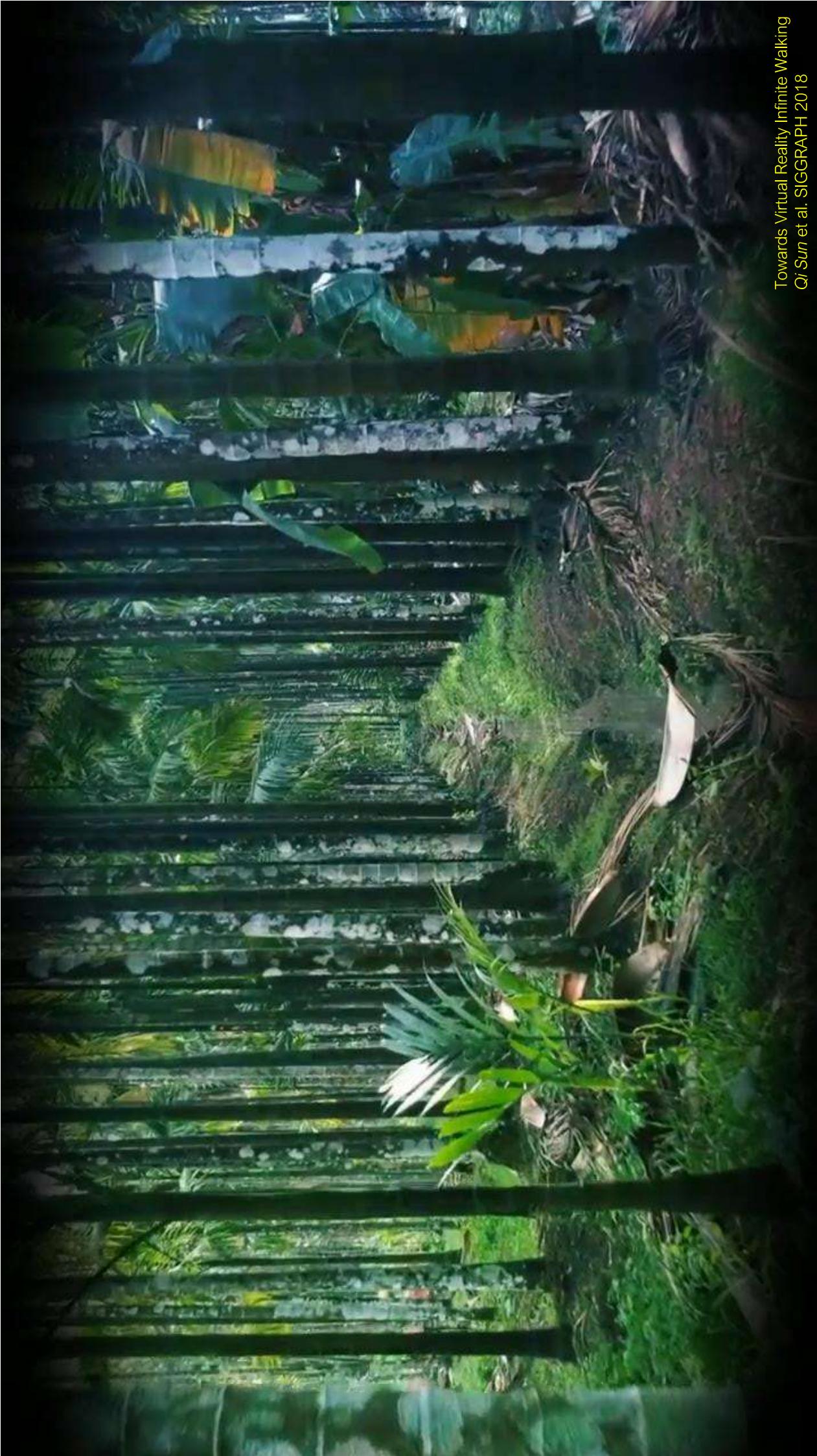
You are UNABLE to move slowly



Spider Saccade



image courtesy: reddit user forte2

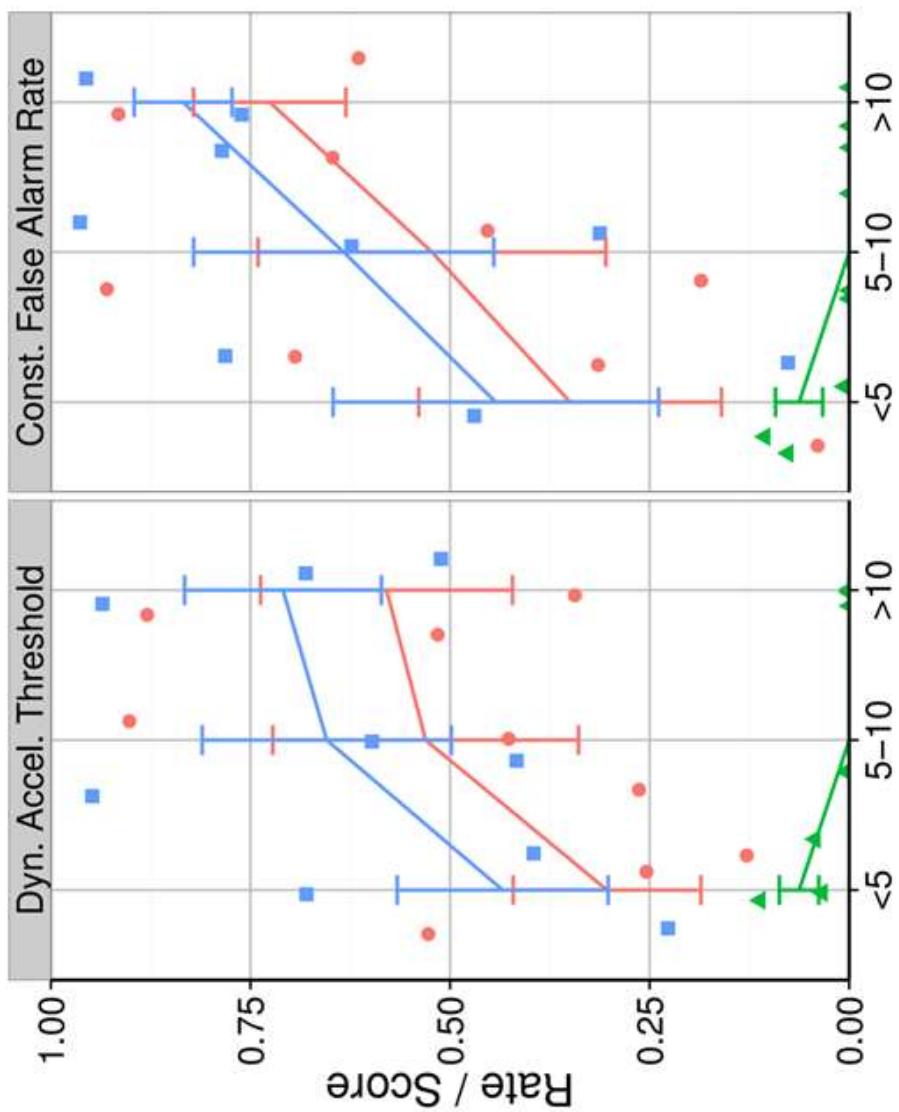


Stopped Clock Effect



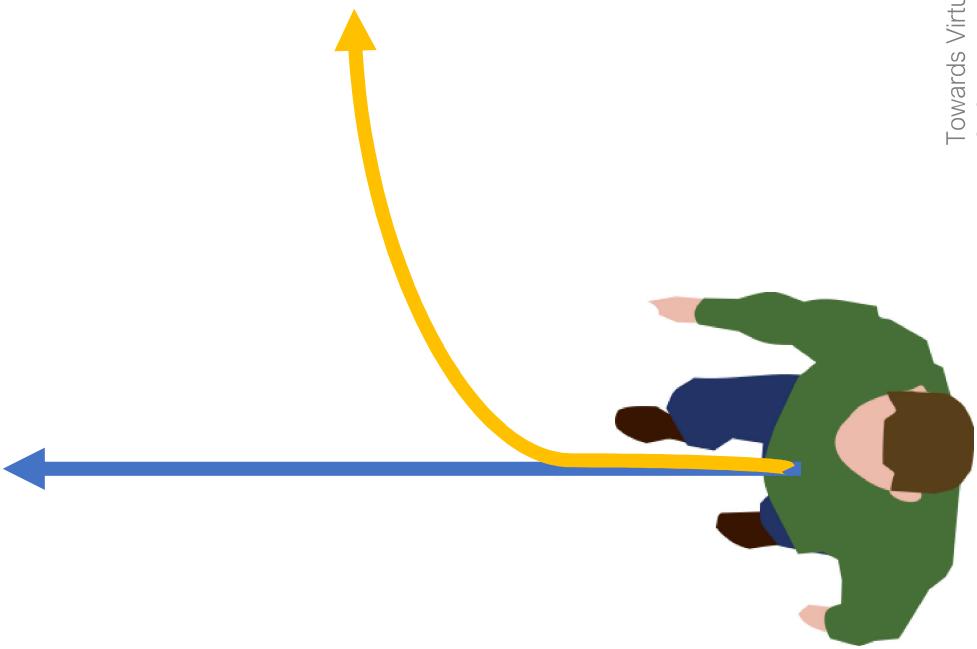
Imperceptible Angular Rotation

12.6 deg/sec





Saccadic Redirection



SACCADIC REDIRECTED WALKING

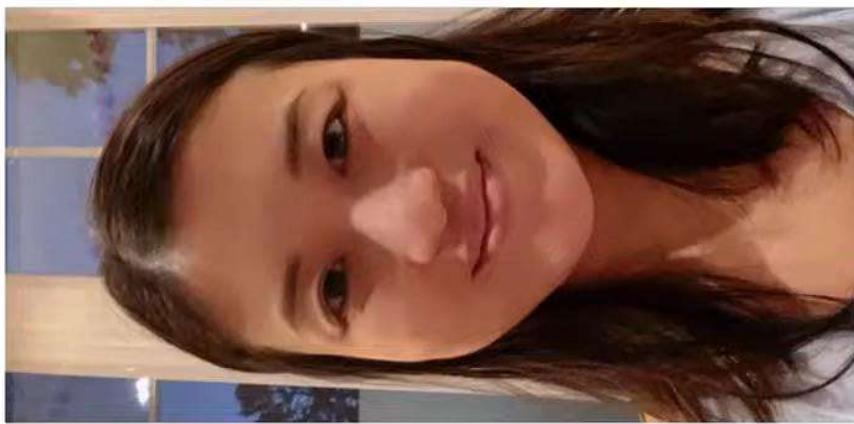
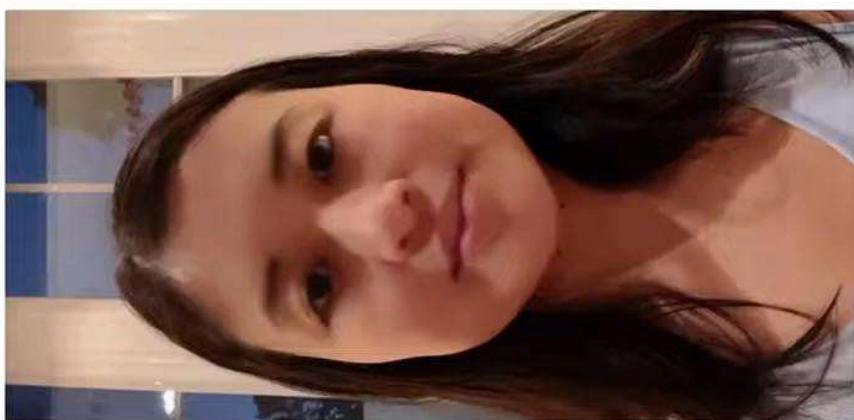
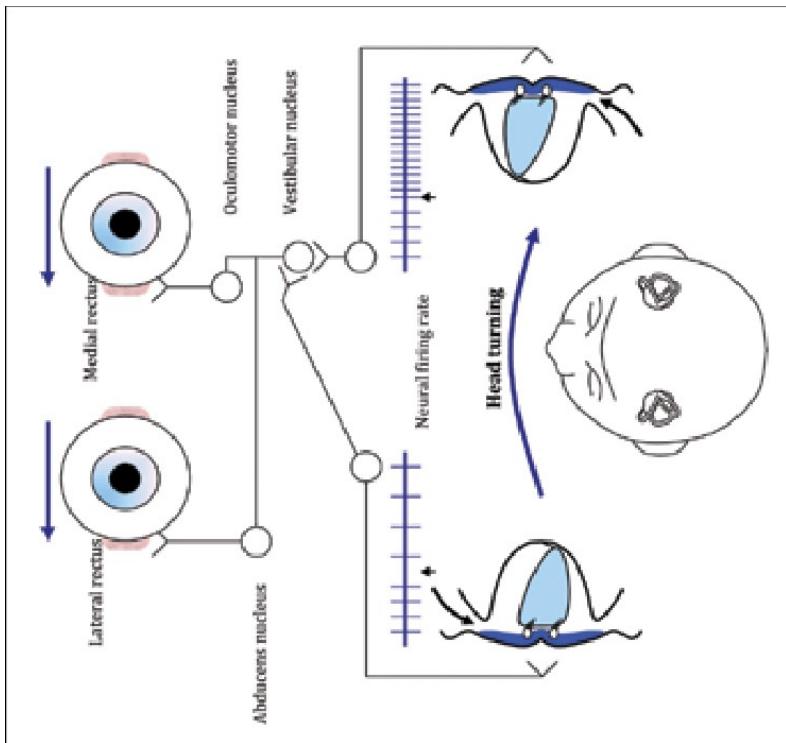
BEYOND ROOM SCALE: EXPLOITING GAZE TO MAKE LARGER VIRTUAL SPACES



NVIDIA RESEARCH AND ADOBE RESEARCH

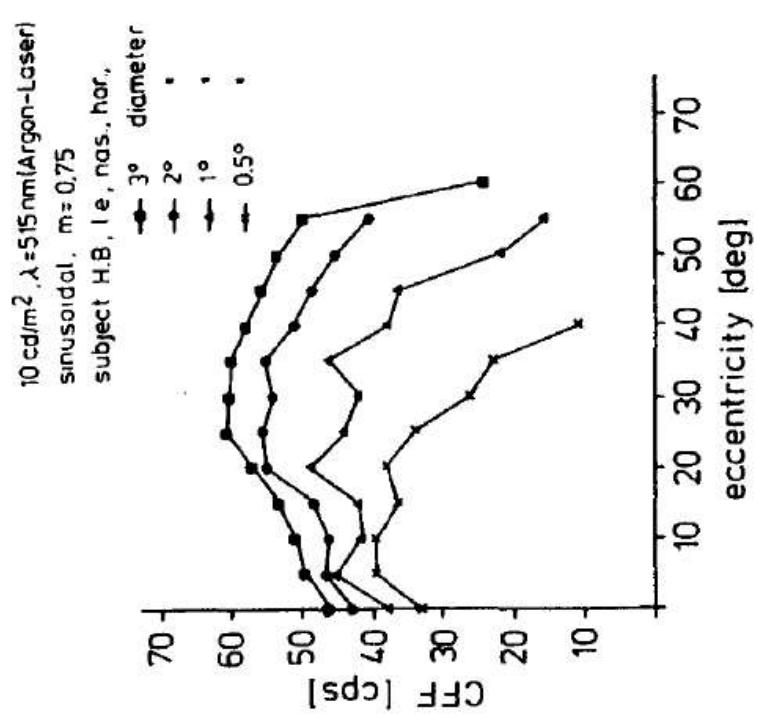


Temporal Behaviors – Vestibular-Ocular Reflex



Temporal Model: Our Eyes Sample@30FPS

Persistence of vision/Flicker Fusion



[Hartman et al.. 1978]