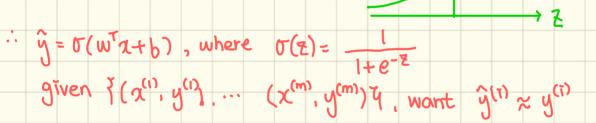


## Logistic Regression 7

X Logistic Regression: y가 o 또는 13 장비져 있는 o건 가 문제에 사용되는 얼[] 문 X: 양적특성 , y: 주어건 x 에 하다당하는 첫제 감사 ,  $\hat{y}$  : y의 제작장 = P(y=1|x) 이때,  $x \in \mathbb{R}^{n_x}$  oi  $x \in \mathbb{R}^{n_x}$   $x \in \mathbb{R}^{n_x}$   $x \in \mathbb{R}^{n_x}$   $x \in \mathbb{R}^{n_x}$ 

$$\Rightarrow$$
 Output  $\hat{y} = \sigma(w^T x + b) = \sigma(z)$ 

ि पुं= भार्यम् निर्म नार्थमः १८ प्रेटा व कार्यः एम्स्यम् क्षेत्रः म् राज्यः । । य स्थारः प्रमास्यः । । । । स्थारः प्रमास्यः ।



#### Logistic Regression Cost Function?

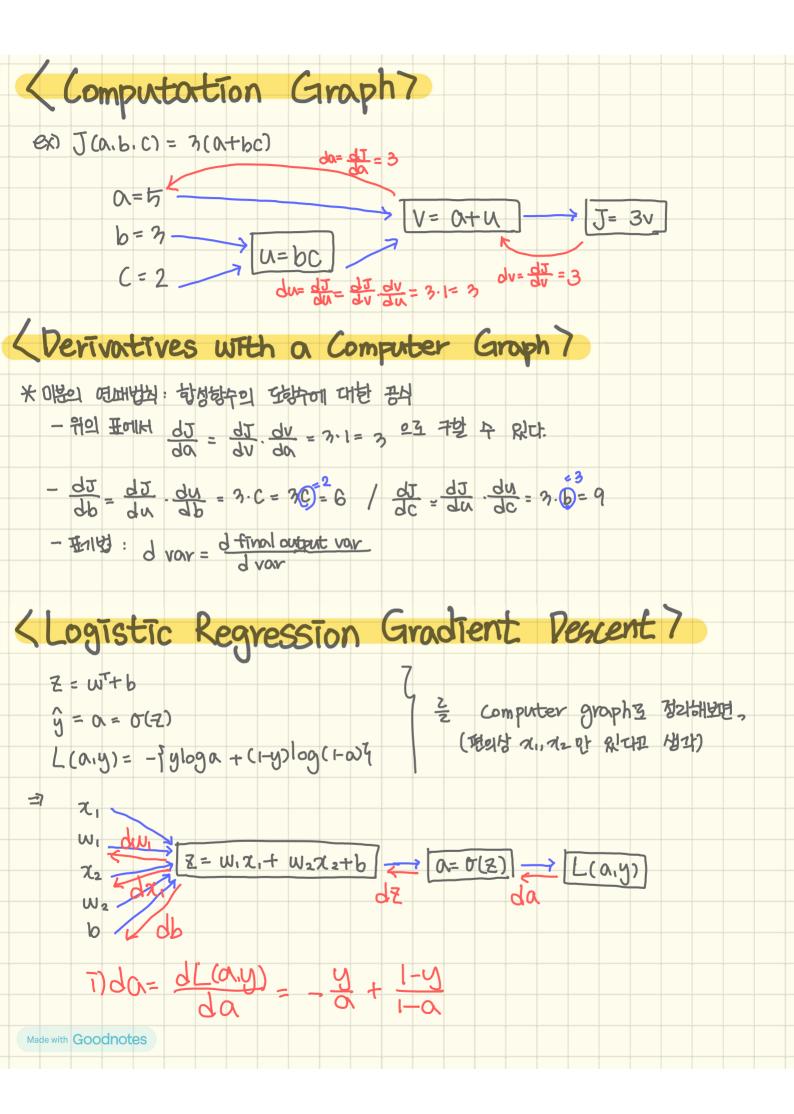
\* 판납하는 아마다 나이 아르트성 (2) 에 대한 상체 많 (4) 과 예약값 ( $\hat{y}$ ) 의 오사를 제안하는 항무 - 인생적으로 만난하는 보통  $L(\hat{y}, y) = \frac{1}{2}(\hat{y} - y)^2$  으로 사용하나, 크지난耳 회귀는 지역 비료값에 바다 수 있으므로 다른 도너하는 사용한다.

- 弘 [ ] (g,y) = - Tylogŷ + (I-y) log (I-ŷ) {

1) If  $y=1: L(\hat{y},y)=-\log \hat{y} \Rightarrow want \log \hat{y} \text{ large } : \text{ want } \hat{y} \text{ large } \approx 1$ 11) If  $y=0: L(\hat{y},y)=-\log(1-\hat{y}) \Rightarrow want \log(1-\hat{y}) \text{ large } : \text{ want } \hat{y} \text{ small } \approx 0$ 

米 비용할수 (Cost Function): अपय ध्येना पार्च 오나는 게산하는 할까 판납하다이며, 모든 일찍 ना पार्च 오나는 게산하는 한다른 비용 하다고고 한다. 즉, 비용하는 모든 일찍 ना 대한 도난하수의 평균

 $J(w,b) = \frac{1}{m} \sum_{\tau=1}^{m} L(\hat{y}^{(\tau)}, y) = -\frac{1}{m} \sum_{\tau=1}^{m} \{y^{(\tau)} \log \hat{y}^{(\tau)} + (1-y^{(\tau)}) \log (1-\hat{y}^{(\tau)})\}$ 本 दिश्चे थे: प्राक्षिकें एवं येक्सर्ट्स wer be प्रध्नेत्र इस्! 女 (Gradient Descent ? 大 月사하기법: UB的時 업际 만단 W와 b를 갖는 것으로, 입의의 장을 된다서 기울기를 따라 회적의 강으로 안데이트 항 learning rate - w: w - d dJ (w, b) 5th dw2115 \$ b: b - d dJ (w.b) (Derivatives (叫出)? /fc0)=30 7) 0=2 ->f(0)=6 0= 2.001 => f(a) = 6.003 6,003 0.003 = height = Slope (derivative) of f(a) at a=2:3 17) 0=5 -> f(a)=15 0=6.001 -> f(0)=16.003 2-12.001 slope at a=+ 3 大生すり(= slope): 地方 の言 なる 地部川東き 四、 f(a)가 your 地質はいきり ちなかと な dof(a) = df(a) 3 Ho (More Derryottives Examples) 計: f(a)  $\alpha^2$ ln (a) 9554 : d fa l



IT)  $dz = \frac{dL(\alpha, y)}{dz} = \frac{dL(\alpha, y)}{d\alpha} \cdot \frac{d\alpha}{dz} = \frac{7}{1} \cdot \frac{y}{\alpha} + \frac{1-y}{1-\alpha} (\frac{7}{1}\alpha(1-\alpha)^{\frac{1}{2}})$ = a-4 TTT) dw. = dl (a.y) = x.dz W1:=W1-ddW1
1 = W2:=W2-ddW2 b := b - xdb dw2 = 22dz उ एता । इंप db = dz (Gradient Descent on m Examples)  $\overline{J}(\omega,b) = \frac{1}{m} \sum_{i=1}^{m} L(\alpha^{(i)}, y^{(i)}),$  $Q^{(\tau)} = \hat{y}^{(\tau)} = \sigma(z^{(\tau)}) = \sigma(w^T z^{(\tau)} + b)$ Tf, J=0; dw1=0; dw2=0; db=0 For T=1 to m, Z(T) = WT z(T) + b  $\Omega^{(T)} = \sigma(z^{(T)})$ J += - [y(1) log a(1) + (1-y(1)) log (1-a(1))  $dz^{(7)} = 0^{(7)} - y^{(7)}$  $dw_1 + = \chi_1^{(T)} dz^{(T)}$   $dw_2 + = \chi_2^{(T)} dz^{(T)}$   $dz^{(T)}$ db += dz(T) Made with Goodnotes

### [2-2. Python and Vectorization]

#### Vectorization ?

大억日中: 亚目에서 for是是 MHHE 准

EX) Z=WTX+b

(Non-vectorization)

7=0

for T in rounge (n-x):

又 += w[i] \* ス[i]

2+=b

(Vectorization)

Z= np. dot (w, x) +b

米らIMD(Gingle Instruction Multiple Data): 時項 亞州山의 も 苦福, 計山의 時 विनम् जिमाभा रहे इभाग भाषां से से प्रमुख्य प्राह्म जोसे गर्सिमा के

ex2)  $v = \begin{bmatrix} v_1 \\ v_n \end{bmatrix}$   $u = \begin{bmatrix} ev_1 \\ ev_n \end{bmatrix}$  (non-vectorization) (vectorization) u = np. exp(v) u = np. exp(v) for t = tonorization

U[T] = math. exp(V[T])

(Vectorizing Logistic Regression)

 $Z^{(2)} = W^{T} \chi^{(2)} + h$ 

 $Q^{(2)} = Q(Z^{(2)})$ 

7 (3) = WT7 (3) +b

 $\mathcal{V}_{(\lambda)} = \mathcal{Q}(\mathcal{S}_{(\lambda)})$ 

 $Z^{(1)} = W^{T} \chi^{(1)} + b$   $Z^{(1)} = \sigma(Z^{(1)})$   $Z^{(1)} = \sigma(Z^{(1)})$ 

 $\left[ \mathbf{Z}^{(1)} \ \mathbf{Z}^{(2)} \cdots \ \mathbf{Z}^{(m)} \right] = \mathbf{W}^{\mathsf{T}} \mathbf{X} + \left[ \mathbf{b} \ \mathbf{b} \cdots \mathbf{b} \right]$ 

 $= \begin{bmatrix} w^{T} x^{(1)} + b & w^{T} x^{(2)} + b & \cdots & w^{T} x^{(m)} \\ = z^{(1)} & = z^{(2)} & = z^{(m)} \end{bmatrix}$ 

u= np. exp(v)

(vectorization coding)

Z= np.dot (np.transpose(w), x) + b

Made with Goodnotes

## ( VectorTzIng LogIstic Regression's Gradient Descent)

$$dz^{(1)} = a^{(1)} - y^{(1)}$$
  $dz^{(2)} = a^{(2)} - y^{(2)}$  ...  $dz^{(m)} = a^{(m)} - y^{(m)}$ 

$$\Rightarrow dz = \left[ dz^{(n)} \ dz^{(2)} \ \dots \ dz^{(m)} \right] \qquad \Rightarrow dz = A - Y$$

$$A = \left[ \alpha^{(n)} \ \alpha^{(2)} \ \dots \ \alpha^{(m)} \right] \qquad = \left[ \alpha^{(n)} - y' \right]$$

$$= [Q_{1}^{(n)} - y_{1}^{(n)} \quad Q_{2}^{(n)} - y_{2}^{(n)} \quad \dots \quad Q_{n}^{(m)} y_{n}^{(m)}]$$

$$\begin{array}{c}
7 \Rightarrow dw = \frac{1}{m} \times dz^{T} \\
= \frac{1}{m} \left[ \chi^{(1)} \cdot \chi^{(m)} \right] \left[ \frac{dz^{(1)}}{dz^{(m)}} \right] \\
= \frac{1}{m} \left[ \chi^{(1)} dz^{(1)} + \chi^{(m)} (m) \right]
\end{array}$$

#### db (m

$$\Rightarrow db = \frac{1}{m} \frac{m}{r=1} dz^{(1)}$$

#### non-vectorizing J = 0, $dw_1 = 0$ , $dw_2 = 0$ , db = 0for i = 1 to m: $z^{(i)} = w^T x^{(i)} + h$ $a^{(i)} = \sigma(z^{(i)})$ $J = -[y^{(i)} \log a^{(i)} + (1 - y^{(i)}) \log(1 - a^{(i)})]$ $dz^{(i)} = a^{(i)} - y^{(i)}$ $dw_1 += x_1^{(i)} dz^{(i)}$ $dw_2 += x_2^{(i)} dz^{(i)}$ $db += dz^{(i)}$ J = J/m, $dw_1 = dw_1/m$ , $dw_2 = dw_2/m$ db = db/mVectorizing > z= wTX+b = np. dot (wT, X) +b A= 0(Z) dz = A - Y dw = Im XdzT $db = \frac{1}{m} np. sum(dz)$ W= W-ddw b = b - &d Made with Goodnotes

```
    Strong constrains in Python 7

                ex1)
              A = \begin{bmatrix} 56.0 & 0.0 & 4.4 & 68.0 \end{bmatrix} \rightarrow (Al = A.5um (ax74=0) \\ 1.2 & 104.0 & 52.0 & 8.0 \end{bmatrix} \rightarrow \frac{(al = A.5um (ax74=0))}{percentage = 100 *A |cal.reshape (1.4)} \\ 1.8 & 175.0 & 99.0 & 0.9 \end{bmatrix}
                                                                                                                                                                                                                                                                                                                    ⇒ (外山) 甜酒是 (山中)五 收益
          \begin{array}{c} (x,y) \\ (x,y) \\
                                (m, n) \begin{pmatrix} + \\ \times \end{pmatrix} ((n, n) \sim ) (m, n)
matrix \begin{pmatrix} + \\ \div \end{pmatrix} (m, n) \sim ) (m, n)
2 = 345444 + 345
```

Made with Goodnotes

# (Explanation of Logistic Regression Cost Function 7 Logistic regression cost function $\hat{y} = \sigma(w^{7}x+b)$ when $\sigma(3) = \frac{1}{1+e^{-2}}$ $\frac{1}{1} y = P(y=1|x)$ $\frac{1}{1} y = 1 - P(y|x) = \hat{y}$ $\frac{1}{1} y = 0 - P(y|x) = 1 - \hat{y}$ $\frac{1}{1} y = 1 - P(y|x) = \hat{y}$ $\frac{1}{1} y = 1 - \hat{y}$ $\frac{1} y = 1 - \hat{y}$ $\frac{1}{1} y = 1 -$ 7f y=0: P(y|x) = yº (+ŷ)' = 1-ŷ 五岁时长 经打合外部的四五, log P(y12) = log (gy (+y)(1-y)) = ylogy+(+y)log(1-y) 红竹到 : 45+55+ L(g,y)= -logP(y1x)=-(gy (1-g)(1-y) M749 इंग्रिमान्य इंग्रिमनाख. P(labels of training upt) = $\prod_{i=1}^{m} P(y^{(i)}|x^{(i)})$ $31 \rightarrow \log P(\text{labels of training set}) = \log \prod_{i=1}^{m} P(y^{(i)}|x^{(i)}) = -\prod_{i=1}^{m} L(\hat{y}^{(i)}, y^{(i)})$ :. UPSET J(W16) = - log P(lobels of training het)