

Lab1 - TDDE01

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Assignment 1

Task 2 - $p(Y = 1|X) > 0.5$

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

Confusion matrix for training set:

Table 1: Confusion matrix for training set using threshold 0.5

	0	1
FALSE	803	81
TRUE	142	344

Confusion matrix for test set:

Table 2: Confusion matrix for test set using threshold 0.5

	0	1
FALSE	791	97
TRUE	146	336

As we can see in Table 1 and Table 2, the results using the formula

$$\hat{Y} = \text{if } p(Y = 1|X) > 0.5, \text{ otherwise } \hat{Y} = 0$$

gives the following statistics:

- Train
 - 142 false positives
 - 81 false negatives
 - total we have 223 out of 1370 wrongful classification
 - missclassification: $223/1370 = 0.163 = 16.3\%$
- Test
 - 146 false positives
 - 97 false negatives
 - total we have 243 out of 1370 wrongful classification
 - missclassification: $243/1370 = 0.177 = 17.7\%$

Task 3 - $p(Y = 1|X) > 0.9$

Confusion matrix for training set:

Table 3: Confusion matrix for train set using threshold 0.9

	0	1
FALSE	944	419
TRUE	1	6

Confusion matrix for test set:

Table 4: Confusion matrix for test set using threshold 0.9

	0	1
FALSE	936	427
TRUE	1	6

What we see from Table 3 and Table 4, is that when we increase the constraint for marking an email as spam, we get way less false positives (1 instead of 50 in test set), but the false negatives are increased.

Missclassifications: * Train: $420/1370 = 0.306 = 30.6\%$ * Test: $434/1370 = 0.312 = 31.2\%$

As we can see, the missclassification is increased, but you could argue that in this case, marking a non-spam email as spam, is way worse than letting through spam. It's easier for the recipient to filter away less spam, than to check through the spam mail to find non-spam emails among them. In this case though, there are barely any true positives, so this "spam-filter" will pretty much do nothing.

Task 4 - knn, $k = 30$

Confusion matrix for train set

Table 5: Confusion matrix for train set using knn with $k = 30$

	0	1
FALSE	807	98
TRUE	138	327

Confusion matrix for test set

Table 6: Confusion matrix for test set using knn with $k = 30$

	0	1
FALSE	672	187
TRUE	265	246

As we can see from Table 5 and Table 6 we get the following missclassification rates:

- Train: $236/1370 = 0.172 = 17.2\%$

- Test: $452/1370 = 0.329 = 32.9\%$

What we see here is that missclassification rate for train set is way lower than in exercise 2, which is reasonable since those will be the nodes that can be neighbors. We see that the missclassification rate for the test set has gone up compared to exercise 2. In both cases, the false positive rate has gone up, which is problematic for this spam classification.

Task 5 - knn, $k = 1$

Confusion matrix for train set

Table 7: Confusion matrix for train set using knn with $k = 1$

	0	1
FALSE	945	0
TRUE	0	425

Confusion matrix for test set

Table 8: Confusion matrix for test set using knn with $k = 1$

	0	1
FALSE	640	177
TRUE	297	256

As we can see from Table 7 and Table 8 we get the following missclassification rates: * Train: $0/1370 = 0\%$ * Test: $474/1370 = 0.346 = 34.6\%$

As can be seen in Table 7, using $k = 1$, makes this model perfect. This is simply because we are using the model to classify the same dataset that is datapoints, meaning the closest neighbor will be the node itself and since there is only one neighbor, we will perfectly match each node.

The test set gets slightly worse than in exercise 4.

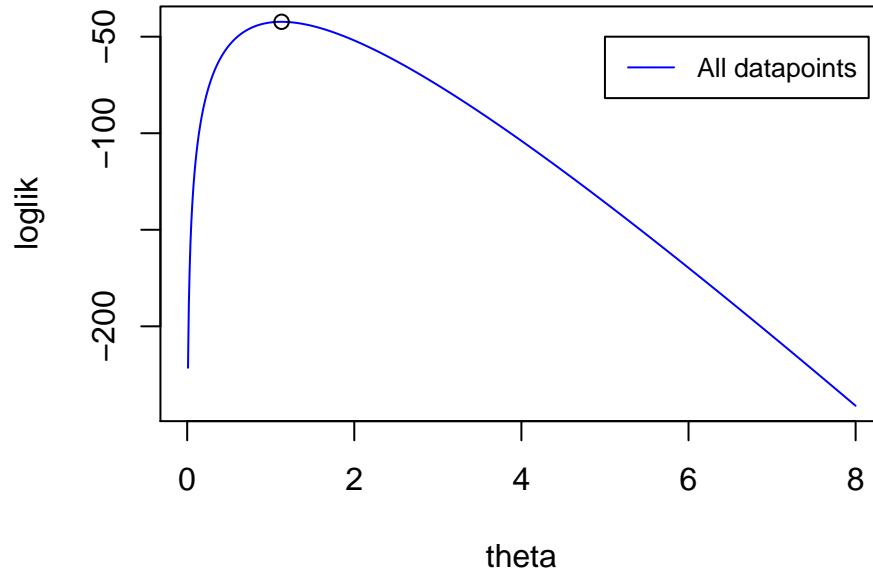


Figure 1: log likelihood for task 2

Assignment 2

Task 2

The distribution type of $p(x|\theta)$ is an exponential distribution, a distribution that models the time between events in a poisson distribution.

As seen in Figure 1, the maximum loglikelihood is given for $\theta = 1.13$ and gives the value $\loglik \approx -42.3$

Task 3

As seen in Figure 2, the maximum log likelihood with just the first six variables from x (red line), is given for $\theta = 1.79$ and gives the value $\loglik \approx -2.52$.

What we can see from these figures is that the loglikelihood has a way pointier graf in the case where all values of x is used, meaning it's more reliable (which is reasonable, since we have more datapoints). Whereas in the case with only the first six values of x , the graph is much more flat top and with more values close to the maximum loglikelihood.

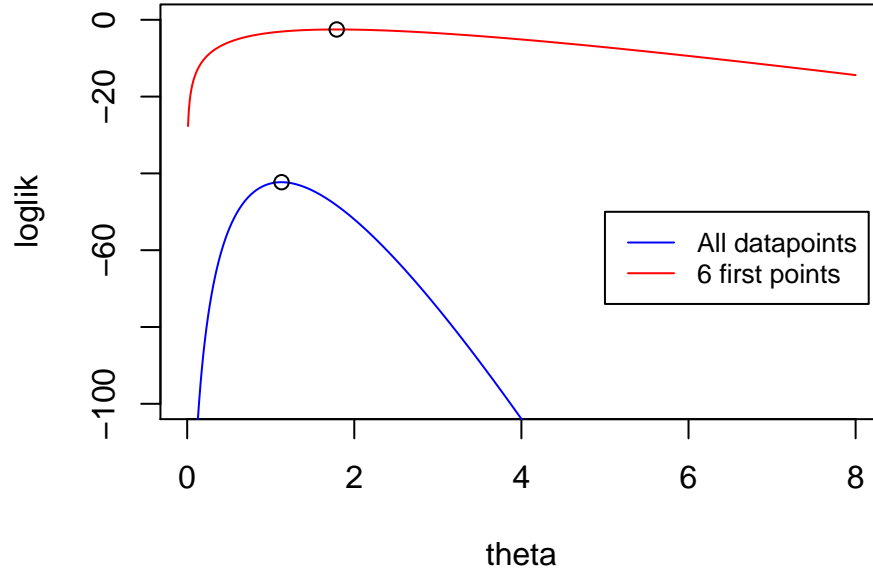


Figure 2: log likelyhood for task 3

Task 4

$$L(\theta) \propto p(\theta|x) \propto p(x|\theta)p(\theta) \propto \theta \left(\prod_{i=1}^n e^{-\theta x_i} \right) 10e^{-10\theta}$$

Gives us

$$l(\theta) \propto \ln \left[\left(\prod_{i=1}^n e^{-\theta x_i} \right) 10e^{-10\theta} \right]$$

The new loglikelihood based on a prior is maximized at $\theta = 1.79$ and gives $\loglik \approx -2.51$, if we compare this to the result given when not using a prior, we get about the same loglikelihood and a similar θ , albeit a bit smaller. If we look at the graph in Figure 3, we see that the one using a prior has a smaller peak, this shows it has a higher certainty (given the conditions) of what θ is.

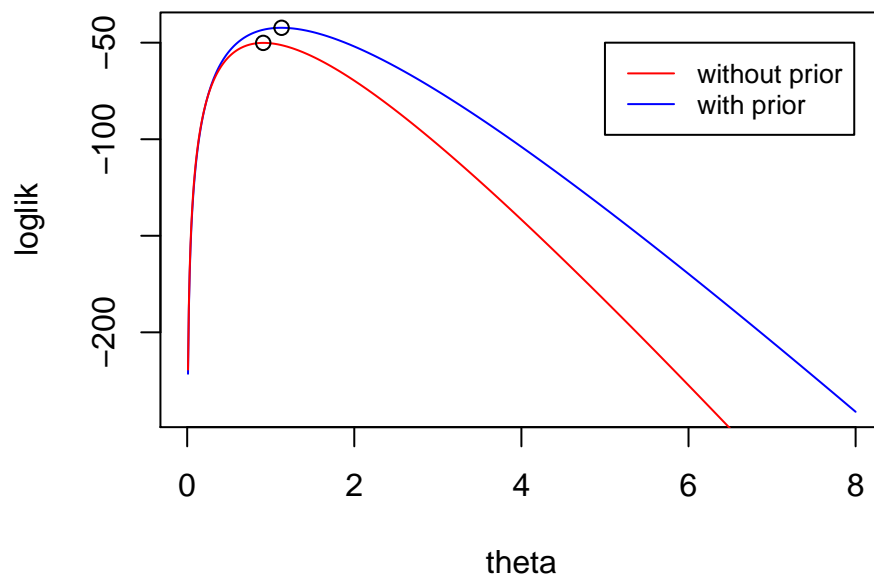
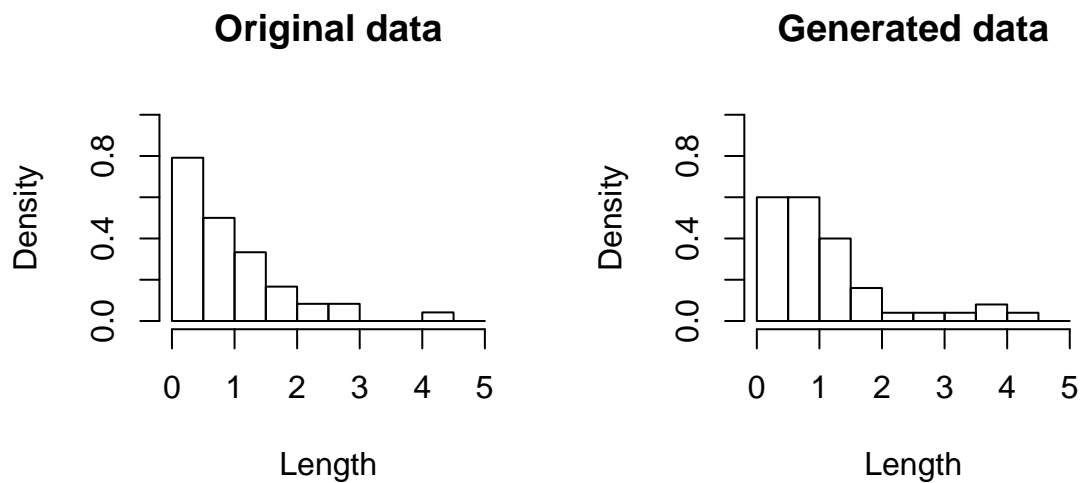


Figure 3: log likelyhood for task 4

Task 5



As seen in the above figures (couldn't for the life of me get captions to work with two histograms), we see that the distributions are very similar.

They are not identical, the value of the original data seems to have more datapoints closer to zero, but we clearly see both have higher values for lower lengths, and then it decreases following approximately an exponential curve.

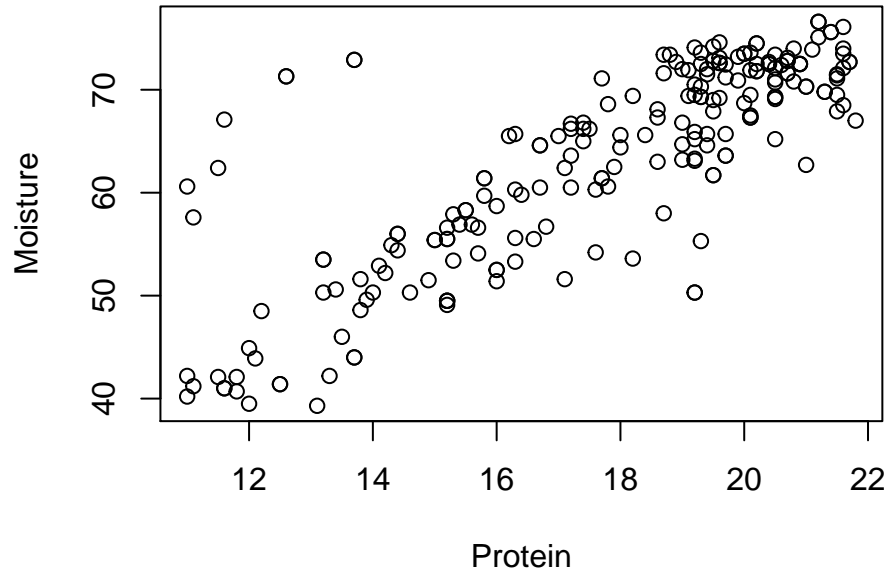


Figure 4: Moisture vs protein

Assignment 4

1

Looking at Figure 4, most of the datapoints are located in a basically linear line, which implies the model is described well by a linear model.

2

A model that describes M_i can be written as

$$y_{\text{tilde}} N \left(\sum_{n=1}^i x^i, \sigma^2 \right)$$

where x is the Protein data.

MSE is appropriate because MSE gives exponentially higher error the bigger the error, this means an overfitted model which work bad on validation data will give a larger error, a decently fitted model will give a smaller error.

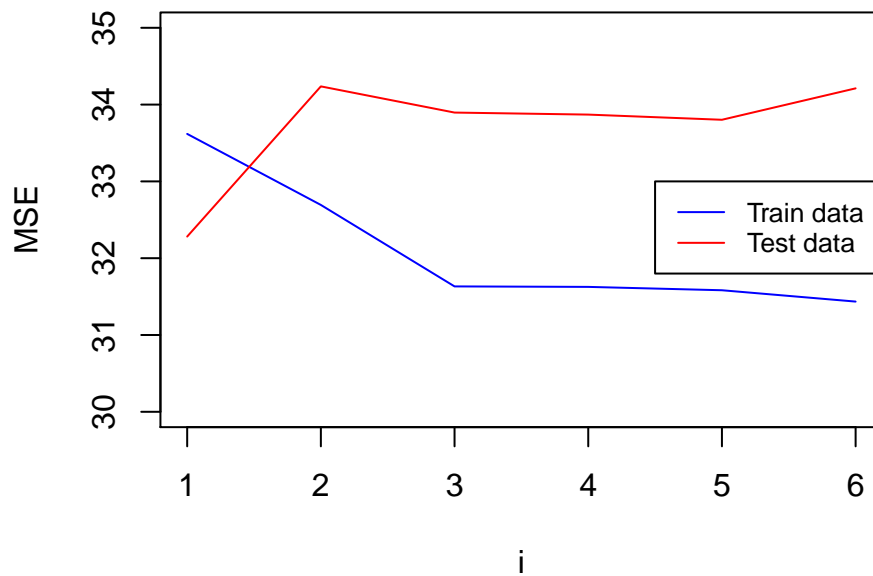


Figure 5: MSE for different i in M_i

3

As seen in Figure 4 we see that model $i = 1$ has the lowest MSE for the test data, and should thus be selected.

We can see that after $i = 2$ the MSE for test data becomes higher while train data gets lower, this is probably due to the more advanced models overfitting the training data (As we can see in Figure ??, the solution looks very linear)

4

The amount of variables selected is 64

5