

ASSIGNMENT/ASSESSMENT ITEM COVER SHEET

Student Name:

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Course Code

Course Title

(Example)

A	B	C	D	1	2	3	4
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(Example)

Intro to University

Campus of Study:

(eg Callaghan, Ourimbah, Port Macquarie)

Assessment Item Title:

Due Date/Time:

Tutorial Group (If applicable):

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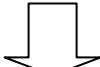
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Problem 1

(a) $\text{double}(a^* b^*)$ is an empty string because in $s = x w w y$, w can either be a, b or ϵ hence ' a ' and ' b ' cannot be adjacent so it has to be empty, $\text{double}(a^* b^*) = \{\epsilon\}$

(b) $\text{doubles}(ab)^*$

The Kleene star of this language means zero or more (ab) so its double is (ab) .

(c) Yes INF is closed under doubles. We know if a language is closed under that double if we apply that operation and it will give answer already in the string. There are two consecutive value of w and L is infinite so $\text{double}(L)$ will also be infinite.

(d) No, Regular languages are not closed under dousler.

Machine might have to immediately go through the part of language already been read. Therefore It can be infinite number and Regular language has to ^{be} finite.

Problem 2

(a) $L = \{0^m 1^n : m=3n+2, n \geq 0\}$

In this we have to maintain equation of $3n+2$ and $0^m 1^n$ mean 0 are followed by 1.

We have to generate Multiple of 3 of '0' compare to '1' and 2 more '0' before 1.

So,

if $n=0$ We generate 2 zero's and rest we generate 3 zero's followed

$$S \rightarrow 00T$$

$$T \rightarrow 000T | iT | \epsilon$$

Problem #2

(b) $L = \{w \in \{0,1\}^*\}$

Ans: In this language, '0' always
or comes in pair with '1', but
one '1' can come by itself e.g.

$$\begin{array}{l} S \rightarrow TS \mid \epsilon \\ T \rightarrow 0U1 \\ U \rightarrow 1T \mid 1 \end{array}$$

(c) $L = \{w \in (L_1 L_2)^*\}$

We need rules for L_1 and L_2
and a S .

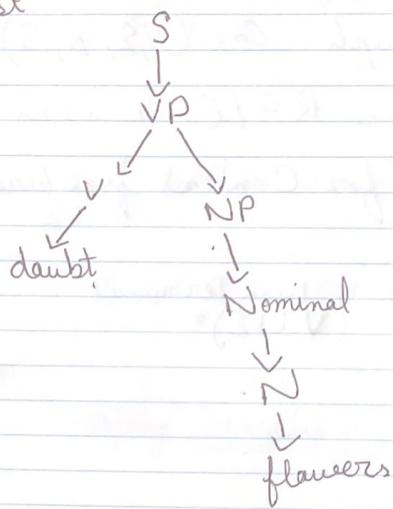
$$\begin{array}{l} S \rightarrow L_1 L_2 S \mid \epsilon \\ L_1 \rightarrow 0L_1 0 \mid 1L_1 1 \mid \epsilon \\ L_2 \rightarrow aL_2 a \mid bL_2 b \mid \epsilon \end{array}$$

Parse Trees

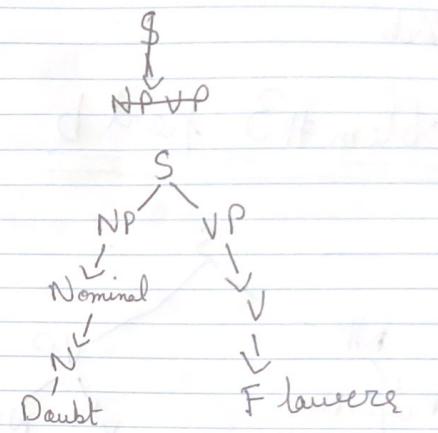
Problem 3

(a) Doubt Flower

First



(a)
2nd Parse Tree

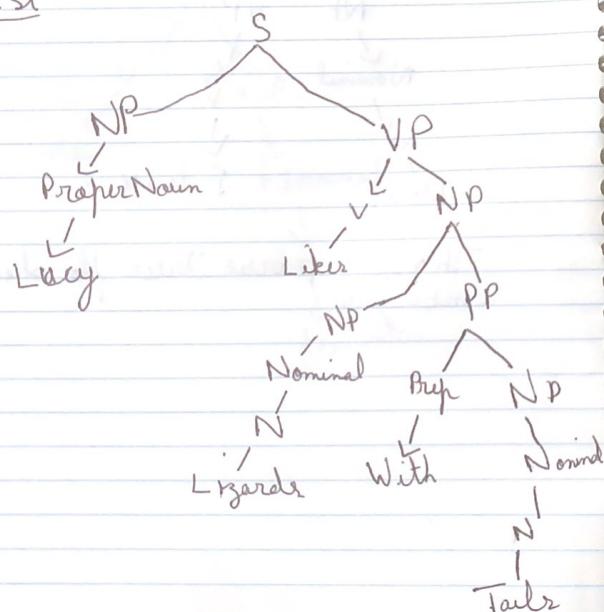


These 2 parse trees do show ambiguity

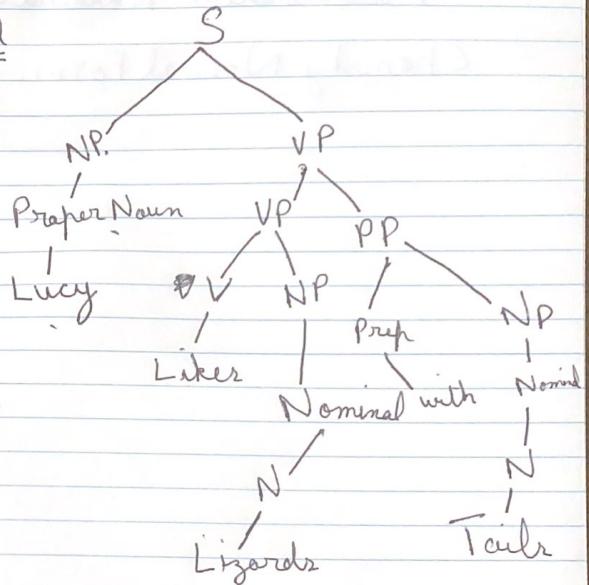
Problem #3
Ppb

Problem #3 part b

1st



2nd



B Above two graphs show ambiguity

Problem # 4

Chomsky normal form.

$$S \rightarrow Xyx$$

$$X \rightarrow yy\bar{y}y$$

$$X \rightarrow Z$$

$$Y \rightarrow xY$$

$$Y \rightarrow \epsilon$$

$$Z \rightarrow zZ$$

$$Z \rightarrow z.$$

To remove epsilon production
or Null production

1st. Nullable: X, Y.

$$S \rightarrow Xyx | y\bar{y}y | Xy | yx$$

$$X \rightarrow yy\bar{y}y | y\bar{y}y | y\bar{y}Z$$

$$Y \rightarrow xY | x$$

$$Z \rightarrow zZ$$

$$Z \rightarrow z.$$

Q#4

2. Removing unit production

$$S \rightarrow XyX|yX|XY|y$$

~~X~~
$$X \rightarrow YY|YY|z|z$$

$$Y \rightarrow zY|z$$

$$Z \rightarrow zZ|z$$

3. Removing Mixed production

Adding rules

$$Ty \rightarrow y, Tx \rightarrow x, Tz \rightarrow z.$$

$$S \rightarrow \cancel{Ty}X|TyX|XY|y.$$

$$X \rightarrow YY|YY|z|z.$$

~~X~~
$$\cancel{Tx}Y \rightarrow TxY|z$$

$$Z \rightarrow TzZ|z$$

4. Removing long production

$$S \rightarrow M, X|TyX|XY|y$$

$$X \rightarrow M_2Y|YY|z|z$$

$$Y \rightarrow TxY|z$$

$$Z \rightarrow TzZ|z$$

$$\begin{array}{l} \overline{T_y} \rightarrow y \\ \overline{T_2} \rightarrow \varnothing \\ \overline{T_x} \rightarrow \varnothing \end{array}$$
$$\begin{array}{l} M_1 \rightarrow X \overline{T_y} \\ M_2 \rightarrow Y \overline{T_y} \end{array}$$

Problem #5

$$K = q_0, q_1, q_2, \cancel{q_3}$$

$$\Sigma = a, b$$

$$\Gamma = A.$$

$$S = q_0$$

$$A = q_0$$

$$\Delta =$$

$$1. (q_0, a, \epsilon) = \{(q_0, A)\}$$

$$2. (q_0, a, A) = \{(q_0, AA)\}$$

$$3. (q_0, b, AA) = \{(q_0, \epsilon)\}$$

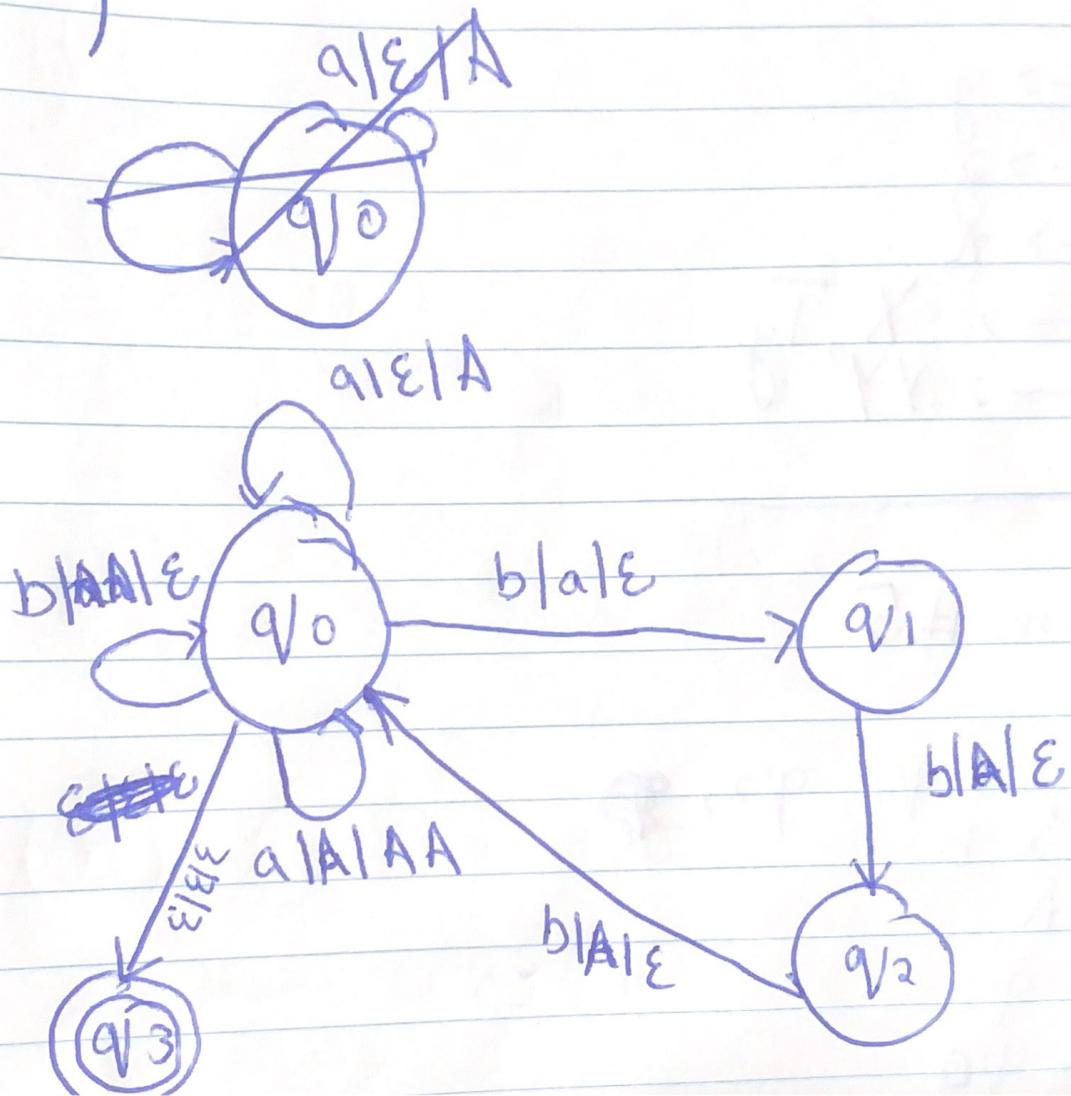
$$4. (q_0, b, A) = \{(q_1, \epsilon)\}$$

$$5. (q_1, b, A) = \{(q_2, \epsilon)\}$$

$$6. (q_2, b, A) = \{(q_0, \epsilon)\}$$

$$7. (q_0, \epsilon, A) = \{(q_3, \epsilon)\}$$

a)



5(b)

$$(q_0, a, \epsilon) = \{q_0, A\}$$

$$(q_0, a, A) = \{q_0, \cancel{A}\}$$

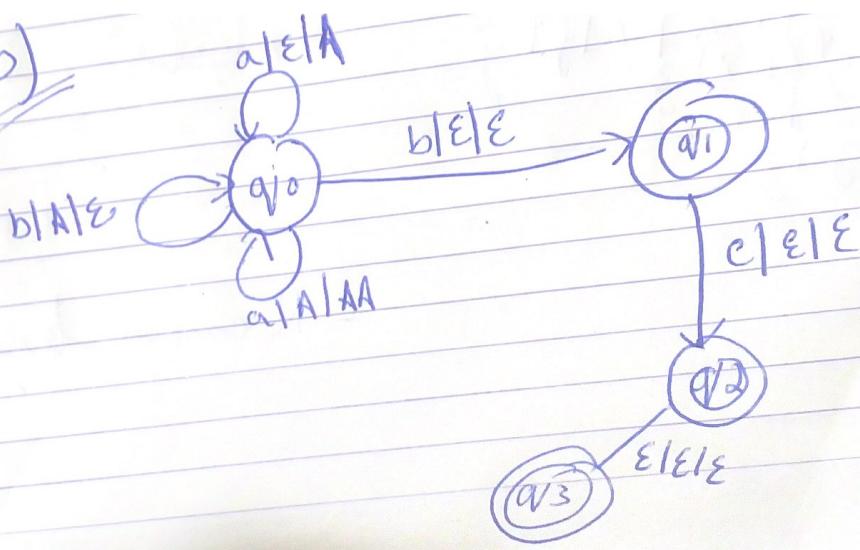
$$(q_0, b, A) = \{q_0, \epsilon\}$$

$$(q_0, b, \epsilon) = \{q_1, \epsilon\}$$

$$(q_1, c, \epsilon) = \{q_2, \epsilon\}$$

$$(q_2, \epsilon, \epsilon) = \{q_3, \epsilon\}$$

5 (b)



Q6

(a)

$L(M) \rightarrow$ This PDA accept
this language if it has same or
3 more number of 'b' as there are
'a'. It start with 'a' and followed
by same or more 'b'.

6(b)

Content-free-Grammer

$$S \rightarrow aSb \mid T$$

$$T \rightarrow bT \mid b$$

(c) No, M is not deterministic,
because for deterministic PDA
There is atmost one clear path. here
M has Multiple path.

(d) To Prove M is deterministic

$$K = q_0, q_1$$

$$\Sigma = a, b$$

$$\Gamma = A$$

$$S = q_0$$

$$A = q_0, q_1$$

$$\Delta = \{q_0, a, \epsilon\} \sim \{q_0, A\}$$

$$= \{q_0, a, A\} = \{q_0, A\}$$

$$(q_0, b, A) = (q_1, \epsilon)$$

$$(q_1, b, A) = (q_1, \epsilon)$$

$$(q_1, b, \epsilon) = \{q_1, \epsilon\}$$

Q7 (a)

L_2 is a superset of L_1
and L_2 is context free and
not regular

We know $a^n b^n$ is not regular

$$L_2 = \{a^n b^n : n \geq 0\}$$

$$L_1 = \{a^n\}$$

Here, L_1 is the set of all possible strings of 'a' consisting of 'a'.

We can say from $L_1 = \{a^n\}$
that it is a regular language
because we can design FSM or
for it and its regular expression
would be a^* .

L_2 is the language of equal number of 'a' followed by equal number of 'b'. and

We know that FSM or cannot be built for that and it is not regular but PDA can recognise that : We can represent in Context free Grammar

$$S \rightarrow a S b | \epsilon$$

Q7(b)

True, because L_1 is a content free language and under closure properties L should be content free as well.

We know that context free languages are closed under Kleene plus (+) and concatenation.

So, if we can make CFG for L_1 , then we can also make it for L_1^+ . so it means L is also context free.

Let $L_1 = \{ w | w \in \{a,b\}^* \text{ and } a \text{ in } w = b \text{ in } w \}$

$S \rightarrow aSb \mid bSa \mid \epsilon$

from it we can say $L = L_1^+$.

Q8

(a) This language is ~~not~~ regular
but context free.

CFG

$$S \rightarrow aSbb \mid \epsilon$$

Pumping Lemma is used to prove
language is ~~not~~ regular or
not and for Context free.

Let

w in a language $w = a^n b^{2n}$ for
some n. According to pumping lemma
theorem we can divide it into
parts, $|xy| \leq n$, when we pump
y which consist of 'a' the string
will change but the value of 'a' in
string remain the same. Therefore
there is a contradiction and it
is not regular.

8

(b) $\{a^n b^m a^n b^m a^n : n, m \geq 0\}$

This language is not regular
and context free

We can assume contradiction
by using pumping lemma
for regular language, consider s ,
such that $|s| \geq p$ can be divided
into 3 parts; for every $i \geq 0$, yiz is
in L .

In 3 sections of 'a' have the same
length and y must consist of
'b'. if we pump string once
either section of 'a' not the same
or 'b' so not in L .

e.g.

9a

Lindenmayer or L-system is a type of formal grammar system that is used to generate fractal. An L-system consists of symbols that transform each symbol into strings of symbols an initial string called axiom.

Koch curve, which is fractal starting with axiom F and applying rule $F \rightarrow F + F - F - F + F$ for each symbol.

ab

To interpret strings as turtle program each string is assigned a meaning that correspond to a turtle command. e.g F means move forward, + means turn left, - mean turn right. following command of symbol. This method are a way of drawing shapes using a relative cursor that moves on cartesian plane.

Q10:

(a) Input \square abab

result: The machine will halt immediately on reading first symbol ' \square '.

(b)

In state R, reading ' \square ' machine will halt immediately and transition to halt state

C This turing machine checks the input of 'a' and 'b'. If this machine sees 'b' after two consecutive 'b' in Mid or final state it moves back to initial state. On receiving 'empty' in R state it will halt immediately.