

# 1

## 1.1

(a)

Let us note that due to the formula that defines each  $\alpha_i$  the sum of all  $\alpha_i$  is 1. Hence, by looking at each value as category we easily get that this is a categorical distribution.

(b)

This would happen if

1. there exists some  $k_j$  where  $k_j^T q$  is large and
2. for all other  $k_i$  where  $i \neq j$   $k_i^T q$  is small.

Let us remember that  $a^T b = |a||b|\cos(\theta)$  where  $\theta$  is the angle between  $a$  and  $b$ . Hence for the conditions above to hold we need that  $k_j$  is parallel to  $q$  and all other  $k_i$  are in the opposite direction to  $q$ .

Plus, we need that either  $q$  is very large (i.e large norm) or that  $k_j$  is very large or that the other  $k_i$  vectors norm is very large.

(c)

Assuming that the conditions above are correct, we get that  $c \approx v_j$

(d)

This means that the output  $c$  will depend almost only on a single  $v_j$  that corresponds to the  $k_j$  that is parallel to  $q$ . This is, obviously, not desirable since we want the output to be contextualized, i.e depend on the full sentence. Without this property the model will not be expressive enough.

## 1.2

(a)

Let us define the following matrix  $M$ :

$$M = c_1 \frac{a_1 a_1^T}{a_1^T a_1} + c_2 \frac{a_2 a_2^T}{a_2^T a_2} + \dots + c_m \frac{a_m a_m^T}{a_m^T a_m}$$

If we multiply  $M$  by  $a_i$  we get that

$$M a_i = c_i a_i$$

i.e,  $a_i$  is an eigenvector of  $M$  with eigenvalue  $c_i$ . That means that

$$Mv_a = M(a_1 + \dots + a_m) = Ma_1 + \dots + Ma_m = c_1a_1 + \dots + c_ma_m = v_a$$

Plus, when multiplying  $M$  by  $v_b$  we get that

$$Mv_b = c_1 \frac{a_1 a_1^T v_b}{a_1^T a_1} + c_2 \frac{a_2 a_2^T v_b}{a_2^T a_2} + \dots + c_m \frac{a_m a_m^T v_b}{a_m^T a_m}$$

we know that  $a_i^T v_b = 0$  for all  $i$  since

$$a_i^T v_b = a_i^T b_1 + \dots + a_i^T b_m = 0$$

which is true because the two basis are supposed to be orthogonal. Hence

$$Mv_b = 0$$

Hence we finally get that

$$Ms = Mv_a + Mv_b = v_a$$

**(b)**

we define  $q$  as follows:

$$q = (k_a + k_b) * H$$

where  $H$  is some Huge number. It holds that

$$k_a q = k_b q = H$$

Plus, it holds that

$$k_i q = 0$$

if  $i \neq a, b$ . We get that  $\alpha_a = \alpha_b = \frac{e^H}{n-2+2e^H}$  and  $\alpha_i = \frac{1}{n-2+2e^H}$  for  $i \neq a, b$ .

For large enough  $H$  we get that  $\alpha_a \approx \alpha_b \approx \frac{1}{2}$  and  $\alpha_i \approx 0$  for  $i \neq a, b$ . Hence  $c \approx \frac{1}{2}(v_a + v_b)$

**2**

**2.d**

The result of london baselinr is -

Correct: 25.0 out of 500.0: 5.0%

The result of the finetuned model is -

Correct: 10.0 out of 500.0: 2.0%

**2.f**

Correct: 115.0 out of 500.0: 23.0%

## 2.g

Let us note that the pretraining data contains the birthplace information about the individuals which are in the birth\_dev dataset. It seems that the model is able to "remember" the birthplace knowledge that it acquires during pretraining, and it is able to infer that knowledge during evaluation. Let us also note that the finetuning process does not make the model forget the knowledge it acquired during pretraining.

## 3

### 3.a

Results for beam search were better for all prompt sizes.

### 3.b

Validation question:

What are Jimmy Reed, Skip James, Elmore James and Big Bill Broonzy best known as?

Prompt:

Answer: Eleonore Roosevelt Question: On which Caribbean island did Princess Diana spend her first Christmas after her divorce was announced? Answer: Barbuda Dependency, Antigua and Barbuda Question: Who wrote the song Mamma Told Me Not To Come? Answer: Randy Newman Question: What is the distance between bases on a little league baseball field? Answer: sixty distance Question: Which NASA space probe was launched to Venus in 1989? Answer: List of things named for Ferdinand Magellan Question: Which member of the Monkees came from Washington DC? Answer: Peter Tork Question: Who was the woman sentenced to six years in jail after the murder of Stompei Seipi? Answer: Winnifred Mandela Question: Which Italian fashion designer was murdered on the orders of his ex-wife? Answer: House of Gucci

Validation question:

For which movie did Katharine Hepburn win her second Oscar?

Prompt:

Question: Which African country is sandwiched between Ghana and Benin? Answer: Religion in Togo Question: Which African country is bordered by Benin, Ghana, Ivory Coast, Niger, and Mali? Answer: Burkina Faso Question: Which country mainly makes up the Horn of Africa? Answer: Somalia Question: In The Banana Splits what sort of animal was Snorky? Answer: Elephantineness Question: What are the two main arms of the River Nile called? Answer: Blue Nile and White Nile Question: Name the East African country which lies on the equator. Answer: Prehistory of Kenya Question: What are the international registration letters of a vehicle from Algeria? Answer: DZ (disambiguation) Question: Banting and Best pioneered the use of what? Answer: Insullin

### 3.c

Some generation examples:

I'm not sure, but I'm pretty sure it's not me. I don't 'Run!|| †Run for your life! ‡‡Run Gummo: "Chico"  
and "Harpo" are my last names. It depends on the type of plant. For example, if the plant is a shrub

## References