

Lab 2 report – Dynamic allocation and recursion

1. Objective:

The student will practice how to

- Implement a simple algorithm using dynamic arrays (STL vectors)
- Design and implement recursive functions.
- Describe the running time of the recursive functions using recurrence relations.

2. Tasks:

2.1. **Tribonacci sequence:**

The Tribonacci sequence T_n is defined as follows:

$T_0 = 0, T_1 = 1, T_2 = 1$, and $T_n = T_{n-1} + T_{n-2} + T_{n-3}$ for $n \geq 3$.

Given n , return the value of T_n .

Required:

- Write a recursive function to calculate T_n .
- Write the recurrence relation of the Tribonacci function.

2.2. **Fibonacci sequence:**

The Fibonacci numbers, commonly denoted $F(n)$ form a sequence, called the Fibonacci sequence, such that each number is the sum of the two preceding ones, starting from 0 and 1. That is, $F(0) = 0, F(1) = 1$,

$F(n) = F(n - 1) + F(n - 2)$, for $n > 1$.

Required:

- Write a function to calculate F_n and consider the range of n .
- What is the time and space complexity for your code?

2.3. **Reverse string recursively:**

you need to design a recursive function that given a string S , returns it in reversed order.

Required:

- Write a recursive function to reverse a string.
- Write the recurrence relation and determine its running time in big O notation.

2.4. **Subarray division:**

Given an array A , find the number of subarrays of length m such that the sum of its elements equals d .

Required:

- Implement your algorithm to solve the problem.
- What's the running time of your algorithm?