

AI Assignment

- 19K41A0469

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→ Draw a decision tree diagram to predict numbers of hours to play based on weather conditions like Outlook, temperature, humidity, windy, consider dataset shown below:

Outlook	Temperature	Humidity	Windy	Hours to play
		High	False	25
Rainy	Hot	High	True	30
Rainy	Hot	High	False	46
Overcast	Hot	High	False	45
Sunny	Mild	High	False	52
Sunny	Cool	Normal	True	43
Overcast	Cool	Normal	False	35
Rainy	Mild	High	False	38
Rainy	Hot	Normal	False	
Rainy	Mild	Normal	True	
Sunny	Mild	Normal	True	46
Rainy	Mild			48
Overcast	Mild	High	True	52
Overcast	Hot	Normal	False	44
Sunny	Mild	High	True	30
Sunny	Cool	Normal	True	23

Termination criteria : $CV \leq 10\%$ or minimum no. of Same
calculating mean, Standard deviation (SD), coefficient of
variation (CV)

$$\text{mean} = \frac{\sum x}{n} = \frac{557}{14} = 39.78$$

$$SD = \sqrt{\frac{\sum (x - \text{mean})^2}{n}} = 9.67$$

$$CV = \frac{SD}{\text{mean}} \times 100 = \frac{9.67}{39.78} \times 100 = 34.50$$

Now, data set is split into different attributes. The SD of each branch is calculated.

$$SD(\text{after}) = \sum w(\text{branch}) \cdot SD(\text{branch})$$

and the result SDR (Standard deviation reduction) is calculated

$$SDR = SD - SD(\text{after})$$

$$\therefore SD = 9.67$$

Outlook :

Outlook	mean	SD	CV	n	w(v)
Rainy	35.2	8.7	24.7	5	5/14
Overcast	46.25	4.03	8.72	4	4/14
Sunny	39.2	12.2	31.0	5	5/14

$$\therefore SD(\text{outlook}) = \frac{5}{14} * 8.7 + \frac{4}{14} * 4.03 + \frac{5}{14} * 12.2 = 8.59$$

$$SDR(\text{outlook}) = SD - SD(\text{outlook}) = 9.67 - 8.59 = 1.08$$

Temperature :

Temperature	Mean	SD	CV	n	w(v)
Hot	36.25	10.34	30.6	4	4/14
Cool	39	12.14	31.1	4	4/14
Mild	42.6	8.38	19.65	6	6/14

$$SD(\text{temperature}) = \frac{4}{14} * 10.34 + \frac{4}{14} * 12.14 + \frac{6}{14} * 8.36 = 10.01$$

$$SDR(\text{temperature}) = SD - SD(\text{temperature}) = 9.67 - 10.01 = -0.34$$

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Humidity :

Humidity	mean	SD	CV	n	w(V)
High	37.51	10.11	26.92	7	7/14
Normal	42	9.4	22.4	7	7/14

$$\therefore SD(\text{humidity}) = \frac{7}{14} \times 10.11 + \frac{7}{14} \times 9.4 = 9.77$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity})$$

$$= 9.67 - 9.77 = -0.1$$

Windy :

Windy	mean	SD	CV	n	w(V)
True	37.6	11.6	30.8	6	6/14
False	41.3	8.41	20.3	8	8/14

$$\therefore SD(\text{windy}) = \frac{6}{14} * 11.6 + \frac{8}{14} * 8.41 = 9.77$$

$$SDR(\text{windy}) = SD - SD(\text{windy}) = 9.67 - 9.77 = -0.1$$

$$SDR(\text{outlook}) = 1.08$$

$$SDR(\text{Temperature}) = -0.34$$

$$SDR(\text{Humidity}) = -0.1$$

$$SDR(\text{windy}) = -0.1$$

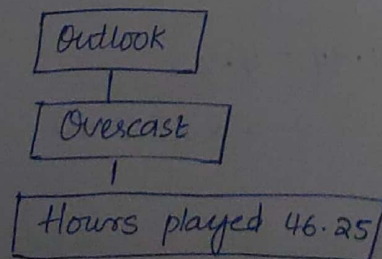
The value that has highest SDR is considered as root node (i.e. decision node)

Considering termination criteria

CV is 10% or CV is ($n \leq 4$)

Over cast has CV of 8% which is less than threshold.

4. Value therefore, we need not go for further splitting.



We need to Split Sunny & rainy columns.

Outlook	Temperature	Humidity	Windy	Hours played
Sunny	mild	High	False	45
Sunny	cool	Normal	False	52
Sunny	cool	Normal	True	23
Sunny	mild	Normal	False	46
Sunny	mild	High	True	50

$$\therefore \text{mean} = 39.2, \text{SD} = 12.2; \text{CV} = 31.0$$

Temperature:

Temperature	mean	SD	CV	n	w(v)
Mild	40.3	8.96	22.23	3	3/5
Cold	37.5	20.50	54.66	2	2/5

$$\text{SD}(\text{temperature}) = \frac{3}{5} * 8.96 + \frac{2}{5} * 20.5 = 13.576$$

$$\text{SDR}(\text{temperature}) = \text{SD} - \text{SD}(\text{temperature}) = 12.2 - 13.576 = -1.37$$

Humidity:

Humidity	mean	SD	CV	n	w(v)
High	37.5	10.6	28.26	2	2/5
Normal	40.3	15.30	37.96	3	3/5

$$\text{SD}(\text{humidity}) = \frac{2}{5} * 10.6 + \frac{3}{5} * 15.30 = 13.44$$

$$\text{SDR}(\text{humidity}) = \text{SD} - \text{SD}(\text{humidity}) = 12.2 - 13.42 = -1.22$$

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Windy:

Windy	mean	SD	CV	n	w(v)
False	47.66	3.78	7.94	3	3/5
True	26.5	4.94	18.65	2	2/5

$$\text{SD}(\text{windy}) = \frac{3}{5} * 3.78 + \frac{2}{5} * 4.94 = 4.23$$

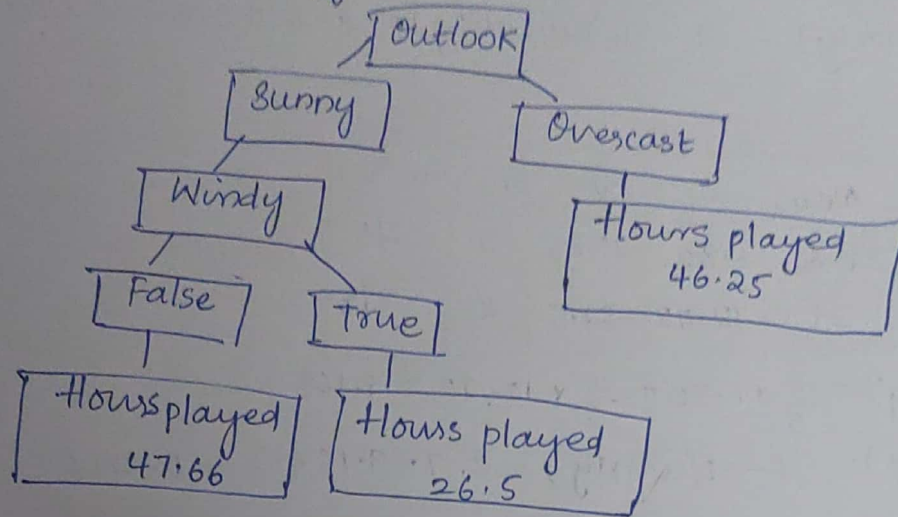
$$\text{SDR}(\text{windy}) = \text{SD} - \text{SD}(\text{windy}) = 12.2 - 4.23 = 7.97$$

In Outlook

among, Temperature, humidity and windy SDR value is high
for windy $SDR = 7.97$

Then, check for cv value

both True & False satisfy the cv value



Rainy :

Outlook	Temperature	Humidity	Windy	Hours played
Rainy	Hot	High	False	25
Rainy	Hot	High	True	30
Rainy	Mild	High	False	35
Rainy	Cool	Normal	False	38
Rainy	Mild	Normal	True	48

6. Mean = 35.2 SD = 8.7, CV = 24.7

Temperature	Mean	SD	CV	n	w(CV)
Hot	29.5	3.53	12.83	2	2/5
Mild	41.5	9.19	22.144	2	2/5
Cool	38	0	0	1	1/5

$$SD(temp) = \frac{2}{5} * 3.53 + \frac{2}{5} * 9.19 + \frac{1}{5} * 0 = 5.088$$

$$SDR(temp) = SD - SD(temp) = 8.7 - 5.088 = 3.612$$

Humidity:

Humidity	Mean	SD	CV	n	w(v)
High	30	5	16.66	3	3/5
Normal	43	7.07	16.64	2	2/5

$$SD(\text{humidity}) = \frac{3}{5} * 5 + \frac{2}{5} * 7.07 = 5.828$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity}) = 8.7 - 5.828 = 2.872$$

Windy:

Windy	Mean	SD	CV	n	w(v)
False	32.66	6.80	20.85	3	3/5
True	39	12.72	32.5	2	2/5

$$SD(\text{windy}) = \frac{3}{5} * 6.80 + \frac{2}{5} * 12.72 = 9.168$$

$$SDR(\text{windy}) = SD - SD(\text{windy}) = 8.7 - 9.168 = -0.468$$

Among, Temperature & windy, SDR value for Temp (3.0612) is high. check cv value of hot, mild & cold satisfy the cv value.

7. Decision tree diagram to predict number of hours to play based on weather conditions.

