



CMPS 460 – Spring 2022

MACHINE LEARNING

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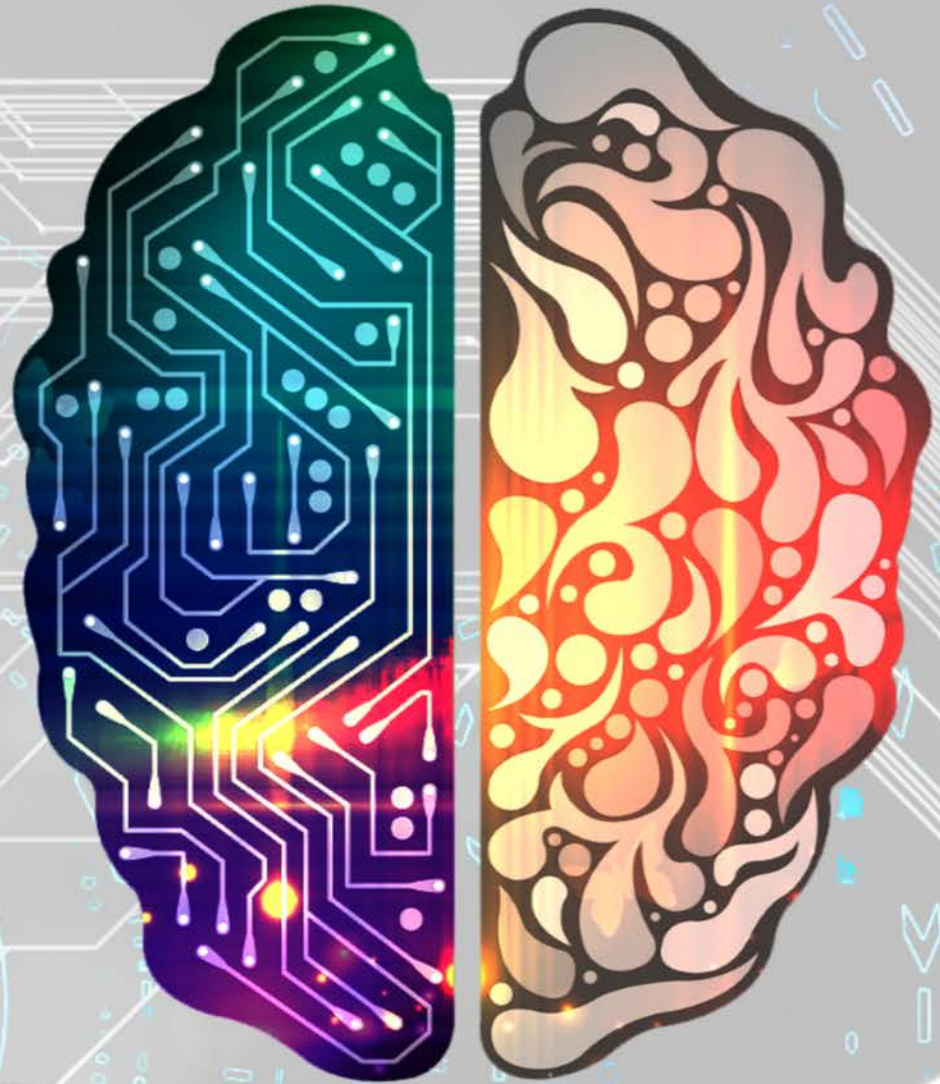


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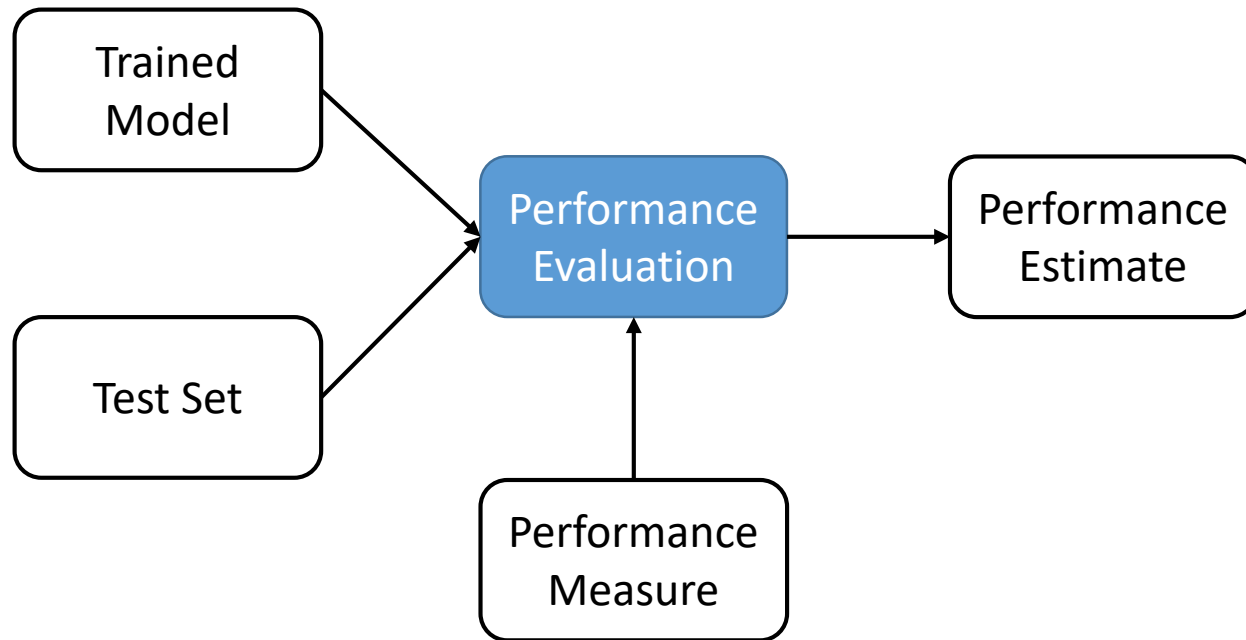
5.b

Practical Issues: Evaluation

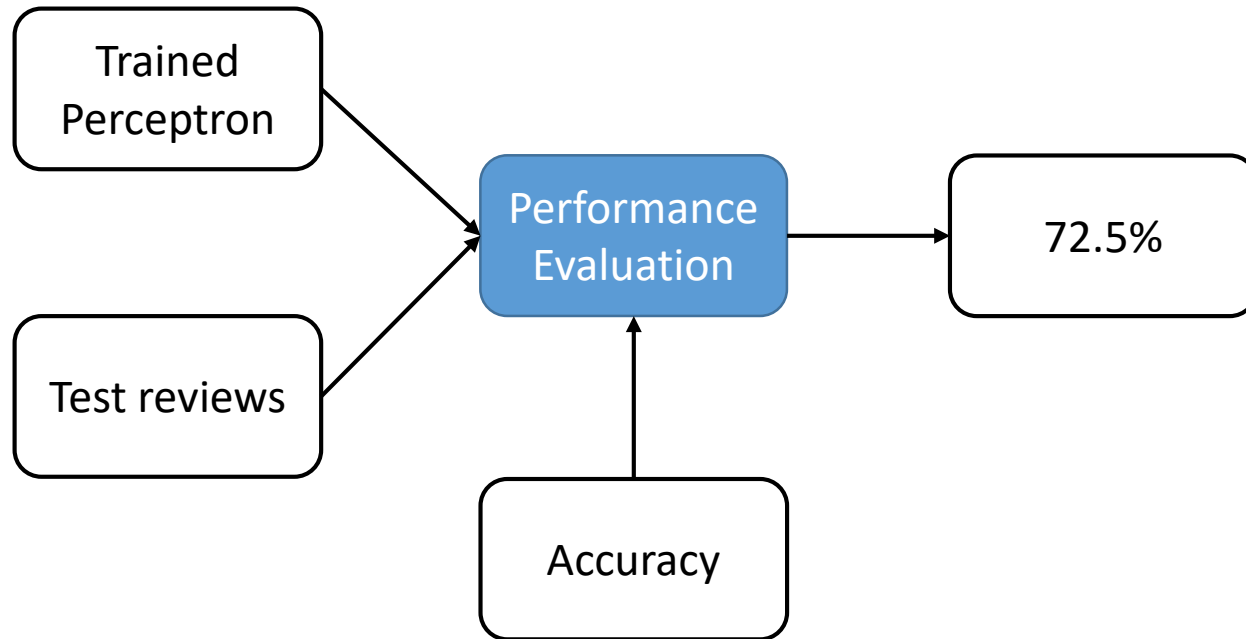


Sec 5.5-5.6

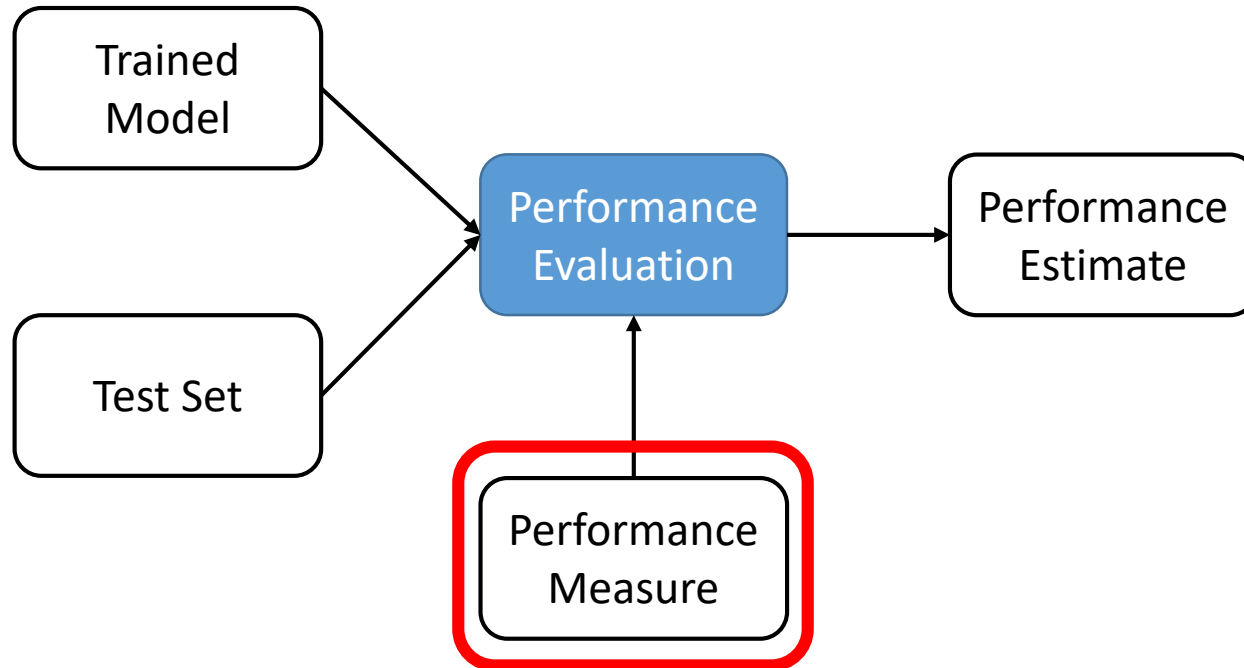
Performance Evaluation



Example



Performance Evaluation

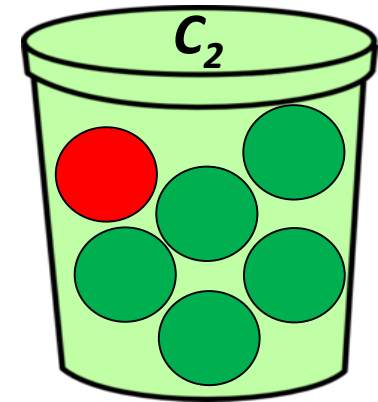
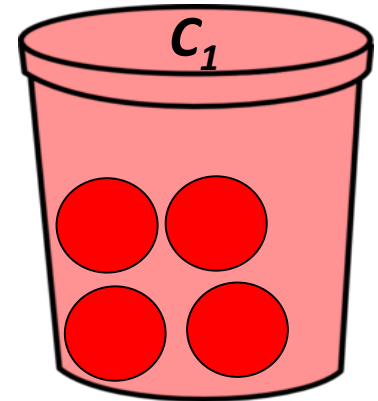
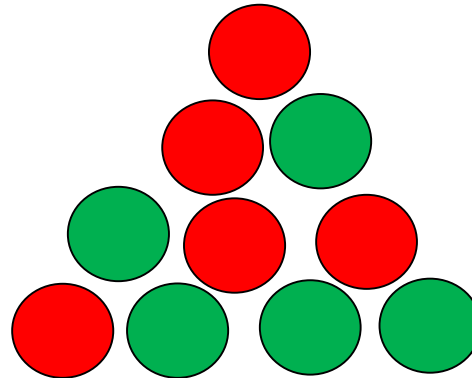


Accuracy

What fraction of the examples are classified correctly?

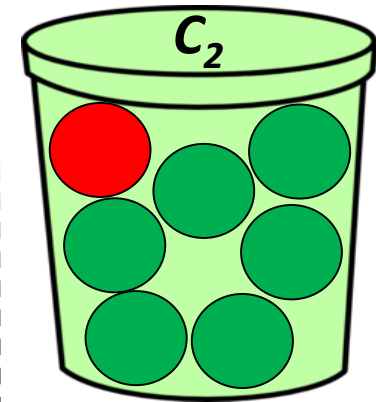
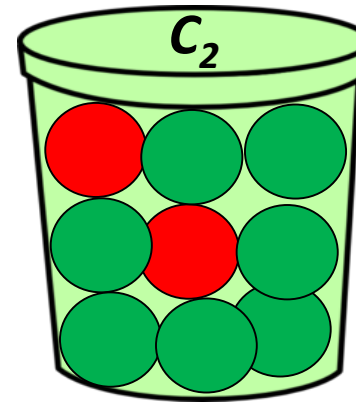
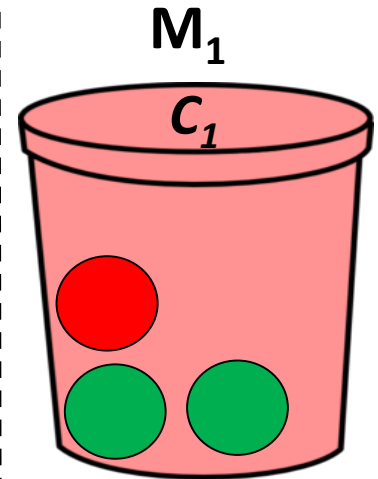
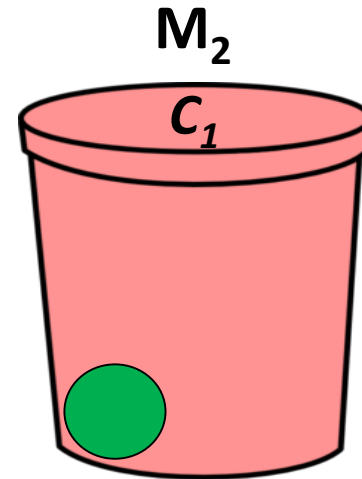
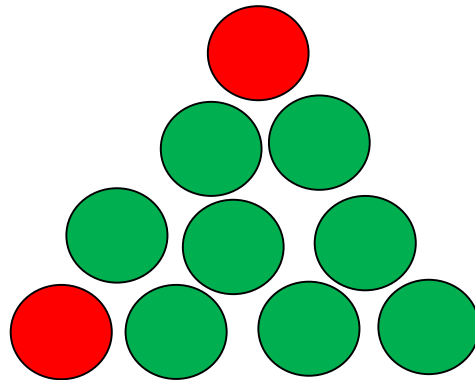
$$\text{Acc} = ?$$

$$= 9/10$$



Accuracy

- $\text{Acc}(M_1) = ?$
- $\text{Acc}(M_2) = ?$



What's the problem?

Problem with Accuracy?

- Imbalanced data (distribution of classes)!
- Some errors matter more than others ...
 - Given medical record, predict patient has COVID or not
 - Given an email, detect spam
- When classes are highly unbalanced, we focus on one target class (usually the rare class), denoted as the “positive” class.

**Precision/Recall/F1
for the target class (positive)**

Confusion Matrix

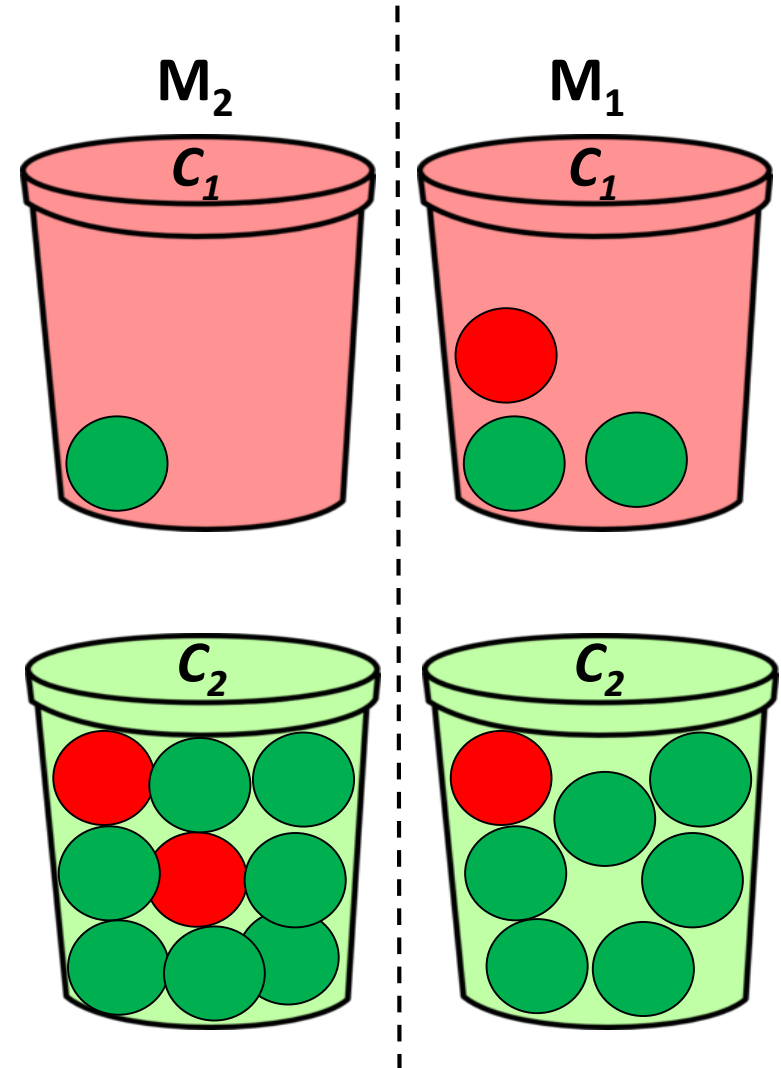
Actual	negative	positive
	negative	positive
Predicted	FP	TP
	TN	FN

Confusion Matrix

M_1	negative	?	?
	positive	?	?
		positive	negative
		Predicted	

M_2	negative	?	?
	positive	?	?
		positive	negative
		Predicted	

● positive

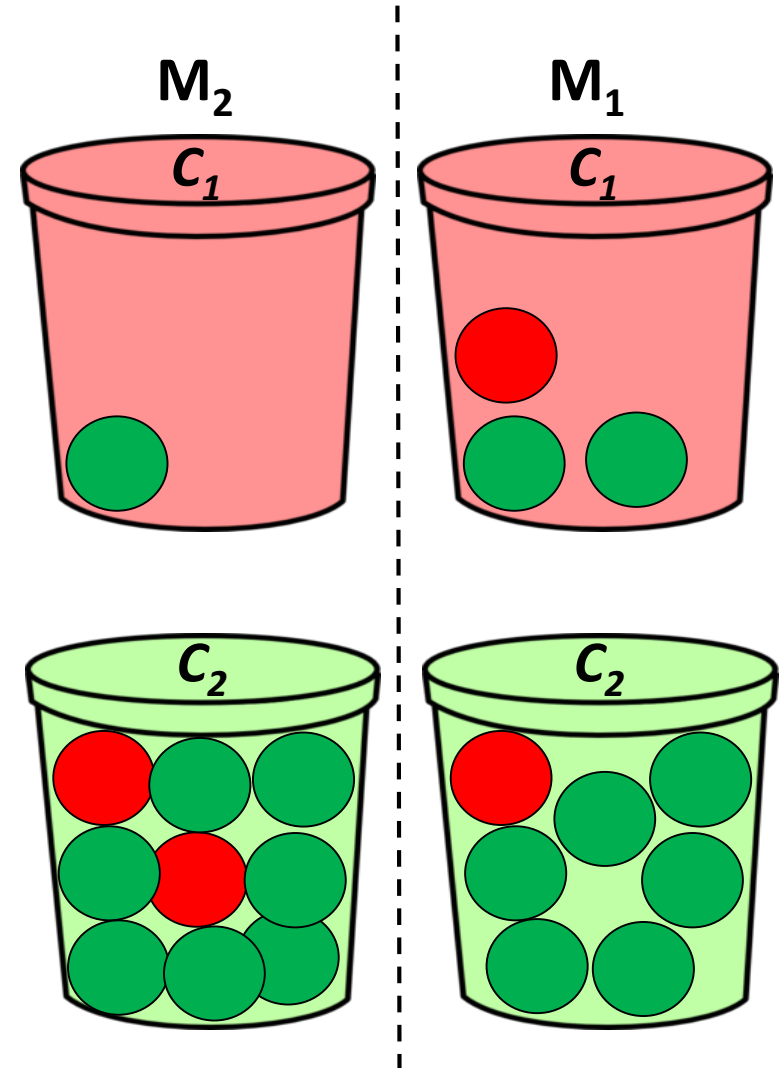


Confusion Matrix

M_1	negative	2	6
	positive	1	1
		positive	negative
		Predicted	

M_2	negative	1	7
	positive	0	2
		positive	negative
		Predicted	

● positive



Precision

M_1

Actual	negative	2	6
	positive	1	1
		positive	negative
		Predicted	

What fraction of those predicted as positive are actually positive?

$$P = \frac{TP}{TP + FP}$$

M_2

Actual	negative	1	7
	positive	0	2
		positive	negative
		Predicted	

$$P(M_1) =$$

$$P(M_2) =$$

Precision: % of positive predictions that are correct

Recall

M_1

Actual	negative	2	6
	positive	1	1
		positive	negative
		Predicted	

What fraction of the actual positive examples are predicted as positive?

$$R = \frac{TP}{TP + FN}$$

M_2

Actual	negative	1	7
	positive	0	2
		positive	negative
		Predicted	

$$R(M_1) =$$

$$R(M_2) =$$

Recall: % of gold positive examples that are found

Trade-off between P & R

Detect few positive examples but misses many others

1

Precision

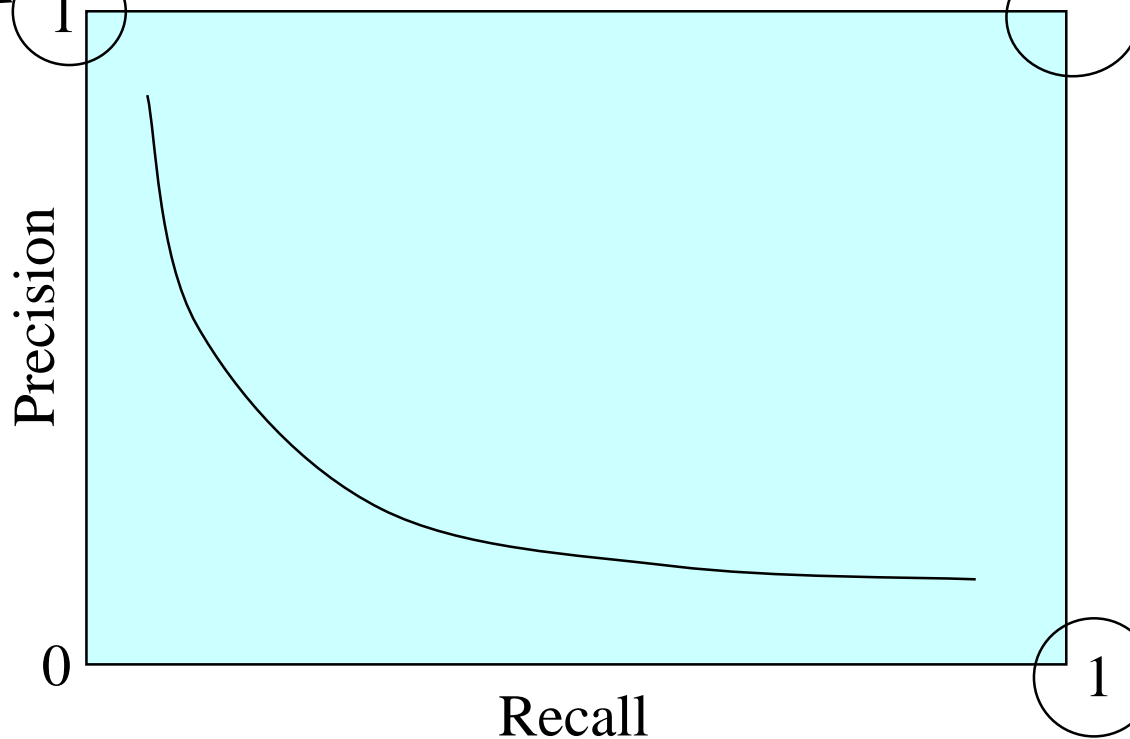
0

Recall

The ideal

Predict everything as positive

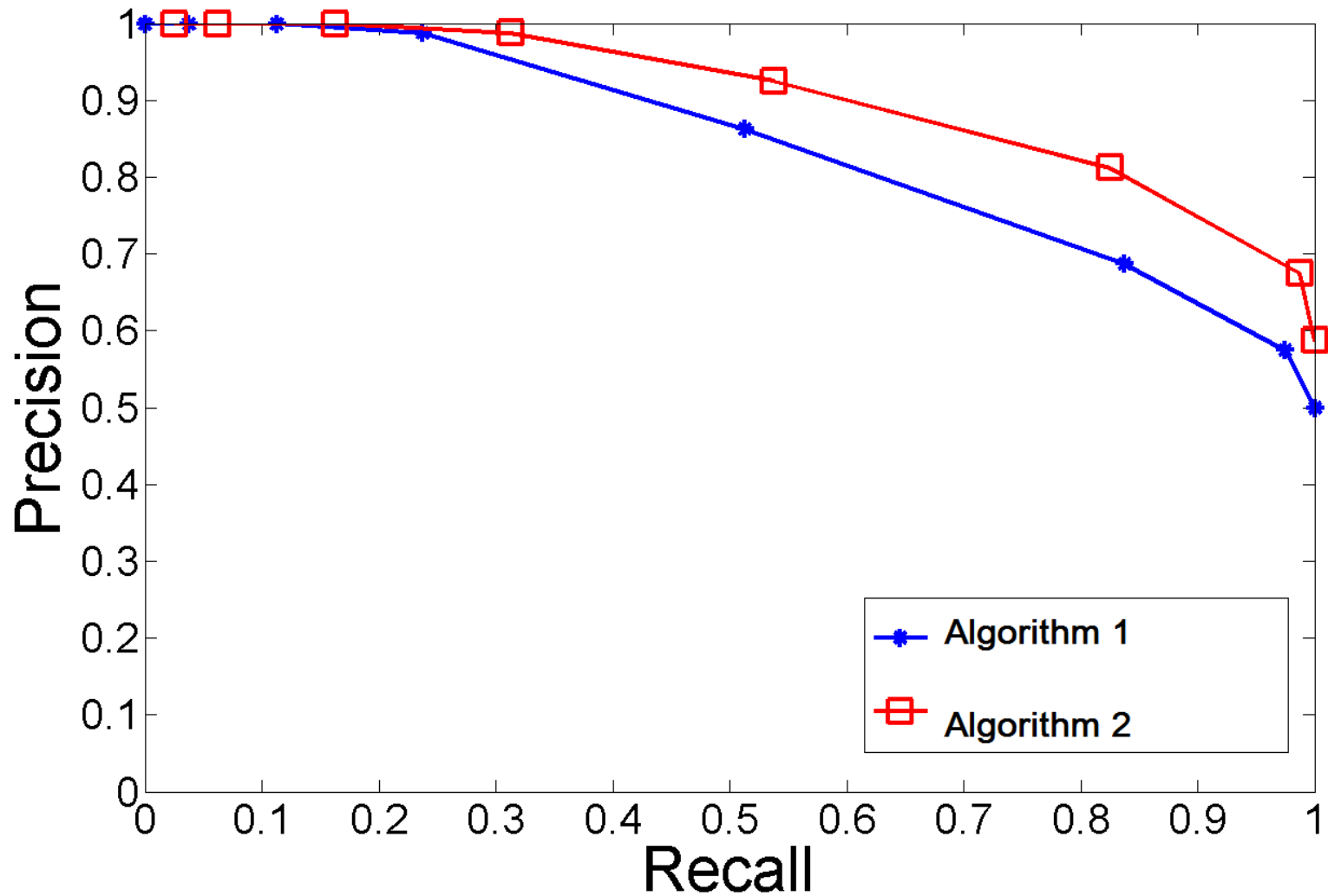
1



Example

Test example	Spam score	
email #25	0.94	
email #37	0.89	
email #2	0.76	
email #15	0.73	P=0.67, R=0.2
email #116	0.61	
email #64	0.54	
email #7	0.42	P=0.5, R=0.3
.....	
.....	
.....	
email #38	0.24	
email #10	0.16	
email #25	0.13	P=0.34, R=0.9
email #168	0.02	

Precision/Recall Curve



A Combined Measure: F -measure

- F_1 measure

$$F_1 = \frac{2 * P * R}{P + R}$$


– Harmonic mean of P and R

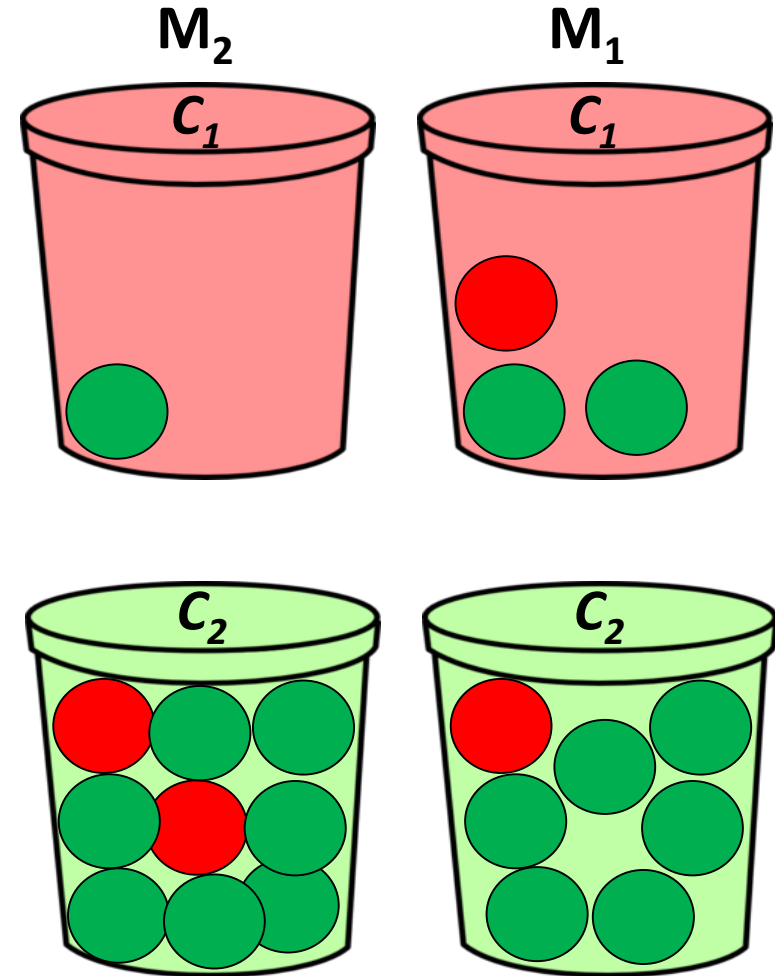
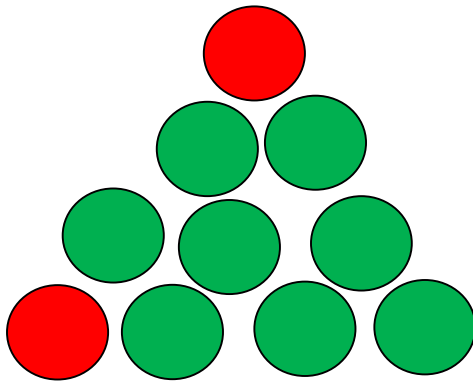
Why?

- Weighted F measure

$$F_\beta = \frac{(\beta^2 + 1) * P * R}{\beta^2 * P + R}$$

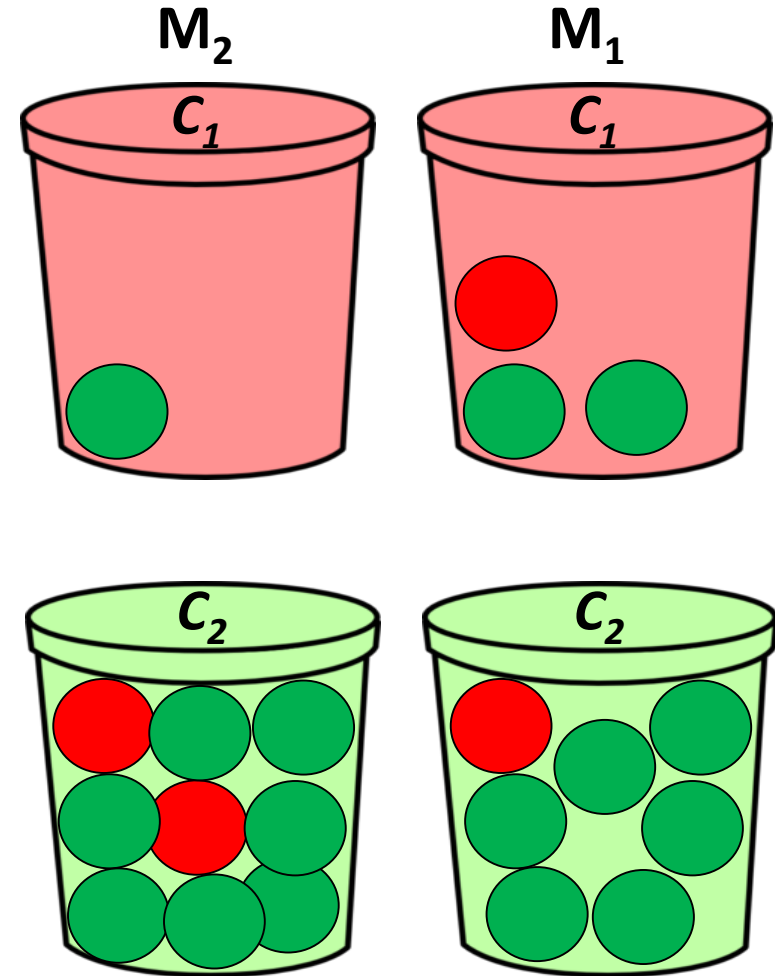
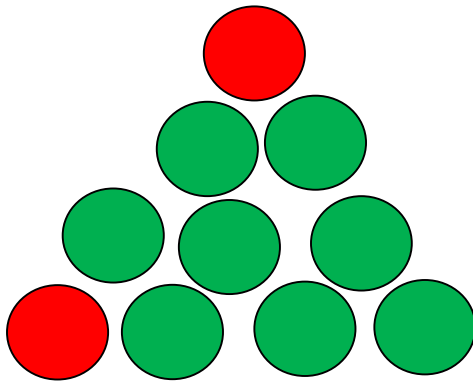
Binary Classification

	M_1	M_2
Precision	?	?
Recall	?	?
F1	?	?



Binary Classification

	M_1	M_2
Precision	$1/3 = 0.33$	$0/1 = 0$
Recall	$1/2 = 0.5$	$0/2 = 0$
F1	0.4	0



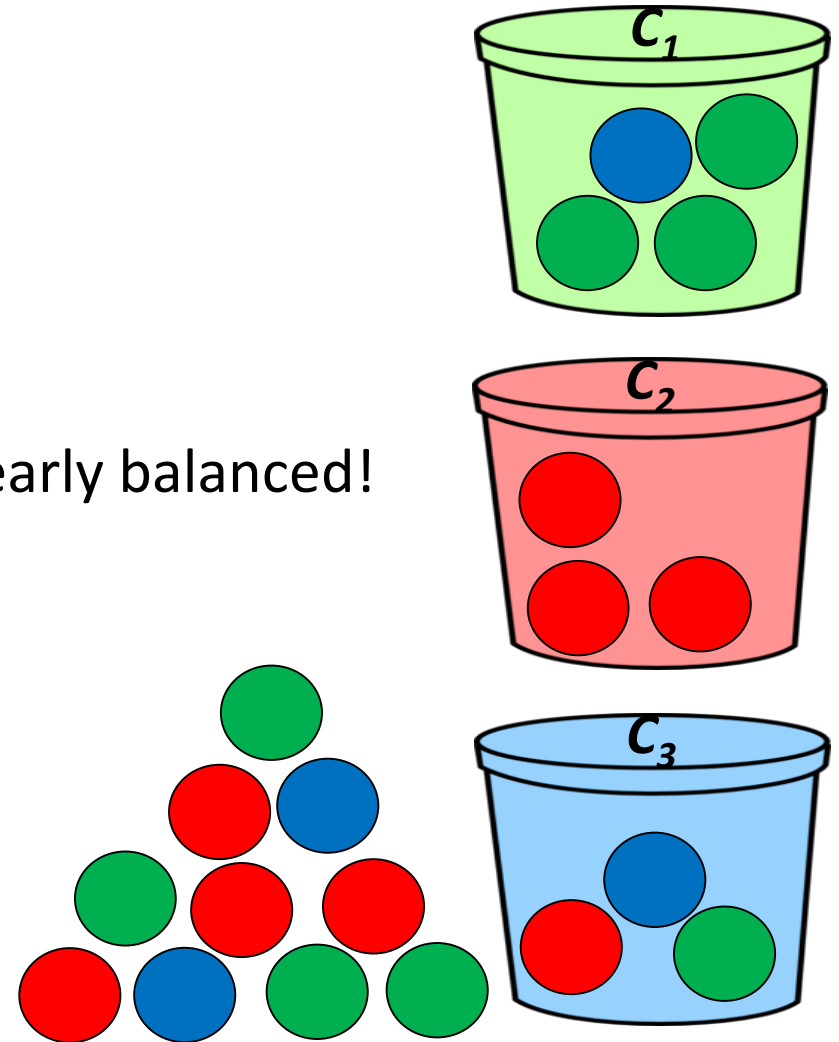
Multi-Class Classification

- Accuracy = ?

$$= (3+3+1)/10 = 0.7$$







What's the problem?

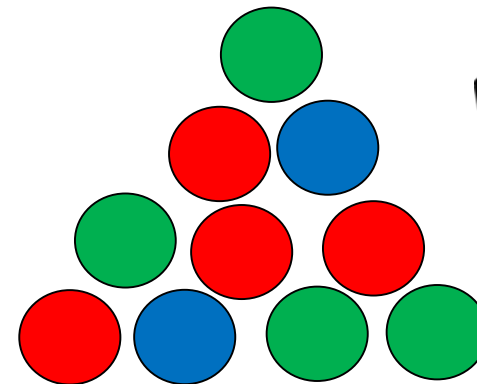
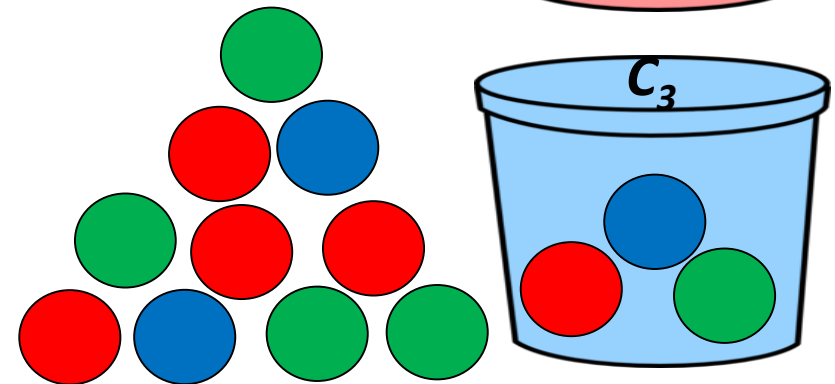
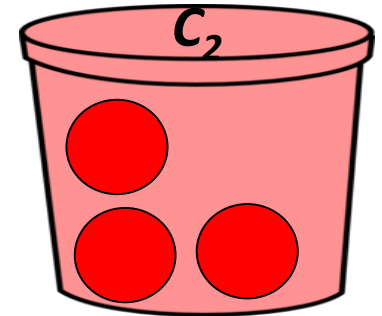
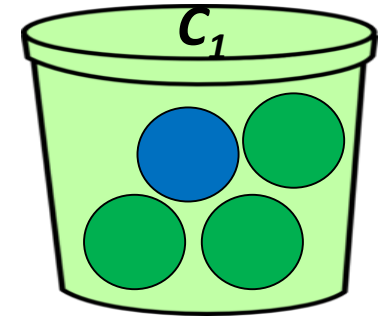
- Good measure when classes are nearly balanced!



Confusion Matrix

Predicted







				
Actual				
				
				






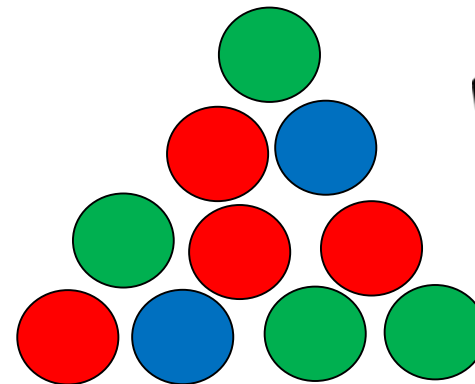
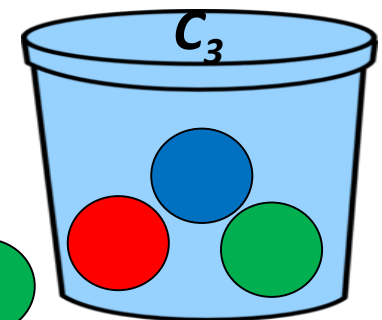
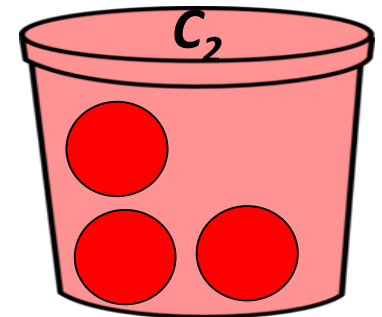
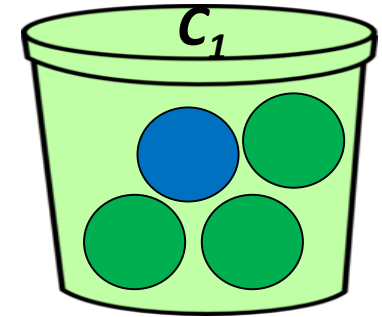
Confusion Matrix

Predicted

Actual

			
	3	0	1
	0	3	1
	1	0	1



			
P			
R			
F1			



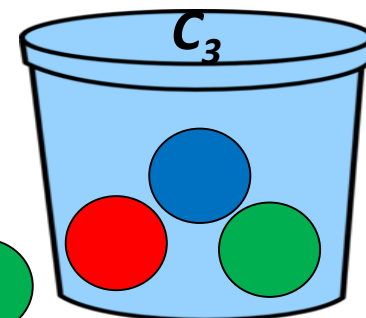
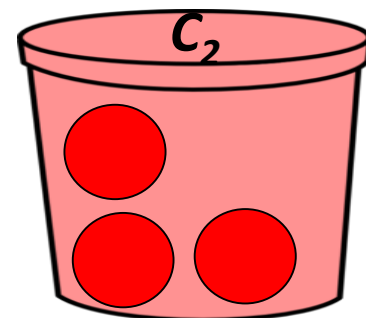
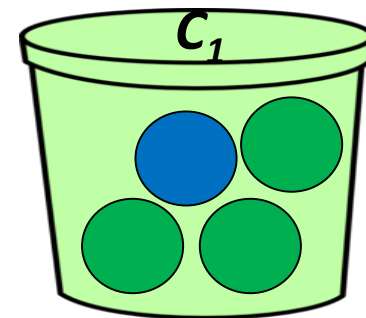
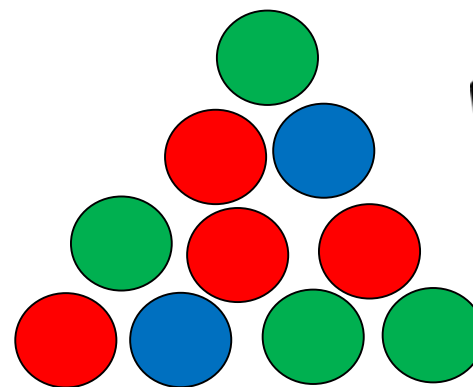
Confusion Matrix

Predicted

Actual

			
	3	0	1
	0	3	1
	1	0	1

			
P	0.75	1	0.333
R	0.75	0.75	0.5
F1	0.75	0.86	0.4



$$\text{Macro-F1} = (0.75 + 0.86 + 0.4) / 3 = 0.67$$