Em - 4

University of Mumbai **Examinations Summer 2022**

SE SemIV (R-19) "ECS" May's

	University of Mumbai SE Semiv (R-19)	
	Examinations Summer 2022 30 minutes Max. Marks: 80	
2hour	30 Himutes Wax. Warks: 80	
jint.		
	Change the same	
Q1.	Choose the correct option for following questions. All the Questions are compulsory and carry equal marks	
1.	Evaluate $\int_{0}^{1+i} (x^2 + iy) dz$ along the path $y = x$	
Option A:	-1+5i	
Option		
Option B:	6	
Option C:	-1	
Option D:	0	
Option 2		
2.	The function $f(z) = \frac{z^2}{(z+2)(z-1)^2}$ has	
Option A:	simple pole at $z = -2$ & pole of order 2 at $z = 1$	
Option B:	simple pole at $z = 2$	
Option C:	simple pole at $z = 0$ & pole of order 1 at $z = 2$	
Option D:	simple pole at z ≥ 0 1 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	
3.	If the line of regression of Y on X is $(Y-33) = (0.72)(X-33)$ then the	
	approximate value of Y for $X = 38$ is	
Option A:		
Option B:		
Option C:		
Option D:		
4.	If for the non-repeated ranks $\sum D^2 = 8$ & n = 5 then the rank correlation coefficient (R) is	
Option A:		
Option B:	70.6×70×70×70×70×70×70×70×70×70×70×70×70×70×	
Option C:		
Option D:		
5.5	Find k if pdf of rv X is	
	X 0 0 1 2 2 3 4 5 6	
4.33.33.6	P(X=x) k 3k 5k 7k 9k 11k 13k	
Option A:	175 変えをある。	
Option B:	\ <u>\2\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\</u>	
Option C:	1/49×68×88	
Option D:] ** 70%%%%%%	
28/27/28/3	NANGARA	
6.	Find E(X) if $f(x) = x$ $0 \le x \le 1$	
Option A:	2 N S S S S S S S S S S S S S S S S S S	
Option B:		
Option C:	1/3	
Option D:	* W - 33 - 500 16 W	
ohnou D:		

	SE t CS
	then their dot product is
7.	SE $\frac{1}{\sqrt{2}}$ If $u=(-2, 3, 4)$ and $v=(3, -2, 3)$ then their dot product is
	11 11 (-2, 3, 4)
Option A:	3
Option B: Option C:	2
Option D:	0
Option D.	
8.	If $u = (2,1,0)$ then $ u $
Option A:	$\sqrt{50}$
Option B:	$\sqrt{3}$
Option C:	$\sqrt{5}$
Option D:	The matrix form of the Quadratic form $x^2 - 2y^2 + 3z^2 - 4xy + xz - 2yz$
	form of the Quadrate row
9	The matrix to $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$
Option A:	$\frac{1}{2} = \frac{1}{2} = \frac{1}$
	The matrix form of the Quade $\begin{bmatrix} x & y & z \end{bmatrix} \begin{bmatrix} 1 & -2 & 1/2 \\ -2 & -2 & -1 \\ 1/2 & -1 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$
	$\begin{bmatrix} 1/2 & -1 & 3 & 2 \\ & & & \end{bmatrix}$
Option B:	$\begin{bmatrix} x \\ y \\ z \end{bmatrix} \begin{bmatrix} 1 & 0 & 2 \\ 2 & -2 & -1 \\ 1/2 & 1 & 3 \end{bmatrix}$
- 1	$\begin{bmatrix} 1 & 1 & 2 & -2 & -1 \end{bmatrix}$
	$\begin{vmatrix} y \end{vmatrix} \begin{vmatrix} 2 & -2 & 1 \\ 1 & 3 \end{vmatrix}$
	$\begin{bmatrix} z \end{bmatrix} \begin{bmatrix} 1/2 & 1 & 3 \end{bmatrix}$
Option C:	7 1/2
O P	$\begin{bmatrix} 1 & -2 & 1/2 \\ -2 & -2 & -1 \\ 1/2 & -1 & 3 \end{bmatrix} \begin{bmatrix} x & y & z \end{bmatrix}$
	$\begin{bmatrix} 1/2 & -1 & 3 \end{bmatrix}$
Option D:	$[x][1 \ 0 \ 0]$
1	
	72
	Find the extremals of $\int_{-\infty}^{\infty} \frac{y'^2}{2} dx$
10.	Find the extremals of $\int_{x_1}^{\infty} \frac{dx}{x^2} dx$
Ontion A:	$y = c_1 x^5 + c_2$
Option A: Option B:	$y = c_1 x + c_2$ $y = c_1 x + c_2$
Option C:	$y = c_1 x + c_2$ $y = c_1 x^3 + c_2$
Option D:	$y = c_1 x^6 + c_2$
opon z.	J

Q2	Solve any Four out of Six	5 marks each
A	Using residue theorem evaluate $\int_{C} \frac{3z^2 + z}{z^2 - 1} dz$	where C is the circle $ z = 2$
P	Fit a straight line to the following data X: 5 6 7 8 9	
	Y: 2 4 5 6 8	
	For a normal variate with mean 2.5 and staprobability that	andard deviation 3.5. Find the
**************************************	i) $2 \le x \le 4.5$	
	ii) $-1.5 \le x \le 5.5$	
D	Find a unit vector in R ³ orthogonal to both u	-(1, 0, 1) and $y = (0, 1, 1)$.

E	Reduce the quadratic form $6x^2+3y^2+14z^2+4xy+4yz+18$ using congruent transformations.	3xz to dia	gonal form
	Find the extremals of $\int_{0}^{1} (xy + y^2 - 2y^2y') dx$		

Q3	Solve any Four out of Six	5 marks each
A	Evaluate $\int_C \frac{dz}{z^3 (z+4)}$ where C is the circle $ z =2$	
В	Given $6y = 5x + 90$; $15x = 8y + 130$. Find i) \overline{x} and \overline{y}	
С	Three factories A, B, C produce 30%, 50% and 20 % of the total production of an item. Out of their production 80%, 50% and 10% are defective. An item is chosen at random and found to be defective. Find the probability that it was produced by the factory A.	
D	Construct an orthonormal basis of R^2 Using Gram-Sc $S = \{ (3, 1), (2, 3) \}$	
Е	Reduce the quadratic form $x^2+2y^2+2z^2-2xy-2yz+xz$ to find its rank & signature.	o canonical form. Al
F	Find the extremals of $\int_{0}^{x} (2xy - y''^{2}) dx$	

	5 marks each
Q4	Solve any Four out of Six 5 marks each
A A	Expand $f(z) = \frac{1}{(z-1)(z-2)}$ in the regions i) $ z < 1$ ii) $1 < z-1 < 2$
B	Calculate R and r from the following data X: 12 17 22 27 32 V: 113 119 117 115 121
C	Fit a poission distribution to the following data No. of deaths: 123 59 14 3 1 Frequencies: 123 59 14 3 1
Ď	Frequencies: 123 59 14 5 14 5 14 15 14 15 14 15 14 15 15 14 15 14 15 15 16 16 16 16 16 16 16 16 16 16 16 16 16
E	Find the singular value decomposition of $\begin{bmatrix} 2 & 3 \\ 0 & 2 \end{bmatrix}$ Using Rayleigh-Ritz method, solve the boundary value problem
	Using Rayleigh-Ritz method, serve as $\int_0^\infty (2xy + y^2 - y'^2) dx; 0 \le x \le 1 \text{ given } y(0) = y(1) = 0$