## Paper / Subject Code: 50922 / Discrete Structures & Graph Theory SE Computer" Sem III (R=2019) (CBCGIS) Nov-Dec 2022 23/11/2022 [Total Marks: 80 (3 Hours) N.B. 1) Q.1 is compulsory. 2) Solve any 3 questions out of remaining 5 questions. 3) Assumptions made should be clearly stated. 4) Draw the figures wherever required. Q.1 Solve any four of the following questions. a) Prove using Mathematical Induction that $n^3+2n$ is divisible by 3 for all $n \ge 1$ b) Explain the following terms with suitable example: i) Partition set ii) Power set. c) State the Pigeonhole principle and show that if any five numbers from 1 to 8 are chosen, 5 then two of them will add to 9. 5 d) Consider the function f(x) = 2x-3. Find a formula for the composition functions i) $f^2 = f \circ f$ ii) $f^3 = f \circ f \circ f$ 5 e) Explain the bipartite graph with suitable example. Q.2a) What is a transitive closure? Find the transitive closure of R using Warshall's algorithm 10 where $A = \{1, 2, 3, 4, 5\} \& R = \{(x,y) \mid x-y = \pm 1\}$ b) What is a ring? Let A= {0, 1, 2, 3, 4, 5, 6, 7}. Determine whether a set A with addition 10 modulo 8 & multiplication modulo 8 is a commutative ring? Justify your answer. Q.3 a) A survey in 1986 asked households whether they had a VCR, a CD player or cable TV. 40 had a VCR. 60 had a CD player; and 50 had cable TV. 25 owned VCR and CD player. 30 owned a CD player and had cable TV. 35 owned a VCR and had cable TV. 10 households had all three. How many households had at least one of the three? How many of them had only CD player? 6 b) Find the complete solution of a recurrence relation $a_n + 2a_{n-1} = n + 3$ for $n \ge 1$ and with $a_0 = 3$ 6 c) Obtain CNF & DNF for the following expression: $p \longleftrightarrow (\sim p \lor \sim q)$

Q.4

- a) What is a group? Let  $A = \{3, 6, 9, 12\}$ 
  - i) Prepare the composition table w.r.t. the operation of multiplication modulo 15,

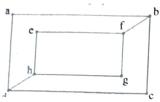
ii) Whether it is an abelian group? Justify your answer.

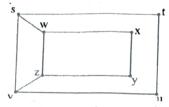
- iii) Find the inverses of all the elements.
- iv) Whether it is a cyclic group?
- b) What are the isomorphic graphs? Determine whether following graphs are isomorphic.



10

5



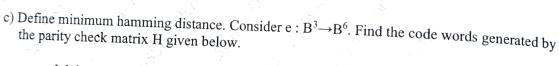


Q.5

- a) Let  $X = \{1, 2, 3, 6, 24, 36\} \& R = \{(x,y) \in R \mid x \text{ divides } y\}$ 
  - i) Write the pairs in a relation set R.
  - ii) Construct the Hasse diagram.
  - iii) What are the Maximal and Minimal elements?
  - iv) Mention Chains and Ant chains from above set.
  - v) Is this poset a lattice?
- b) Define the term bijective function.

Let 
$$f: R \to (7/5) \to R - \left(\frac{2}{5}\right)$$
 be defined by  $f(x) = \frac{2x-3}{5x-7}$ .  
Whether a function is bijective? First  $f(x) = \frac{2x-3}{5x-7}$ .

Whether a function is bijective? Justify your answer.

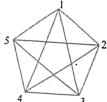


$$H= 0.11$$

001

Q.6

a) Define with example Euler path, Euler circuit, Hamiltonian path, and Hamiltonian circuit. Determine if the following diagram has Euler circuit and Hamiltonian circuit. Mention the



11566

## paper / Subject Code: 50922 / Discrete Structures & Graph Theory

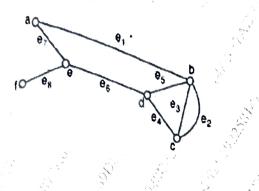
b) Let p denote the statement 'The food is good', Let p denote the statement 'The service is good', & denote the statement 'The rating is 2 q denote the statement 'The rating is 3 star.' r denote the following statements in a symbolic form-write ther food is good or service in the following statements in a symbolic form-

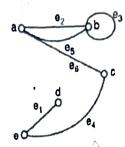
Either food is good or service is good or both.

The food is good but service is not good. i) If both food & service are good then the rating is 3 star. ji)

It is not true that a 3 star rating always means good food & good service. jii)

c) Find out the incidence matrix of following graphs.





8