## paper / Subject Code: 51121 / Engineering Mathematics-III

gt SemII

-R-2019

C 3 cheme

Mov. Dec - 2022

111/2022 Time: 3 hour

Max. Marks: 80

Note: 1. Question no. 1 is compulsory.

2. Attempt any three questions out of remaining five questions. 3, Figures to the right indicate full marks.

$$\lim_{Q_1(a)} \operatorname{Find} L\left[\frac{(\cos at - \cos bt)}{t}\right],$$

(05)

(05)

(b) Find the constants k, if  $f(z) = r^3 \cos k\theta + i r^k \sin 3\theta$  is analytic.

(c) If 
$$A = \begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$$
 Rind  $A^{50}$ 

(05)

(d) If the vector  $\vec{F} = (x + 2y + az)i + (bx - 3y - z)j + (4x + cy + 2z)k$  is is irrotational; find the constants a, b, c (05)

Q2 (a) Find the analytic function f(z) in terms of z whose real part

is 
$$u = sinxcoshy$$

(0.6)

(b) Obtain the Fourier series for 
$$f(x) = e^{ax} \ln (0.2\pi)$$
 (0)

(c) (i) If 
$$L\{f(t)\}=\frac{1}{s\sqrt{s+1}}$$
, then find  $L\{f(2t)\}$ 

Q3 (a) Find L<sup>-1</sup> 
$$\left[\frac{s}{(s^2+4)(s^2+1)}\right]$$
 by convolution theorem.

(b) Find Fourier expansion of 
$$f(x) = 2x - x^2$$
 in (0,3)

(ii) Find  $L(t^5 \cosh t)$ 

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Evaluate by using Green's theorem 
$$\int_C (x^2 - y) dx + (2y^2 + x) dy$$
,  
(c) Evaluate by using Green's theorem  $\int_C (x^2 - y) dx + (2y^2 + x) dy$ ,  
(c) Evaluate by using Green's theorem  $\int_C (x^2 - y) dx + (2y^2 + x) dy$ ,

If 
$$v = 3x^2y + 6xy - y^3$$
 show that V is Harmonic function (06)

Find the Eigenvalues of matrix 
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}$$
 and Show that

and Show that

Evaluate (i) 
$$L^{-1}\left\{\frac{1}{s}\tan^{-1}\frac{1}{s}\right\}$$
 (ii)  $L^{-1}\left\{\frac{1}{(S+1)^2+1}\right\}$  (08)

Obtain the half range Fourier cosine series expansion for 
$$f(x) = x(2-x) \text{ in } (0,2).$$
 (06)

Find Eigen value and Eigen Vector Of Matrix 
$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$$
 (06)

(c) Show that 
$$\vec{F} = (y^2 \cos x + z^3)i + (2y \sin x - 4)j + (3xz^2 + 2)k$$
 is conservative Field. Find (i) Scalar potential for  $\vec{F}$  (ii) the work done in moving an object in this field From  $(0,1,-1)$  to  $(\frac{\pi}{2}, -1, 2)$ 

Q6 (a) Find the orthogonal trajectory of family of curves given by 
$$2x - x^3 + 3xy^2 = a$$

(b) Evaluate 
$$\int_{0}^{\infty} e^{-3t} t \sin t \, dt$$
 (06)

(b) Evaluate 
$$\int_0^\infty e^{-3t} t \sin t \, dt$$
 (06)

(c) Show that the Matrix 
$$\begin{bmatrix} -9 & 4 & 4 \\ -8 & 3 & 4 \\ -16 & 8 & 7 \end{bmatrix}$$
 is diagonalisable. Find the diagonal form D

And diagonalizing matrix M. (08)

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