Duration: 3hrs

[Max Marks: 80]

[20]

- N.B.: (1) Question No 1 is Compulsory.
  - (2) Attempt any three questions out of the remaining five. (3) All questions carry equal marks.

  - (4) Assume suitable data, if required and state it clearly.
  - Attempt any FOUR

If R be a relation in the set of integers z defined by

 $R = \{(x,y): x \in z, y \in z, x - y \text{ is divisible by } 3\}$ 

Show that the relation R is an equivalence relation.

Prove using Mathematical Induction that  $P(n) = 1.1! + 2.2! + \dots + 3.3! = (n+1)! - 1$ 

Design an FSM in which input is valid if it ends in "1011" over  $\Sigma = \{0,1\}$ 

Design NFA for the regular expression

$$R = (0(0+1)^*10)$$

Differentiate between DFA and NFA

Define Poset. Draw Hasse diagram which represents the partial order relation. [10]

 $R = \{(a, b) | a \text{ divides } b \} \text{ on } \{1, 2, 3, 4, 6, 8, 12\}$ Convert the following NFA to DFA:

0  $Q/\Sigma$ p,q p r,s t q ť r p,r s\* ф ф  $t^*$ ф ф

Simplify the following CFG:

[10]  $S \rightarrow aAa \mid bBb \mid BB$ 

$$A \to C$$

$$B \to A|S$$

$$C \to S| \in$$

Write a short note on Warshall's algorithm.

[10]

[10]

Let  $A = \{a1, a2, a3\}$  and R be a relation on A whose matrix is:

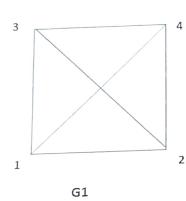
 $Mr = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 1 & 0 \end{bmatrix}$  . Find transitive closure of R using Warshall's algorithm.

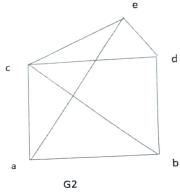
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- a Design PDA to check odd palindrome over  $\Sigma = \{0,1\}$ 
  - Give and explain formal definition of pumping lemma for regular language and prove that the following language is not regular.

$$L = \{ a^m b^{m-1} | m > 0 \}$$

- Design Moore machine for the following: If input ends in '101'then output should be 'A', if input ends in '101' output should be 'B', otherwise output should be 'C' and convert it into Mealy machine.
  - Design a finite automaton to check divisibility by 3 to binary number.
- Determine if the following graphs G1 and G2 are isomorphic or not.





[10]

[10]

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[10] [10] 141

- [10] Define injective, surjective and bijective functions. If  $f: R \to R$  and  $g: R \to R$ are defined by the formulas: f(x) = x + 2 and  $g(x) = x^2$ . Find
  - 1. f.g.f
  - 2. g.f.g