|         | Paper / Subject Code: 38911 / Engineering Mathematics-IV  | ~ \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\   |
|---------|---|--|
| E Serr  | 1 (R-2019 C Scheme) "AI & DS"   | Dec 2023                                 |
| 12 2023 |   |  |
| Time: 3 |   | Marks: 80                                |
| Note:   |   |  |
| 1) (    | 2. No. 01 is compulsory.  |  |
| 2) 8    | olve any three from O. No. 02 to 06.  |  |
| 3) 1    | cumpers to the right indicate full marks.   |  |
| 1, 0    | se of statistical tables is allowed.  |  |
| Q. 1.   | Solve.  |  |
| a)      | 8 -6 2]   | .5                                       |
|         | If $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ find the sum and product of Eigen values $A$ .                                     |  |
| b)      |   | \$ 5°                                    |
|         | Integrate the function $f(z) = z^2$ from A(0, 0) to B(1, 1) along straight lin  | e AB. 5                                  |
| c)      | Find the Z-Transform of $(k) = a^k$ , $k < 0$ .   | <b>5</b>                                 |
| d)      | A transmission channel has a per-digit error probability $p = 0.01$ . Calculat probability of more than 1 error in 10 received digits using Poisson distribution. | te the 5 oution.                         |
| Q. 2.   |   |  |
| a)      |   | 7  |
|         | Find the Eigenvalues and Eigenvectors of the matrix $A = \begin{bmatrix} 3 & -1 & 1 \\ -1 & 5 & -1 \\ 1 & -1 & 3 \end{bmatrix}$                                   |  |
| A 1 1   |   | ] 6                                      |
| b)      | Find the Z-Transform of $Cos\left(\frac{k\pi}{4} + \alpha\right) \ k \ge 0$ .   | 6  |
| c) -    | Use the dual simplex method to solve the LPP  |  |
|         | Min.: $Z = 2X_1 + 2X_2 + 4X_3$<br>$2X_1 + 3X_2 + 5X_3 \ge 2$ , $3X_1 + X_2 + 7X_3 \le 3$ , $X_1 + 4X_2 + 6X_3 \le 5$ $X_1, X_2$                                   | $0, X_3 > 0$ 8                           |
| Q. 3.   | 41 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158 - 158  | ,, |
|         |   |  |
| a)      | Evaluate $\int_C \frac{z^2}{(z-1)(z-2)} dz$ Where C is a circle $ z-1 =1$ .   | 6  |
| b)      | Verify Caley-Hamilton theorem and hence find $A^{-1}$ and $A^4$ where $A =$   |  |
|         |   | 6  |
|         | $\begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 4 \\ 3 & 1 & -1 \end{bmatrix}.$  | v  |
| c) .    | Solve the LPP by Big -M method  |  |
| , G     | Maximize $Z = 3X_1 - 2X_2$<br>subject to $2X_1 + X_2 \le 2$ , $X_1 + 3 \ge 3$ , $X_1, X_2, \ge 0$ .   | 8  |
| .<.     | Subject to 2A1 1A2 = 2, A1 10 = 3, A1, A2, = 0  |  |

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Q. 4.

- Find inverse Z transform of  $F(z) = \frac{1}{(z-1)(z-3)}$  for i) |z| < 1, ii) 1 < |z| < 3. a)
- The following data represent the marks obtained by 12 students in two tests, one held b) before the coaching and the other after the coaching. 55, 60, 65, 75, 49, 25, 18, 30, 35, 51, 61, 72.

63, 70, 70, 81, 54, 29, 21, 38, 32, 50, 70, 80. Do the data indicate that the coaching was effective in improving the performance

Find all possible Laurent's series expansions of the function  $f(z) = \frac{1}{(z-1)(z+2)}$  about of the students? c) z = 0 indicating the region of convergence in each case.

Q. 5.

Determine all basic solutions to the following problem a) Max.  $Z = x_1 - 2x_2 + 4x_3$ 

 $x_1 + 2x_2 + 3x_3 = 7$ ,  $3x_1 + 4x_2 + 6x_3 = 15$ ,  $x_1, x_2, x_3 \ge 0$ . Using Normal distribution, find the probability of getting 55 heads in the toss of 100 b) fair coins.

Solve the NLPP c) Optimize  $Z = 10x_1 + 8x_2 + 6x_3 + 2x_1^2 + x_2^2 + 3x_3^2 - 100$ Subject to  $x_1 + x_2 + x_3 = 20$ ,  $x_1$ ,  $x_2$ ,  $x_3 \ge 0$ .

Q. 6.

- Show that the given matrix is diagonalizable and hence find diagonal form and a) transforming matrix where  $A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -5 & -2 \end{bmatrix}$ .
- Of the 64 off springs of a certain cross between guinea pigs 34 were red, 10 were b) black and 20 were white. According to the generic model these numbers should be in the ratio 9:3:4. Use 2- test to check whether the data are consistent with the model.

Max.  $Z = 4x_1 + 6x_2 - x_1^2 - x_2^2 - x_3^2$ , Subject to  $x_1 + x_2 \le 2$  and  $2x_1 + 3x_2 \le 2$ c) 12,  $x_1$ ,  $x_2 \ge 0$  by K-T condition.

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