Sem IV (Mech) R 2019 May 12022 92122 se Code: PEC401

Option A:

Option B:

Option C:

17/5/2022

Course Name: Engineering Mathematics-4

ourse to 30 minutes	Max. Marks; 80
110.	· 运动动物理智型 原设计 医阿朗斯氏病性皮肤炎 學問一時期 明明 集四层 在学说的 医

Choose the correct option for following questions. All the Questions are compulsory and carry equal marks Q1.

Find the angle between the normals to the surface $xy = z^2at$ the points (1,4,2) and (-3,-3,3).

$$sec^{-1}(\frac{1}{\sqrt{22}})$$

$$cos^{-1}(\frac{1}{\sqrt{22}})$$

 $sec^{-1}(\frac{1}{\sqrt{2}})$

Option D: Using Stoke's theorem, $\int_C \bar{F} \cdot d\bar{r}$ where $\bar{F} = yzi + xzj + xyk$ and C 2. is the boundary of the circle $x^2 + y^2 + z^2 = 1$, z = 0 is

-13 Option A: Option B: Option C: 13

If correlation coefficient, r = 0.6 then $b_{yx} = 1.2$ then $b_{xy} = ?$ Option D: 3.

0.45 Option A: 0.2 Option B: 0.72 Option C: -

If two variables oppose each other then the correlation will be Option D:

Positive correlation Option A: Negative correlation Option B:

Perfect correlation Option C: No correlation In a Poisson distribution if P(X = 2) = P(X = 3) then P(X = 5) is Option D:

0.084125

Option B:

0.84125 Option A: 1 | Page

Option C:	0.37256
Option D:	0.037256
6.	table density function of a continuous random variable
	the probability of a single point is
Option A:	
Option B:	
Option C:	
Option D:	constant
7.	Which of the following tests would be used to test the mean of a continuous random variable to a population mean?
Option A:	One-sample t-test
Option B:	Independent-samples t-test
Option C:	Chi-squared t-test
Option D:	Dependent-samples t-test
Option D.	Dependent sumpression?
8.	Which of the following is not true for a normal distribution?
Option A:	It is a symmetrical distribution.
Option B:	my in altrave 7et0
	The mean, median, mode are always equal. The mean, median, mode are always equal.
Option C:	It is a bell-shaped-distribution.
Option D:	It is a ben-shaped district
	6 6 9 9 9 5 5 5 5 8 6 9 9 5 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
9.	The value of $\int_{c}^{\infty} \frac{\sin z dz}{z^{6}}$, where c is the circle $ z = 1$ is
Option A:	2πi 25- 25- 25- 25- 25- 25- 25- 25- 25- 25-
Option B:	
32.00	
Option C:	3ni se
92000	A 20 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
Option D	√ 5πi √ 5 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3 × 3 ×
	<u> </u>
10.	The value of integral $\oint_c \frac{1}{z-1} dz$, where c is $ z-1 = 2$ is
Option A	マーンバート ペヤルイグンパンさして
Option B	
Option C	
Option D	(2πi (2) (2 (2) (2

Solve any Four out of Six	5 marks each
Obtain Laurent's expansion of $f(z)$ =	$=\frac{z-1}{z^2-2z-3}$ in (i) $1 < z < 3$ (ii)

	z > 3				
1	The following resul	ts of ranks of were	recorded for 11 students. Find		
19	spearman's rank co	rrelation coefficient	between the ranks obtained.		
	Pre-module	Post-module			
11	18	22			
1	21	25			
11	16	17			
	22	24			
1	19	16			
	24	29			
	17	20			
	21	23			
1	23	19 5000000			
	18	20 4 2 2 8 3 3 3			
			a sumle		
\perp	A margan draws 3 h	alls from a had cont	aining 7 blue, 5 yellow, 3 purple		
	A person draws 5 of	Res 7 Re 5 Re 3 i	aining 7 blue, 5 yellow, 3 purple f he draws 3 balls of same		
	balls. He is office	ma colour I ball of	each colour respectively. Find		
	colour, 2 balls of se		each colour respectively. Find		
	his expectation.		States that many states that the		
	A brochure inviting	subscriptions tor a	new diet program states that the average 22 pounds in five he five-week weight losses of 26 he five-week weight losses of 26		
- 1	- APTICIDATION ATO CAL	Cotou to lobe out was	The local of the last of the l		
- 1	WOOKS SHOULD IN	it, momento dam or o	the state of the s		
	to be 23.5 and 10.2	, respectively. Could	Test at the $\alpha = 0.05$ level 01		
	participants, the sample mean and sample standard deviation to be 23.5 and 10.2, respectively. Could the statement in the brochure to be 23.5 and 10.2, respectively. Could the statement in the brochure be substantiated based on these findings? Test at the $\alpha = 0.05$ level of				
- K	contilicance.				
7	significance. Evaluate using Green's theorem $\int_{C} (x^2ydx + y^3dy)$ where c is the boundary of the region bounded by $y = x^2$ and $y = x$ from $(0,0)$ to $(1,1)$ then boundary of the region bounded by $y = x^2$ and $y = x$ from $(0,0)$ to $(1,1)$ then				
~~~	A the regi	On DOUBLECA OF J. C. C.			
33	boundary of the region to $(0,0)$ traversed in positive sense to $(0,0)$ traversed in positive sense. Show that the vector, $\overline{F} = (x^2 - yz)i + (y^2 - xz)j + (z^2 - xy)k$ is Show that the vector, $\overline{F} = (x^2 - yz)i + (y^2 - xz)j + (z^2 - xy)k$ is				
100	to (0,0) that the	vector, $\bar{F} = (x^2 - y^2)$	$z(i+(y^2-\lambda z))$		
	Show that the irrotational and hence	e, find Ø such that F =	= VØ. 5 marks each		
igit.	The state of the s	if of SIXC. Com	- t c . the mentally		
7.50	Solve any rodividi	ials admitted to a sta	ate school for the mentally stributed with a mean of 60 and		
3.73	The IQS OF market	imately normally di	stributed with a mossi		
50	retarded are appro- a standard deviatio	n of 10.	ndividual picked at random will that is the lowest IQ of top 30%		
	a standard deviation	robability that an ir	that is the lowest IQ of top 30%		
	(a) What is the P	55 and 75? (b) w	that is the lowest 2		
	have an IQ between	0, 30,	tion is 52:4		
359	A disadinated very		1 '- on occumation is 22 '		
170	If the mean age at	death of or all 10.2 y	rears, what are the 98%		
5.0	have an 10 octave individuals?  If the mean age at death of 64 men engaged in an occupation is 52.4  If the mean age at death of 10.2 years, what are the 98% years with standard deviation of 10.2 years, what are the 98% confidence limits for the mean age of all men in that population? confidence limits for the mean age at 5% level of significance that Also determine can it be safely assume at 5% level of significance that age of death of population is 56?				
03	confidence limits f	or the moan ag	at 5% level of significance that		
Sec. 7.	' oot	1 If De Salory	= (0		
20%	Also determine car that mean age of d	eath of population is	(1.1.1) is maximum in the		
12.	that mean age of c	ivative of $\emptyset = ax^2 + b$	y+2z at (1,1,1) is maximum = 1		
<del>,</del>	If the directional der	t find a and b.	y+2z at $(1,1,1)$ is maximum in the		
21	direction of $i + j + j$	7) dz where c is the	e circle (i) $ z+i  = \sqrt{3}$		
0,0	Evaluate ( 122	(2z+3), WHOLO 0 12 12			
1.1.	76 (Z-1)		3   Pag		

D

Q3 A

Do

-	$\int_{C} \overline{E} dx \text{ where } \overline{E} = (x^2 - y^2)i + 2xyi$			
Е	Use Stokes' theorem to evaluate $\int_c \bar{F} \cdot d\bar{r}$ where $\bar{F} = (x^2 - y^2)i + 2xyj$ and			
	c is the boundary of region bounded by y			
F	For given the table of points			
	X 0 2 4 6 3 30 30			
	Use normal equations, fit the straight line $y = ax + b$ to the data and find			
	the value of $v(22)$			
Q4	Salar Barra out of Six			
A	In a study of the effectiveness of an insecucide against a certain insect,			
	inacete by randomly selecting squares and counting the number of live			
	insects per square. Past experience has snown the average number of			
	live insects per square after spraying to be 0.5. If the humber of live			
	insects per square follows a Poisson distribution, find the probability			
	that a selected square will contain:			
	(a) One or more live insects			
	(b) Two live insects			
В	On an average 20% of population in an area, suffer from T.B. What is the probability that out of 6 persons chosen at random from this area (a) at least 2, (b) none suffer from T.B.?			
	Evaluate $\int_{C} \vec{F} \cdot d\vec{r}$ where $\vec{F} = yzi + (xz + 1)j + xyk$ along the line			
	joining A (1,0,0) to B (2,1,4).			
C				
D N	D The following figures show the distribution of the digits in numbers			
chosen at random chosen from a telephone directory. Test at 5% level				
	whether the digits may be taken to occur equally frequently in the			
	directory.			
	Digits 0 1 2 3 4 5 6 7 8 9			
	Frequ. 1026 1107 997 966 1075 933 1107 972 964 853			
ENGO	Show that $\overline{F} = (y^2 - z^2 + 3yz - 2x)i + (3xz + 2xy)j + (3xy - 2xz +$			
	$(3x)^2 + (3x)^2 + ($			
	Use divergence theorem to show that $\iint_{S} \overline{N} \cdot \nabla r^2 ds = 6V$ where S is			
	any enclosed surface enclosing volume V.			