Paper / Subject Code: 38911 / Engineering Mathematics-IV Sem IV (C Scheme) R-2019 "Alor DS"

SE

N.B.

(Time: 3 hours) (1) Question No. 1 is compulsory.

- (2) Answer any three questions from Q.2 to Q.6. (3) Use of Statistical Tables permitted.
- (4) Figures to the right indicate full marks.

Q1 a) If
$$A = \begin{bmatrix} 2 & 4 \\ 0 & 3 \end{bmatrix}$$
 then find the Eigen values of $A^3 + 6A^{-1} + 2I$

b) Evaluate $\int_0^{1+i} (x^2 + iy) dz$, along the path (i) y = x, (ii) $y = x^2$

c) Write the dual of the following problem

Maximise $z = 3x_1 + 10x_2 + 2x_3$ subject to $2x_1 + 3x_2 + 2x_3 \le 8$

 $3x_1 - 2x_2 + 4x_3 = 4$ $x_1, x_2, x_3 \ge 0$

d) A certain drug administered to 12 patients resulted in the following change in their Blood

Pressure 5, 2, 8, -1, 3, 0, 6, -2, 1, 5, 0, 4 Can we conclude that drug increase the Blood Pressure?

Q2 (a) Using Cauchy's residue theorem evaluate

 $\int_C \frac{1-2z}{z(z-1)(z-2)} dz$, Where c is |z|=1.5 (b) Verify Cayley-Hamilton theorem and find A^{-1} for $A = \begin{bmatrix} 1 & 8 \\ 2 & 1 \end{bmatrix}$. Hence, find $2A^3 - A^2 -$

35A - 44I. (c) Solve by Simplex Method $z=4x_1+10x_2$ Maximise? $2x_1 + x_2 \le 50$ Subject to

 $2x_1 + 5x_2 \le 100$ $2x_1 + 3x_2 \le 90$ $x_1, x_2 \ge 0$

Max. Marks: 80

[5]

[5]

[5]

[6]

[6] [8]

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Q3 a) Based on the following data determine if there is a relation between literacy and smoking

	Smokers 83	Non-smokers					[6]
Literates				57			 رما
Illiterates	45			68			

(Given that Critical value of chi-square 1 d. f and 5% L.O.S is 3.841

b) Obtain Laurent's series expansion of
$$f(z) = \frac{1}{z^2 + 4z + 3}$$
 [6]

when (i)
$$|z| < 1$$
 (ii) $1 < |z| < 3$ (ii) $|z| > 3$

 $z = x_1^2 + x_2^2 + x_3^2$

Subject to
$$x_1 + x_2 + 3x_3 = 2$$

 $5x_1 + 2x_2 + x_3 = 5$

Optimise

$$x_1, x_2, x_3 \ge 0$$

Q4a) Using the method of Lagrange's multipliers solve the following N.L.P.P

Optimise
$$z = x_1^2 + x_2^2 + x_3^2 - 10x_1 - 6x_2 - 4x_3$$

Subject to
$$x_1 + x_2 + x_3 = 7$$

$$x_1, x_2, x_3 \ge 0$$

b) Find the inverse Z-transform of
$$\frac{1}{z^2-3z+2}$$
, if ROC is (i) $|z| < 1$ (ii) $|z| > 2$ [6]

c) Show that the matrix $A = \begin{bmatrix} 8 & -6 & 2 \\ -6 & 7 & -4 \\ 2 & -4 & 3 \end{bmatrix}$ is diagonalizable. Find the transforming matrix and the diagonal matrix. [8]

Q5a) Find
$$Z\{f(k) * g(k)\}$$
 if $f(k) = \left(\frac{1}{2}\right)^k$, $g(k) = \cos \pi k$ [6]

b) Find the Eigen values and Eigen Vectors of the following matrix. [6]

$$A = \begin{bmatrix} 4 & 6 & 6 \\ 1 & 3 & 2 \\ -1 & -5 & -2 \end{bmatrix}$$

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Solve by the dual Simplex Method [8] $Min^{imise} z = x_1 + x_2$ $2x_1 + x_2 \ge 2$ Subject to $-x_1 - x_2 \ge 1$ $x_1, x_2 \ge 0$ $Q^{(8)}$ Find $Z\{2^k \cos(3k+2)\}, k \ge 0$. [6] b) If the heights of 500 students is normally distributed with mean 68 inches and standard b) If the inches, estimate the number of students having heights (i) greater than 72 inches deviation 4 inches (iii) between (ii) less than 62 inches (iii) between 65 and 71 inches [6] c) Using Kuhn Tucker conditions, solve the following NLPP [8] $z = 2x_1^2 - 7x_2^2 + 12x_1x_2$ Maximise $2x_1 + 5x_2 \le 98$ Subject to $x_1, x_2 \ge 0$