Practical deep learning Assignment 1

GitHub project:



Part 1: the classifier and optimizer

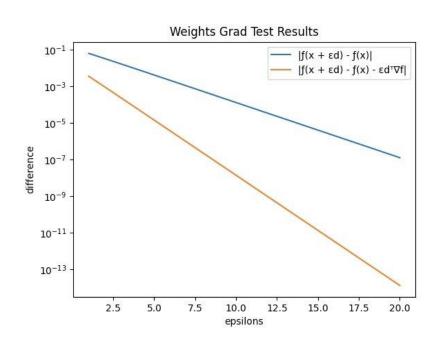
1. We implemented the soft max regression function as type of layer in the neural network, called "SoftMaxLayer", which extends the basic Layer class:

```
def forward(self, X):
    :return: loss score, and probabilities matrix for each class,x
    n = self.X.shape[0]
    if len(self.X.shape) > 1:
       m = self.X.shape[1]
    self.dW = np.zeros((1, n))
    loss = np.sum(Y * np.log(probabilities))
        self.db = (1 / m) * np.sum((probabilities - Y), axis=1).reshape(-
```

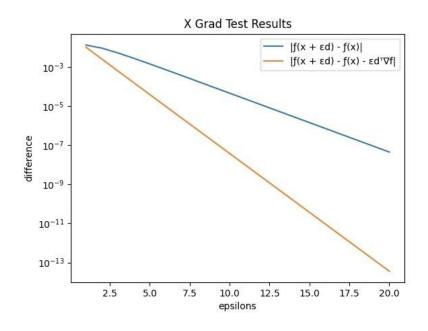
Gradient Tests for loss:

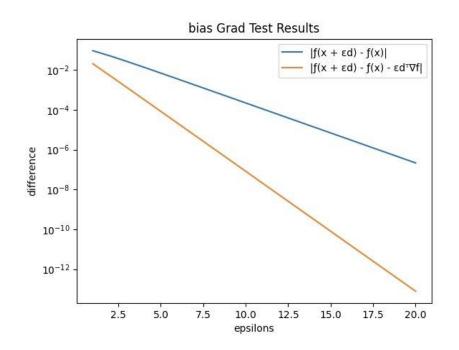
Weights:

```
diff = np.zeros(iter num)
epsilons = [0.5 ** i for i in range(iter num)]
n = X.shape[0]
1 = Y.shape[0]
if len(X.shape) > 1:
   m = X.shape[1]
W orig = soft max layer.W.copy()
fw, = soft max layer.soft max(out, Y)
grad w = soft max layer.dW
    fw epsilon, = soft max layer.soft max(out epsilon, Y)
   diff[i] = abs(fw epsilon - fw)
```



Input(X):





2.SGD Optimizer:

We implemented the SGD optimizer as a class which keeps a pointer to the network, and uses it to update the parameters during the step() call using the gradients.

```
class SGD:
    def __init__(self, net: NeuralNetwork, lr=0.001):
        self.net = net
        self.lr = lr

    def step(self):
        for layer in self.net.layers:
            layer.W = layer.W - self.lr * layer.dw
            layer.b = layer.b - self.lr * layer.db
```

For the train code itself, we used the generic code we wrote for training a neural network, but created the network with the policy = "loss" parameter indicating it will only have 1 layer, the soft max regression:

```
def train_network(data_path: str, num_layers=1, batch size: int = 32, lr: int
           net.backward pass()
   plt.plot(np.arange(0, epochs, 1), validation accuracy)
```

```
plt.legend("loss")
  plt.title(f"loss: batchsize = {batch_size} lr = {lr}")
  plt.show()

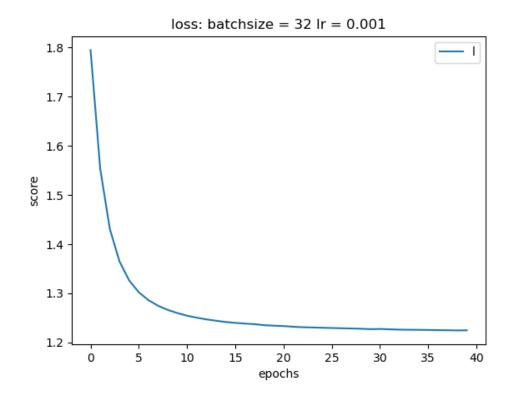
def validate(net: NeuralNetwork, X_test, Y_test):
    net.eval_mode()
    out = net.forward_pass(X_test)
    _, probabilities = net.soft_max_layer.soft_max(out, Y_test)
    acc = get_acc(probabilities, Y_test)
    return acc
```

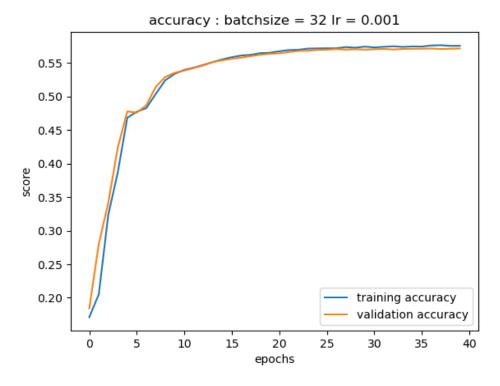
we tried any combination of the parameters: batch sizes = [32,64,128], learning rates = [0.0001, 0.001, 0.05].

the results:

Learning rate/	Loss	Train accuracy	Validate accuracy
batch size			
0.0001,32	1.344	0.42	0.42
0.0001,64	1.48	0.27	0.28
0.0001,128	1.65	0.18	0.18
0.001,32	1.22	0.57	0.57
0.001,64	1.23	0.56	0.56
0.001,128	1.26	0.53	0.53
0.05,32	1.22	0.57	0.56
0.05,64	1.22	0.57	0.57
0.05,128	1.22	0.57	0.57

We chose Ir = 0.001, batch size =32, as it provided us with the best results:





```
if policy == "constant" or num of layers == 1
    self.layers = [SoftMaxLayer(input size, num of classes)]
       self.layers = [Layer(input size, 6)] +
       [Layer(2 * (i + 2), 2 * (i + 3))
       for i in range(1, (num of layers) // 2)] \
       + [Layer(2 * (i + 3), \overline{2} * (i + 2))
       for i in range((num of layers) // 2 - 1, 0, -1)] \
    out = layer.forward(out)
for layer in self.layers:
    layer.train mode()
```

```
:param out dimensions: dimensions of output
       :param activation: activation function used by the layer
   def backward(self, V):
       self.db = np.sum(temp, axis=1).reshape(-1, 1)
       :param Y: a matrix of size lxm,
       :return: loss score, and probabilities matrix for each class,x
(Included Above In Part 1)
```

Activation functions:

```
class ReLU:
    @staticmethod
    def activate(x):
        return np.maximum(0, x)

    @staticmethod
    def deriviative(x):
        f = lambda t: 1 if t >= 0 else 0
        vfunc = np.vectorize(f)

        return vfunc(x)

class tanh:
    @staticmethod
    def activate(x):
        return np.tanh(x)

    @staticmethod
    def deriviative(x):
        f = lambda X: 1 - np.tanh(X) ** 2
        return f(x)
```

Jacobian Tests (conducted with tanh) we used the shortcut version, defining a function $g(x) = \langle f(x), u \rangle$ and performing a grad test for it, as $\nabla g(x) = J^T u$.

Input(X):

```
def jacobian_test_layer_X(X):
    layer = Layer(2, 3)
    n, m = X.shape
    out_dimensions = layer.b.shape[0]
    U = normalize(np.random.rand(out_dimensions, m))

iter_num = 20
    diff = np.zeros(iter_num)
    diff_grad = np.zeros(iter_num)
    epsilons = [0.5 ** i for i in range(iter_num)]
    d = normalize(np.random.rand(*X.shape))

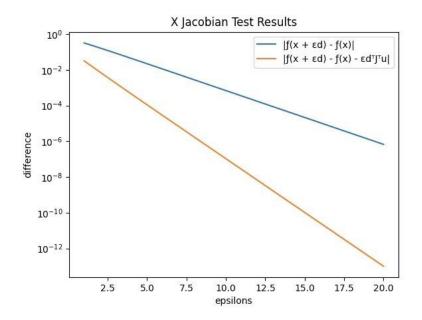
fx = np.dot(layer.forward(X).T, U).item()
    layer.backward(U)
    JacTu_X = layer.dX

for i, epsilon in enumerate(epsilons):
        X_diff = X.copy()
        X_diff = X.copy()
        X_diff = d * epsilon
        fx epsilon = np.dot(layer.forward(X_diff).T, U).item()
        d_flat = d.reshape(-1, 1)
        JacTu_X_flat = JacTu_X.reshape(-1, 1)

        diff[i] = abs(fx_epsilon - fx)
        diff_grad[i] = abs(fx_epsilon - fx - epsilon * d_flat.T @

JacTu_X_flat)

plt.semilogy(np.arange(1, iter_num + 1, 1), diff)
    plt.semilogy(np.arange(1, iter_num + 1, 1), diff_grad)
    plt.xlabel('epsilons')
    plt.ylabel('difference')
    plt.title('X_Jacobian_Test_Results')
    plt.legend(("diff_without_grad", "diff_with_grad"))
```



Weights:

```
def jacobian_test_layer_W(X):
    layer = Layer(2, 3)
    n, m = X.shape
    out_dimensions = layer.b.shape[0]
    U = normalize(np.random.rand(out_dimensions, m))
    original_W = layer.W.copy()

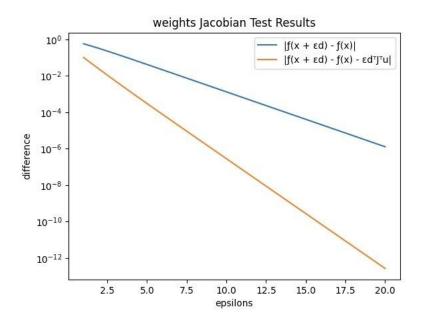
    iter_num = 20
    diff = np.zeros(iter_num)
    diff_grad = np.zeros(iter_num)
    epsilons = [0.5 ** i for i in range(iter_num)]
    d = normalize(np.random.rand(*layer.W.shape))
    fw = np.dot(layer.forward(X).T, U).item()
    layer.backward(U)
    JacTu_W = layer.dW

for i, epsilon in enumerate(epsilons):
        W_diff = original_W.copy()
        W_diff += d * epsilon
        layer.W = W_diff
        fw_epsilon = np.dot(layer.forward(X).T, U).item()
        diff[i] = abs(fw_epsilon - fw)
        d_flat = d.reshape(-1, 1)
        JacTu_W_flat = JacTu_W.reshape(-1, 1)
        diff_grad[i] = abs(fw_epsilon - fw - epsilon * d_flat.T @

JacTu_W_flat)

plt.semilogy(np.arange(1, iter_num + 1, 1), diff)
    plt.semilogy(np.arange(1, iter_num + 1, 1), diff_grad)
    plt.ylabel('epsilons')
    plt.ylabel('difference')
    plt.fitle('weights_Jacobian_Test_Results')
    plt.show()

plt.show()
```

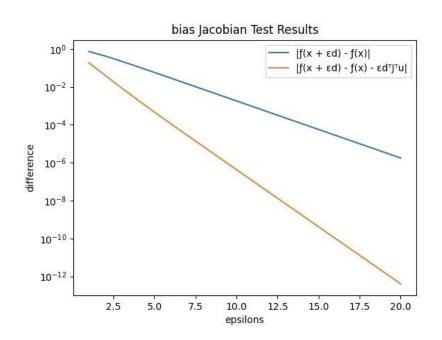


Bias:

```
def jacobian_test_layer_b(X):
    layer = Layer(2, 3)
    n, m = X.shape
    out_dimensions = layer.b.shape[0]
    U = normalize(np.random.rand(out_dimensions, m))
    original_b = layer.b.copy()

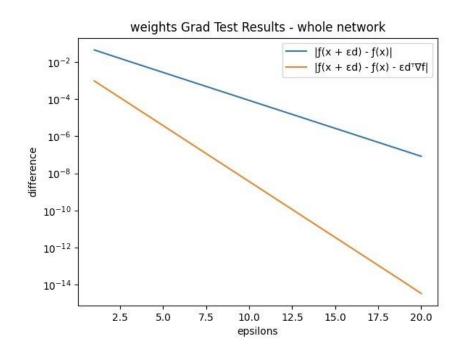
    iter_num = 20
    diff = np.zeros(iter_num)
    diff_grad = np.zeros(iter_num)
    epsilons = [0.5 ** i for i in range(iter_num)]
    d = normalize(np.random.rand(*layer.b.shape))
    fb = np.dot(layer.forward(X).T, U).item()
    layer.backward(U)
    JacTu_b = layer.db
    for i, epsilon in enumerate(epsilons):
        b_diff = original_b.copy()
        b_diff + d * epsilon
        layer.b = b_diff
        fb_epsilon = np.dot(layer.forward(X).T, U).item()
        diff[i] = abs(fb_epsilon - fb)
        diff_grad[i] = abs(fb_epsilon - fb - epsilon * d.T @ JacTu_b)

plt.semilogy(np.arange(1, iter_num + 1, 1), diff)
    plt.semilogy(np.arange(1, iter_num + 1, 1), diff_grad)
    plt.slabel('epsilons')
    plt.ylabel('difference')
    plt.title('bias Jacobian Test Results')
    plt.legend(("diff without grad", "diff with grad"))
    plt.show()
```

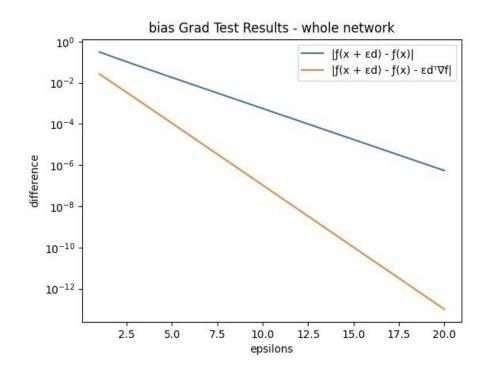


2.2.3 check if should add more output Grad Tests for the whole network:

Weights:



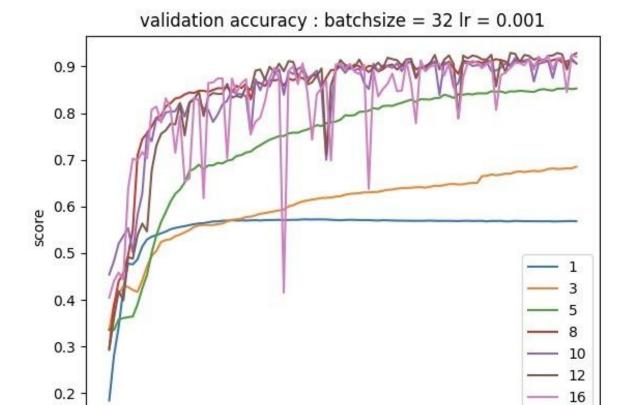
Bias:

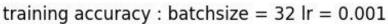


3. Expiriments:

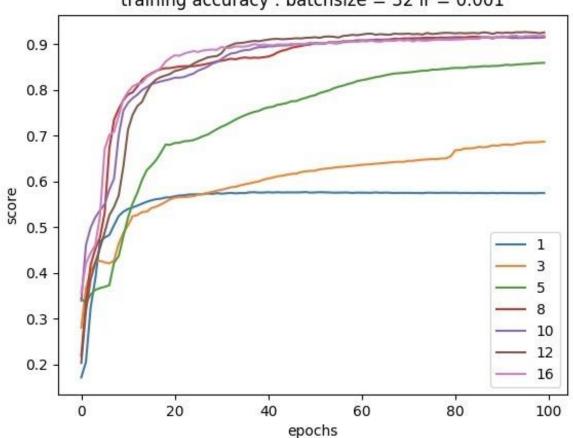
We experimented with a few layer sizes ranging between 1-16, where in the first 1/2 layers the dimensions increase by 2 in each forward pass, then in the last 1/2 layers we decrease back by 2 each pass.

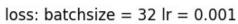
Peaks Data

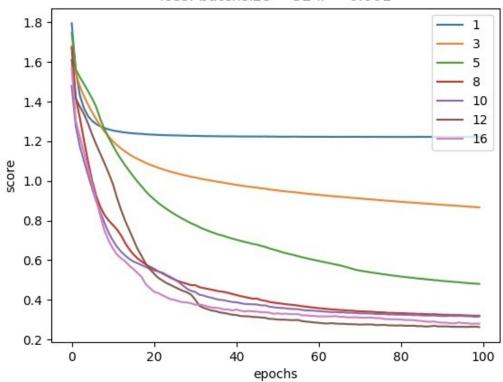




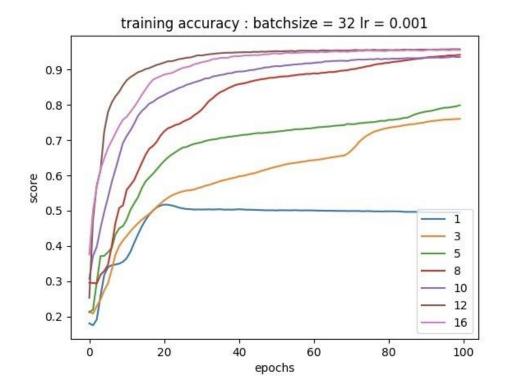
epochs

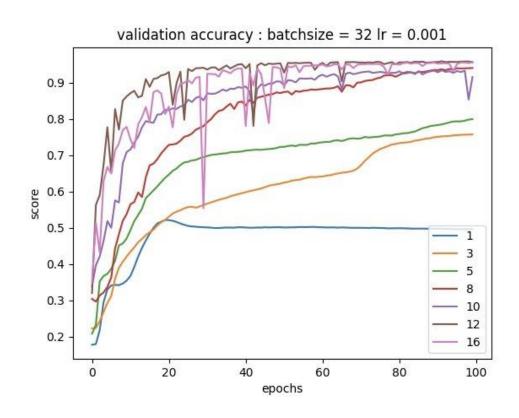


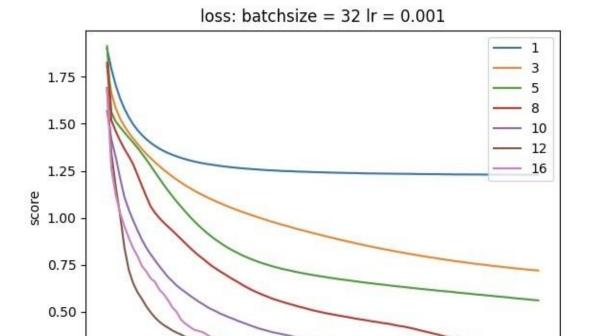




GMM Data







epochs

0.25 -

Ó

Conclusions:

As we can see from the graphs above, in both the data sets of GMM and Peaks, the best results were achieved using a network with 12 layers (

In GMM: best epoch achieved 95.8% train accuracy, 95.9% validation accuracy, and 0.2 loss score.

In Peaks: best epoch achieved 92.6% train accuracy,

92.9% validation accuracy, and 0.26 loss score.

Between 1 - 12 layers we can the results (both accuracy and loss) improve as the layer number increase, and in the 16 layers version we witness a decrease in performance.

Also, as we increase in the layers number (especially with 12 and 16) we can see that the validation accuracy becomes less stable, with substantial changes between epochs.