



$$\mathbf{Y} = \mathbf{K} * \mathbf{X}.$$

Calculating the dot product over patches of  $\mathbf{X}$  of similar size to  $\mathbf{K}$ .

# Convolution Hyperparameters

- The filter dimensions.
- The filter values.
- The stride between patches.
- The padding of the input.

Demo (see 2.3)

# Convolution Output Dimensions

$$\mathbf{Y}_w = \frac{\mathbf{X}_w - \mathbf{K}_w + 2p}{s} + 1,$$
$$\mathbf{Y}_h = \frac{\mathbf{X}_h - \mathbf{K}_h + 2p}{s} + 1,$$

# Example Filters - Identity

$$\mathbf{K}_{\text{Identity}} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

returns the original image.

# Example Filters - Gaussian Blur

$$\mathbf{K}_{\text{Gaussian Blur}} = \begin{bmatrix} \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \\ \frac{1}{8} & \frac{1}{4} & \frac{1}{8} \\ \frac{1}{16} & \frac{1}{8} & \frac{1}{16} \end{bmatrix}$$

adds a blur to the image following the Gaussian distribution.

# Example Filters - Box Blur

$$\mathbf{K}_{\text{Box Blur}} = \begin{bmatrix} \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \\ \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \\ \frac{1}{9} & \frac{1}{9} & \frac{1}{9} \end{bmatrix}$$

adds a blur to the image equally across the point's neighbors.



# Example Filters - Sharpen

$$\mathbf{K}_{\text{Sharpen}} = \begin{bmatrix} 0 & -1 & 0 \\ -1 & 5 & -1 \\ 0 & -1 & 0 \end{bmatrix}$$

sharpens the image by adding some contrast between the pixel and its neighbors.

# Example Filters - Line Detection

$$\mathbf{K}_{\text{Horizontal Lines}} = \begin{bmatrix} -1 & -1 & -1 \\ 2 & 2 & 2 \\ -1 & -1 & -1 \end{bmatrix}, \mathbf{K}_{\text{Vertical Lines}} = \begin{bmatrix} -1 & 2 & -1 \\ -1 & 2 & -1 \\ -1 & 2 & -1 \end{bmatrix},$$

$$\mathbf{K}_{45^\circ \text{ lines}} = \begin{bmatrix} -1 & -1 & 2 \\ -1 & 2 & -1 \\ 2 & -1 & -1 \end{bmatrix}, \mathbf{K}_{-45^\circ \text{ lines}} = \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix}$$

detect lines at a particular angle in the image.

# Example Filters - Outline Detection

$$\mathbf{K}_{\text{Outline}} = \begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$$

detect key outlines within an image.

# Example Filters - Gradient

$$\mathbf{K}_{x \text{ gradient}} = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}, \mathbf{K}_{y \text{ gradient}} = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix},$$

# Example Filters - Sobel

$$\mathbf{K}_{x \text{ gradient}} = \begin{bmatrix} -1 & 0 & 1 \end{bmatrix}, \mathbf{K}_{y \text{ gradient}} = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix},$$

$$\mathbf{K}_{\text{Horizontal Sobel}} = \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix} \times \mathbf{K}_{x \text{ gradient}}, \mathbf{K}_{\text{Vertical Sobel}} = \begin{bmatrix} 1 & 2 & 1 \end{bmatrix} \times \mathbf{K}_{y \text{ gradient}}$$

# Example Filters - Sobel

$$\mathbf{K}_{\text{Horizontal Sobel}} = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{bmatrix}, \mathbf{K}_{\text{Vertical Sobel}} = \begin{bmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{bmatrix}$$

determine the image gradients.

## Demo

# Pooling

- Average pooling
- Max pooling



# Pooling Example

$2 \times 2$  filter with a stride of 2.

$$\mathbf{X} = \begin{bmatrix} 1 & 2 & 5 & 7 \\ 8 & 9 & 6 & 2 \\ 1 & 1 & 4 & 7 \\ 2 & 0 & 3 & 2 \end{bmatrix},$$

$$\mathbf{P}_{\text{average}} = \begin{bmatrix} 5 & 5 \\ 1 & 4 \end{bmatrix}, \mathbf{P}_{\text{max}} = \begin{bmatrix} 9 & 7 \\ 2 & 7 \end{bmatrix}.$$

# Pooling Example - Dimension Check

$2 \times 2$  filter with a stride of 2.

$$\mathbf{X} = \begin{bmatrix} 1 & 2 & 5 & 7 \\ 8 & 9 & 6 & 2 \\ 1 & 1 & 4 & 7 \\ 2 & 0 & 3 & 2 \end{bmatrix},$$

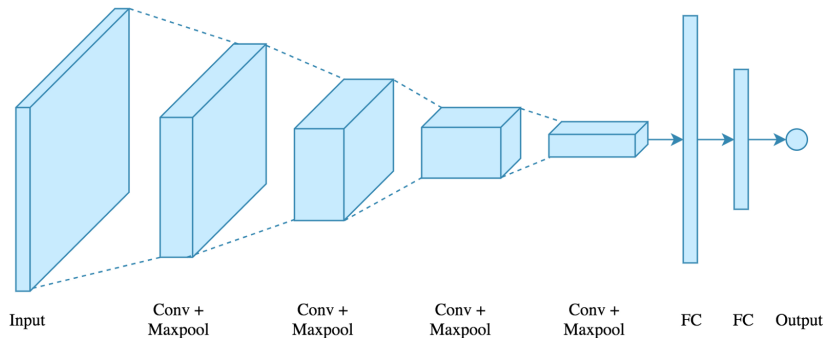
$$\begin{aligned} w &= \frac{\mathbf{X}_w - \mathbf{K}_w + 2p}{s} + 1, \\ &= \frac{4 - 2 + 2 * (0)}{2} + 1, \\ &= 2 \end{aligned}$$

# Pooling Issue

Pooling is effective in practice despite being a very simple approach.

# Convolutional Neural Networks (CNNs)

# CNN



# Convolutional Layer

- Layer has a number of filters,  $f$  (hyperparameter)
- Filter values are learned during model training
- Each filter applies to all of the image (shared weights)
- Output is similar to input shape with additional dimension  $f$

# Pooling Layer

- Applies pooling to input
- Lowers the dimensionality of the features

The training process is similar to other feed forward neural networks.

- Apply a forward pass to determine a prediction
- Calculate error / loss function
- Update weights based on gradient
- Backpropagate the error and update previous weights



# Overfitting

- Dropout
- Start with low number of filters then increase them

# Questions

These slides are designed for educational purposes, specifically the CSCI-470 Introduction to Machine Learning course at the Colorado School of Mines as part of the Department of Computer Science.

Some content in these slides are obtained from external sources and may be copyright sensitive. Copyright and all rights therein are retained by the respective authors or by other copyright holders. Distributing or reposting the whole or part of these slides not for academic use is HIGHLY prohibited, unless explicit permission from all copyright holders is granted.