

Generative Models

Generative models are "general" models that learn the attributes that exist for each particular class in a data set.

A generative model can provide the probability of a data point \mathbf{x} existing given that it is from class k , $p(\mathbf{x}|C_k)$.

Discriminative Models

Discriminative models are "task-specific" models that learn the attributes that differentiate between different classes/groups.

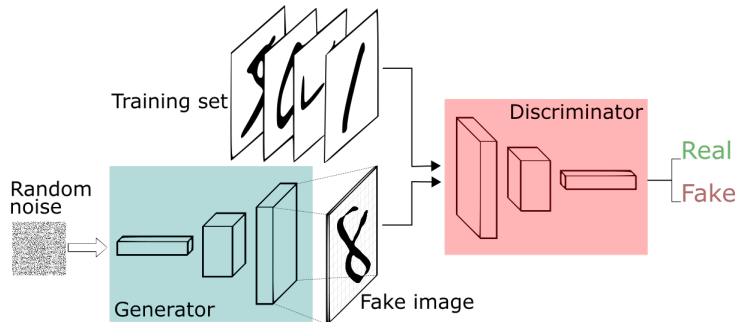
A discriminative model provides the probability of a particular class k given a particular data point \mathbf{x} , $p(C_k|\mathbf{x})$.

Generative vs Discriminative Models

- Generative: $p(\mathbf{x}|C_k)$
- Discriminative: $p(C_k|\mathbf{x})$

- **Generative** - generate samples of data similar to input
- **Adversarial** - train by competing against another model
- **Networks** - a neural network

GANs



Binary Cross Entropy

$$H(p, q) = -(y \log p + (1 - y) \log(1 - p)),$$

where y is the indicator for the class and we assume that $1 - p = q$ since the data sample can only be one of the classes.

Discriminator Objective

$$\begin{aligned} & \min_D -E_{x \sim p_{data}}[\log D(\mathbf{x})] - E_{z \sim p_z}[1 - \log D(G(\mathbf{z}))], \\ & = \max_D E_{x \sim p_{data}}[\log D(\mathbf{x})] + E_{z \sim p_z}[1 - \log D(G(\mathbf{z}))]. \end{aligned}$$

Geenrator Objective

$$\begin{aligned} \max_G & -E_{\mathbf{x} \sim p_{data}}[\log D(\mathbf{x})] - E_{\mathbf{z} \sim p_z}[1 - \log D(G(\mathbf{z}))], \\ &= \min_G E_{\mathbf{x} \sim p_{data}}[\log D(\mathbf{x})] + E_{\mathbf{z} \sim p_z}[1 - \log D(G(\mathbf{z}))]. \end{aligned}$$

Minmax Problem

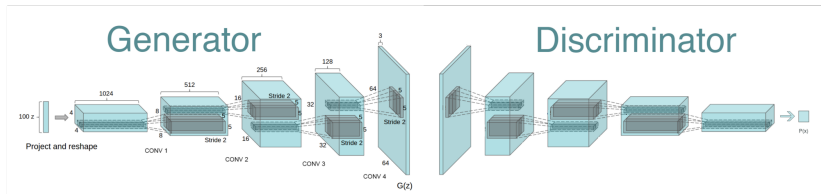
$$\min_G \max_D E_{x \sim p_{data}} [\log D(\mathbf{x})] + E_{z \sim p_z} [1 - \log D(G(\mathbf{z}))].$$

Mode Collapse

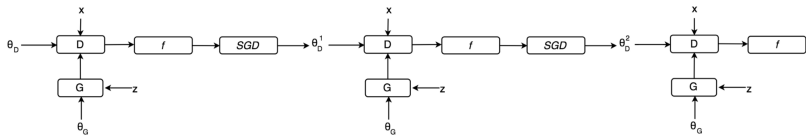
$$\min_G \max_D V(G, D) \neq \max_D \min_G V(G, D).$$

GAN Variations

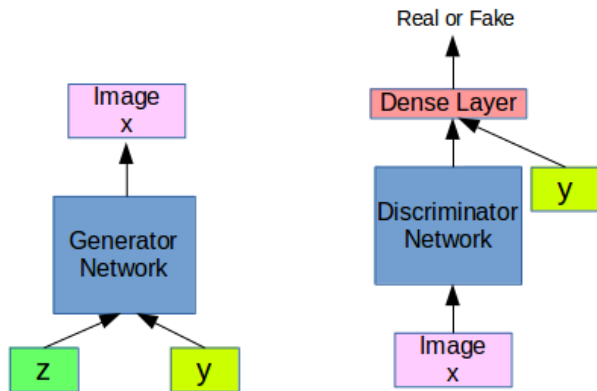
- Deep Convolutional GAN (DCGAN)
- Unrolled GAN
- Wasserstein GAN (WGAN)
- Conditional GAN (CGAN)



Unrolled GAN



$$W(\mathbb{P}_r, \mathbb{P}_\theta) = \sup_{\|f\|_L \leq 1} \mathbb{E}_{x \sim \mathbb{P}_r}[f(x)] - \mathbb{E}_{x \sim \mathbb{P}_\theta}[f(x)]$$

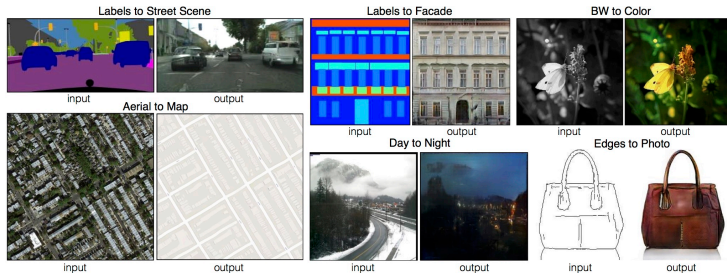


GAN Zoo

Example Applications of GANs

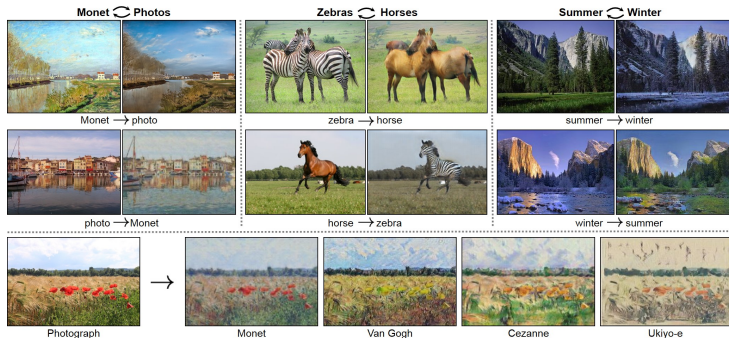
- Image style transfer
- Generating photos of nonexistent objects, animals or people
- Music composition
- Poetry / text authorship

Image Style Transfer



pix2pix

Image Style Transfer



CycleGAN

Photo Generation



Progressive Growing of GANs

MIT Nightmare

Questions

These slides are designed for educational purposes, specifically the CSCI-470 Introduction to Machine Learning course at the Colorado School of Mines as part of the Department of Computer Science.

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