

Mining Imaging Genetics Data via Sparsity-Induced Machine Learning Models

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Machine Learning and Data Mining Are Everywhere of Our Lives





Game playing and problem solving

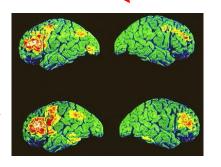


Industrial and engineering applications

Medicine, bioinformatics and systems biology



Machine Learning and Data Mining



Intelligent virtual environments for treatment and rehabilitation

Homeland security applications



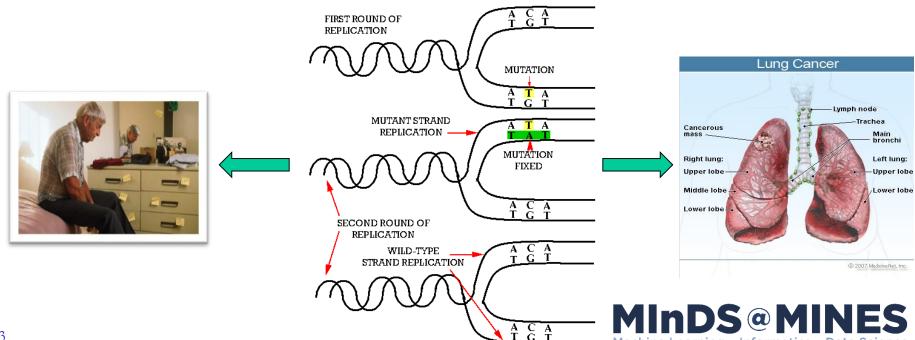
Economics, business and forecasting applications

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Many Major Human Diseases Have Been Connected to Gene Mutations

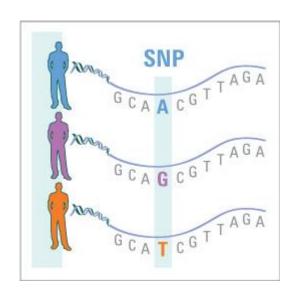


- Many major human diseases, such as cancer and neurodegenerative disorders, affects millions of people worldwide.
- Cause of these diseases: gene mutations (such as singlenucleotide polymorphism (SNP) or copy number variations).

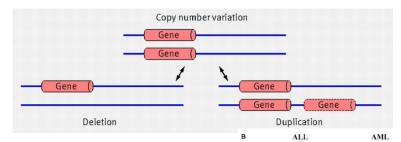


Identification of Genetic/Genomic Biomarker for Diagnosis And Therapy

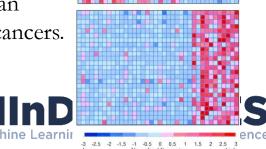
- Genetic variations characterized by SNP underlie differences in our susceptibility to, or protection from all kinds of diseases.
 - For example, a single base difference in the *Apolipoprotein E* is associated with a higher risk for Alzheimer's disease.



 CGH is a molecular-cytogenetic method for the analysis of copy number changes (gains/losses) in the DNA content of a given subject's DNA and often in tumor cells.



Abnormal gene expression level could also indicate human diseases, such as cancers.

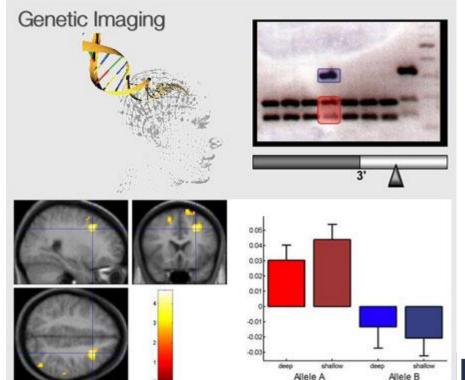


Imaging Genetics via Machine Learning



Imaging genetics refers to the use of anatomical or physiological imaging technologies as phenotypic assays to evaluate variations.

----wikipedia.org

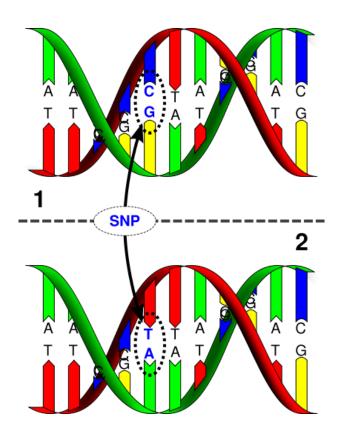




Genotypes: Human Genome and SNP



- SNP (Single Nucleotide
 Polymorphism) single
 nucleotide site where two or
 more different nucleotides
 occur in a large percentage of
 population.
- Total number of SNP: In the current dbSNP build, 132, the number of uniquely mapped refSNP (rs) numbers has grown to about 59 million+. (October 2011)

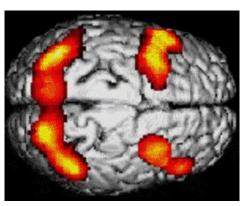


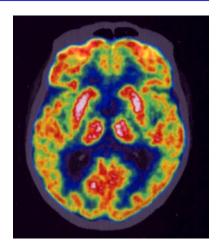


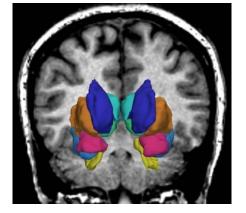
Quantitative Phenotypes

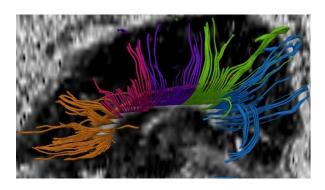










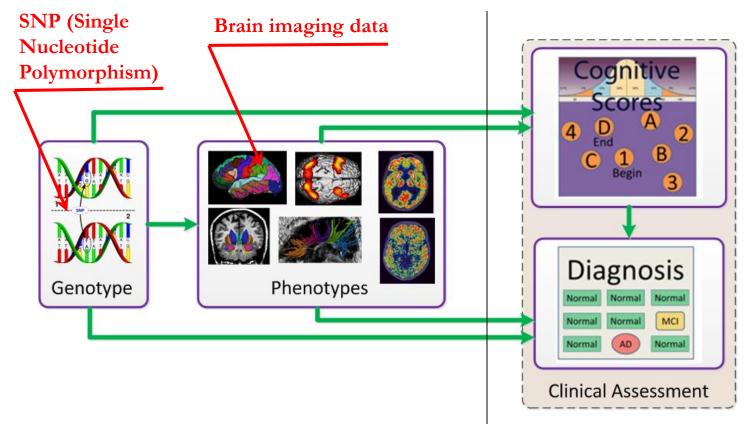


Structural, functional, diffusion MRI FDG, PiB PET Fluid, cognitive biomarkers



A Comprehensive Research Platform to Study Alzheimer's Disease - ADNI

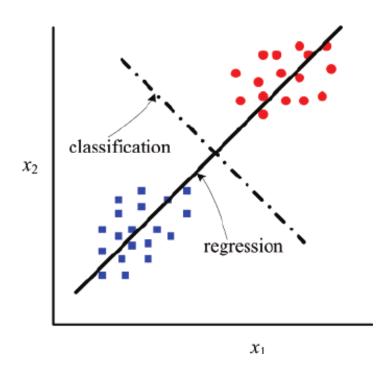




• NIH recently funded the ADNI (Alzheimer's Disease Seuroimaging Inbut Initiative) project, which has provided a comprehensive platform for imaging genetics studies.

Association Studies in Statistical Learning





$$\min_{\mathbf{w}} f(\mathbf{w}; \mathbf{X}, \mathbf{y}) + r(\mathbf{w})$$

- Classification: associate a set of input samples into a set of predefined discrete targets.
- **Regression**: associate a set of input samples into a set of predefined continuous targets.



Structured Sparse Learning for Biomarker Identification

- Sparse learning has recently been successfully applied to solve a number of machine learning and data mining problems.
- Our structured sparse learning based biomarker selection approaches are able to
 - impose sparsity and
 - incorporate useful structural information contained in imaging and genetic data.



Sparsity Is Achieved by ℓ_1 -Norm Regularization



• In traditional statistical learning, in order to avoid over-fitting of the learning model, ℓ_2 -norm regularization is used, which leads to non-sparse result.

$$\min_{\mathbf{w}} f(\mathbf{w}; \mathbf{X}, \mathbf{y}) + a \|\mathbf{w}\|_{2}^{2}$$

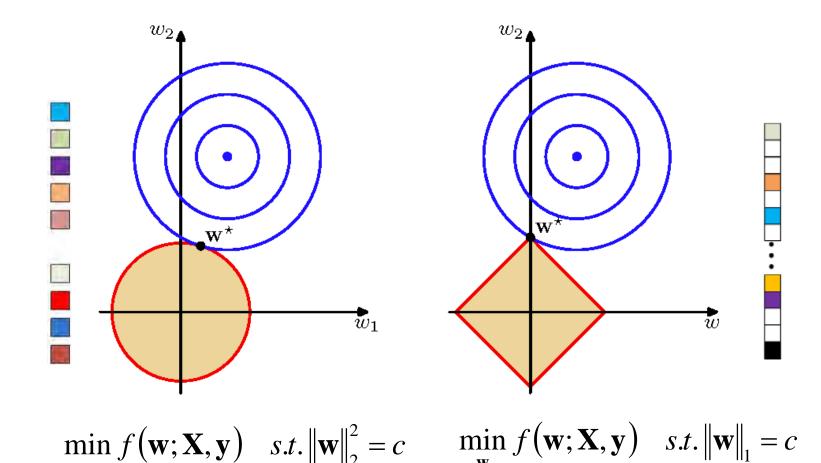
• Recent progress in compressed sensing shows that sparsity is can be achieved by ℓ_1 -norm regularization:

$$\min_{\mathbf{w}} f(\mathbf{w}; \mathbf{X}, \mathbf{y}) + a \|\mathbf{w}\|_{1}$$



Sparsity Is Achieved by ℓ_1 -Norm Regularization (cont.)

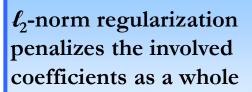






Structured Sparsity Is Achieved by Mixed Norm Regularization





ℓ₁-norm regularization impose sparsity over the penalized coefficients

$$\|W\|_{2,1} = \sum_{i=1}^d \|\mathbf{w}^i\|_2$$

Mixed ℓ_{21} -norm regularization impose structured sparsity

Either select an entire row, or discard an entire row

A unified structured sparse learning framework for imaging genetics studies



Heterogeneous Tasks Homogeneous Tasks Regression tasks only Regression tasks + Classification tasks From task (class) perspective **Single-Modality Data Multi-Modality Data** Ungrouped (flat) Grouped From data (feature) perspective **Features Features Time Series Data and Tasks**

Outline

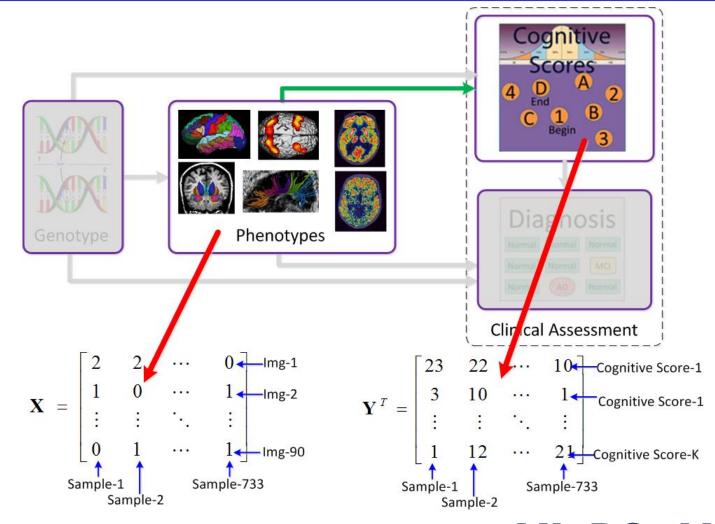


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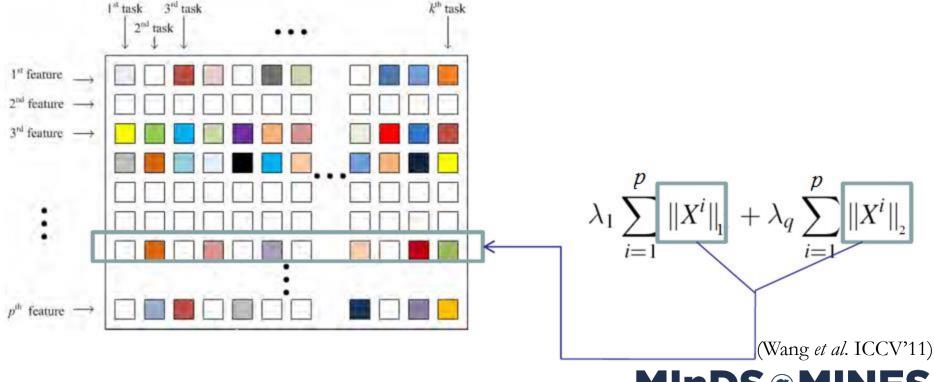




A Convex Learning Objective



$$\min_{W} \left\| \boldsymbol{X}^T \boldsymbol{W} - \boldsymbol{Y} \right\|_F^2 + \gamma_1 \left\| \boldsymbol{W} \right\|_1 + \gamma_2 \left\| \boldsymbol{W} \right\|_{2,1}$$



An Efficient Iterative Algorithm with Global Convergence

Algorithm 1: Algorithm

Input: X, Y

Initialize $W^1 \in \mathbb{R}^{d \times c}$, t = 1;

while not converge do

1. Calculate the diagonal matrices $D_i^{(t)}(1 \le i \le c)$ and $\tilde{D}^{(t)}$, where the k-th diagonal element of $D_i^{(t)}$ is $\frac{1}{2|w_{ki}^{(t)}|}$, the k-th

diagonal element of $\tilde{D}^{(t)}$ is $\frac{1}{2\|(w^{(t)})^k\|_2}$;

2. For each $i(1 \le i \le c)$, $w_i^{(t+1)} = (XX^T + \gamma_1 D_i^{(t)} + \gamma_2 \tilde{D}^{(t)})^{-1} X y_i$; 3. t = t+1;

Output: $W^{(t)} \in \mathbb{R}^{d \times c}$.

(Wang et al. ICCV'11)







Table 2. Prediction performance measured by RMSE.

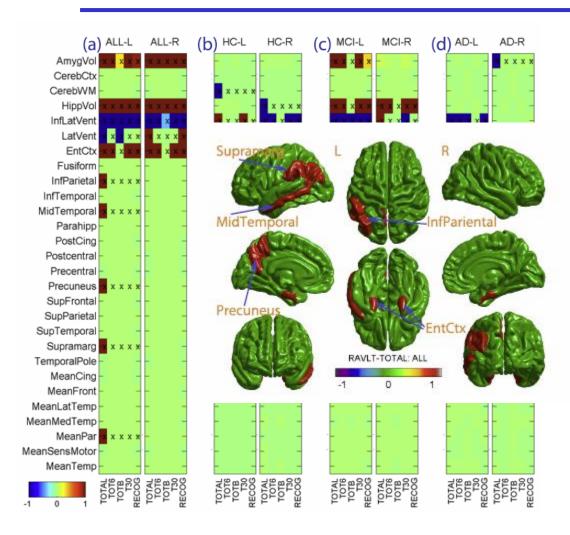
Test cases		TOTAL	ТОТ6	TOTB	T30	RECOG
FreeSurfer_HC _	MVR	8.762	4.362	3.281	4.305	4.021
	SMART	6.645	2.940	2.235	2.806	3.621
FreeSurfer_MCI _	MVR	6.998	2.765	2.399	2.480	3.427
	SMART	5.600	1.990	1.953	1.709	3.181
FreeSurfer_AD _	MVR	5.897	1.768	2.058	1.382	3.390
	SMART	5.042	1.452	1.716	1.050	2.830
FreeSurfer_all	MVR	5.926	2.238	2.036	2.090	3.342
	SMART	5.736	2.139	1.961	1.966	3.196
VBM_HC	MVR	8.651	3.772	2.885	3.496	4.776
	SMART	6.705	2.844	2.139	2.656	3.584
VBM_MCI	MVR	11.495	4.256	4.621	4.032	5.598
	SMART	5.584	1.832	1.931	1.669	3.017
VBM_AD	MVR	7.223	2.162	2.622	1.479	4.163
V BINIZAD	SMART	5.120	1.518	1.826	0.904	2.781
VBM_all	MVR	6.090	2.290	2.140	2.141	3.396
	SMART	5.718	2.103	1.993	1.921	3.182
VBM+FreeSurfer_HC_	MVR	12.265	5.416	4.349	5.089	6.703
	SMART	6.664	2.829	2.230	2.683	3.577
VBM+FreeSurfer_MCI	MVR	68.222	26.146	23.489	30.033	34.306
, Bill i leesaner wet	SMART	5.533	1.901	1.869	1.606	3.114
VBM+FreeSurfer_AD_	MVR	14.552	4.307	5.141	4.297	8.430
. Diff i recourse AD	SMART	4.805	1.218	1.731	0.858	2.865
VBM+FreeSurfer_all _	MVR	6.505	2.596	2.258	2.540	3.582
· Diff i recourier_air -	SMART	5.809	2.208	2.000	2.051	3.214

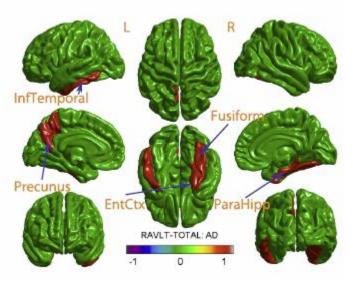
(Wang et al. ICCV'11)

- IDS@MINES
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Experimental Results (Cont.)







(Wang et al. ICCV'11)



Outline

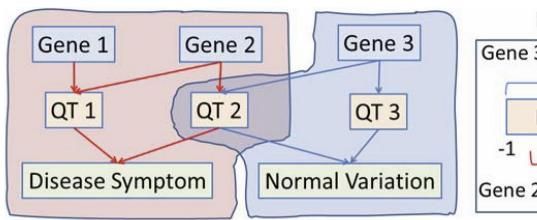


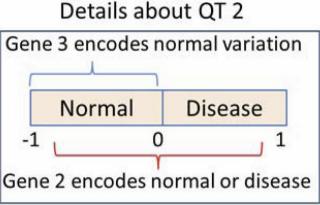
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Learning with Heterogeneous Tasks

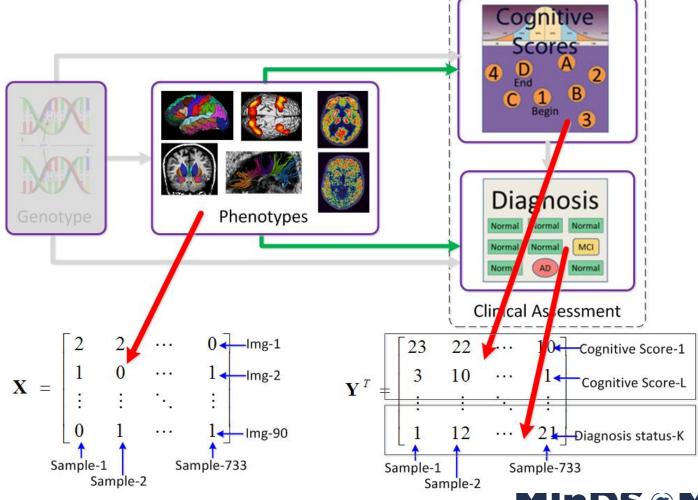






- A simplified schematic example of two pathways from gene to QTs to phenotypic endpoints:
 - the red one is disease relevant
 - while the blue one yields only normal variation.
- Traditional two-stage imaging genetic strategy identifies QT 1 and QT 2 first and then Genes 1, 2, 3.
- Our new method will identify only disease relevant genes (i.e., Gene 1 and Gene 2); and Gene 3 wont be identified because it cannot be used to classify disease status.





Our Objective for Joint Classification and Regression



• Out joint learning objective

min
$$J(\mathbf{V}) = l_1(\mathbf{W}) + l_2(\mathbf{P}) + \gamma ||\mathbf{V}||_{2,1}$$
,

where
$$V = [W P] \in \mathbb{R}^{d \times (c1+c2)}$$
.

• Logistic loss for disease status classification:

$$l_1\left(\mathbf{W}\right) = -\log \prod_{i=1}^n p\left(\mathbf{y}^i \mid \mathbf{x}_i, \mathbf{W}\right) = \sum_{i=1}^n \sum_{k=1}^{c_1} \left(y_{ik} \log \sum_{l=1}^{c_1} e^{\mathbf{w}_l^T \mathbf{x}_i} - y_{ik} \mathbf{w}_k^T \mathbf{x}_i\right).$$

• Least square loss for memory degradation score regression:

$$l_2\left(\mathbf{P}\right) = \left\|\mathbf{X}^T \mathbf{P} - \mathbf{Z}\right\|_{\mathrm{F}}^2,$$

(Wang et al. MICCAI'11)



An Efficient Iterative Algorithm with Global Convergence

Algorithm 1. An efficient algorithm to solve Eq. (3)

Input: $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_n] \in \mathbb{R}^{d \times n}$, $\mathbf{Y} = [\mathbf{y}_1, \dots, \mathbf{y}_n]^T \in \mathbb{R}^{n \times c_1}$, and $\mathbf{Z} = [\mathbf{z}_1, \dots, \mathbf{z}_n]^T \in \mathbb{R}^{n \times c_2}$. 1. Initialize $\mathbf{W} \in \mathbb{R}^{d \times c_1}$, $\mathbf{P} \in \mathbb{R}^{d \times c_2}$, and let $\mathbf{V} = [\mathbf{W} \ \mathbf{P}] \in \mathbb{R}^{d \times (c_1 + c_2)}$; while not converge do

- **2.** Calculate the diagonal matrix **D**, of which the k-th element is $\frac{1}{2\|\mathbf{v}^k\|_2}$;
- **3.** Update \mathbf{w} by $\mathbf{w} \mathbf{B}^{-1}\mathbf{a}$, where $(d \times (p-1) + u)$ -th element of $\mathbf{a} \in \mathbb{R}^{dc_1 \times 1}$ is

$$\frac{\partial \left[l_1(\mathbf{W}) + \gamma \operatorname{tr}\left(\mathbf{W}^T \mathbf{D} \mathbf{W}\right)\right]}{\partial \mathbf{W} u p} \text{ for } 1 \leq u \leq d, 1 \leq p \leq c_1, \text{ the } (d \times (p-1) + u, d \times (q-1) + v)\text{-th}$$

element of
$$\mathbf{B} \in \mathbb{R}^{dc_1 \times dc_1}$$
 is $\frac{\partial \left[l_1(\mathbf{W}) + \gamma \operatorname{tr}\left(\mathbf{W}^T \mathbf{D} \mathbf{W}\right)\right]}{\partial \mathbf{W}_{up} \partial \mathbf{W}_{vq}}$ for $1 \leq u, v \leq d$ and $1 \leq p, q \leq c_1$.

Construct the updated $\mathbf{W} \in \mathbb{R}^{d \times c_1}$ by the updated vector $\mathbf{w} \in \mathbb{R}^{dc_1}$, where the (u, p)-th element of \mathbf{W} is the $(d \times (p-1) + u)$ -th element of \mathbf{w} ;

- 4. Update **P** by $\mathbf{P} = (\mathbf{X}\mathbf{X}^T + \gamma\mathbf{D})^{-1}\mathbf{X}\mathbf{Z};$
- 5. Update \mathbf{V} by $\mathbf{V} = [\mathbf{W} \ \mathbf{P}];$

end

Output: $\mathbf{W} \in \mathbb{R}^{d \times c_1}$ and $\mathbf{P} \in \mathbb{R}^{d \times c_2}$.

(Wang et al. MICCAI'11)

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Experimental Results



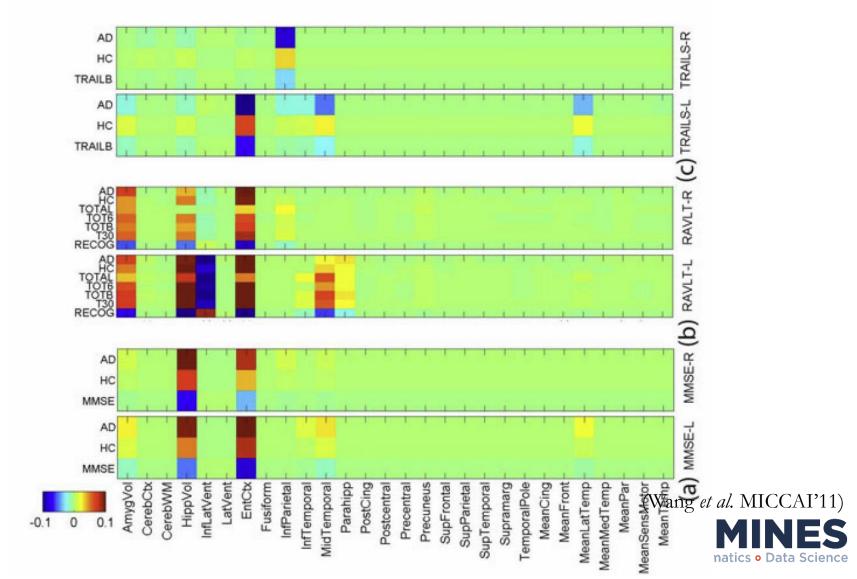
Table 1. Comparison of classification and regression performance

			Our method		Classification accuracy			RMSE (mean ± std)		
Memory				Classification	Regression	Logistic			Multivariate	Ridge
score	# subjects	# AD	# HC	accuracy	RMSE	regression		SVM	regression	regression
MMSE	378	175	203	0.881	0.034 ± 0.002		0.783	(linear kernel)	0.041 ± 0.003	0.039 ± 0.004
RAVLT	371	172	199	0.884	0.019 ± 0.001	0.832	0.839	(Polynomial kernel)	0.028 ± 0.002	0.024 ± 0.003
TRAILS	369	166	203	0.864	0.043 ± 0.002		0.796	(Gausssian kernel)	0.049 ± 0.003	0.046 ± 0.003



Experimental Results (Cont.)





Outline

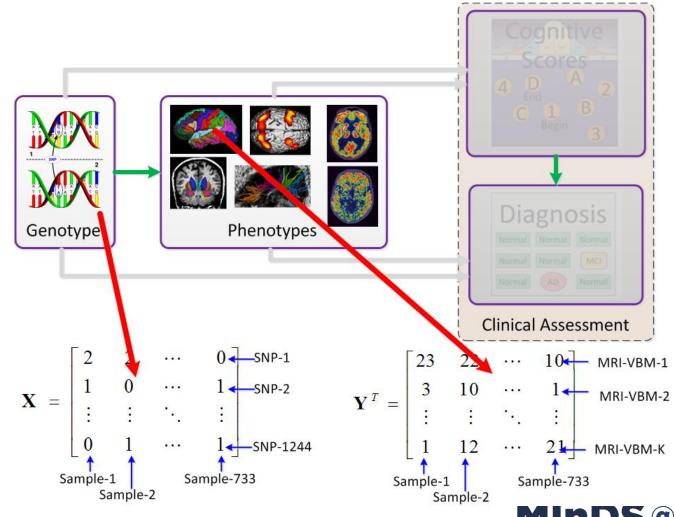


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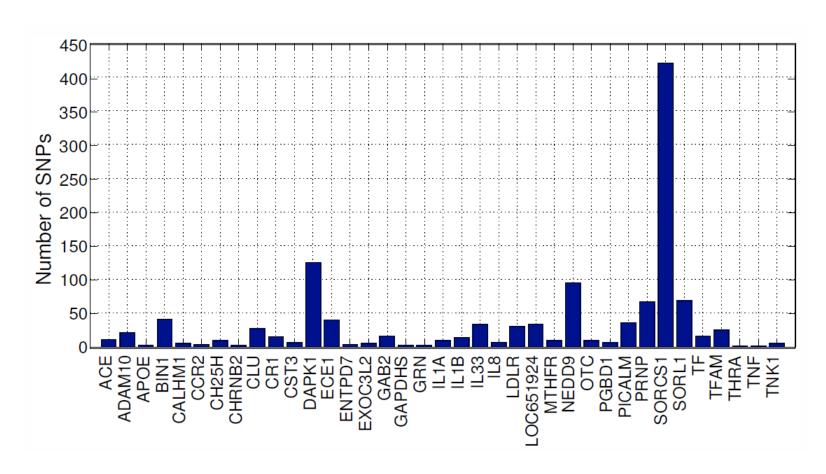
From Genotype to Phenotype





SNPs are Genetically Linked with Group Structures — Genes

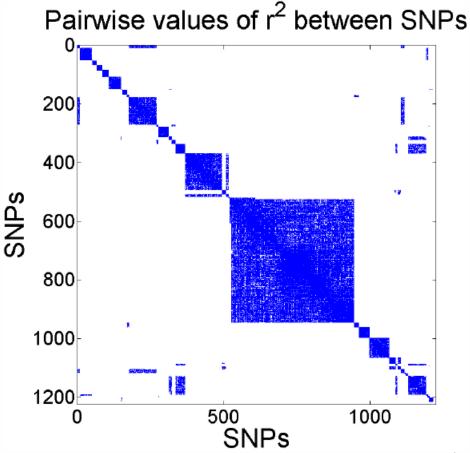




(Wang et al. Bioinformatics'12)



SNPs are Genetically Linked with Group Structures — Linkage Disequilibrium (LD)



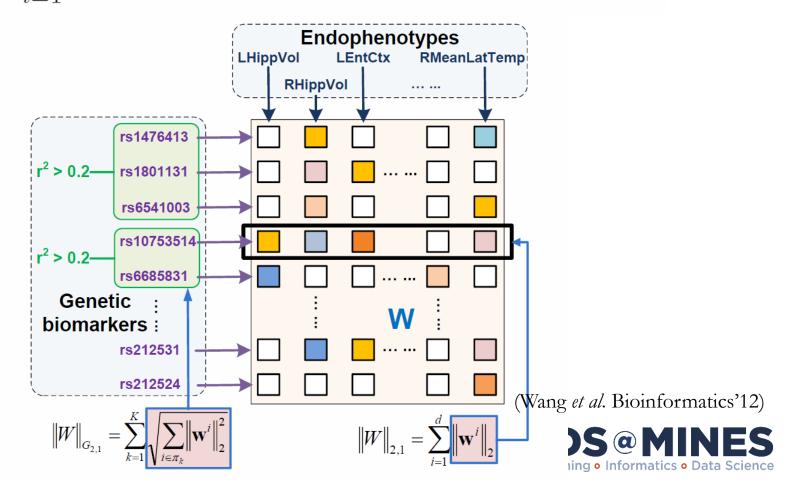
(Wang et al. Bioinformatics'12)



A Novel Group-2,1 Norm to Capture Grouping Structures



$$\min_{\mathbf{W}} \sum_{i=1}^{n} ||\mathbf{W}^{T}\mathbf{X} - \mathbf{Y}||_{F}^{2} + \gamma_{1}||\mathbf{W}||_{G_{2,1}} + \gamma_{2}||\mathbf{W}||_{2,1}$$



An Efficient Iterative Algorithm with Global Convergence

Input:
$$\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, \cdots, \mathbf{x}_n] \in \mathbb{R}^{d \times n}$$
, $\mathbf{Y} = [\mathbf{y}_1, \mathbf{y}_2, \cdots, \mathbf{y}_n] \in \mathbb{R}^{c \times n}$. Initialize $\mathbf{W}_1 \in \mathbb{R}^{d \times c}$, $t = 1$;

while not converge do

1. Calculate the block diagonal matrix \mathbf{D}_t , where the k-th diagonal is $\frac{1}{2\|\mathbf{W}_t^k\|_F}\mathbf{I}_k$; Calculate the diagonal matrix $\tilde{\mathbf{D}}_t$, where the i-th diagonal element is $\frac{1}{2\|\mathbf{w}_i^i\|_2}$;

2.
$$\mathbf{W}_{t+1} = (\mathbf{X}\mathbf{X}^T + \gamma_1\mathbf{D}_t + \gamma_2\tilde{\mathbf{D}}_t)^{-1}\mathbf{X}\mathbf{Y}^T$$
;
3. $t = t + 1$;

end

Output: $\mathbf{W}_t \in \mathbb{R}^{d \times c}$.

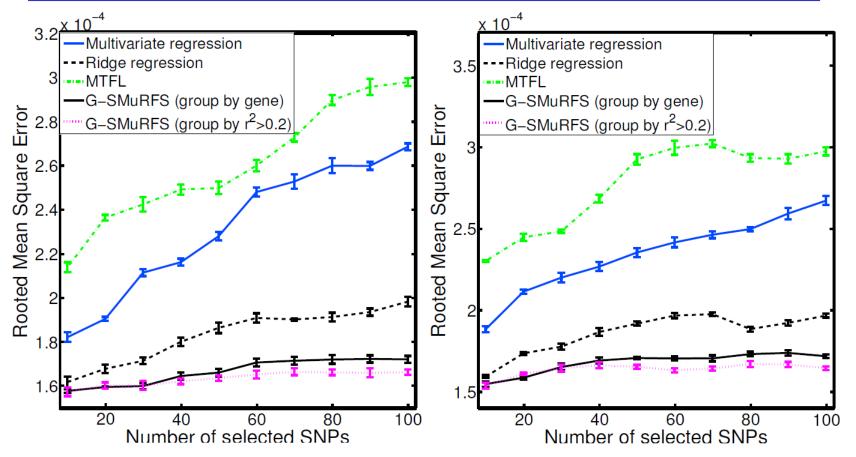
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Experimental Results



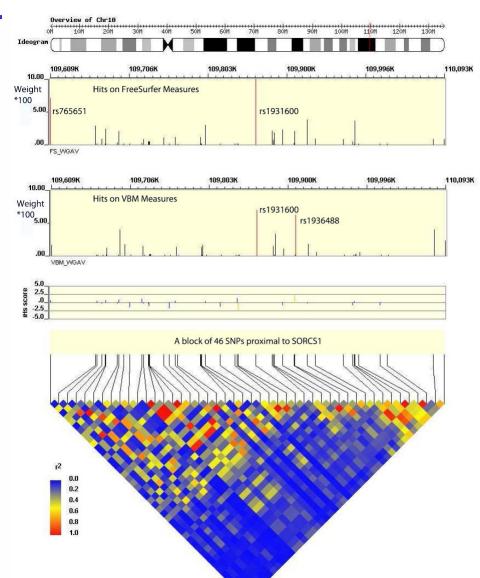


(a) FreeSurfer imaging genotypes.

(b) VBM imaging genotypes. (Wang et al. Bioinformatics'12)

Experimental Results (Cont.)





(Wang et al. Bioinformatics'12)



Outline

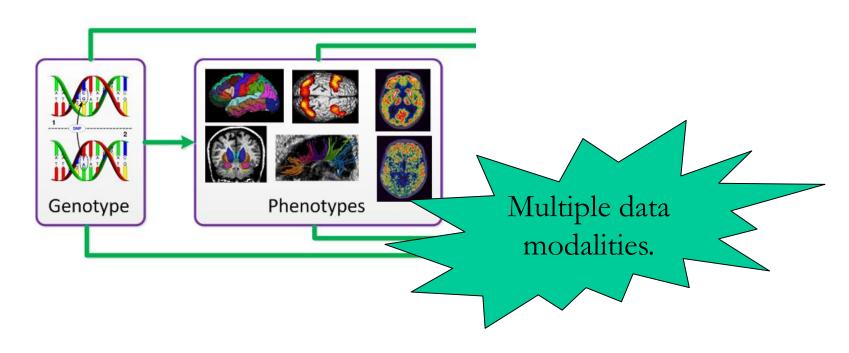


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Integration of Genotypes and Phenotypes Select Multi-Modal Biomarkers





Feature Selection



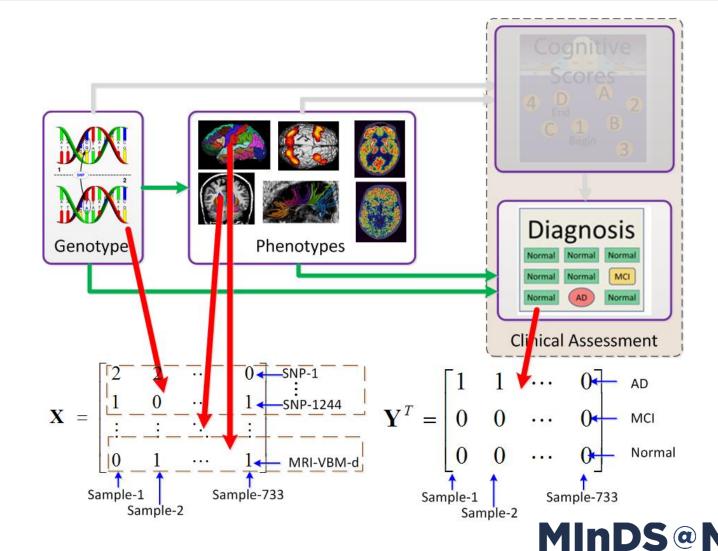
Data Fusion



Integration of Genotypes and Phenotypes Select Multi-Modal Biomarkers



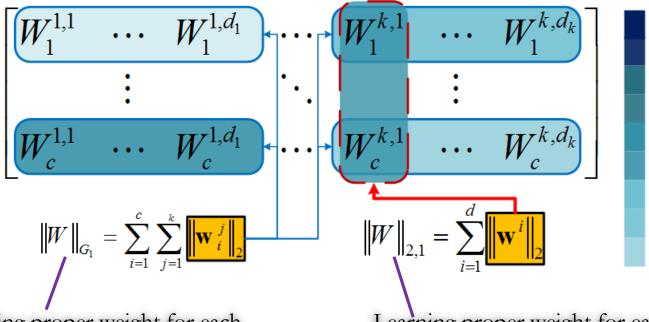
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New Objective Function for Multi-Modal Biomarker Integration



$$\min_{\mathbf{W}} \left\| \mathbf{X}^{T} \mathbf{W} - \mathbf{Y} \right\|_{F}^{2} + \gamma_{1} \left\| \mathbf{W} \right\|_{G_{1}} + \gamma_{2} \left\| \mathbf{W} \right\|_{2,1}$$



Learning proper weight for each modality

Learning proper weight for each individual feature

(Wang et al. ISMB'12)



New Objective Function for Multi-Modal Biomarker Integration (cont.)



• The formulated objective is highly non-smooth due to the ℓ_{21} -norm regularization term and our new group ℓ_1 -norm regularization term.

Input: $\mathbf{X} = [\mathbf{x}_1, \mathbf{x}_2, ..., \mathbf{x}_n] \in \mathbb{R}^{d \times n}, \ \mathbf{Y} = [\mathbf{y}_1, \mathbf{y}_2, ..., \mathbf{y}_c] \in \mathbb{R}^{n \times c}.$ Output: $\mathbf{W}_t \in \mathbb{R}^{d \times c}.$ 1. Let t = 1. Initialize $\mathbf{W}_t \in \mathbb{R}^{d \times c}.$ repeat
2. Calculate the block diagonal matrices $\mathbf{D}_t^i (1 < 1)$

2. Calculate the block diagonal matrices $\mathbf{D}_t^i (1 \leq i \leq c)$, where the *j*-th diagonal block of \mathbf{D}_t^i is $\frac{1}{2\|(\mathbf{w}_t)_i^j\|_2} \mathbf{I}_j$. Calculate the diagonal matrix $\tilde{\mathbf{D}}_t$, where the *i*-th diagonal element is $\frac{1}{2\|\mathbf{w}_t^i\|_2}$.

3. For each $\mathbf{w}_i (1 \leq i \leq c)$, $(\mathbf{w}_{t+1})_i = (\mathbf{X}\mathbf{X}^T + \gamma_1 \mathbf{D}_t^i + \gamma_2 \tilde{\mathbf{D}}_t)^{-1} \mathbf{X} \mathbf{y}_i$.

Simple, efficient,

gasy to implement

4. t = t + 1.

until Converges -

Theorem: The objective value of

$$\min_{\mathbf{W}} \left\| \mathbf{X}^T \mathbf{W} - \mathbf{Y} \right\|_F^2 + \gamma_1 \left\| \mathbf{W} \right\|_{G_1} + \gamma_2 \left\| \mathbf{W} \right\|_{2,1}$$

decreases in each iteration of the algorithm.

(Wang et al. ISMB'12)



Improved Early Alzheimer's Disease Detection

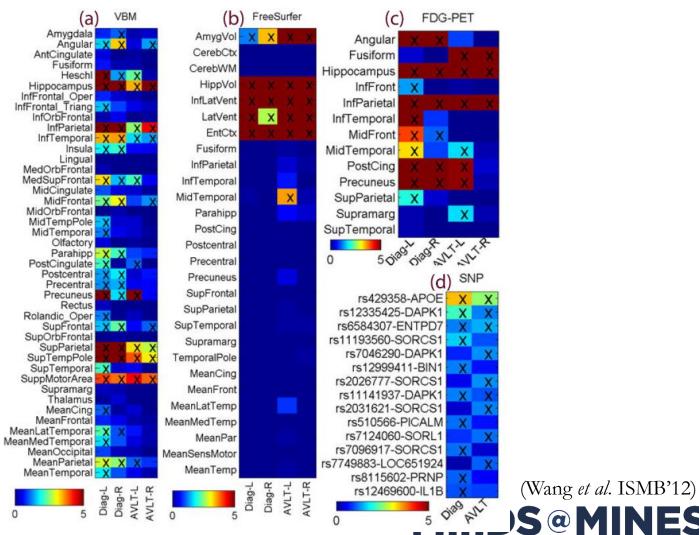


Methods	Accuracy (mean+std)
SVM (SNP)	0.561 ± 0.026
SVM (FreeSurfer)	0.573 ± 0.012
SVM (VBM)	0.541 ± 0.032
SVM (PET)	0.535 ± 0.026
SVM (all)	0.575 ± 0.019
SVM ℓ_{∞} MKL method	0.624 ± 0.031
SVM ℓ_1 MKL method	0.593 ± 0.042
SVM ℓ_2 MKL method	0.561 ± 0.037
LSSVM ℓ_{∞} MKL method	0.614 ± 0.031
LSSVM ℓ_1 MKL method	0.585 ± 0.018
LSSVM ℓ_2 MKL method	0.577 ± 0.033
Our method	$\boldsymbol{0.674\pm0.021}$



Biomarker Selection





Outline

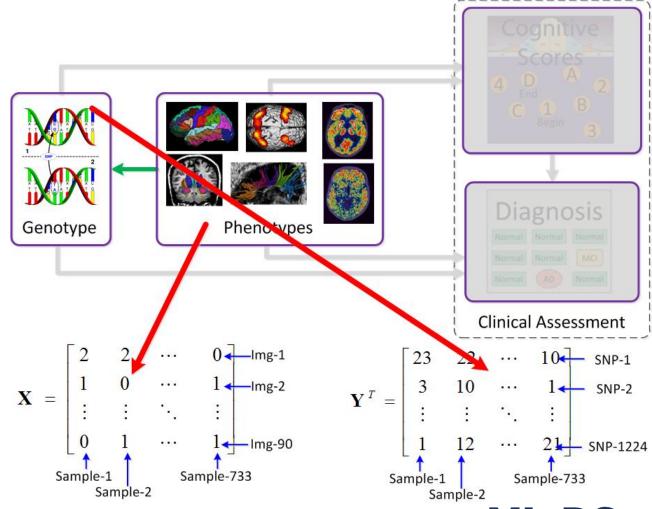


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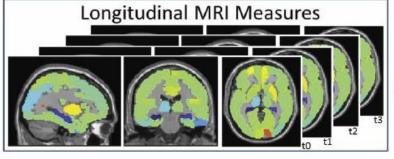
Association from Phenotypes to Genotype



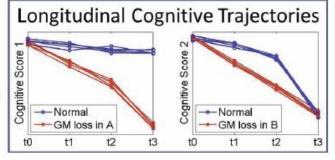


Longitudinal Multi-Task Regression Model





to select MRI markers predicting cognitive trajectories





Learning A Tensor of Regression Model



• We need to learn T regression coefficient matrices, which forms up a tensor:

$$\min_{\mathcal{B}} J_2 = \mathcal{L}(\mathcal{B}) + \gamma_1 \sum_{k=1}^{d} \sqrt{\sum_{t=1}^{T} ||\mathbf{b}_t^k||_2^2 + \gamma_2 ||B||_*}$$

where longitudinal loss is defined as:

$$\mathcal{L}(\mathcal{B}) = ||\mathcal{B} \otimes_1 \mathcal{X}^T - Y||_F^2 = \sum_{t=1}^T ||X_t^T B_t - Y||_F^2.$$

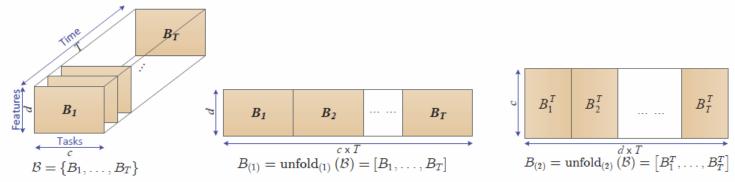


Figure 2: **Left**: visualization of the coefficient tensor \mathcal{B} learned for the association study on longitudinal data. **Middle**: the matrix unfolded from \mathcal{B} along the first mode (feature dimension). **Right**: the matrix unfolded from \mathcal{B} along the second mode (task dimension).

An Efficient Iterative Algorithm with Global Convergence

Algorithm 1: A new algorithm to minimize J_2 in Eq. (4).

Data: $\mathcal{X} \in \mathbb{R}^{d \times n \times T}$, $Y \in \mathbb{R}^{n \times c}$.

1. Initialize $\mathcal{B}^{(0)} \in \mathbb{R}^{d \times c \times T}$ using the regression results at each individual time point.

repeat

- 2. Calculate the diagonal matrix D, where the k-th diagonal element is computed as $\frac{1}{2\sqrt{\sum_{t=1}^{T}||\mathbf{b}_{t}^{k}||_{2}^{2}}}.$
- 3. Calculate $\bar{D} = \frac{1}{2} \left(BB^T \right)^{-\frac{1}{2}}$.
- **4.** Update B_t by $\vec{B_t} = (X_t X_t^T + \gamma_1 D + \gamma_2 \bar{D})^{-1} X_t Y$.

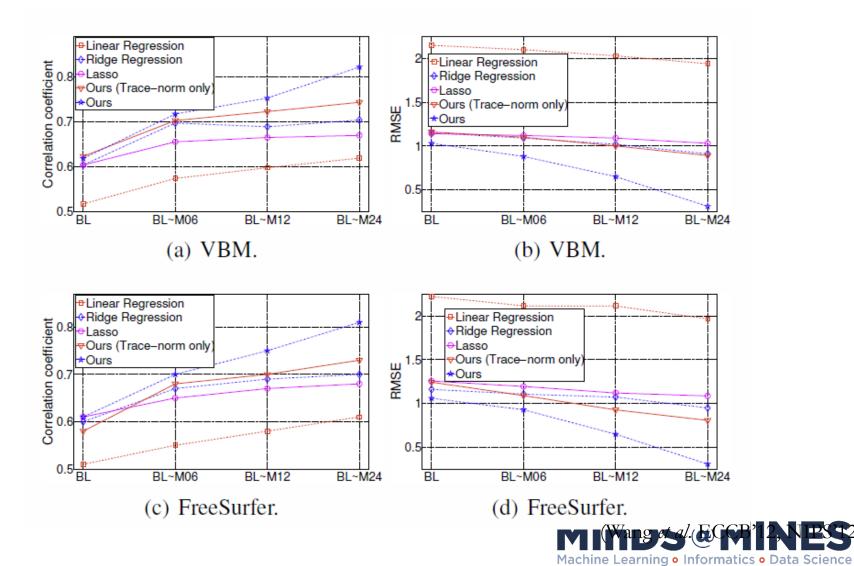
until Converges

Result: $\mathcal{B} = \{B_1, B_2, \dots, B_T\} \in \mathbb{R}^{d \times c \times T}$.



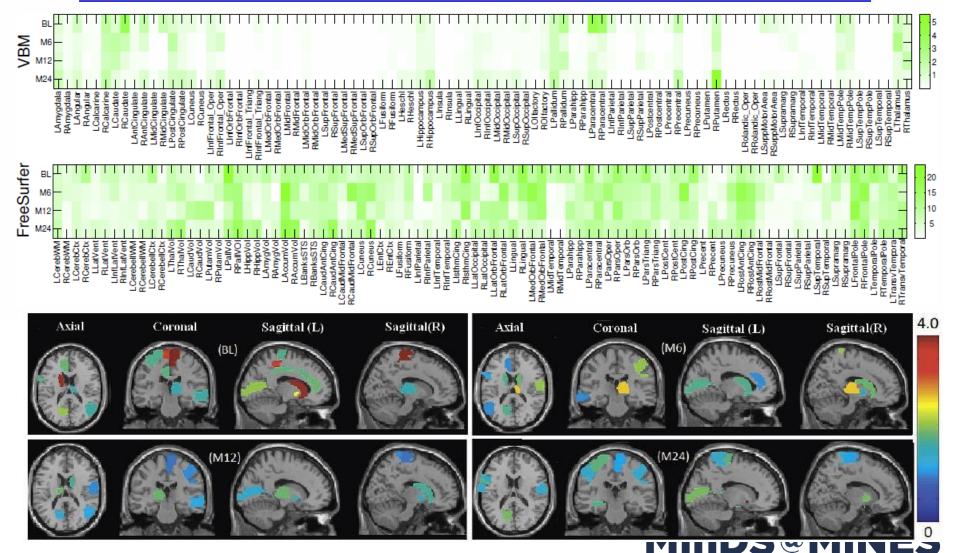
Experimental Results





Experimental Results (Cont.)









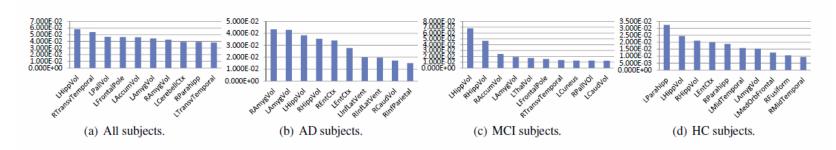


Fig. 4. Top 10 FreeSurfer markers identified for rs423958-APOE.

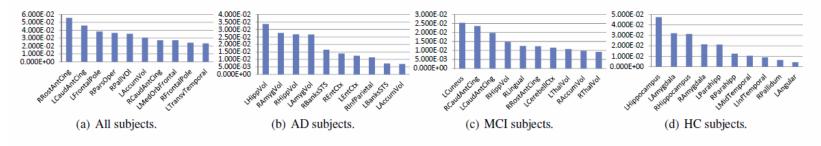


Fig. 5. Top 10 FreeSurfer markers identified for rs11136000-CLU.



Conclusions



- Our research results have shown the effectiveness of using multi-modal data in early AD detection.
- Our algorithms have proven to be theoretically elegant and computationally efficient.

