Read the following resource about different algorithms to calculate Fibonacci numbers, their time & space complexities:

- 1. http://www.ics.uci.edu/~eppstein/161/960109.html
 - This article lists 5 algorithms, namely
 - 1. Recursive
 - 2. Dynamic Programming
 - 3. Space optimized Dynamic Programming
 - 4. Recursive Powering (using the power of matrices)
 - 5. Time optimized (log n) Recursive Powering
- 2. <u>This article</u> introduces another algorithm (let's call it algorithm 6), which is named *Intelligent Recursive Fibonacci Solution*.

Assignment

Write 6 programs, to calculate the first n fibonacci numbers using the 6 algorithms identified above, and print them in order. Your program(s) should get n as a user input. e.g., if n = 5, your program should output

$$F(1) = 1$$

$$F(2) = 1$$

$$F(3) = 2$$

$$F(4) = 3$$

$$F(5) = 5$$

- For each program, get the time taken by the program to print the first 100 Fibonacci numbers. (hint: you can use the time command in Linux to get the time used by the program)
 - For Algorithm 1 you will get a nice (easily comparable) value for this with any computer. For the rest, it may be better to use an old computer OR calculate up to a large number (e.g., 10,000). Note that Fibonacci numbers you'll get at larger values will be wrong.
- o It's better to use *unsigned long* to calculate the Fibonacci numbers!