

# Team Notebook

NSU\_NoAC

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## Contents

<b>1</b>	<b>src</b>	<b>2</b>			
1.1	-Starters-	2	1.3.6	DSU [MB]	5
1.1.1	C++ Include GNU PBDS [NK]	2	1.3.7	DSU [NK]	6
1.1.2	C++ Starter [MB]	2	1.3.8	LCA [MB]	6
1.1.3	C++ Starter [NK]	2	1.3.9	Lazy Segment Tree [MB]	7
1.1.4	C++ Starter [SK]	2	1.3.10	Lazy Segment Tree [SK]	8
1.1.5	C++ Starter debug[MB]	2	1.3.11	Mos Algorithm [MB]	8
1.1.6	Unordered Map [MB]	3	1.3.12	SCC, Condens Graph [NK]	9
1.2	Brute-force	3	1.3.13	Segment Tree [SK]	9
1.2.1	Power Set [NK]	3	1.3.14	Segment Tree[MB]	10
1.3	Data Structures	3	1.3.15	SparseTable[MB]	11
1.3.1	Articulation Points in $O(N + M)$ [NK]	3	1.3.16	Treap[MB]	11
1.3.2	BIT [MB]	3	1.4	Graph	11
1.3.3	Bigint (string) operations [NK]	4	1.4.1	Edge Remove CC [MB]	11
1.3.4	Bridges Online [NK]	4	1.4.2	Kruskal's [NK]	12
1.3.5	Bridges in $O(N + M)$ [NK]	5	1.4.3	Tree Rooting [MB]	13
			1.5	Math	13
			1.5.1	Combinatrics [MB]	13
			1.5.2	Extended GCD [NK]	14
			1.5.3	Fraction-Functions [SK]	14
			1.5.4	Fraction[MB]	14
			1.5.5	Miller-Rabin-for-prime-checking [SK]	14
			1.5.6	Modular Binary Exponentiation (Power) [NK]	15
			1.5.7	Modular Int [MB]	15
			1.5.8	Modular inverse [NK]	15
			1.5.9	Prime Phi Sieve [MB]	15
			1.5.10	Prime Sieve [MB]	16
			1.5.11	Segmented sieve phi [NK]	17
			1.5.12	Segmented sieve primes [NK]	17
			1.5.13	Sieve phi [NK]	17
			1.5.14	nCr mod p in $O(1)$ [SK]	17
			1.6	String	18
			1.6.1	Hashing [MB]	18
			1.6.2	Hashing [NK]	19
			1.6.3	Hashing [SK]	20
			1.6.4	Z-Function [MB]	21

# 1 src

## 1.1 -Starters-

### 1.1.1 C++ Include GNU PBDS [NK]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
namespace pbds = __gnu_pbds;

template <class T>
using ordered_set = pbds::tree<T, pbds::null_type, std::less<T>,
                             pbds::rb_tree_tag,
                             pbds::tree_order_statistics_node_update>;

template <class K, class V>
using hash_map = pbds::gp_hash_table<K, V>;
```

### 1.1.2 C++ Starter [MB]

```
#if defined LOCAL && !defined ONLINE_JUDGE
#include "debug.cpp"
#else
#include <bits/stdc++.h>
using namespace std;
#define dbg(...) ;
#endif

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)(x).size())
#define vec vector

inline bool read(auto &...a) { return (((cin >> a) ? true : false) && ...); }

inline void print(const auto &...a) { ((cout << a), ...); }
inline void println(const auto &...a) { print(a..., '\n'); }

void run_case([[maybe_unused]] const int &TC)
{
```

```
}

int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);

    int tt = 1;
    read(tt);

    for (int tc = 1; tc <= tt; tc++)
        run_case(tc);

    return 0;
}
```

### 1.1.3 C++ Starter [NK]

```
#include <bits/stdc++.h>
using namespace std;

constexpr double eps = 1e-9;
constexpr int inf = 1 << 30;
constexpr int mod = 1e9 + 7;
constexpr int nmax = 1e6;

void runcase(int casen) {

    // cout << "Case " << casen << ": " << '\n';
}

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);

    int ncases = 1;
    cin >> ncases; // Comment out for single-case tests
    for (int casen = 1; casen <= ncases; ++casen) {
        runcase(casen);
    }

    return 0;
}
```

### 1.1.4 C++ Starter [SK]

```
#include<bits/stdc++.h>
using namespace std;
```

```
typedef long long ll;
typedef unsigned long long ull;
#define endl "\n"
#define pi 3.142
const double eps = 1e-10;
int dx[] = {1,0,-1,0};
int dy[] = {0,1,0,-1};
```

```
const ll M = (ll)(1e9) + 7;
const ll inf = (ll)1e17;
const int N = (ll)(1e6 + 10);
```

```
int main()
{
    cin.tie(0);
    cout.tie(0);
    ios_base::sync_with_stdio(false);

    //freopen("two.in", "r", stdin);
    //freopen("out.txt", "w", stdout);

}

/*
*/
```

### 1.1.5 C++ Starter debug[MB]

```
#include <bits/stdc++.h>
using namespace std;

template <typename T, typename C = typename T::value_type>
typename enable_if<!is_same<T, string>::value, ostream &>::
    type operator<<(ostream &out, const T &c)
{
    for (auto it = c.begin(); it != c.end(); it++)
        out << (it == c.begin() ? "{ " : ", ") << *it;
    return out << (c.empty() ? "{ " : ", ") << " }";
}

template <typename T, typename S>
ostream &operator<<(ostream &out, const pair<T, S> &p)
```

```

{
    return out << "{" << p.first << ", " << p.second << "}";
}

#define dbg(...) _dbg_print(__VA_ARGS__, __VA_ARGS__);

template <typename Arg1>
void _dbg_print(const char *name, Arg1 &&arg1)
{
    if (name[0] == ' ')
        name++;
    cout << "[" << name << ": " << arg1 << "]"
        << "\n";
}

template <typename Arg1, typename... Args>
void _dbg_print(const char *names, Arg1 &&arg1, Args &&...
    args)
{
    const char *comma = strchr(names + 1, ',');
    cout << "[";
    cout.write(names, comma - names) << ": " << arg1 << "]" << " ";
    _dbg_print(comma + 1, args...);
}

```

### 1.1.6 Unordered Map [MB]

```

#include <bits/stdc++.h>

// For gp_hash_table
#include <ext/pb_ds/assoc_container.hpp>

using namespace __gnu_pbds;

using namespace std;

struct custom_hash
{
    static uint64_t splitmix64(uint64_t x)
    {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const
    {

```

```

        static const uint64_t FIXED_RANDOM = chrono::steady_clock
            ::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};

// Example Use
unordered_map<int, int, custom_hash> mp;

// Faster
gp_hash_table<int, int, custom_hash> mp;

```

## 1.2 Brute-force

### 1.2.1 Power Set [NK]

```

template <class T>
vector<vector<T>> power_set(const vector<T>& vec) {
    vector<vector<T>> res;
    list<T> buf;
    function<void(int)> recurse = [&](int i) -> void {
        if (i == vec.size()) {
            res.emplace_back(buf.begin(), buf.end());
            return;
        }
        recurse(i + 1);
        buf.push_back(vec[i]), recurse(i + 1), buf.pop_back();
    };
    recurse(0);
    return res;
}

```

## 1.3 Data Structures

### 1.3.1 Articulation Points in $O(N + M)$ [NK]

```

int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph

vector<bool> visited;
vector<int> tin, low;
int timer;

void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;

```

```

    int children=0;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);
            low[v] = min(low[v], low[to]);
            if (low[to] >= tin[v] && p != -1)
                IS_CUTPOINT(v);
            ++children;
        }
    }
    if (p == -1 && children > 1)
        IS_CUTPOINT(v);
}

```

```

void find_cutpoints() {
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i) {
        if (!visited[i])
            dfs(i);
    }
}

```

### 1.3.2 BIT [MB]

```

struct BIT
{
private:
    std::vector<long long> mArray;

public:
    BIT(int sz) // Max size of the array
    {
        mArray.resize(sz + 1, 0);
    }

    void build(const std::vector<long long> &list)
    {
        for (int i = 1; i <= list.size(); i++)
        {
            mArray[i] = list[i];
        }

        for (int ind = 1; ind <= mArray.size(); ind++)

```

```

{
    int ind2 = ind + (ind & -ind);
    if (ind2 <= mArray.size())
    {
        mArray[ind2] += mArray[ind];
    }
}

long long prefix_query(int ind)
{
    int res = 0;
    for (; ind > 0; ind -= (ind & -ind))
    {
        res += mArray[ind];
    }
    return res;
}

long long range_query(int from, int to)
{
    return prefix_query(to) - prefix_query(from - 1);
}

void add(int ind, long long add)
{
    for (; ind < mArray.size(); ind += (ind & -ind))
    {
        mArray[ind] += add;
    }
}
};

```

### 1.3.3 Bigint (string) operations [NK]

```

string add(const string& a, const string& b) {
    string sum;
    int i = a.length() - 1, j = b.length() - 1, carry = 0;
    while (i >= 0 || j >= 0) {
        int temp = carry;
        if (i >= 0) {
            temp += (int)(a[i--] - '0');
        }
        if (j >= 0) {
            temp += (int)(b[j--] - '0');
        }
        carry = temp / 10;
        sum += (char)((temp % 10) + '0');
    }
}

```

```

    if (carry > 0) {
        sum += (char)(carry + '0');
    }
    for (int k = sum.length() - 1; k > 0 && sum[k] == '0'; k--) {
        sum.pop_back();
    }
    reverse(sum.begin(), sum.end());
    return sum;
}

string multiply(const string& a, const string& b) {
    if (a.length() == 0 || b.length() == 0) {
        return "0";
    }
    string prod = "0";
    int shift = 0, carry = 0;
    for (int j = b.length() - 1; j >= 0; j--) {
        string prod_temp;
        for (int i = 0; i < shift; i++) {
            prod_temp += '0';
        }
        shift++;
        carry = 0;
        for (int i = a.length() - 1; i >= 0; i--) {
            int temp = ((int)(a[i] - '0') * (int)(b[j] - '0')) + carry;
            carry = temp / 10;
            prod_temp += (char)((temp % 10) + '0');
        }
        if (carry > 0) {
            prod_temp += (char)(carry + '0');
        }
        reverse(prod_temp.begin(), prod_temp.end());
        prod = add(prod, prod_temp);
    }
    return prod;
}

struct division_t {
    string quot;
    int64_t rem;
};

```

```

division_t divide(const string& num, int64_t divisor) {
    string quot;
    int idx = 0;
    int64_t temp = num[idx++] - '0';
    while (temp < divisor && idx < num.length()) {
        temp = (temp * 10) + (int)(num[idx++] - '0');
    }
}

```

```

    }
    quot += (char)((temp / divisor) + '0');
    while (idx < num.length()) {
        temp = ((temp % divisor) * 10) + (int)(num[idx++] - '0');
        quot += (char)((temp / divisor) + '0');
    }
    int cnt = 0;
    while (cnt < quot.length() - 1 && quot[cnt] == '0') {
        cnt++;
    }
    quot = quot.substr(cnt);
    return (division_t){quot, temp % divisor};
}

```

### 1.3.4 Bridges Online [NK]

```

vector<int> par, dsu_2ecc, dsu_cc, dsu_cc_size;
int bridges;
int lca_iteration;
vector<int> last_visit;

void init(int n) {
    par.resize(n);
    dsu_2ecc.resize(n);
    dsu_cc.resize(n);
    dsu_cc_size.resize(n);
    lca_iteration = 0;
    last_visit.assign(n, 0);
    for (int i=0; i<n; ++i) {
        dsu_2ecc[i] = i;
        dsu_cc[i] = i;
        dsu_cc_size[i] = 1;
        par[i] = -1;
    }
    bridges = 0;
}

int find_2ecc(int v) {
    if (v == -1)
        return -1;
    return dsu_2ecc[v] == v ? v : dsu_2ecc[v] = find_2ecc(dsu_2ecc[v]);
}

int find_cc(int v) {
    v = find_2ecc(v);
    return dsu_cc[v] == v ? v : dsu_cc[v] = find_cc(dsu_cc[v]);
}

```

```

}

void make_root(int v) {
    v = find_2ecc(v);
    int root = v;
    int child = -1;
    while (v != -1) {
        int p = find_2ecc(par[v]);
        par[v] = child;
        dsu_cc[v] = root;
        child = v;
        v = p;
    }
    dsu_cc_size[root] = dsu_cc_size[child];
}

void merge_path (int a, int b) {
    ++lca_iteration;
    vector<int> path_a, path_b;
    int lca = -1;
    while (lca == -1) {
        if (a != -1) {
            a = find_2ecc(a);
            path_a.push_back(a);
            if (last_visit[a] == lca_iteration){
                lca = a;
                break;
            }
            last_visit[a] = lca_iteration;
            a = par[a];
        }
        if (b != -1) {
            b = find_2ecc(b);
            path_b.push_back(b);
            if (last_visit[b] == lca_iteration){
                lca = b;
                break;
            }
            last_visit[b] = lca_iteration;
            b = par[b];
        }
    }

    for (int v : path_a) {
        dsu_2ecc[v] = lca;
        if (v == lca)
            break;
        --bridges;
    }
}

```

```

    for (int v : path_b) {
        dsu_2ecc[v] = lca;
        if (v == lca)
            break;
        --bridges;
    }
}

void add_edge(int a, int b) {
    a = find_2ecc(a);
    b = find_2ecc(b);
    if (a == b)
        return;

    int ca = find_cc(a);
    int cb = find_cc(b);

    if (ca != cb) {
        ++bridges;
        if (dsu_cc_size[ca] > dsu_cc_size[cb]) {
            swap(a, b);
            swap(ca, cb);
        }
        make_root(a);
        par[a] = dsu_cc[a] = b;
        dsu_cc_size[cb] += dsu_cc_size[a];
    } else {
        merge_path(a, b);
    }
}

```

### 1.3.5 Bridges in $O(N + M)$ [NK]

```

int n; // number of nodes
vector<vector<int>> adj; // adjacency list of graph

vector<bool> visited;
vector<int> tin, low;
int timer;

void dfs(int v, int p = -1) {
    visited[v] = true;
    tin[v] = low[v] = timer++;
    for (int to : adj[v]) {
        if (to == p) continue;
        if (visited[to]) {
            low[v] = min(low[v], tin[to]);
        } else {
            dfs(to, v);

```

```

            low[v] = min(low[v], low[to]);
            if (low[to] > tin[v])
                IS_BRIDGE(v, to);
        }
    }
}

void find_bridges() {
    timer = 0;
    visited.assign(n, false);
    tin.assign(n, -1);
    low.assign(n, -1);
    for (int i = 0; i < n; ++i) {
        if (!visited[i])
            dfs(i);
    }
}

```

### 1.3.6 DSU [MB]

```

#include <bits/stdc++.h>

// 0 based
class DSU
{
    std::vector<int> p, csz;

public:
    DSU() {}
    // Max size
    DSU(int dsz)
    {
        //Default empty
        p.resize(dsz + 5, 0), csz.resize(dsz + 5, 0);

        init(dsz);
    }

    void init(int n)
    {
        // n = size
        for (int i = 0; i <= n; i++)
        {
            p[i] = i, csz[i] = 1;
        }
    }

    //Return parent Recursively
    int get(int x)

```

```

{
    if (p[x] != x)
        p[x] = get(p[x]);

    return p[x];
}

// Return Size
int get_comp_size(int component) { return csz[get(component)]; }

// Return if Union created Successfully or false if they
// are already in Union
bool merge(int x, int y)
{
    x = get(x), y = get(y);
    if (x == y)
        return false;

    if (csz[x] > csz[y])
        std::swap(x, y);

    p[x] = y;
    csz[y] += csz[x];

    return true;
}
};

```

### 1.3.7 DSU [NK]

```

struct DSU {
    int n_nodes = 0;
    int n_components = 0;
    vector<int> component_size;
    vector<int> component_root;

    DSU(int n_nodes, bool make_all_nodes = false)
        : n_nodes(n_nodes),
          component_root(n_nodes, -1),
          component_size(n_nodes, 0) {
        if (make_all_nodes) {
            for (int i = 0; i < n_nodes; ++i) {
                make_node(i);
            }
        }
    }

    void make_node(int v) {
        if (component_root[v] == -1) {

```

```

            component_root[v] = v;
            component_size[v] = 1;
            ++n_components;
        }
    }

    int root(int v) {
        auto res = v;
        while (component_root[res] != res) {
            res = component_root[res];
        }
        while (v != res) {
            auto u = component_root[v];
            component_root[v] = res;
            v = u;
        }
        return res;
    }

    int connect(int u, int v) {
        u = root(u), v = root(v);
        if (u == v) return u;
        if (component_size[u] < component_size[v]) {
            swap(u, v);
        }
        component_root[v] = u;
        component_size[u] += component_size[v];
        --n_components;
    }
};

```

### 1.3.8 LCA [MB]

```

struct LCA
{
private:
    int n, lg;
    std::vector<int> depth;
    std::vector<std::vector<int>> up;
    std::vector<std::vector<int>> g;

public:
    LCA() : n(0), lg(0) {}

    LCA(int _n)
    {
        this->n = _n;
        lg = (int)log2(n) + 2;
        depth.resize(n + 5, 0);

```

```

        up.resize(n + 5, std::vector<int>(lg, 0));
        g.resize(n + 1);
    }

    LCA(std::vector<std::vector<int>> &graph) : LCA((int)graph.size())
    {
        for (int i = 0; i < (int)graph.size(); i++)
            g[i] = graph[i];

        dfs(1, 0);
    }

    void dfs(int curr, int p)
    {
        up[curr][0] = p;
        for (int next : g[curr])
        {
            if (next == p)
                continue;
            depth[next] = depth[curr] + 1;
            up[next][0] = curr;
            for (int j = 1; j < lg; j++)
                up[next][j] = up[up[next][j - 1]][j - 1];
            dfs(next, curr);
        }
    }

    void clear_v(int a)
    {
        g[a].clear();
    }

    void clear(int n_ = -1)
    {
        if (n_ == -1)
            n_ = ((int)(g.size())) - 1;

        for (int i = 0; i <= n_; i++)
        {
            g[i].clear();
        }
    }

    void add(int a, int b)
    {
        g[a].push_back(b);
    }

    int par(int a)

```

```

{
    return up[a][0];
}

int get_lca(int a, int b)
{
    if (depth[a] < depth[b])
        std::swap(a, b);

    int k = depth[a] - depth[b];
    for (int j = lg - 1; j >= 0; j--)
    {
        if (k & (1 << j))
            a = up[a][j];
    }

    if (a == b)
        return a;

    for (int j = lg - 1; j >= 0; j--)
        if (up[a][j] != up[b][j])
        {
            a = up[a][j];
            b = up[b][j];
        }

    return up[a][0];
}

int get_dist(int a, int b)
{
    return depth[a] + depth[b] - 2 * depth[get_lca(a, b)];
}
};

```

### 1.3.9 Lazy Segment Tree [MB]

```

template <typename T, typename F, T(*op)(T, T), F(*
    lazy_to_lazy)(F, F), T(*lazy_to_seg)(T, F, int, int)>
struct LazySegTree
{
private:
    std::vector<T> segt;
    std::vector<F> lazy;
    int n;
    T neutral;
    F lazyE;
    int left(int si) { return si * 2; }
    int right(int si) { return si * 2 + 1; }

```

```

    int midpoint(int ss, int se) { return (ss + (se - ss) / 2);
    }
    T query(int ss, int se, int si, int qs, int qe)
    {
        // **** //
        if (lazy[si] != lazyE)
        {
            F curr = lazy[si];
            lazy[si] = lazyE;
            segt[si] = lazy_to_seg(segt[si], curr, ss, se);
            if (ss != se)
            {
                lazy[left(si)] = lazy_to_lazy(lazy[left(si)], curr);
                lazy[right(si)] = lazy_to_lazy(lazy[right(si)], curr);
            }
        }
        if (se < qs || qe < ss)
            return neutral;
        if (qs <= ss && qe >= se)
            return segt[si];
        int mid = midpoint(ss, se);
        return op(query(ss, mid, left(si), qs, qe), query(mid + 1,
            se, right(si), qs, qe));
    }

    void update(int ss, int se, int si, int qs, int qe, F val)
    {
        // **** //
        if (lazy[si] != lazyE)
        {
            F curr = lazy[si];
            lazy[si] = lazyE;
            segt[si] = lazy_to_seg(segt[si], curr, ss, se);
            if (ss != se)
            {
                lazy[left(si)] = lazy_to_lazy(lazy[left(si)], curr);
                lazy[right(si)] = lazy_to_lazy(lazy[right(si)], curr);
            }
        }
        if (se < qs || qe < ss)
            return;
        if (qs <= ss && qe >= se)
        {
            // **** //
            segt[si] = lazy_to_seg(segt[si], val, ss, se);

            if (ss != se)
            {
                lazy[left(si)] = lazy_to_lazy(lazy[left(si)], val);
                lazy[right(si)] = lazy_to_lazy(lazy[right(si)], val);
            }
        }
    }

```

```

    }
    return;
}

    int mid = midpoint(ss, se);

    update(mid + 1, se, si * 2 + 1, qs, qe, val);
    update(ss, mid, left(si), qs, qe, val);

    segt[si] = op(segt[left(si)], segt[right(si)]);
}

void build(const std::vector<T> &a, int si, int ss, int se)
{
    if (ss == se)
    {
        segt[si] = a[ss];
        return;
    }
    int mid = midpoint(ss, se);
    build(a, left(si), ss, mid);
    build(a, right(si), mid + 1, se);
    segt[si] = op(segt[left(si)], segt[right(si)]);
}

public:
    LazySegTree() : n(0) {}
    LazySegTree(int sz, T ini, T _neutral, F _lazyE)
    {
        this->n = sz + 1;
        this->neutral = _neutral;
        this->lazyE = _lazyE;
        segt.resize(n * 4 + 5, ini);
        lazy.resize(n * 4 + 5, _lazyE);
    }
    LazySegTree(const std::vector<T> &arr, T ini, T _neutral, F
        _lazyE) : LazySegTree((int)arr.size(), ini, _neutral,
        _lazyE)
    {
        init(arr);
    }
    void init(const std::vector<T> &arr) { this->n = (int)arr.
        size(); build(arr, 1, 0, n - 1); }
    T get(int qs, int qe) { return query(0, n - 1, 1, qs, qe);
    }
    void set(int from, int to, F val) { update(0, n - 1, 1,
        from, to, val); }
};

int op(int a, int b)
{
    return a + b;
}

```

```

}

int lazy_to_seg(int seg, int lazy_v, int l, int r)
{
    return seg + (lazy_v * (r - l + 1));
}

int lazy_to_lazy(int curr_lazy, int input_lazy)
{
    return curr_lazy + input_lazy;
}

```

### 1.3.10 Lazy Segment Tree [SK]

```

ll v[4*N];
ll add[4*N];
int arr[N];

void push(int cur)
{
    add[cur*2] += add[cur];
    add[cur*2 + 1] += add[cur];
    add[cur] = 0;
}

/*
void build(int cur,int l,int r)
{
    if(l==r)
    {
        v[cur] = arr[l];
        return;
    }

    int mid = 1 + (r-l)/2;

    build(cur*2,l,mid);
    build(cur*2 + 1,mid+1,r);

    v[cur]= v[cur*2] + v[cur*2 + 1];

    return;
}
*/

ll query(int cur,int l,int r,int x,int y)
{
    if(x>r || y<l)

```

```

{
    return 0;
}

if(l==r)
{
    return v[cur] + add[cur];
}

if(l==x && r==y)
{
    return v[cur] + add[cur]*(r-l+1);
}

int mid = 1 + (r-l)/2;

v[cur] += add[cur]*(r-l+1);
push(cur);

ll left = query(cur*2,l,mid,x,min(mid,y));
ll right = query(cur*2 + 1,mid+1,r,max(mid+1,x),y);

ll res = 0;

res = left + right ;

return res;
}

void update(int cur,int l,int r,int s,int e,int val)
{
    if(l==s && r==e)
    {
        add[cur] += val;
        return;
    }

    if(s>r || e<l)
    {
        return;
    }

    int mid = 1 + (r-l)/2;

    push(cur);

    update(cur*2,l,mid,s,min(e,mid),val);
    update(cur*2 + 1,mid+1,r,max(s,mid+1),e,val);

```

```

    v[cur] = (v[cur*2] + add[cur*2]*(mid-l+1)) + (v[cur*2 + 1] + add[cur*2 + 1]*(r-mid));

    return;
}

```

### 1.3.11 Mos Algorithm [MB]

```

#include <bits/stdc++.h>

using namespace std;

const int N = 3e4 + 5;
const int blk = sqrt(N) + 1;

struct Query
{
    int l, r, i;
    bool operator<(const Query q) const
    {
        if (this->l / blk == q.l / blk)
            return this->r < q.r;
        return this->l / blk < q.l / blk;
    }
};

vector<int> mos_algorithm(vector<Query> &queries, vector<int> &a)
{
    vector<int> answers(queries.size());
    sort(queries.begin(), queries.end());

    int sza = 1e6 + 5;
    vector<int> freq(sza);

    int cnt = 0;

    auto add = [&](int x) -> void
    {
        freq[x]++;
        if (freq[x] == 1)
            cnt++;
    };

    auto remove = [&](int x) -> void
    {
        freq[x]--;
        if (freq[x] == 0)

```



```

    cnt--;
};

int l = 0;
int r = -1;
for (Query q : queries)
{
    while (l > q.l)
    {
        l--;
        add(a[l]);
    }
    while (r < q.r)
    {
        r++;
        add(a[r]);
    }
    while (l < q.l)
    {
        remove(a[l]);
        l++;
    }
    while (r > q.r)
    {
        remove(a[r]);
        r--;
    }
    answers[q.i] = cnt;
}
return answers;
}

int main()
{
    int n;
    cin >> n;

    vector<int> a(n);
    for (int i = 0; i < n; i++)
        cin >> a[i];

    int q;
    cin >> q;

    vector<Query> qr(q);

    for (int i = 0; i < q; i++)
    {
        int l, r;
        cin >> l >> r;

```

```

        l--, r--;
        qr[i].l = l, qr[i].r = r, qr[i].i = i;
    }

    vector<int> res = mos_algorithm(qr, a);

    for (int i = 0; i < q; i++)
        cout << res[i] << endl;

    return 0;
}

```

### 1.3.12 SCC, Condens Graph [NK]

```

#include <bits/stdc++.h>
using namespace std;

vector<vector<int>> adj, adj_rev;
vector<bool> used;
vector<int> order, component;

void dfs1(int v) {
    used[v] = true;

    for (auto u : adj[v])
        if (!used[u])
            dfs1(u);

    order.push_back(v);
}

void dfs2(int v) {
    used[v] = true;
    component.push_back(v);

    for (auto u : adj_rev[v])
        if (!used[u])
            dfs2(u);
}

int main() {
    int n;
    // ... read n ...

    for (;;) {
        int a, b;
        // ... read next directed edge (a,b) ...
        adj[a].push_back(b);

```

```

        adj_rev[b].push_back(a);
    }

    used.assign(n, false);

    for (int i = 0; i < n; i++)
        if (!used[i])
            dfs1(i);

    used.assign(n, false);
    reverse(order.begin(), order.end());

    for (auto v : order)
        if (!used[v]) {
            dfs2(v);

            // ... processing next component ...

            component.clear();
        }

    vector<int> roots(n, 0);
    vector<int> root_nodes;
    vector<vector<int>> adj_scc(n);

    for (auto v : order)
        if (!used[v]) {
            dfs2(v);

            int root = component.front();
            for (auto u : component) roots[u] = root;
            root_nodes.push_back(root);

            component.clear();
        }

    for (int v = 0; v < n; v++)
        for (auto u : adj[v]) {
            int root_v = roots[v],
                root_u = roots[u];

            if (root_u != root_v)
                adj_scc[root_v].push_back(root_u);
        }
}

```

### 1.3.13 Segment Tree [SK]

```

pair<int,int>v[4*N];

```

```

int arr[N];

void build(int cur,int l,int r)
{
    if(l==r)
    {
        pair<int,int> tmp = {0,0};
        if(arr[l]==0)
        {
            tmp.second++;
        }
        else if(arr[l]<0)
        {
            tmp.first++;
        }
        v[cur] = tmp;
        return;
    }

    int mid = l + (r-1)/2;

    build(cur*2,l,mid);
    build(cur*2 + 1,mid+1,r);

    v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
    v[cur].second = v[cur*2].second + v[cur*2 + 1].second;
    return;
}

pair<int,int>query(int cur,int l,int r,int x,int y)
{
    if(l==x && r==y)
    {
        return v[cur];
    }

    if(x>r || y<l)
    {
        return {-1,-1};
    }

    int mid = l + (r-1)/2;
    pair<int,int> left = query(cur*2,l,mid,x,min(mid,y));
    pair<int,int> right = query(cur*2 + 1,mid+1,r,max(mid+1,x),y);

    pair<int,int> res = {0,0};
    res.first = ((left.first!=-1)?left.first:0) + ((right.first!=-1)?right.first:0);
    res.second = ((left.second!=-1)?left.second:0) + ((right.second!=-1)?right.second:0);
}

```

```

        return res;
    }

    void update(int cur,int l,int r,int pos,int val)
    {
        if(l==r)
        {
            arr[l] = val;
            pair<int,int> tmp = {0,0};
            if(arr[l]==0)
            {
                tmp.second++;
            }
            else if(arr[l]<0)
            {
                tmp.first++;
            }
            v[cur] = tmp;
            return;
        }

        int mid = l + (r-1)/2;

        if(pos<=mid)
        {
            update(cur*2,l,mid,pos,val);
        }
        else
        {
            update(cur*2 + 1,mid+1,r,pos,val);
        }

        v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
        v[cur].second = v[cur*2].second + v[cur*2 + 1].second;
        return;
    }
}

```

### 1.3.14 Segment Tree[MB]

```

template <typename T, T(*op)(T, T)>
struct SegTree
{
private:
    std::vector<T> segt;
    int n;
    T e;
}

```

```

int left(int si) { return si * 2; }
int right(int si) { return si * 2 + 1; }
int midpoint(int ss, int se) { return (ss + (se - ss) / 2); }

T query(int ss, int se, int qs, int qe, int si)
{
    if (se < qs || qe < ss)
        return e;
    if (qs <= ss && qe >= se)
        return segt[si];
    int mid = midpoint(ss, se);
    return op(query(ss, mid, qs, qe, left(si)), query(mid + 1, se, qs, qe, right(si)));
}

void update(int ss, int se, int key, int si, T val)
{
    if (ss == se)
    {
        segt[si] = val;
        return;
    }
    int mid = midpoint(ss, se);
    if (key > mid)
        update(mid + 1, se, key, right(si), val);
    else
        update(ss, mid, key, left(si), val);
    segt[si] = op(segt[left(si)], segt[right(si)]);
}

void build(const std::vector<T> &a, int si, int ss, int se)
{
    if (ss == se)
    {
        segt[si] = a[ss];
        return;
    }
    int mid = midpoint(ss, se);
    build(a, left(si), ss, mid);
    build(a, right(si), mid + 1, se);
    segt[si] = op(segt[left(si)], segt[right(si)]);
}

public:
    SegTree() : n(0) {}
    SegTree(int sz, T _e)
    {
        this->e = _e;
        this->n = sz;
        segt.resize(n * 4 + 5, _e);
    }
    SegTree(const std::vector<T> &arr, T _e) : SegTree((int)arr.size(), _e) { init(arr); }
}

```

```

void init(const std::vector<T> &arr) { this->n = (int)(arr.
    size());build(arr, 1, 0, n - 1); }
T get(int qs, int qe) { return query(0, n - 1, qs, qe, 1);
}
void set(int key, T val) { update(0, n - 1, key, 1, val); }
};

int op(int a, int b)
{
    return min(a, b);
}

```

### 1.3.15 SparseTable[MB]

```

template <typename T, T (*op)(T, T)>
struct SparseTable
{
private:
    std::vector<std::vector<T>> st;
    int n, lg;
    std::vector<int> logs;
    T e;

public:
    SparseTable() : n(0) {}

    SparseTable(int _n)
    {
        this->n = _n;
        int bit = 0;
        while ((1 << bit) <= n)
            bit++;
        this->lg = bit;

        st.resize(n, std::vector<T>(lg));
        logs.resize(n + 1, 0);
        logs[1] = 0;
        for (int i = 2; i <= n; i++)
        {
            logs[i] = logs[i / 2] + 1;
        }
    }

    SparseTable(const std::vector<T> &a) : SparseTable((int)a.
        size())
    {
        init(a);
    }
}

```

```

void init(const std::vector<T> &a)
{
    this->n = (int)a.size();

    for (int i = 0; i < n; i++)
    {
        st[i][0] = a[i];
    }

    for (int j = 1; j <= lg; j++)
    {
        for (int i = 0; i + (1 << j) <= n; i++)
        {
            st[i][j] = op(st[i][j - 1], st[std::min(i + (1 << (j - 1)
                ), n - 1)][j - 1]);
        }
    }
}

T get(int l, int r)
{
    int j = logs[r - l + 1];
    return op(st[l][j], st[r - (1 << j) + 1][j]);
}

int min(int a, int b)
{
    return std::min(a, b);
}

```

### 1.3.16 Treap[MB]

```

#include <bits/stdc++.h>

#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define endl "\n"

#include <ext/pb_ds/assoc_container.hpp> // Common file
// using namespace __gnu_pbds;

// https://codeforces.com/blog/entry/11080
//cout<<*X.find_by_order(4)<<endl; // 16
// cout<<(end(X)==X.find_by_order(6))<<endl; // true
// cout<<X.order_of_key(-5)<<endl; // 0
template <typename T, typename order = std::less<T>>

```

```

using ordered_set = __gnu_pbds::tree<T, __gnu_pbds::
    null_type, order, __gnu_pbds::rb_tree_tag, __gnu_pbds::
    tree_order_statistics_node_update>;

int main()
{
    ordered_set<int> X;

    std::cout << *X.find_by_order(4) << endl; // 16
    std::cout << (std::end(X) == X.find_by_order(6)) << endl;
        // true
    std::cout << X.order_of_key(-5) << endl; // 0

    return 0;
}

```

## 1.4 Graph

### 1.4.1 Edge Remove CC [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

#define var(...) " [" << #__VA_ARGS__ " : " << (__VA_ARGS__)
    << "]"
#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)x.size())
#define vec vector
#define endl "\n"

class DSU
{
    std::vector<int> p, csz;

public:
    DSU() {}

    DSU(int dsz) // Max size
    {
        //Default empty
        p.resize(dsz + 5, 0), csz.resize(dsz + 5, 0);

        init(dsz);
    }
}

```

```

void init(int n)
{
    // n = size
    for (int i = 0; i <= n; i++)
    {
        p[i] = i, csz[i] = 1;
    }
}

//Return parent Recursively
int get(int x)
{
    if (p[x] != x)
        p[x] = get(p[x]);

    return p[x];
}

// Return Size
int getSize(int x) { return csz[get(x)]; }
// Return if Union created Successfully or false if they
// are already in Union
bool merge(int x, int y)
{
    x = get(x), y = get(y);
    if (x == y)
        return false;

    if (csz[x] > csz[y])
        std::swap(x, y);

    p[x] = y;
    csz[y] += csz[x];

    return true;
}

void runCase([[maybe_unused]] const int &TC)
{
    int n, m;
    cin >> n >> m;

    auto g = vec(n + 1, set<int>());

    auto dsu = DSU(n + 1);

    for (int i = 0; i < m; i++)
    {
        int u, v;

```

```

        cin >> u >> v;

        g[u].insert(v);
        g[v].insert(u);
    }

    set<int> elligible;

    for (int i = 1; i <= n; i++)
    {
        elligible.insert(i);
    }

    int i = 1;
    int cnt = 0;

    while (sz(elligible))
    {
        cnt++;
        queue<int> q;
        q.push(*elligible.begin());
        elligible.erase(elligible.begin());

        while (sz(q))
        {
            int fr = q.front();
            q.pop();

            auto v = elligible.begin();

            while (v != elligible.end())
            {
                if (g[fr].find(*v) == g[fr].end())
                {
                    q.push(*v);
                    v = elligible.erase(v);
                }
                else
                {
                    v++;
                }
            }
        }

        cout << cnt - 1 << endl;
    }

    int main()
    {

```

```

        ios_base::sync_with_stdio(false), cin.tie(0);

        int t = 1;
        //cin >> t;

        for (int tc = 1; tc <= t; tc++)
            runCase(tc);

        return 0;
    }

```

### 1.4.2 Kruskal's [NK]

```

struct Edge {
    using weight_type = long long;
    static const weight_type bad_w; // Indicates non-existent
    edge

    int u = -1; // Edge source (vertex id)
    int v = -1; // Edge destination (vertex id)
    weight_type w = bad_w; // Edge weight

#define DEF_EDGE_OP(op) \
    friend bool operator op(const Edge& lhs, const Edge& rhs) \
    { \
        return make_pair(lhs.w, make_pair(lhs.u, lhs.v)) op \
            make_pair(rhs.w, make_pair(rhs.u, rhs.v)); \
    }

    DEF_EDGE_OP(==)
    DEF_EDGE_OP(!=)
    DEF_EDGE_OP(<)
    DEF_EDGE_OP(<=)
    DEF_EDGE_OP(>)
    DEF_EDGE_OP(>=)
};

constexpr Edge::weight_type Edge::bad_w = numeric_limits<
    Edge::weight_type>::max();

template <class EdgeCompare = less<Edge>>
constexpr vector<Edge> kruskal(const int n, vector<Edge>
    edges, EdgeCompare compare = EdgeCompare()) {
    // define dsu part and initlaize forests

    vector<int> parent(n);
    iota(parent.begin(), parent.end(), 0);
    vector<int> size(n, 1);
    auto root = [&](int x) {

```

```

    int r = x;
    while (parent[r] != r) {
        r = parent[r];
    }
    while (x != r) {
        int tmp_id = parent[x];
        parent[x] = r;
        x = tmp_id;
    }
    return r;
};

auto connect = [&](int u, int v) {
    u = root(u);
    v = root(v);
    if (size[u] > size[v]) {
        swap(u, v);
    }
    parent[v] = u;
    size[u] += size[v];
    size[v] = 0;
};

// connect components (trees) with edges in order from
// the sorted list

sort(edges.begin(), edges.end(), compare);
vector<Edge> edges_mst;
int remaining = n - 1;
for (const Edge& e : edges) {
    if (!remaining) break;
    const int u = root(e.u);
    const int v = root(e.v);
    if (u == v) continue;
    --remaining;
    edges_mst.push_back(e);
    connect(u, v);
}

return edges_mst;
}

```

### 1.4.3 Tree Rooting [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

```

```

const int N = 2e5 + 5;

vector<int> g[N];
ll sz[N], dist[N], sum[N];

void dfs(int s, int p)
{
    sz[s] = 1;
    dist[s] = 0;
    for (int nxt : g[s])
    {
        if (nxt == p)
            continue;
        dfs(nxt, s);
        sz[s] += sz[nxt];
        dist[s] += (dist[nxt] + sz[nxt]);
    }
}

void dfs1(int s, int p)
{
    if (p != 0)
    {
        ll my_size = sz[s];
        ll my_contrib = (dist[s] + sz[s]);

        sum[s] = sum[p] - my_contrib + sz[1] - sz[s] + dist[s];
    }
    for (int nxt : g[s])
    {
        if (nxt == p)
            continue;
        dfs1(nxt, s);
    }
}

// problem link: https://cses.fi/problemset/task/1133

int main()
{
    int n;
    cin >> n;

    for (int i = 1, u, v; i < n; i++)
        cin >> u >> v, g[u].push_back(v), g[v].push_back(u);

    dfs(1, 0);

    sum[1] = dist[1];
}

```

```

dfs1(1, 0);

for (int i = 1; i <= n; i++)
    cout << sum[i] << " ";
cout << endl;

return 0;
}

```

## 1.5 Math

### 1.5.1 Combinatorics [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

struct Combinatorics
{
    vector<ll> fact, fact_inv, inv;
    ll mod, nl;

    Combinatorics() {}

    Combinatorics(ll n, ll _mod)
    {
        this->nl = n;
        this->mod = _mod;
        fact.resize(n + 1, 1), fact_inv.resize(n + 1, 1), inv.
            resize(n + 1, 1);
        init();
    }

    void init()
    {
        fact[0] = 1;

        for (int i = 1; i <= nl; i++)
        {
            fact[i] = (fact[i - 1] * i) % mod;
        }

        inv[0] = inv[1] = 1;
        for (int i = 2; i <= nl; i++)
            inv[i] = inv[mod % i] * (mod - mod / i) % mod;
    }
}

```

```

fact_inv[0] = fact_inv[1] = 1;

for (int i = 2; i <= nl; i++)
    fact_inv[i] = (inv[i] * fact_inv[i - 1]) % mod;
}

ll ncr(ll n, ll r)
{
    if (n < r) {
        return 0;
    }

    if (n > nl)
        return ncr(n, r, mod);
    return (((fact[n] * 1LL * fact_inv[r]) % mod) * 1LL *
            fact_inv[n - r]) % mod;
}

ll npr(ll n, ll r)
{
    if (n < r) {
        return 0;
    }

    if (n > nl)
        return npr(n, r, mod);
    return (fact[n] * 1LL * fact_inv[n - r]) % mod;
}

ll big_mod(ll a, ll p, ll m = -1)
{
    m = (m == -1 ? mod : m);
    ll res = 1 % m, x = a % m;
    while (p > 0)
        res = ((p & 1) ? ((res * x) % m) : res), x = ((x * x) % m), p >>= 1;
    return res;
}

ll mod_inv(ll a, ll p)
{
    return big_mod(a, p - 2, p);
}

ll ncr(ll n, ll r, ll p)
{
    if (n < r)
        return 0;
    if (r == 0)
        return 1;

```

```

    return (((fact[n] * mod_inv(fact[r], p)) % p) * mod_inv(
        fact[n - r], p)) % p;
}

ll npr(ll n, ll r, ll p)
{
    if (n < r)
        return 0;
    if (r == 0)
        return 1;
    return (fact[n] * mod_inv(fact[n - r], p)) % p;
}
};

```

```
const int N = 1e6, MOD = 998244353;
```

```
Combinatrics comb(N, MOD);
```

### 1.5.2 Extended GCD [NK]

```

template <class Z>
constexpr Z extended_gcd(Z a, Z b, Z& x_ref, Z& y_ref) {
    x_ref = 1, y_ref = 0;
    Z x1 = 0, y1 = 1, tmp = 0, q = 0;
    while (b > 0) {
        q = a / b;
        tmp = a, a = b, b = tmp - (q * b);
        tmp = x_ref, x_ref = x1, x1 = tmp - (q * x1);
        tmp = y_ref, y_ref = y1, y1 = tmp - (q * y1);
    }
    return a;
}

```

### 1.5.3 Fraction-Functions [SK]

```

pair<ll,ll> frac_add(pair<ll,ll> a,pair<ll,ll> b)
{
    ll g = a.second*b.second;
    pair<ll,ll> x;
    x.second = g;
    x.first = a.first * (b.second) + b.first * (a.second);
    ll y = __gcd(x.first,x.second);
    x.first/=y;
    x.second/=y;
    return x;
}

pair<ll,ll> frac_mult(pair<ll,ll> a,pair<ll,ll> b)

```

```

{
    pair<ll,ll> x;

    x.first = a.first * b.first;
    x.second = a.second * b.second;
    ll y = __gcd(x.first,x.second);
    x.first/=y;
    x.second/=y;
    return x;
}

```

### 1.5.4 Fraction[MB]

```

struct Fraction {
    int p, q;

    Fraction (int _p, int _q) : p(_p), q(_q) {}

    std::strong_ordering operator<=> (const Fraction &oth)
        const {
            return p * oth.q <=> q * oth.p;
        }
};

```

### 1.5.5 Miller-Rabin-for-prime-checking [SK]

```

typedef long long ll;

ll mulmod(ll a, ll b, ll c) {
    ll x = 0, y = a % c;
    while (b) {
        if (b & 1) x = (x + y) % c;
        y = (y << 1) % c;
        b >>= 1;
    }
    return x % c;
}

ll fastPow(ll x, ll n, ll MOD) {
    ll ret = 1;
    while (n) {
        if (n & 1) ret = mulmod(ret, x, MOD);
        x = mulmod(x, x, MOD);
        n >>= 1;
    }
    return ret;
}

```

```

}

bool isPrime(ll n) {
    ll d = n - 1;
    int s = 0;
    while (d % 2 == 0) {
        s++;
        d >>= 1;
    }

    // It's guranteed that these values will work for any
    // number smaller than 3*10**18 (3 and 18 zeros)
    int a[9] = { 2, 3, 5, 7, 11, 13, 17, 19, 23 };
    for(int i = 0; i < 9; i++) {
        bool comp = fastPow(a[i], d, n) != 1;
        if(comp) for(int j = 0; j < s; j++) {
            ll fp = fastPow(a[i], (1LL << (11)j)*d, n);
            if (fp == n - 1) {
                comp = false;
                break;
            }
        }
        if(comp) return false;
    }
    return true;
}

```

### 1.5.6 Modular Binary Exponentiation (Power) [NK]

```

template <class B, class E, class M>
constexpr B power(B base, E expo, M mod = 0) {
    assert(expo >= 0);
    if (mod == 1) return 0;
    if (base == 0 || base == 1) return base;
    B res = 1;
    if (!mod) {
        while (expo) {
            if (expo & 1) res *= base;
            base *= base;
            expo >>= 1;
        }
    } else {
        assert(mod > 0);
        base %= mod;
        if (base <= 1) return base;
        while (expo) {
            if (expo & 1) res = (res * base) % mod;
            base = (base * base) % mod;

```

```

        expo >>= 1;
    }
    return res;
}

```

### 1.5.7 Modular Int [MB]

```

#include <bits/stdc++.h>
// Tested By Ac
// submission : https://atcoder.jp/contests/abc238/submissions/29247261
// problem : https://atcoder.jp/contests/abc238/tasks/abc238\_c

template <const int MOD>
struct ModInt
{
    int val;
    ModInt() { val = 0; }
    ModInt(long long v) { v += (v < 0 ? MOD : 0), val = (int)(v % MOD); }
    ModInt &operator+=(const ModInt &rhs)
    {
        val += rhs.val, val -= (val >= MOD ? MOD : 0);
        return *this;
    }
    ModInt &operator-=(const ModInt &rhs)
    {
        val -= rhs.val, val += (val < 0 ? MOD : 0);
        return *this;
    }
    ModInt &operator*=(const ModInt &rhs)
    {
        val = (int)((val * 1ULL * rhs.val) % MOD);
        return *this;
    }
    ModInt pow(long long n) const
    {
        ModInt x = *this, r = 1;
        while (n)
            r = ((n & 1) ? r * x : r), x = (x * x), n >>= 1;
        return r;
    }
    ModInt inv() const { return this->pow(MOD - 2); }
    ModInt &operator/=(const ModInt &rhs) { return *this = *this * rhs.inv(); }
    friend ModInt operator+(const ModInt &lhs, const ModInt &rhs) { return ModInt(lhs) += rhs; }

```

```

    friend ModInt operator-(const ModInt &lhs, const ModInt &rhs) { return ModInt(lhs) -= rhs; }
    friend ModInt operator*(const ModInt &lhs, const ModInt &rhs) { return ModInt(lhs) *= rhs; }
    friend ModInt operator/(const ModInt &lhs, const ModInt &rhs) { return ModInt(lhs) /= rhs; }
    friend bool operator==(const ModInt &lhs, const ModInt &rhs) { return lhs.val == rhs.val; }
    friend bool operator!=(const ModInt &lhs, const ModInt &rhs) { return lhs.val != rhs.val; }
    friend std::ostream &operator<<(std::ostream &out, const ModInt &m) { return out << m.val; }
    friend std::istream &operator>>(std::istream &in, ModInt &m) { return in >> m.val; }
    operator int() const { return val; }
};

```

```

const int MOD = 1e9 + 7;
using mint = ModInt<MOD>;

```

### 1.5.8 Modular inverse [NK]

```

template <class Z>
constexpr Z inverse(Z num, Z mod) {
    assert(mod > 1);
    if (!(0 <= num && num < mod)) {
        num %= mod;
        if (num < 0) num += mod;
    }
    Z res = 1, tmp = 0;
    assert(extended_gcd(num, mod, res, tmp) == 1);
    if (res < 0) res += mod;
    return res;
}

```

### 1.5.9 Prime Phi Sieve [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

struct PrimePhiSieve
{
private:

```

```

ll n;
vector<ll> primes, phi;
vector<bool> is_prime;

public:
PrimePhiSieve() {}

PrimePhiSieve(ll n)
{
    this->n = n, is_prime.resize(n + 5, true), phi.resize(n +
        5, 1);
    phi_sieve();
}
void phi_sieve()
{
    is_prime[0] = is_prime[1] = false;

    for (ll i = 1; i <= n; i++)
        phi[i] = i;

    for (ll i = 1; i <= n; i++)
        if (is_prime[i])
        {
            primes.push_back(i);
            phi[i] *= (i - 1), phi[i] /= i;

            for (ll j = i + i; j <= n; j += i)
                is_prime[j] = false, phi[j] /= i, phi[j] *= (i - 1);
        }
}

ll get_divisors_count(int number, int divisor)
{
    return phi[number / divisor];
}

vector<pll> factorize(ll num)
{
    vector<pll> a;
    for (int i = 0; i < (int)primes.size() && primes[i] * 1LL
        * primes[i] <= num; i++)
        if (num % primes[i] == 0)
        {
            int cnt = 0;
            while (num % primes[i] == 0)
                cnt++, num /= primes[i];
            a.push_back({primes[i], cnt});
        }

    if (num != 1)

```

```

        a.push_back({num, 1});
    return a;
}

ll get_phi(int n)
{
    return phi[n];
}
// (n/p) * (p-1) => n- (n/p);
void segmented_phi_sieve(ll l, ll r)
{
    vector<ll> current_phi(r - l + 1);
    vector<ll> left_over_prime(r - l + 1);

    for (ll i = l; i <= r; i++)
        current_phi[i - l] = i, left_over_prime[i - l] = i;

    for (ll p : primes)
    {
        ll to = ((l + p - 1) / p) * p;

        if (to == p)
            to += p;

        for (ll i = to; i <= r; i += p)
        {
            while (left_over_prime[i - l] % p == 0)
                left_over_prime[i - l] /= p;
            current_phi[i - l] -= current_phi[i - l] / p;
        }
    }

    for (ll i = l; i <= r; i++)
    {
        if (left_over_prime[i - l] > 1)
            current_phi[i - l] -= current_phi[i - l] /
                left_over_prime[i - l];
        cout << current_phi[i - l] << endl;
    }
}

ll phi_sqrt(ll n)
{
    ll res = n;

    for (ll i = 1; i * i <= n; i++)
    {
        if (n % i == 0)
        {
            res /= i;

```

```

            res *= (i - 1);

            while (n % i == 0)
                n /= i;
        }
    }

    if (n > 1)
        res /= n, res *= (n - 1);
    return res;
}
};

```

---

### 1.5.10 Prime Sieve [MB]

---

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

struct PrimeSieve
{
public:
    vector<int> primes;
    vector<bool> isprime;
    int n;

    PrimeSieve() {}

    PrimeSieve(int _n)
    {
        this->n = _n, isprime.resize(_n + 5, true), primes.clear()
            ;
        sieve();
    }

    void sieve()
    {
        isprime[0] = isprime[1] = false;

        primes.push_back(2);
        for (int i = 4; i <= n; i += 2)
            isprime[i] = false;

        for (int i = 3; 1LL * i * i <= n; i += 2)
            if (isprime[i])

```



```

    for (int j = i * i; j <= n; j += 2 * i)
        isprime[j] = false;

    for (int i = 3; i <= n; i += 2)
        if (isprime[i])
            primes.push_back(i);
}

```

```

vector<pll> factorize(ll num)
{
    vector<pll> a;
    for (int i = 0; i < (int)primes.size() && primes[i] * 1LL
        * primes[i] <= num; i++)
        if (num % primes[i] == 0)
        {
            int cnt = 0;
            while (num % primes[i] == 0)
                cnt++, num /= primes[i];
            a.push_back({primes[i], cnt});
        }

    if (num != 1)
        a.push_back({num, 1});
    return a;
}

```

```

vector<ll> segmented_sieve(ll l, ll r)
{
    vector<ll> seg_primes;
    vector<bool> current_primes(r - l + 1, true);
    for (ll p : primes)
    {
        ll to = (l / p) * p;
        if (to < l)
            to += p;
        if (to == p)
            to += p;
        for (ll i = to; i <= r; i += p)
        {
            current_primes[i - l] = false;
        }
    }
}

```

```

for (ll i = l; i <= r; i++)
{
    if (i < 2)
        continue;
    if (current_primes[i - l])
    {

```

```

        seg_primes.push_back(i);
    }
}
return seg_primes;
}
};

```

### 1.5.11 Segmented sieve phi [NK]

```

vector<int64_t> phi_seg;

void seg_sieve_phi(const int64_t a, const int64_t b) {
    phi_seg.assign(b - a + 2, 0);
    vector<int64_t> factor(b - a + 2, 0);
    for (int64_t i = a; i <= b; i++) {
        auto m = i - a + 1;
        phi_seg[m] = i;
        factor[m] = i;
    }

    auto lim = sqrt(b) + 1;
    sieve(lim);
    for (auto p : primes) {
        int64_t a1 = p * ((a + p - 1) / p);
        for (int64_t j = a1; j <= b; j += p) {
            auto m = j - a + 1;
            while (factor[m] % p == 0) {
                factor[m] /= p;
            }
            phi_seg[m] -= (phi_seg[m] / p);
        }
    }

    for (int64_t i = a; i <= b; i++) {
        auto m = i - a + 1;
        if (factor[m] > 1) {
            phi_seg[m] -= (phi_seg[m] / factor[m]);
            factor[m] = 1;
        }
    }
}

```

### 1.5.12 Segmented sieve primes [NK]

```

vector<bool> isprime_seg;
vector<int64_t> seg_primes;

void seg_sieve(const int64_t a, const int64_t b) {
    isprime_seg.assign(b - a + 1, true);
    int lim = sqrt(b) + 1;

```

```

    sieve(lim);
    for (auto p : primes) {
        auto a1 = p * max((int64_t)(p), ((a + p - 1) / p));
        for (auto j = a1; j <= b; j += p) {
            isprime_seg[j - a] = false;
        }
    }

    for (auto i = a; i <= b; i++) {
        if (isprime_seg[i - a]) {
            seg_primes.push_back(i);
        }
    }
}

```

### 1.5.13 Sieve phi [NK]

```

vector<int> phi;

void sieve_phi(int n) {
    phi.assign(n + 1, 0);
    iota(phi.begin(), phi.end(), 0);
    for (int i = 2; i <= n; i++) {
        if (phi[i] == i) {
            for (int j = i; j <= n; j += i) {
                phi[j] -= (phi[j] / i);
            }
        }
    }
}

```

### 1.5.14 nCr mod p in O(1) [SK]

```

// array to store inverse of 1 to N
ll factorialNumInverse[N + 1];

// array to precompute inverse of 1! to N!
ll naturalNumInverse[N + 1];

// array to store factorial of first N numbers
ll fact[N + 1];

// Function to precompute inverse of numbers
void InverseofNumber(ll p)
{
    naturalNumInverse[0] = naturalNumInverse[1] = 1;
    for (int i = 2; i <= N; i++)
        naturalNumInverse[i] = naturalNumInverse[p % i] * (p
            - p / i) % p;
}

```

```

}
// Function to precompute inverse of factorials
void InverseofFactorial(ll p)
{
    factorialNumInverse[0] = factorialNumInverse[1] = 1;

    // precompute inverse of natural numbers
    for (int i = 2; i <= N; i++)
        factorialNumInverse[i] = (naturalNumInverse[i] *
            factorialNumInverse[i - 1]) % p;
}

// Function to calculate factorial of 1 to N
void factorial(ll p)
{
    fact[0] = 1;

    // precompute factorials
    for (int i = 1; i <= N; i++) {
        fact[i] = (fact[i - 1] * i) % p;
    }
}

// Function to return nCr % p in O(1) time
ll Binomial(ll N, ll R, ll p)
{
    // n C r = n!*inverse(r!)*inverse((n-r)!)
    ll ans = ((fact[N] * factorialNumInverse[R])
        % p * factorialNumInverse[N - R])
        % p;
    return ans;
}

```

## 1.6 String

### 1.6.1 Hashing [MB]

```
#include <bits/stdc++.h>
```

```
using namespace std;
```

```
typedef long long ll;
```

```
const int PRIMES[] = {2147462393, 2147462419, 2147462587,
    2147462633, 2147462747, 2147463167, 2147463203,
    2147463569, 2147463727, 2147463863, 2147464211,
    2147464549, 2147464751, 2147465153, 2147465563,
    2147465599, 2147465743, 2147465953, 2147466457,
    2147466463, 2147466521, 2147466721, 2147467009,
```

```

    2147467057, 2147467067, 2147467261, 2147467379,
    2147467463, 2147467669, 2147467747, 2147468003,
    2147468317, 2147468591, 2147468651, 2147468779,
    2147468801, 2147469017, 2147469041, 2147469173,
    2147469229, 2147469593, 2147469881, 2147469983,
    2147470027, 2147470081, 2147470177, 2147470673,
    2147470823, 2147471057, 2147471327, 2147471581,
    2147472137, 2147472161, 2147472689, 2147472697,
    2147472863, 2147473151, 2147473369, 2147473733,
    2147473891, 2147473963, 2147474279, 2147474921,
    2147474929, 2147475107, 2147475221, 2147475347,
    2147475397, 2147475971, 2147476739, 2147476769,
    2147476789, 2147476927, 2147477063, 2147477107,
    2147477249, 2147477807, 2147477933, 2147478017,
    2147478521};

// ll base_pow, base_pow_1;
ll base1 = 43, base2 = 47, mod1 = 1e9 + 7, mod2 = 1e9 + 9;

// **** Enable this function for codeforces
void generateRandomBM()
{
    unsigned int seed = chrono::system_clock::now().
        time_since_epoch().count();
    srand(seed); /// to avoid getting hacked in CF, comment
        this line for easier debugging

    int q_len = (sizeof(PRIMES) / sizeof(PRIMES[0])) / 4;
    base1 = PRIMES[rand() % q_len];
    mod1 = PRIMES[rand() % q_len + q_len];
    base2 = PRIMES[rand() % q_len + 2 * q_len];
    mod2 = PRIMES[rand() % q_len + 3 * q_len];
}

```

```

struct Hash
{
public:
    vector<int> base_pow, f_hash, r_hash;
    ll base, mod;

    Hash() {}
    // Update it make it more dynamic like segTree class and
    DSU
    Hash(int mxSize, ll base, ll mod) // Max size
    {
        this->base = base;
        this->mod = mod;
        base_pow.resize(mxSize + 2, 1), f_hash.resize(mxSize + 2,
            0), r_hash.resize(mxSize + 2, 0);
    }
}

```

```

for (int i = 1; i <= mxSize; i++)
{
    base_pow[i] = base_pow[i - 1] * base % mod;
}

void init(string s)
{
    int n = s.size();

    for (int i = 1; i <= n; i++)
    {
        f_hash[i] = (f_hash[i - 1] * base + int(s[i - 1])) % mod;
    }

    for (int i = n; i >= 1; i--)
    {
        r_hash[i] = (r_hash[i + 1] * base + int(s[i - 1])) % mod;
    }
}

int forward_hash(int l, int r)
{
    int h = f_hash[r + 1] - (1LL * base_pow[r - l + 1] *
        f_hash[l]) % mod;
    return h < 0 ? mod + h : h;
}

int reverse_hash(int l, int r)
{
    int h = r_hash[l + 1] - (1LL * base_pow[r - l + 1] *
        r_hash[r + 2]) % mod;
    return h < 0 ? mod + h : h;
}
};

```

```

class DHash
{
public:
    Hash sh1, sh2;
    DHash() {}

    DHash(int mx_size)
    {
        sh1 = Hash(mx_size, base1, mod1);
        sh2 = Hash(mx_size, base2, mod2);
    }

    void init(string s)
    {

```

```

    sh1.init(s);
    sh2.init(s);
}

ll forward_hash(int l, int r)
{
    return (ll(sh1.forward_hash(l, r)) << 32) | (sh2.
        forward_hash(l, r));
}

ll reverse_hash(int l, int r)
{
    return ((ll(sh1.reverse_hash(l, r)) << 32) | (sh2.
        reverse_hash(l, r)));
}
};

```

### 1.6.2 Hashing [NK]

```

// Primes suitable for use as the constant base in a
// polynomial rolling hash function.
constexpr std::array<int, 10>
    prime_bases = {257, 263, 269, 271, 277, 281, 283, 293,
        307, 311};
// Primes suitable for use as modulus.
constexpr std::array<int, 10>
    prime_moduli = {1000000007, 1000000009, 1000000021,
        1000000033, 1000000087,
        1000000093, 1000000097, 1000000103,
        1000000123, 1000000181};

/**
 * @brief A data structure for computing polynomial hashes
 * of sequence keys.
 * For a given key defined as an integral sequence of n
 * elements S[0], S[1], ...,
 * S[n - 1], this structure builds and stores for each
 * prefix S[0...i] the hash value
 * H(i) = S[0] * Bi + S[1] * B(i - 1) + ... + S[i] * B0,
 * modulo M.
 * @param Base The base B. Should be a prime to reduce
 * chances of collision.
 * @param Modulus The modulus M. Should be a prime to
 * reduce chances of collision.
 */
template <std::uint64_t Base, std::uint64_t Modulus>
class Polynomial_hasher {
public:
    using int_type = std::uint64_t;

```

```

    using value_type = int_type;
    using size_type = std::size_t;

    static constexpr int_type B = Base;
    static constexpr int_type M = Modulus;

protected:
    // Base power
    static std::vector<int_type> bpow_;
    // Prefix hash
    std::vector<int_type> pref_hash_;
    // Suffix hash
    std::vector<int_type> suff_hash_;
    // Flag for hashing bidirectionally
    bool bidir_ = false;

public:
    /**
     * @brief Default constructor
     */
    Polynomial_hasher() {}

    /**
     * @brief Constructors and builds the hash from a range (
     * a "key").
     * @tparam InputIter Type of the iterator of the range
     * @param from Iterator pointing to the start of the
     * range
     * @param until Iterator pointing to the end (one past
     * the last element) of the range
     * @param bidir Flag for hashing bidirectionally
     */
    template <class InputIter>
    Polynomial_hasher(InputIter from, InputIter until, bool
        bidir = false) {
        build_hash(from, until, bidir);
    }

    /**
     * @brief Builds the hash from a range (a "key").
     * @tparam InputIter Type of the iterator of the range
     * @param from Iterator pointing to the start of the
     * range
     * @param until Iterator pointing to the end (one past
     * the last element) of
     * the range
     * @param bidir Flag for hashing bidirectionally
     */
    template <class InputIter>

```

```

    void build_hash(InputIter from, InputIter until, bool
        bidir = false) {
        const auto n = std::distance(from, until);
        while (bpow_.size() < n) {
            bpow_.push_back((bpow_.back() * B) % M);
        }
        // Build forward hash
        {
            pref_hash_.resize(n + 1);
            pref_hash_[0] = 0;
            auto it = from;
            for (size_type i = 0; i < n; ++i) {
                pref_hash_[i + 1] =
                    (((pref_hash_[i] * B) % M) + static_cast<
                        int_type>(*it)) % M;
                ++it;
            }
        }
        // Set and test flag, and build reverse hash
        bidir_ = bidir;
        if (bidir_) {
            suff_hash_.resize(n + 1);
            suff_hash_[n] = 0;
            auto it = prev(until);
            for (size_type i = n; i; --i) {
                suff_hash_[i - 1] =
                    (((suff_hash_[i] * B) % M) + static_cast<
                        int_type>(*it)) % M;
                --it;
            }
        }
    }

    /**
     * @brief Returns the polynomial hash value of the
     * subsegment S[i], S[i + 1], ...,
     * S[i + n - 1], which is the value S[i] * B(n - 1) + S[
     * i + 1] * B(n - 2) +
     * ... + S[i + n - 1] * B0, modulo M.
     * @param i Starting index/position of the subsegment
     * @param n Length of the subsegment
     */
    value_type get(size_type i = 0,
        size_type n = std::numeric_limits<size_type>
            >::max()) const {
        assert(i < pref_hash_.size());
        n = std::min(n, pref_hash_.size() - 1 - i);
        return (pref_hash_[i + n] - ((pref_hash_[i] * bpow_[n
            ]) % M) + M) % M;
    }
}

```

```

/**
 * @brief Returns the polynomial hash value of the
 *         subsegment S[i], S[i + 1], ...,
 *         S[i + n - 1] in reverse order, which is the value S[i]
 *         * B^i + S[i + 1] *
 *         * B^(i + 1) + ... + S[i + n - 1] * B^(i + n - 1), modulo
 *         M.
 * @param i Starting index/position of the subsegment
 * @param n Length of the subsegment
 */
value_type get_rev(size_type i = 0,
                  size_type n = std::numeric_limits<
                  size_type>::max()) const {
    assert(bidir_);
    assert(i < suff_hash_.size());
    n = std::min(n, suff_hash_.size() - 1 - i);
    return (suff_hash_[i] - ((suff_hash_[i + n] * bpow_[n]
    ]) % M) + M) % M;
}

/**
 * @brief Erases hash values of all prefixes (and
 *         suffixes if hashed
 *         bidirectionally) calling 'clear()' on the internal
 *         vector(s). Resets
 *         bidirectional flag.
 */
void clear() {
    pref_hash_.clear();
    suff_hash_.clear();
    bidir_ = false;
}

/**
 * @brief Number of elements in the hashed key.
 */
size_type size() const { return pref_hash_.size() ?
    pref_hash_.size() - 1 : 0; }

/**
 * @brief Returns true if no hash values are stored.
 */
bool empty() const { return pref_hash_.empty(); }

/**
 * @brief Returns true if the stored hash value is
 *         bidirectional (i.e., both
 *         'hash' and 'hash_rev' can be called).
 */

```

```

    bool bidirectional() const { return bidir_; }
};

template <std::uint64_t Base, std::uint64_t Modulus>
std::vector<std::uint64_t> Polynomial_hasher<Base, Modulus>::bpow_ = {1ULL};

using Hasher0 = Polynomial_hasher<prime_bases[0],
    prime_moduli[0]>;
using Hasher1 = Polynomial_hasher<prime_bases[1],
    prime_moduli[1]>;

```

### 1.6.3 Hashing [SK]

```

int powhash1[ 1000000 + 10] = {};
int powhash2[ 1000000 + 10] = {};
int f_prefhash1[1000000 + 10];
int f_prefhash2[1000000 + 10];
int r_prefhash1[1000000 + 10];
int r_prefhash2[1000000 + 10];

int add(ll x, ll y, ll mod)
{
    return (x+y>=mod)?(x+y-mod):(x+y);
}

int subtract(ll x, ll y, ll mod)
{
    return (x-y<0)?(x-y+mod):(x-y);
}

int multp(ll x, ll y, ll mod)
{
    return (x*y)%mod;
}

const int BASE1 = 125;
const int MOD1 = 1e9 + 9;

const int BASE2 = 250;
const int MOD2 = 1e9 + 7;

void f_prefhashcalc(string& s, int base, int mod, int*prefhash)
{
    ll sum = 0;
    int ns = s.size();

    for(int i=0; i<ns; i++)
    {

```

```

        sum = add(((ll)sum*base)%mod, s[i], mod);
        prefhash[i]=sum;
    }
}

void r_prefhashcalc(string& s, ll base, ll mod, int*prefhash)
{
    ll sum = 0;
    int ns = s.size();
    prefhash[ns]=0;

    for(int i=ns-1; i>=0; i--)
    {
        sum = add((sum*base)%mod, s[i], mod);
        prefhash[i]=sum;
    }
}

int f_strhash(string& s, int base, int mod)
{
    ll sum = 0;
    int ns = s.size();

    for(int i=0; i<ns; i++)
    {
        sum = add(((ll)sum*base)%mod, s[i], mod);
    }
    return sum;
}

int r_strhash(string& s, ll base, ll mod)
{
    ll sum = 0;
    int ns = s.size();

    for(int i=ns-1; i>=0; i--)
    {
        sum = add((sum*base)%mod, s[i], mod);
    }
    return sum;
}

void powhashfill(int base, int mod, int*powhash)
{
    for(int i=0; i<1000000 + 10; i++)

```

```

{
    if(i==0)
    {
        powhash[0]=1;
        continue;
    }

    powhash[i] = multp(powhash[i-1],base,mod);
}

int f_substrhash(int l,int r,ll mod,int*prefhash,int*powhash)
{
    ll x = subtract( prefhash[r], multp(prefhash[l-1],powhash
        [r-l+1],mod), mod );

    return x;
}

```

```

}
int r_substrhash(int l,int r,ll mod,int*prefhash,int*powhash)
{
    ll x = subtract( prefhash[l], multp(prefhash[r+1],powhash
        [r-l+1],mod), mod );

    return x;
}

```

---

### 1.6.4 Z-Function [MB]

---

```

#include<bits/stdc++.h>

/*
tested by ac

```

submission: <https://codeforces.com/contest/432/submission/145953901>  
 problem: <https://codeforces.com/contest/432/problem/D>

```

*/
std::vector<int> z_function(const std::string &s)
{
    int n = (int)s.size();
    std::vector<int> z(n, 0);
    for (int i = 1, l = 0, r = 0; i < n; i++)
    {
        if (i <= r)
            z[i] = std::min(r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            z[i]++;
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1;
    }
    return z;
}

```

---