# Team Notebook

# $NSU\_ACDodgers$

# July 28, 2022

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#### 1 -Starters-

# 1.1 C++ Include GNU PBDS [NK]

# 1.2 C++ Starter debug[MB]

```
#include <bits/stdc++.h>
using namespace std;
template <typename T, typename C = typename T::value_type>
typename enable_if<!is_same<T, string>::value, ostream &>::
    type operator << (ostream &out, const T &c)
for (auto it = c.begin(); it != c.end(); it++)
 out << (it == c.begin() ? "{" : ",") << *it;
return out << (c.emptv() ? "{" : "") << "}":
template <typename T, typename S>
ostream &operator<<(ostream &out, const pair<T, S> &p)
return out << "{" << p.first << ", " << p.second << "}";</pre>
#define dbg(...) _dbg_print(#__VA_ARGS__, __VA_ARGS__);
template <typename Arg1>
void _dbg_print(const char *name, Arg1 &&arg1)
if (name[0] == ' ')
cout << "[" << name << ": " << arg1 << "]"
 << "\n":
```

# tree\_order\_statistics\_node\_update3 C++ Starter [MB]

```
#if defined LOCAL && !defined ONLINE JUDGE
#include "debug.cpp"
#else
#include <bits/stdc++.h>
using namespace std;
#define dbg(...);
#endif
typedef long long 11;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;
#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)(x).size())
#define vec vector
inline bool read(auto &...a) { return (((cin >> a) ? true :
    false) && ...); }
inline void print(const auto &...a) { ((cout << a), ...); }</pre>
inline void println(const auto &...a) { print(a..., '\n'); }
void run_case([[maybe_unused]] const int &TC)
int main()
ios base::svnc with stdio(false), cin.tie(0):
int tt = 1:
read(tt):
```

```
for (int tc = 1; tc <= tt; tc++)
  run_case(tc);

return 0;
}</pre>
```

#### 1.4 C++ Starter [NK]

```
#include <bits/stdc++.h>
using namespace std;
constexpr double eps = 1e-9:
constexpr int inf = 1 << 30:</pre>
constexpr int mod = 1e9 + 7;
constexpr int nmax = 1e6;
void runcase(int casen) {
   // cout << "Case " << casen << ": " << '\n':
int main() {
   ios_base::sync_with_stdio(false);
   cin.tie(nullptr);
   int ncases = 1;
   cin >> ncases; // Comment out for single-case tests
   for (int casen = 1: casen <= ncases: ++casen) {</pre>
       runcase(casen):
   return 0;
```

# 1.5 C++ Starter [SK]

```
#include<bits/stdc++.h>
using namespace std;

typedef long long ll;
typedef unsigned long long ull;
#define endl "\n"
#define pi 3.142
const double eps = 1e-10;
int dx[] = {1,0,-1,0};
int dy[] = {0,1,0,-1};
```

```
const ll M = (ll)(le9) + 7;
const ll inf = (ll)le17;
const int N = (ll)(le6 + 10);

int main()
{
    cin.tie(0);
    cout.tie(0);
    ios_base::sync_with_stdio(false);
    //freopen("two.in", "r", stdin);
    //freopen("out.txt", "w", stdout);
}
//*
*/
```

# 1.6 Unordered Map [MB]

```
#include <bits/stdc++.h>

// For gp_hash_table
#include <ext/pb_ds/assoc_container.hpp>
using namespace __gnu_pbds;
using namespace std;

struct custom_hash
{
    static uint64_t splitmix64(uint64_t x)
    {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
    return x ^ (x >> 31);
}

size_t operator()(uint64_t x) const
{
```

# 2 Algebra

# 2.1 Combinatrics [MB]

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
const int N = 1e6, MOD = 998244353;
struct Combinatrics
vector<ll> fact, fact_inv, inv;
ll mod, nl;
Combinatrics() {}
Combinatrics(ll n, ll mod)
 this \rightarrow nl = n;
 this->mod = mod;
 fact.resize(n + 1, 1), fact_inv.resize(n + 1, 1), inv.
      resize(n + 1, 1);
 init():
void init()
 fact[0] = 1;
 for (int i = 1; i <= nl; i++)</pre>
  fact[i] = (fact[i - 1] * i) % mod;
```

```
inv[0] = inv[1] = 1:
 for (int i = 2; i <= nl; i++)</pre>
 inv[i] = inv[mod % i] * (mod - mod / i) % mod:
 fact inv[0] = fact inv[1] = 1:
for (int i = 2; i <= nl; i++)</pre>
 fact_inv[i] = (inv[i] * fact_inv[i - 1]) % mod;
ll ncr(ll n. ll r)
if (n < r)
 return 0;
if (n > n1)
 return ncr(n, r, mod);
return (((fact[n] * 1LL * fact_inv[r]) % mod) * 1LL *
     fact inv[n - r]) % mod:
ll npr(ll n, ll r)
if (n < r)
 return 0;
if (n > n1)
 return npr(n, r, mod);
return (fact[n] * 1LL * fact_inv[n - r]) % mod;
11 big_mod(l1 a, l1 p, l1 m = -1)
m = (m == -1 ? mod : m);
ll res = 1 \% m, x = a \% m;
 res = ((p \& 1) ? ((res * x) % m) : res), x = ((x * x) % m)
      ), p >>= 1;
return res;
ll mod_inv(ll a, ll p)
return big_mod(a, p - 2, p);
```

## 2.2 Extended GCD [NK]

```
template <class Z>
constexpr Z extended_gcd(Z a, Z b, Z& x_ref, Z& y_ref) {
    x_ref = 1, y_ref = 0;
    Z x1 = 0, y1 = 1, tmp = 0, q = 0;
    while (b > 0) {
        q = a / b;
        tmp = a, a = b, b = tmp - (q * b);
        tmp = x_ref, x_ref = x1, x1 = tmp - (q * x1);
        tmp = y_ref, y_ref = y1, y1 = tmp - (q * y1);
    }
    return a;
}
```

# 2.3 Fraction-Functions [SK]

```
pair<11,11> frac_add(pair<11,11> a,pair<11,11> b)
{
    ll g = a.second*b.second;
    pair<11,11> x;
    x.second = g;
    x.first = a.first * (b.second) + b.first * (a.second);
    ll y = __gcd(x.first,x.second);
    x.first/=y;
```

```
x.second/=y;
return x;
}
pair<ll,ll> frac_mult(pair<ll,ll> a,pair<ll,ll> b)
{
   pair<ll,ll> x;

   x.first = a.first * b.first;
   x.second = a.second * b.second;
   ll y = __gcd(x.first,x.second);
   x.first/=y;
   x.second/=y;
   return x;
}
```

# 2.4 Fraction[MB]

```
struct Fraction {
   int p, q;

Fraction (int _p, int _q) : p(_p), q(_q) {
   }

std::strong_ordering operator<=> (const Fraction &oth)
        const {
      return p * oth.q <=> q * oth.p;
   }
};
```

# 2.5 Miller-Rabin-for-prime-checking [SK]

```
typedef long long ll;

ll mulmod(ll a, ll b, ll c) {
    ll x = 0, y = a % c;
    while (b) {
        if (b & 1) x = (x + y) % c;
        y = (y << 1) % c;
        b >>= 1;
    }
    return x % c;
}

ll fastPow(ll x, ll n, ll MOD) {
    ll ret = 1;
    while (n) {
```

```
if (n & 1) ret = mulmod(ret, x, MOD);
   x = mulmod(x, x, MOD);
   n >>= 1:
 return ret;
bool isPrime(ll n) {
 11 d = n - 1;
 int s = 0;
 while (d % 2 == 0) {
   s++;
   d >>= 1;
 // It's guranteed that these values will work for any
      number smaller than 3*10**18 (3 and 18 zeros)
 int a[9] = { 2, 3, 5, 7, 11, 13, 17, 19, 23 };
 for(int i = 0: i < 9: i++) {</pre>
   bool comp = fastPow(a[i], d, n) != 1;
   if(comp) for(int j = 0; j < s; j++) {</pre>
     ll fp = fastPow(a[i], (1LL << (ll)j)*d, n);
     if (fp == n - 1) {
       comp = false;
       break;
   if(comp) return false;
 return true:
```

# 2.6 Modular Binary Exponentiation (Power) [NK]

```
template <class B, class E, class M>
constexpr B power(B base, E expo, M mod = 0) {
   assert(expo >= 0);
   if (mod == 1) return 0;
   if (base == 0 || base == 1) return base;
   B res = 1;
   if (!mod) {
     while (expo) {
        if (expo & 1) res *= base;
        base *= base;
        expo >>= 1;
     }
  } else {
```

```
assert(mod > 0):
   base %= mod:
   if (base <= 1) return base:</pre>
   while (expo) {
       if (expo & 1) res = (res * base) % mod;
       base = (base * base) % mod:
       expo >>= 1;
return res;
```

# Modular Int [MB]

```
#include <bits/stdc++.h>
// Tested By Ac
// submission : https://atcoder.jp/contests/abc238/
    submissions/29247261
// problem : https://atcoder.jp/contests/abc238/tasks/
    abc238 c
template <const int MOD>
struct ModInt
 int val;
 ModInt() { val = 0; }
ModInt(long long v) { v += (v < 0 ? MOD : 0), val = (int)(v | 2.8 Modular inverse [NK]
      % MOD): }
 ModInt &operator+=(const ModInt &rhs)
 val += rhs.val. val -= (val >= MOD ? MOD : 0):
 return *this:
 ModInt &operator -= (const ModInt &rhs)
 val -= rhs.val, val += (val < 0 ? MOD : 0);</pre>
 return *this:
 ModInt &operator *= (const ModInt &rhs)
 val = (int)((val * 1ULL * rhs.val) % MOD);
 return *this:
 ModInt pow(long long n) const
 ModInt x = *this, r = 1;
 while (n)
  r = ((n \& 1) ? r * x : r), x = (x * x), n >>= 1:
 return r;
```

```
ModInt inv() const { return this->pow(MOD - 2); }
ModInt &operator/=(const ModInt &rhs) { return *this = *
     this * rhs.inv(): }
friend ModInt operator+(const ModInt &lhs, const ModInt &
     rhs) { return ModInt(lhs) += rhs: }
friend ModInt operator-(const ModInt &lhs, const ModInt &
     rhs) { return ModInt(lhs) -= rhs; }
friend ModInt operator*(const ModInt &lhs, const ModInt &
     rhs) { return ModInt(lhs) *= rhs; }
friend ModInt operator/(const ModInt &lhs. const ModInt &
     rhs) { return ModInt(lhs) /= rhs: }
friend bool operator==(const ModInt &lhs, const ModInt &rhs
     ) { return lhs.val == rhs.val; }
friend bool operator!=(const ModInt &lhs, const ModInt &rhs
     ) { return lhs.val != rhs.val; }
friend std::ostream &operator<<(std::ostream &out. const</pre>
     ModInt &m) { return out << m.val; }</pre>
friend std::istream &operator>>(std::istream &in. ModInt &m
     ) { return in >> m.val: }
operator int() const { return val; }
const int MOD = 1e9 + 7;
using mint = ModInt<MOD>;
```

```
template <class Z>
constexpr Z inverse(Z num, Z mod) {
   assert(mod > 1):
   if (!(0 <= num && num < mod)) {</pre>
      num %= mod:
       if (num < 0) num += mod:
   Z res = 1. tmp = 0:
   assert(extended_gcd(num, mod, res, tmp) == 1);
   if (res < 0) res += mod:
   return res:
```

# $2.9 \quad \text{nCrp-O}(1) \text{ [SK]}$

```
// array to store inverse of 1 to N
ll factorialNumInverse[N + 1]:
// array to precompute inverse of 1! to N!
```

```
11 naturalNumInverse[N + 1]:
// array to store factorial of first N numbers
11 fact[N + 1]:
// Function to precompute inverse of numbers
void InverseofNumber(11 p)
   naturalNumInverse[0] = naturalNumInverse[1] = 1:
   for (int i = 2; i <= N; i++)</pre>
      naturalNumInverse[i] = naturalNumInverse[p % i] * (p
           - p / i) % p:
// Function to precompute inverse of factorials
void InverseofFactorial(11 p)
   factorialNumInverse[0] = factorialNumInverse[1] = 1:
   // precompute inverse of natural numbers
   for (int i = 2: i <= N: i++)
      factorialNumInverse[i] = (naturalNumInverse[i] *
            factorialNumInverse[i - 1]) % p;
// Function to calculate factorial of 1 to N
void factorial(ll p)
   fact[0] = 1:
   // precompute factorials
   for (int i = 1; i <= N; i++) {</pre>
      fact[i] = (fact[i - 1] * i) % p;
// Function to return nCr % p in O(1) time
11 Binomial(11 N, 11 R, 11 p)
   // n C r = n!*inverse(r!)*inverse((n-r)!)
   ll ans = ((fact[N] * factorialNumInverse[R])
            % p * factorialNumInverse[N - R])
   return ans:
```

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# 2.10 Prime Phi Sieve [MB]

```
#include <bits/stdc++.h>
```

```
using namespace std;
typedef long long 11;
typedef pair<int, int> pii;
typedef pair<11, 11> pll;
struct PrimePhiSieve
private:
11 n;
vector<ll> primes, phi;
vector<bool> is prime:
public:
PrimePhiSieve() {}
PrimePhiSieve(11 n)
 this->n = n, is prime.resize(n + 5, true), phi.resize(n +
 phi_sieve();
void phi_sieve()
 is_prime[0] = is_prime[1] = false;
 for (ll i = 1; i <= n; i++)
  phi[i] = i:
 for (ll i = 1: i <= n: i++)
  if (is_prime[i])
   primes.push_back(i);
   phi[i] *= (i - 1), phi[i] /= i;
   for (ll i = i + i: i <= n: i += i)
    is_prime[j] = false, phi[j] /= i, phi[j] *= (i - 1);
}
ll get divisors count(int number, int divisor)
 return phi[number / divisor];
vector<pll> factorize(ll num)
 vector<pll> a;
 for (int i = 0; i < (int)primes.size() && primes[i] * 1LL</pre>
      * primes[i] <= num: i++)
```

```
if (num % primes[i] == 0)
  int cnt = 0:
  while (num % primes[i] == 0)
   cnt++, num /= primes[i];
  a.push_back({primes[i], cnt});
if (num != 1)
 a.push_back({num, 1});
return a:
11 get_phi(int n)
return phi[n];
// (n/p) * (p-1) => n- (n/p);
void segmented phi sieve(ll l. ll r)
vector<ll> current_phi(r - 1 + 1);
vector<ll> left_over_prime(r - 1 + 1);
for (ll i = l; i <= r; i++)</pre>
 current_phi[i - 1] = i, left_over_prime[i - 1] = i;
for (11 p : primes)
 11 to = ((1 + p - 1) / p) * p;
 if (to == p)
  to += p;
 for (11 i = to; i <= r; i += p)</pre>
  while (left_over_prime[i - 1] % p == 0)
   left_over_prime[i - 1] /= p;
  current_phi[i - 1] -= current_phi[i - 1] / p;
}
 for (11 i = 1; i <= r; i++)</pre>
 if (left_over_prime[i - 1] > 1)
  current_phi[i - 1] -= current_phi[i - 1] /
       left_over_prime[i - 1];
 cout << current_phi[i - 1] << endl;</pre>
```

```
ll phi_sqrt(ll n)
{
    ll res = n;

for (ll i = 1; i * i <= n; i++)
{
    if (n % i == 0)
    {
        res /= i;
        res *= (i - 1);

    while (n % i == 0)
        n /= i;
    }
}

if (n > 1)
    res /= n, res *= (n - 1);

return res;
}
};
```

#### 2.11 Prime Sieve [MB]

```
#include <bits/stdc++.h>
using namespace std;

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

struct PrimeSieve
{
  public:
    vector<int> primes;
    vector<bool> isprime;
    int n;

PrimeSieve() {}

PrimeSieve(int n)
{
    this->n = n, isprime.resize(n + 5, true), primes.clear();
    sieve();
}

void sieve()
```

```
isprime[0] = isprime[1] = false:
primes.push_back(2);
for (int i = 4: i <= n: i += 2)
 isprime[i] = false;
for (int i = 3; 1LL * i * i <= n; i += 2)
 if (isprime[i])
  for (int j = i * i; j <= n; j += 2 * i)
   isprime[j] = false;
for (int i = 3: i \le n: i += 2)
 if (isprime[i])
  primes.push_back(i);
vector<pll> factorize(ll num)
vector<pll> a:
for (int i = 0; i < (int)primes.size() && primes[i] * 1LL</pre>
     * primes[i] <= num; i++)
 if (num % primes[i] == 0)
 {
  int cnt = 0:
  while (num % primes[i] == 0)
   cnt++, num /= primes[i];
  a.push_back({primes[i], cnt});
if (num != 1)
 a.push_back({num, 1});
return a:
}
vector<ll> segemented_sieve(ll l, ll r)
vector<ll> seg_primes;
vector<bool> current_primes(r - 1 + 1, true);
for (ll p : primes)
{
 11 \text{ to = } (1 / p) * p;
 if (to < 1)
  to += p:
 if (to == p)
  to += p;
 for (ll i = to; i <= r; i += p)</pre>
  current primes[i - 1] = false:
}
```

```
for (int i = 1; i <= r; i++)
{
    if (i < 2)
        continue;
    if (current_primes[i - 1])
    {
        seg_primes.push_back(i);
    }
}
return seg_primes;
}
};</pre>
```

#### 3 Brute-force

# 3.1 Power Set [NK]

```
template <class T>
vector<vector<T>> power_set(const vector<T>& vec) {
   vector<vector<T>> res;
   list<T> buf;
   function<void(int)> recurse = [&](int i) -> void {
      if (i == vec.size()) {
        res.emplace_back(buf.begin(), buf.end());
        return;
    }
    recurse(i + 1);
    buf.push_back(vec[i]), recurse(i + 1), buf.pop_back()
    ;
};
recurse(0);
return res;
}
```

# 4 Graph

# 4.1 DSU [MB]

```
#include <bits/stdc++.h>
// 0 based
class DSU
{
```

```
std::vector<int> p. csz:
public:
DSU() {}
//0 based
DSU(int mx_size)
 //Default empty
 p.resize(mx_size, 0), csz.resize(mx_size, 0);
 init(mx size):
void init(int n)
// n = size
 for (int i = 0; i < n; i++)</pre>
 p[i] = i, csz[i] = 1;
//Return parent Recursively
int get(int x)
 if (p[x] != x)
 p[x] = get(p[x]);
 return p[x];
// Return Size
int get_comp_size(int component) { return csz[get(component
// Return if Union created Successfully or false if they
     are already in Union
bool merge(int x, int y)
 x = get(x), y = get(y);
 if (x == v)
 return false;
 if (csz[x] > csz[y])
  std::swap(x, y);
 y = [x]q
 csz[y] += csz[x];
 return true:
```

```
}
};
```

# 4.2 DSU [NK]

struct DSU {

```
int n_nodes = 0;
int n_components = 0;
vector<int> component_size;
vector<int> component_root;
DSU(int n_nodes, bool make_all_nodes = false)
   : n nodes(n nodes).
     component_root(n_nodes, -1),
     component_size(n_nodes, 0) {
   if (make_all_nodes) {
       for (int i = 0; i < n_nodes; ++i) {</pre>
           make node(i):
   }
void make node(int v) {
   if (component_root[v] == -1) {
       component_root[v] = v;
       component_size[v] = 1;
       ++n_components;
int root(int v) {
   auto res = v:
   while (component_root[res] != res) {
       res = component_root[res];
   while (v != res) {
       auto u = component_root[v];
       component_root[v] = res;
       v = u:
   }
   return res;
int connect(int u, int v) {
   u = root(u), v = root(v):
   if (u == v) return u;
   if (component_size[u] < component_size[v]) {</pre>
       swap(u, v);
```

```
component_root[v] = u;
component_size[u] += component_size[v];
--n_components;
}
};
```

# 4.3 Edge Remove CC [MB]

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
#define var(...) " [" << # VA ARGS ": " << ( VA ARGS )
    << "]
#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)x.size())
#define vec vector
#define endl "\n"
class DSU
std::vector<int> p, csz;
public:
DSU() {}
DSU(int dsz) // Max size
 //Default empty
 p.resize(dsz + 5, 0), csz.resize(dsz + 5, 0);
 init(dsz):
void init(int n)
 // n = size
 for (int i = 0; i <= n; i++)</pre>
 p[i] = i, csz[i] = 1;
//Return parent Recursively
int get(int x)
```

```
if (p[x] != x)
  p[x] = get(p[x]);
 return p[x];
// Return Size
int getSize(int x) { return csz[get(x)]; }
// Return if Union created Successfully or false if they
     are already in Union
bool merge(int x, int y)
 x = get(x), y = get(y);
 if (x == y)
  return false;
 if (csz[x] > csz[y])
  std::swap(x, y);
 p[x] = y;
 csz[v] += csz[x];
 return true;
};
void runCase([[maybe_unused]] const int &TC)
int n, m;
cin >> n >> m:
auto g = vec(n + 1, set<int>());
auto dsu = DSU(n + 1);
for (int i = 0: i < m: i++)</pre>
 int u, v;
 cin >> u >> v;
 g[u].insert(v):
 g[v].insert(u);
set<int> elligible;
for (int i = 1; i <= n; i++)
 elligible.insert(i);
```

Q

# int i = 1: int cnt = 0; while (sz(elligible)) cnt++; queue<int> q; q.push(\*elligible.begin()); elligible.erase(elligible.begin()); while (sz(q)) int fr = q.front(); q.pop(); auto v = elligible.begin(); while (v != elligible.end()) if (g[fr].find(\*v) == g[fr].end()) q.push(\*v); v = elligible.erase(v); else { v++; cout << cnt - 1 << endl; int main() ios\_base::sync\_with\_stdio(false), cin.tie(0); int t = 1: //cin >> t; for (int tc = 1; tc <= t; tc++)</pre> runCase(tc); return 0;

NSU

#### 4.4 LCA [MB]

```
struct LCA
private:
int n, lg;
std::vector<int> depth;
std::vector<std::vector<int>> up;
std::vector<std::vector<int>> g;
public:
LCA(): n(0), lg(0) {}
LCA(int _n)
 this \rightarrow n = n;
 lg = log2(n) + 2;
 depth.resize(n + 5, 0);
 up.resize(n + 5, std::vector<int>(lg, 0));
 g.resize(n + 1);
LCA(std::vector<std::vector<int>> &graph) : LCA(graph.size
     ())
 for (int i = 0; i < (int)graph.size(); i++)</pre>
  g[i] = graph[i];
 dfs(1, 0);
void dfs(int curr, int p)
 up[curr][0] = p;
 for (int next : g[curr])
  if (next == p)
   continue:
  depth[next] = depth[curr] + 1;
  up[next][0] = curr;
  for (int j = 1; j < lg; j++)</pre>
   up[next][j] = up[up[next][j - 1]][j - 1];
  dfs(next, curr);
 }
void clear_v(int a)
 g[a].clear();
```

```
void clear(int n_ = -1)
if (n == -1)
 n_{-} = ((int)(g.size())) - 1;
 for (int i = 0; i <= n_; i++)</pre>
 g[i].clear();
void add(int a, int b)
g[a].push_back(b);
int par(int a)
return up[a][0];
int get_lca(int a, int b)
if (depth[a] < depth[b])</pre>
 std::swap(a, b);
 int k = depth[a] - depth[b];
 for (int j = lg - 1; j >= 0; j--)
 if (k & (1 << j))
  a = up[a][j];
 if (a == b)
 return a;
 for (int j = lg - 1; j >= 0; j--)
 if (up[a][j] != up[b][j])
 {
  a = up[a][j];
  b = up[b][j];
return up[a][0];
int get_dist(int a, int b)
return depth[a] + depth[b] - 2 * depth[get_lca(a, b)];
```

```
}
};
```

# 4.5 Tree Rooting [MB]

#include <bits/stdc++.h>

```
using namespace std;
typedef long long 11;
const int N = 2e5 + 5;
vector<int> g[N];
11 sz[N], dist[N], sum[N];
void dfs(int s, int p)
 sz[s] = 1;
 dist[s] = 0;
 for (int nxt : g[s])
 if (nxt == p)
  continue:
 dfs(nxt, s);
 sz[s] += sz[nxt];
 dist[s] += (dist[nxt] + sz[nxt]);
void dfs1(int s, int p)
 if (p != 0)
 11 mv_size = sz[s];
 11 my_contrib = (dist[s] + sz[s]);
 sum[s] = sum[p] - my\_contrib + sz[1] - sz[s] + dist[s];
 for (int nxt : g[s])
 if (nxt == p)
  continue;
 dfs1(nxt, s):
// problem link: https://cses.fi/problemset/task/1133
```

```
int main()
{
   int n;
   cin >> n;

for (int i = 1, u, v; i < n; i++)
   cin >> v >> v, g[u].push_back(v), g[v].push_back(u);

dfs(1, 0);

sum[1] = dist[1];

dfs1(1, 0);

for (int i = 1; i <= n; i++)
   cout << sum[i] << " ";
   cout << endl;

return 0;
}</pre>
```

# 5 Range query

# 5.1 BIT [MB]

```
struct BIT
{
private:
    std::vector<long long> mArray;

public:
    BIT(int sz) // Max size of the array
{
        mArray.resize(sz + 1, 0);
}

void build(const std::vector<long long> &list)
{
    for (int i = 1; i <= list.size(); i++)
    {
        mArray[i] = list[i];
}

for (int ind = 1; ind <= mArray.size(); ind++)
{
    int ind2 = ind + (ind & -ind);
    if (ind2 <= mArray.size())</pre>
```

```
{
    mArray[ind2] += mArray[ind];
}
}
long long prefix_query(int ind)
{
    int res = 0;
    for (; ind > 0; ind -= (ind & -ind))
{
        res += mArray[ind];
}
    return res;
}
long long range_query(int from, int to)
{
    return prefix_query(to) - prefix_query(from - 1);
}

void add(int ind, long long add)
{
    for (; ind < mArray.size(); ind += (ind & -ind))
    {
        mArray[ind] += add;
    }
};</pre>
```

#### 5.2 Lazy Segment Tree [MB]

```
// **** //
if (lazy[si] != lazyE)
 T curr = lazy[si];
 lazv[si] = lazvE:
 segt[si] = lazy_to_seg(segt[si], curr, ss, se);
 if (ss != se)
  lazv[left(si)] = lazv to lazv(lazv[left(si)], curr);
  lazv[right(si)] = lazv to lazv(lazv[right(si)], curr);
if (se < qs || qe < ss)
 return neutral:
if (as <= ss && ae >= se)
 return segt[si]:
int mid = midpoint(ss, se);
return op(query(ss, mid, left(si), qs, qe), query(mid + 1,
      se, right(si), qs, qe));
void update(int ss. int se. int si. int gs. int ge. F val)
// **** //
if (lazy[si] != lazyE)
 F curr = lazy[si];
 lazy[si] = lazyE;
 segt[si] = lazy_to_seg(segt[si], curr, ss, se);
 if (ss != se)
  lazy[left(si)] = lazy_to_lazy(lazy[left(si)], curr);
  lazy[right(si)] = lazy_to_lazy(lazy[right(si)], curr);
if (se < qs || qe < ss)
 return;
if (qs <= ss && qe >= se)
 // **** //
```

```
segt[si] = lazy_to_seg(segt[si], val, ss, se);
  if (ss != se)
   lazy[left(si)] = lazy_to_lazy(lazy[left(si)], val);
   lazv[right(si)] = lazv to lazv(lazv[right(si)], val);
 return;
 int mid = midpoint(ss. se);
 update(mid + 1, se, si * 2 + 1, qs, qe, val);
 update(ss, mid, left(si), qs, qe, val);
 segt[si] = op(segt[left(si)], segt[right(si)]);
public:
LazvSegTree() : n(0) {}
LazySegTree(int sz, T ini, T _neutral, F _lazyE)
 this \rightarrow n = sz + 1:
 this->neutral = _neutral;
 this->lazyE = _lazyE;
 segt.resize(n * 4 + 5, ini);
 lazv.resize(n * 4 + 5, lazvE):
LazySegTree(const std::vector<T> &arr, T ini, T _neutral, F
      _lazyE) : LazySegTree((int)arr.size(), ini, _neutral,
     _lazyE)
init(arr):
void init(const std::vector<T> &arr)
 this->n = (int)arr.size():
 for (int i = 0: i < n: i++)
 set(i, i, arr[i]);
T get(int qs, int qe)
return query(0, n - 1, 1, qs, qe);
void set(int from, int to, F val)
```

```
{
  update(0, n - 1, 1, from, to, val);
};

int op(int a, int b)
{
  return a + b;
}

int lazy_to_seg(int seg, int lazy_v, int 1, int r)
{
  return seg + (lazy_v * (r - 1 + 1));
}

int lazy_to_lazy(int curr_lazy, int input_lazy)
{
  return curr_lazy + input_lazy;
}
```

# 5.3 Lazy Segment Tree [SK]

```
11 v[4*N];
11 add[4*N];
int arr[N];

void push(int cur)
{
    add[cur*2] += add[cur];
    add[cur*2 + 1] += add[cur];
    add[cur] = 0;
}

/*

void build(int cur,int l,int r)
{
    if(l==r)
    {
        v[cur] = arr[1];
        return;
    }

    int mid = 1 + (r-1)/2;

    build(cur*2,1,mid);
    build(cur*2 + 1,mid+1,r);

    v[cur] = v[cur*2] + v[cur*2 + 1];
```

```
return:
}
*/
11 query(int cur,int l,int r,int x,int y)
    if(x>r || y<1)</pre>
       return 0;
    if(l==r)
       return v[cur] + add[cur];
    if(l==x && r==y)
       return v[cur] + add[cur]*(r-l+1);
    int mid = 1 + (r-1)/2;
    v[cur] += add[cur]*(r-l+1);
    push(cur);
    11 left = query(cur*2,1,mid,x,min(mid,y));
    ll right = query(cur*2 + 1, mid+1, r, max(mid+1, x), y);
   11 \text{ res} = 0;
    res = left + right ;
    return res:
void update(int cur.int l.int r.int s.int e.int val)
    if(l==s && r==e)
        add[cur] += val;
       return;
    if(s>r || e<1)
       return;
```

```
int mid = 1 + (r-1)/2;
push(cur);

update(cur*2,1,mid,s,min(e,mid),val);
update(cur*2 + 1,mid+1,r,max(s,mid+1),e,val);

v[cur] = (v[cur*2] + add[cur*2]*(mid-1+1)) + (v[cur*2 + 1] + add[cur*2 + 1]*(r-mid));

return;
```

# 5.4 Mos Algorithm [MB]

```
#include <bits/stdc++.h>
using namespace std;
const int N = 3e4 + 5;
const int blck = sqrt(N) + 1;
struct Query
int 1, r, i;
bool operator<(const Query q) const</pre>
 if (this->1 / blck == q.1 / blck)
 return this->r < q.r;</pre>
 return this->1 / blck < q.1 / blck;</pre>
vector<int> mos_alogorithm(vector<Query> &queries, vector<</pre>
    int> &a)
vector<int> answers(queries.size());
sort(queries.begin(), queries.end());
int sza = 1e6 + 5;
vector<int> freq(sza);
int cnt = 0:
auto add = [&](int x) -> void
 freq[x]++;
```

```
if (freq[x] == 1)
  cnt++;
auto remove = [&](int x) -> void
 freq[x]--;
 if (freq[x] == 0)
  cnt--;
int 1 = 0;
int r = -1;
for (Query q : queries)
 while (1 > q.1)
 1--;
  add(a[1]):
 while (r < q.r)</pre>
  r++;
  add(a[r]);
 while (1 < q.1)
  remove(a[1]):
  1++;
 while (r > q.r)
  remove(a[r]):
  r--;
 answers[q.i] = cnt;
return answers;
int main()
int n:
cin >> n;
vector<int> a(n):
for (int i = 0; i < n; i++)</pre>
 cin >> a[i]:
int q;
```

```
cin >> q;
vector<Query> qr(q);
for (int i = 0; i < q; i++)
{
  int l, r;
  cin >> l >> r;

l--, r--;
  qr[i].l = l, qr[i].r = r, qr[i].i = i;
}
vector<int> res = mos_alogorithm(qr, a);
for (int i = 0; i < q; i++)
  cout << res[i] << endl;
return 0;
}</pre>
```

# 5.5 Segment Tree [MB]

# 5.6 Segment Tree [SK]

```
pair<int,int>v[4*N];
int arr[N];

void build(int cur,int 1,int r)
{
    if(1==r)
    {
        pair<int,int> tmp = {0,0};
        if(arr[1]==0)
        {
            tmp.second++;
        }
        else if(arr[1]<0)
        {
            tmp.first++;
        }
        v[cur] = tmp;
        return;
    }

int mid = 1 + (r-1)/2;</pre>
```

```
build(cur*2,1,mid);
   build(cur*2 + 1,mid+1,r);
   v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
   v[cur].second = v[cur*2].second + v[cur*2 + 1].second:
pair<int,int>query(int cur,int l,int r,int x,int y)
   if(1==x && r==v)
       return v[cur];
   if(x>r || y<1)
       return {-1,-1}:
   int mid = 1 + (r-1)/2;
   pair<int,int> left = query(cur*2,1,mid,x,min(mid,y));
   pair<int,int> right = query(cur*2 + 1,mid+1,r,max(mid+1,x)
        ),y);
   pair < int, int > res = \{0,0\};
   res.first = ((left.first!=-1)?left.first:0) + ((right.
        first!=-1)?right.first:0):
   res.second = ((left.second!=-1)?left.second:0) + ((right.
        second!=-1)?right.second:0):
   return res;
void update(int cur.int l.int r.int pos.int val)
   if(1==r)
       arr[1] = val:
       pair<int,int> tmp = {0,0};
      if(arr[1]==0)
          tmp.second++;
       else if(arr[1]<0)
          tmp.first++;
       v[cur] = tmp;
```

```
return;
}
int mid = 1 + (r-1)/2;
if(pos<=mid)
{
    update(cur*2,1,mid,pos,val);
}
else
{
    update(cur*2 + 1,mid+1,r,pos,val);
}

v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
v[cur].second = v[cur*2].second + v[cur*2 + 1].second;
return;
}</pre>
```

# 5.7 Sparse Table [MB]

# 6 String

# 6.1 Hashing [MB]

```
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
const int PRIMES[] = \{2147462393, 2147462419, 2147462587, \dots \}
    2147462633, 2147462747, 2147463167, 2147463203,
    2147463569, 2147463727, 2147463863, 2147464211,
    2147464549, 2147464751, 2147465153, 2147465563,
    2147465599, 2147465743, 2147465953, 2147466457,
    2147466463, 2147466521, 2147466721, 2147467009,
    2147467057, 2147467067, 2147467261, 2147467379,
    2147467463, 2147467669, 2147467747, 2147468003,
    2147468317, 2147468591, 2147468651, 2147468779,
    2147468801, 2147469017, 2147469041, 2147469173,
    2147469229, 2147469593, 2147469881, 2147469983,
    2147470027, 2147470081, 2147470177, 2147470673,
    2147470823, 2147471057, 2147471327, 2147471581,
```

```
2147472137, 2147472161, 2147472689, 2147472697,
     2147472863, 2147473151, 2147473369, 2147473733,
    2147473891, 2147473963, 2147474279, 2147474921,
    2147474929, 2147475107, 2147475221, 2147475347,
    2147475397, 2147475971, 2147476739, 2147476769,
    2147476789, 2147476927, 2147477063, 2147477107,
     2147477249, 2147477807, 2147477933, 2147478017,
     2147478521}:
// ll base_pow,base_pow_1;
ll base1 = 43, base2 = 47, mod1 = 1e9 + 7, mod2 = 1e9 + 9;
// **** Enable this function for codeforces
void generateRandomBM()
 unsigned int seed = chrono::system_clock::now().
     time since epoch().count():
 srand(seed); /// to avoid getting hacked in CF, comment
     this line for easier debugging
 int q_len = (sizeof(PRIMES) / sizeof(PRIMES[0])) / 4;
 base1 = PRIMES[rand() % q_len];
 mod1 = PRIMES[rand() % q_len + q_len];
 base2 = PRIMES[rand() % q_len + 2 * q_len];
mod2 = PRIMES[rand() % q_len + 3 * q_len];
struct Hash
public:
vector<int> base_pow, f_hash, r_hash;
11 base, mod;
 Hash() {}
 // Update it make it more dynamic like segTree class and
 Hash(int mxSize, ll base, ll mod) // Max size
 this->base = base;
 this->mod = mod:
 base_pow.resize(mxSize + 2, 1), f_hash.resize(mxSize + 2,
      0), r_hash.resize(mxSize + 2, 0);
 for (int i = 1; i <= mxSize; i++)</pre>
  base_pow[i] = base_pow[i - 1] * base % mod;
 void init(string s)
```

```
int n = s.size():
 for (int i = 1: i <= n: i++)
  f \cdot hash[i] = (f \cdot hash[i - 1] * base + int(s[i - 1])) % mod:
 for (int i = n; i >= 1; i--)
  r hash[i] = (r hash[i + 1] * base + int(s[i - 1])) % mod:
}
int forward hash(int 1. int r)
 int h = f hash[r + 1] - (1LL * base pow[r - 1 + 1] *
      f_hash[1]) % mod;
 return h < 0? mod + h: h:
}
int reverse hash(int 1, int r)
 int h = r_hash[l + 1] - (1LL * base_pow[r - l + 1] *
      r_hash[r + 2]) \% mod;
 return h < 0? mod + h : h;
class DHash
public:
Hash sh1, sh2:
DHash() {}
DHash(int mx size)
 sh1 = Hash(mx_size, base1, mod1);
 sh2 = Hash(mx_size, base2, mod2);
void init(string s)
 sh1.init(s);
 sh2.init(s);
ll forward hash(int 1, int r)
```

## 6.2 Hashing [NK]

```
namespace roll_hash_util {
   constexpr int MaxDim = 4:
   constexpr array<int, MaxDim> primes = {257, 263, 269,
   constexpr array<int, MaxDim> primes_minus1e9 = {7, 9, 21,
   constexpr int modulus(int dim) { return primes_minus1e9[
        dim] + 1e9; }
   array<vector<int>, MaxDim> p_pow = {};
   void resize(int n) {
       for (int d = 0: d < MaxDim: ++d) {
          auto& pp = p_pow[d];
          if (pp.empty()) {
              pp.push_back(1);
          while (pp.size() < n) {</pre>
              pp.push_back(((long long)pp.back() * primes[d
                   1) % modulus(d));
      }
} // namespace roll_hash_util
template <int Dim = 2>
class Rolling_hash {
private:
   size_t len_;
   array<vector<int>, Dim> pref_hash_;
   array<vector<int>, Dim> suff_hash_;
public:
   template <class InputIter>
   Rolling_hash(InputIter first, InputIter last, bool bidir
        = false) {
       len_ = distance(first, last);
       roll_hash_util::resize(len_);
```

```
for (int d = 0: d < Dim: ++d) {
       vector<int>& ph = pref_hash_[d];
       const int m = roll_hash_util::modulus(d);
       const long long p = roll_hash_util::primes[d];
       ph.resize(len + 1):
       ph[0] = 0;
       auto it = first;
       for (int i = 0; i < len_; ++i) {</pre>
          ph[i + 1] = (((ph[i] * p) % m) + *it) % m;
          ++it:
       }
   }
   if (!bidir) return:
   for (int d = 0: d < Dim: ++d) {</pre>
       vector<int>& sh = suff hash [d]:
       const int m = roll hash util::modulus(d):
       const long long p = roll_hash_util::primes[d];
       sh.resize(len_ + 1);
       sh[len_] = 0;
       auto it = prev(last);
       for (int i = len_; i > 0; --i) {
          sh[i - 1] = ((sh[i] * p) % m + *it) % m;
          --it;
       }
   }
array<int, Dim> get(size_t i, size_t n) const {
   array<int, Dim> res;
   for (int d = 0: d < Dim: ++d) {
       const vector<int>& ph = pref_hash_[d];
       const int m = roll hash util::modulus(d):
       const long long pp = roll_hash_util::p_pow[d][n];
       res[d] = ((ph[i + n] - (ph[i] * pp) % m) % m + m)
            % m;
   }
   return res:
array<int, Dim> getrev(size_t i, size_t n) const {
   assert(!suff_hash_[0].empty());
   array<int, Dim> res;
   for (int d = 0: d < Dim: ++d) {
       const vector<int>& sh = suff_hash_[d];
       const int m = roll hash util::modulus(d):
       const long long pp = roll_hash_util::p_pow[d][n];
```

```
res[d] = ((sh[i] - (sh[i + n] * pp) % m) % m + m)
      }
       return res:
   }
   size_t size() const { return len_; }
   array<int, Dim> pref(size_t i) const {
       array<int, Dim> res;
       for (int d = 0: d < Dim: ++d) {
          res[d] = pref hash [d][i]:
      }
       return res;
   }
   arrav<int, Dim> suff(size t i) const {
       array<int, Dim> res;
       for (int d = 0: d < Dim: ++d) {</pre>
           res[d] = suff hash [d][i]:
       return res;
   }
};
```

# 6.3 Hashing [SK]

```
int powhash1[ 1000000+ 10]= {};
int powhash2[ 1000000+ 10]= {};
int f_prefhash1[1000000+ 10];
int f_prefhash2[1000000+ 10];
int r_prefhash1[1000000+ 10];
int r_prefhash2[1000000+ 10];
int add(11 x,11 y,11 mod)
{
    return (x+y>=mod)?(x+y-mod):(x+y);
}
int subtract(11 x,11 y,11 mod)
{
    return (x-y<0)?(x-y+mod):(x-y);
}
int multp(11 x,11 y,11 mod)
{
    return (x*y)%mod;
}</pre>
```

```
const int BASE1 = 125:
const int MOD1 = 1e9 + 9:
const int BASE2 = 250:
const int MOD2 = 1e9 + 7;
void f_prefhashcalc(string& s,int base,int mod,int*prefhash)
   11 sum = 0:
   int ns = s.size();
   for(int i=0: i<ns: i++)</pre>
   {
       sum = add(((11)sum*base)%mod.s[i].mod):
       prefhash[i]=sum;
void r prefhashcalc(string& s.ll base.ll mod.int*prefhash)
   11 sum = 0;
   int ns = s.size():
   prefhash[ns]=0;
   for(int i=ns-1; i>=0; i--)
       sum = add((sum*base)%mod.s[i].mod):
       prefhash[i]=sum;
int f_strhash(string& s,int base,int mod)
   11 \text{ sum} = 0:
   int ns = s.size();
   for(int i=0: i<ns: i++)</pre>
       sum = add(((11)sum*base)%mod,s[i],mod);
   return sum:
int r_strhash(string& s,ll base,ll mod)
   11 sum = 0:
   int ns = s.size();
```

15

```
for(int i=ns-1; i>=0; i--)
{
    sum = add((sum*base)%mod,s[i],mod);
}
return sum;
}

void powhashfill(int base,int mod,int*powhash)
{
    for(int i=0; i<1000000 + 10; i++)
    {
        if(i==0)
        {
            powhash[0]=1;
            continue;
        }
        powhash[i] = multp(powhash[i-1],base,mod);
}</pre>
```

# 6.4 Z-Function [MB]

```
#include<bits/stdc++.h>

/*
    tested by ac
    submission: https://codeforces.com/contest/432/submission
    /145953901
    problem: https://codeforces.com/contest/432/problem/D
    */
    std::vector<int> z_function(const std::string &s)
{
      int n = (int)s.size();
      std::vector<int> z(n, 0);
      for (int i = 1, 1 = 0, r = 0; i < n; i++)
      {
       if (i <= r)
          z[i] = std::min(r - i + 1, z[i - 1]);
      while (i + z[i] < n && s[z[i]] == s[i + z[i]])
          z[i]++;
      if (i + z[i] - 1 > r)
          1 = i, r = i + z[i] - 1;
    }
    return z;
}
```