

# Team Notebook

NSU\_ACDodgers

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## Contents

### 1 -Starters-

1.1 C++ Include GNU PBDS [NK]	2
1.2 C++ Starter debug[MB]	2
1.3 C++ Starter [MB]	2
1.4 C++ Starter [NK]	2
1.5 C++ Starter [SK]	2
1.6 Unordered Map [MB]	3

### 2 Algebra

2.1 Combinatrics [MB]	3
2.2 Extended GCD [NK]	4
2.3 Fraction-Functions [SK]	4
2.4 Fraction[MB]	4
2.5 Miller-Rabin-for-prime-checking [SK]	4

### 2

2.6 Modular Binary Exponentiation (Power) [NK]	4
2.7 Modular Int [MB]	5
2.8 Modular inverse [NK]	5
2.9 nCrp-O(1) [SK]	5
2.10 Prime Phi Sieve [MB]	5
2.11 Prime Sieve [MB]	6

### 3 Brute-force

3.1 Power Set [NK]	7
--------------------	---

### 4 Graph

4.1 DSU [MB]	7
4.2 DSU [NK]	8
4.3 Edge Remove CC [MB]	8
4.4 LCA [MB]	9
4.5 Tree Rooting [MB]	10

### 5 Range query

5.1 BIT [MB]	10
5.2 Lazy Segment Tree [MB]	10
5.3 Lazy Segment Tree [SK]	11
5.4 Mos Algorithm [MB]	12
5.5 Segment Tree [MB]	13
5.6 Segment Tree [SK]	13
5.7 Sparse Table [MB]	13

### 6 String

6.1 Hashing [MB]	13
6.2 Hashing [NK]	14
6.3 Hashing [SK]	15
6.4 Z-Function [MB]	16

### 10

### 13

# 1 -Starters-

## 1.1 C++ Include GNU PBDS [NK]

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
namespace pbds = __gnu_pbds;

template <class T>
using ordered_set = pbds::tree<T, pbds::null_type, std::less<T>,
                                pbds::rb_tree_tag,
                                pbds::tree_order_statistics_node_update>;

template <class K, class V>
using hash_map = pbds::gp_hash_table<K, V>;
```

## 1.2 C++ Starter debug[MB]

```
#include <bits/stdc++.h>

using namespace std;

template <typename T, typename C = typename T::value_type>
typename enable_if<!is_same<T, string>::value, ostream &>::
    type operator<<(ostream &out, const T &c)
{
    for (auto it = c.begin(); it != c.end(); it++)
        out << (it == c.begin() ? "{ " : ", ") << *it;
    return out << (c.empty() ? "{ " : ", ") << "}";
}

template <typename T, typename S>
ostream &operator<<(ostream &out, const pair<T, S> &p)
{
    return out << "{ " << p.first << ", " << p.second << "}";
}

#define dbg(...) _dbg_print(#__VA_ARGS__, __VA_ARGS__);

template <typename Arg1>
void _dbg_print(const char *name, Arg1 &&arg1)
{
    if (name[0] == ' ')
        name++;
    cout << "[" << name << ": " << arg1 << "]"
         << "\n";
}
```

```
}

template <typename Arg1, typename... Args>
void _dbg_print(const char *names, Arg1 &&arg1, Args &&...
               args)
{
    const char *comma = strchr(names + 1, ',');
    cout << "[";
    cout.write(names, comma - names) << ": " << arg1 << "] ";
    _dbg_print(comma + 1, args...);
}
```

## 1.3 C++ Starter [MB]

```
#if defined LOCAL && !defined ONLINE_JUDGE
#include "debug.cpp"
#else
#include <bits/stdc++.h>
using namespace std;
#define dbg(...) ;
#endif

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)(x).size())
#define vec vector

inline bool read(auto &...a) { return (((cin >> a) ? true :
false) && ...); }

inline void print(const auto &...a) { ((cout << a), ...); }
inline void println(const auto &...a) { print(a..., '\n'); }

void run_case([[maybe_unused]] const int &TC)
{
}

int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);

    int tt = 1;
    read(tt);
}
```

```
for (int tc = 1; tc <= tt; tc++)
    run_case(tc);

return 0;
}
```

## 1.4 C++ Starter [NK]

```
#include <bits/stdc++.h>
using namespace std;

constexpr double eps = 1e-9;
constexpr int inf = 1 << 30;
constexpr int mod = 1e9 + 7;
constexpr int nmax = 1e6;

void runcase(int casen) {
    // cout << "Case " << casen << ": " << '\n';
}

int main() {
    ios_base::sync_with_stdio(false);
    cin.tie(nullptr);

    int ncases = 1;
    cin >> ncases; // Comment out for single-case tests
    for (int casen = 1; casen <= ncases; ++casen) {
        runcase(casen);
    }

    return 0;
}
```

## 1.5 C++ Starter [SK]

```
#include <bits/stdc++.h>
using namespace std;

typedef long long ll;
typedef unsigned long long ull;
#define endl "\n"
#define pi 3.142
const double eps = 1e-10;
int dx[] = {1,0,-1,0};
int dy[] = {0,1,0,-1};
```

```

const ll M = (1ll)(1e9) + 7;
const ll inf = (1ll)1e17;
const int N = (1ll)(1e6 + 10);

int main()
{
    cin.tie(0);
    cout.tie(0);
    ios_base::sync_with_stdio(false);

    //freopen("two.in", "r", stdin);
    //freopen("out.txt", "w", stdout);

```

```

}

/*

*/

```

## 1.6 Unordered Map [MB]

```

#include <bits/stdc++.h>

// For gp_hash_table
#include <ext/pb_ds/assoc_container.hpp>

using namespace __gnu_pbds;

using namespace std;

struct custom_hash
{
    static uint64_t splitmix64(uint64_t x)
    {
        // http://xorshift.di.unimi.it/splitmix64.c
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }

    size_t operator()(uint64_t x) const
    {

```

```

        static const uint64_t FIXED_RANDOM = chrono::steady_clock
            ::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};

// Example Use
unordered_map<int, int, custom_hash> mp;

// Faster
gp_hash_table<int, int, custom_hash> mp;

```

## 2 Algebra

### 2.1 Combinatrics [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

const int N = 1e6, MOD = 998244353;

struct Combinatrics
{
    vector<ll> fact, fact_inv, inv;
    ll mod, nl;

    Combinatrics() {}

    Combinatrics(ll n, ll mod)
    {
        this->nl = n;
        this->mod = mod;
        fact.resize(n + 1, 1), fact_inv.resize(n + 1, 1), inv.
            resize(n + 1, 1);
        init();
    }

    void init()
    {
        fact[0] = 1;

        for (int i = 1; i <= nl; i++)
        {
            fact[i] = (fact[i - 1] * i) % mod;
        }
    }

```

```

    inv[0] = inv[1] = 1;
    for (int i = 2; i <= nl; i++)
        inv[i] = inv[mod % i] * (mod - mod / i) % mod;

    fact_inv[0] = fact_inv[1] = 1;

    for (int i = 2; i <= nl; i++)
        fact_inv[i] = (inv[i] * fact_inv[i - 1]) % mod;
}

ll ncr(ll n, ll r)
{
    if (n < r)
    {
        return 0;
    }

    if (n > nl)
        return ncr(n, r, mod);
    return (((fact[n] * 1LL * fact_inv[r]) % mod) * 1LL *
        fact_inv[n - r]) % mod;
}

ll npr(ll n, ll r)
{
    if (n < r)
    {
        return 0;
    }

    if (n > nl)
        return npr(n, r, mod);
    return (fact[n] * 1LL * fact_inv[n - r]) % mod;
}

ll big_mod(ll a, ll p, ll m = -1)
{
    m = (m == -1 ? mod : m);
    ll res = 1 % m, x = a % m;
    while (p > 0)
        res = ((p & 1) ? ((res * x) % m) : res), x = ((x * x) % m
            ), p >>= 1;
    return res;
}

ll mod_inv(ll a, ll p)
{
    return big_mod(a, p - 2, p);
}

```

```

11 ncr(11 n, 11 r, 11 p)
{
    if (n < r)
        return 0;
    if (r == 0)
        return 1;
    return (((fact[n] * mod_inv(fact[r], p)) % p) * mod_inv(
        fact[n - r], p)) % p;
}

11 npr(11 n, 11 r, 11 p)
{
    if (n < r)
        return 0;
    if (r == 0)
        return 1;
    return (fact[n] * mod_inv(fact[n - r], p)) % p;
}
};

```

## 2.2 Extended GCD [NK]

```

template <class Z>
constexpr Z extended_gcd(Z a, Z b, Z& x_ref, Z& y_ref) {
    x_ref = 1, y_ref = 0;
    Z x1 = 0, y1 = 1, tmp = 0, q = 0;
    while (b > 0) {
        q = a / b;
        tmp = a, a = b, b = tmp - (q * b);
        tmp = x_ref, x_ref = x1, x1 = tmp - (q * x1);
        tmp = y_ref, y_ref = y1, y1 = tmp - (q * y1);
    }
    return a;
}

```

## 2.3 Fraction-Functions [SK]

```

pair<11,11> frac_add(pair<11,11> a,pair<11,11> b)
{
    11 g = a.second*b.second;
    pair<11,11> x;
    x.second = g;
    x.first = a.first * (b.second) + b.first * (a.second);
    11 y = __gcd(x.first,x.second);
    x.first/=y;

```

```

    x.second/=y;
    return x;
}
pair<11,11> frac_mult(pair<11,11> a,pair<11,11> b)
{
    pair<11,11> x;

    x.first = a.first * b.first;
    x.second = a.second * b.second;
    11 y = __gcd(x.first,x.second);
    x.first/=y;
    x.second/=y;
    return x;
}

```

## 2.4 Fraction[MB]

```

struct Fraction {
    int p, q;

    Fraction (int _p, int _q) : p(_p), q(_q) {}

    std::strong_ordering operator<=> (const Fraction &oth)
        const {
            return p * oth.q <=> q * oth.p;
        }
};

```

## 2.5 Miller-Rabin-for-prime-checking [SK]

```

typedef long long ll;

11 mulmod(11 a, 11 b, 11 c) {
    11 x = 0, y = a % c;
    while (b) {
        if (b & 1) x = (x + y) % c;
        y = (y << 1) % c;
        b >>= 1;
    }
    return x % c;
}

11 fastPow(11 x, 11 n, 11 MOD) {
    11 ret = 1;
    while (n) {

```

```

        if (n & 1) ret = mulmod(ret, x, MOD);
        x = mulmod(x, x, MOD);
        n >>= 1;
    }
    return ret;
}

```

```

bool isPrime(11 n) {
    11 d = n - 1;
    int s = 0;
    while (d % 2 == 0) {
        s++;
        d >>= 1;
    }

```

// It's guranteed that these values will work for any number smaller than 3\*10\*\*18 (3 and 18 zeros)

```

int a[9] = { 2, 3, 5, 7, 11, 13, 17, 19, 23 };
for(int i = 0; i < 9; i++) {
    bool comp = fastPow(a[i], d, n) != 1;
    if(comp) for(int j = 0; j < s; j++) {
        11 fp = fastPow(a[i], (1LL << (11)j)*d, n);
        if (fp == n - 1) {
            comp = false;
            break;
        }
    }
    if(comp) return false;
}
return true;
}

```

## 2.6 Modular Binary Exponentiation (Power) [NK]

```

template <class B, class E, class M>
constexpr B power(B base, E expo, M mod = 0) {
    assert(expo >= 0);
    if (mod == 1) return 0;
    if (base == 0 || base == 1) return base;
    B res = 1;
    if (!mod) {
        while (expo) {
            if (expo & 1) res *= base;
            base *= base;
            expo >>= 1;
        }
    }
    else {

```

```

    assert(mod > 0);
    base %= mod;
    if (base <= 1) return base;
    while (expo) {
        if (expo & 1) res = (res * base) % mod;
        base = (base * base) % mod;
        expo >>= 1;
    }
    return res;
}

```

## 2.7 Modular Int [MB]

```

#include <bits/stdc++.h>
// Tested By Ac
// submission : https://atcoder.jp/contests/abc238/
// submissions/29247261
// problem : https://atcoder.jp/contests/abc238/tasks/
// abc238_c

template <const int MOD>
struct ModInt
{
    int val;
    ModInt() { val = 0; }
    ModInt(long long v) { v += (v < 0 ? MOD : 0), val = (int)(v
        % MOD); }
    ModInt &operator+=(const ModInt &rhs)
    {
        val += rhs.val, val -= (val >= MOD ? MOD : 0);
        return *this;
    }
    ModInt &operator-=(const ModInt &rhs)
    {
        val -= rhs.val, val += (val < 0 ? MOD : 0);
        return *this;
    }
    ModInt &operator*=(const ModInt &rhs)
    {
        val = (int)((val * 1ULL * rhs.val) % MOD);
        return *this;
    }
    ModInt pow(long long n) const
    {
        ModInt x = *this, r = 1;
        while (n)
            r = ((n & 1) ? r * x : x), x = (x * x), n >>= 1;
        return r;
    }
}

```

```

}
ModInt inv() const { return this->pow(MOD - 2); }
ModInt &operator/=(const ModInt &rhs) { return *this = *
    this * rhs.inv(); }
friend ModInt operator+(const ModInt &lhs, const ModInt &
    rhs) { return ModInt(lhs) += rhs; }
friend ModInt operator-(const ModInt &lhs, const ModInt &
    rhs) { return ModInt(lhs) -= rhs; }
friend ModInt operator*(const ModInt &lhs, const ModInt &
    rhs) { return ModInt(lhs) *= rhs; }
friend ModInt operator/(const ModInt &lhs, const ModInt &
    rhs) { return ModInt(lhs) /= rhs; }
friend bool operator==(const ModInt &lhs, const ModInt &rhs
    ) { return lhs.val == rhs.val; }
friend bool operator!=(const ModInt &lhs, const ModInt &rhs
    ) { return lhs.val != rhs.val; }
friend std::ostream &operator<<(std::ostream &out, const
    ModInt &m) { return out << m.val; }
friend std::istream &operator>>(std::istream &in, ModInt &m
    ) { return in >> m.val; }
operator int() const { return val; }
};

const int MOD = 1e9 + 7;
using mint = ModInt<MOD>;

```

## 2.8 Modular inverse [NK]

```

template <class Z>
constexpr Z inverse(Z num, Z mod) {
    assert(mod > 1);
    if (!(0 <= num && num < mod)) {
        num %= mod;
        if (num < 0) num += mod;
    }
    Z res = 1, tmp = 0;
    assert(extended_gcd(num, mod, res, tmp) == 1);
    if (res < 0) res += mod;
    return res;
}

```

## 2.9 nCrp-O(1) [SK]

```

// array to store inverse of 1 to N
ll factorialNumInverse[N + 1];

// array to precompute inverse of 1! to N!

```

```

ll naturalNumInverse[N + 1];

// array to store factorial of first N numbers
ll fact[N + 1];

// Function to precompute inverse of numbers
void InverseofNumber(ll p)
{
    naturalNumInverse[0] = naturalNumInverse[1] = 1;
    for (int i = 2; i <= N; i++)
        naturalNumInverse[i] = naturalNumInverse[p % i] * (p
            - p / i) % p;
}

// Function to precompute inverse of factorials
void InverseofFactorial(ll p)
{
    factorialNumInverse[0] = factorialNumInverse[1] = 1;

    // precompute inverse of natural numbers
    for (int i = 2; i <= N; i++)
        factorialNumInverse[i] = (naturalNumInverse[i] *
            factorialNumInverse[i - 1]) % p;
}

// Function to calculate factorial of 1 to N
void factorial(ll p)
{
    fact[0] = 1;

    // precompute factorials
    for (int i = 1; i <= N; i++) {
        fact[i] = (fact[i - 1] * i) % p;
    }
}

// Function to return nCr % p in O(1) time
ll Binomial(ll N, ll R, ll p)
{
    // n C r = n! * inverse(r!) * inverse((n-r)!)
    ll ans = ((fact[N] * factorialNumInverse[R])
        % p * factorialNumInverse[N - R])
        % p;
    return ans;
}

```

## 2.10 Prime Phi Sieve [MB]

```

#include <bits/stdc++.h>

```

```

using namespace std;

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

struct PrimePhiSieve
{
private:
    ll n;
    vector<ll> primes, phi;
    vector<bool> is_prime;

public:
    PrimePhiSieve() {}

    PrimePhiSieve(ll n)
    {
        this->n = n, is_prime.resize(n + 5, true), phi.resize(n + 5, 1);
        phi_sieve();
    }
    void phi_sieve()
    {
        is_prime[0] = is_prime[1] = false;

        for (ll i = 1; i <= n; i++)
            phi[i] = i;

        for (ll i = 1; i <= n; i++)
            if (is_prime[i])
            {
                primes.push_back(i);
                phi[i] *= (i - 1), phi[i] /= i;

                for (ll j = i + i; j <= n; j += i)
                    is_prime[j] = false, phi[j] /= i, phi[j] *= (i - 1);
            }

        ll get_divisors_count(int number, int divisor)
        {
            return phi[number / divisor];
        }

        vector<pll> factorize(ll num)
        {
            vector<pll> a;
            for (int i = 0; i < (int)primes.size() && primes[i] * 1LL
                * primes[i] <= num; i++)

```

```

        if (num % primes[i] == 0)
        {
            int cnt = 0;
            while (num % primes[i] == 0)
                cnt++, num /= primes[i];
            a.push_back({primes[i], cnt});
        }

        if (num != 1)
            a.push_back({num, 1});
        return a;
    }

    ll get_phi(int n)
    {
        return phi[n];
    }
    // (n/p) * (p-1) => n - (n/p);
    void segmented_phi_sieve(ll l, ll r)
    {
        vector<ll> current_phi(r - l + 1);
        vector<ll> left_over_prime(r - l + 1);

        for (ll i = 1; i <= r; i++)
            current_phi[i - l] = i, left_over_prime[i - l] = i;

        for (ll p : primes)
        {
            ll to = ((l + p - 1) / p) * p;

            if (to == p)
                to += p;

            for (ll i = to; i <= r; i += p)
            {
                while (left_over_prime[i - l] % p == 0)
                    left_over_prime[i - l] /= p;
                current_phi[i - l] -= current_phi[i - l] / p;
            }
        }

        for (ll i = 1; i <= r; i++)
        {
            if (left_over_prime[i - l] > 1)
                current_phi[i - l] -= current_phi[i - l] /
                    left_over_prime[i - l];
            cout << current_phi[i - l] << endl;
        }
    }

```

```

    ll phi_sqrt(ll n)
    {
        ll res = n;

        for (ll i = 1; i * i <= n; i++)
        {
            if (n % i == 0)
            {
                res /= i;
                res *= (i - 1);

                while (n % i == 0)
                    n /= i;
            }
        }

        if (n > 1)
            res /= n, res *= (n - 1);
        return res;
    }
};

```

## 2.11 Prime Sieve [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;
typedef pair<int, int> pii;
typedef pair<ll, ll> pll;

struct PrimeSieve
{
public:
    vector<int> primes;
    vector<bool> isprime;
    int n;

    PrimeSieve() {}

    PrimeSieve(int n)
    {
        this->n = n, isprime.resize(n + 5, true), primes.clear();
        sieve();
    }

    void sieve()
    {

```

```

isprime[0] = isprime[1] = false;

primes.push_back(2);
for (int i = 4; i <= n; i += 2)
    isprime[i] = false;

for (int i = 3; 1LL * i * i <= n; i += 2)
    if (isprime[i])
        for (int j = i * i; j <= n; j += 2 * i)
            isprime[j] = false;

for (int i = 3; i <= n; i += 2)
    if (isprime[i])
        primes.push_back(i);
}

vector<pll> factorize(ll num)
{
    vector<pll> a;
    for (int i = 0; i < (int)primes.size() && primes[i] * 1LL
        * primes[i] <= num; i++)
        if (num % primes[i] == 0)
        {
            int cnt = 0;
            while (num % primes[i] == 0)
                cnt++, num /= primes[i];
            a.push_back({primes[i], cnt});
        }

    if (num != 1)
        a.push_back({num, 1});
    return a;
}

vector<ll> segmented_sieve(ll l, ll r)
{
    vector<ll> seg_primes;
    vector<bool> current_primes(r - l + 1, true);
    for (ll p : primes)
    {
        ll to = (l / p) * p;
        if (to < l)
            to += p;
        if (to == p)
            to += p;
        for (ll i = to; i <= r; i += p)
        {
            current_primes[i - l] = false;
        }
    }
}

```

```

for (int i = 1; i <= r; i++)
{
    if (i < 2)
        continue;
    if (current_primes[i - 1])
    {
        seg_primes.push_back(i);
    }
}
return seg_primes;
}
};

```

## 3 Brute-force

### 3.1 Power Set [NK]

```

template <class T>
vector<vector<T>> power_set(const vector<T>& vec) {
    vector<vector<T>> res;
    list<T> buf;
    function<void(int)> recurse = [&](int i) -> void {
        if (i == vec.size()) {
            res.emplace_back(buf.begin(), buf.end());
            return;
        }
        recurse(i + 1);
        buf.push_back(vec[i]), recurse(i + 1), buf.pop_back()
        ;
    };
    recurse(0);
    return res;
}

```

## 4 Graph

### 4.1 DSU [MB]

```

#include <bits/stdc++.h>

// 0 based
class DSU
{

```

```

    std::vector<int> p, csz;

public:
    DSU() {}

    //0 based
    DSU(int mx_size)
    {
        //Default empty
        p.resize(mx_size, 0), csz.resize(mx_size, 0);

        init(mx_size);
    }

    void init(int n)
    {
        // n = size
        for (int i = 0; i < n; i++)
        {
            p[i] = i, csz[i] = 1;
        }
    }

    //Return parent Recursively
    int get(int x)
    {
        if (p[x] != x)
            p[x] = get(p[x]);

        return p[x];
    }

    // Return Size
    int get_comp_size(int component) { return csz[get(component)]; }

    // Return if Union created Succesfully or false if they
    // are already in Union
    bool merge(int x, int y)
    {
        x = get(x), y = get(y);
        if (x == y)
            return false;

        if (csz[x] > csz[y])
            std::swap(x, y);

        p[x] = y;
        csz[y] += csz[x];

        return true;
    }
}

```

```

}
};

```

## 4.2 DSU [NK]

```

struct DSU {
    int n_nodes = 0;
    int n_components = 0;
    vector<int> component_size;
    vector<int> component_root;

    DSU(int n_nodes, bool make_all_nodes = false)
        : n_nodes(n_nodes),
          component_root(n_nodes, -1),
          component_size(n_nodes, 0) {
        if (make_all_nodes) {
            for (int i = 0; i < n_nodes; ++i) {
                make_node(i);
            }
        }
    }

    void make_node(int v) {
        if (component_root[v] == -1) {
            component_root[v] = v;
            component_size[v] = 1;
            ++n_components;
        }
    }

    int root(int v) {
        auto res = v;
        while (component_root[res] != res) {
            res = component_root[res];
        }
        while (v != res) {
            auto u = component_root[v];
            component_root[v] = res;
            v = u;
        }
        return res;
    }

    int connect(int u, int v) {
        u = root(u), v = root(v);
        if (u == v) return u;
        if (component_size[u] < component_size[v]) {
            swap(u, v);
        }
    }
}

```

```

        component_root[v] = u;
        component_size[u] += component_size[v];
        --n_components;
    }
};

```

## 4.3 Edge Remove CC [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

#define var(...) " [" << #__VA_ARGS__ ": " << (__VA_ARGS__) << "]"
#define mem(x, n) memset(x, n, sizeof(x))
#define all(x) x.begin(), x.end()
#define sz(x) ((int)x.size())
#define vec vector
#define endl "\n"

class DSU
{
public:
    DSU() {}

    DSU(int dsz) // Max size
    {
        //Default empty
        p.resize(dsz + 5, 0), csz.resize(dsz + 5, 0);

        init(dsz);
    }

    void init(int n)
    {
        // n = size
        for (int i = 0; i <= n; i++)
        {
            p[i] = i, csz[i] = 1;
        }
    }

    //Return parent Recursively
    int get(int x)
    {

```

```

        if (p[x] != x)
            p[x] = get(p[x]);

        return p[x];
    }
}

```

```

// Return Size
int getSize(int x) { return csz[get(x)]; }
// Return if Union created Successfully or false if they
// are already in Union
bool merge(int x, int y)
{
    x = get(x), y = get(y);
    if (x == y)
        return false;

    if (csz[x] > csz[y])
        std::swap(x, y);

    p[x] = y;
    csz[y] += csz[x];

    return true;
}
};

void runCase([[maybe_unused]] const int &TC)
{
    int n, m;
    cin >> n >> m;

    auto g = vec(n + 1, set<int>());

    auto dsu = DSU(n + 1);

    for (int i = 0; i < m; i++)
    {
        int u, v;
        cin >> u >> v;

        g[u].insert(v);
        g[v].insert(u);
    }

    set<int> eligible;

    for (int i = 1; i <= n; i++)
    {
        eligible.insert(i);
    }
}

```



```

int i = 1;
int cnt = 0;

while (sz(elligible))
{
    cnt++;
    queue<int> q;
    q.push(*elligible.begin());
    elligible.erase(elligible.begin());

    while (sz(q))
    {
        int fr = q.front();
        q.pop();

        auto v = elligible.begin();

        while (v != elligible.end())
        {
            if (g[fr].find(*v) == g[fr].end())
            {
                q.push(*v);
                v = elligible.erase(v);
            }
            else
            {
                v++;
            }
        }
    }
}

cout << cnt - 1 << endl;
}

int main()
{
    ios_base::sync_with_stdio(false), cin.tie(0);

    int t = 1;
    //cin >> t;

    for (int tc = 1; tc <= t; tc++)
        runCase(tc);

    return 0;
}

```

## 4.4 LCA [MB]

```

struct LCA
{
private:
    int n, lg;
    std::vector<int> depth;
    std::vector<std::vector<int>> up;
    std::vector<std::vector<int>> g;

public:
    LCA() : n(0), lg(0) {}

    LCA(int _n)
    {
        this->n = _n;
        lg = log2(n) + 2;
        depth.resize(n + 5, 0);
        up.resize(n + 5, std::vector<int>(lg, 0));
        g.resize(n + 1);
    }

    LCA(std::vector<std::vector<int>> &graph) : LCA(graph.size()
        ())
    {
        for (int i = 0; i < (int)graph.size(); i++)
            g[i] = graph[i];

        dfs(1, 0);
    }

    void dfs(int curr, int p)
    {
        up[curr][0] = p;
        for (int next : g[curr])
        {
            if (next == p)
                continue;
            depth[next] = depth[curr] + 1;
            up[next][0] = curr;
            for (int j = 1; j < lg; j++)
                up[next][j] = up[up[next][j - 1]][j - 1];
            dfs(next, curr);
        }
    }

    void clear_v(int a)
    {
        g[a].clear();
    }
}

```

```

void clear(int n_ = -1)
{
    if (n_ == -1)
        n_ = ((int)(g.size())) - 1;

    for (int i = 0; i <= n_; i++)
    {
        g[i].clear();
    }
}

void add(int a, int b)
{
    g[a].push_back(b);
}

int par(int a)
{
    return up[a][0];
}

int get_lca(int a, int b)
{
    if (depth[a] < depth[b])
        std::swap(a, b);

    int k = depth[a] - depth[b];
    for (int j = lg - 1; j >= 0; j--)
    {
        if (k & (1 << j))
            a = up[a][j];
    }

    if (a == b)
        return a;

    for (int j = lg - 1; j >= 0; j--)
        if (up[a][j] != up[b][j])
        {
            a = up[a][j];
            b = up[b][j];
        }

    return up[a][0];
}

int get_dist(int a, int b)
{
    return depth[a] + depth[b] - 2 * depth[get_lca(a, b)];
}

```

```

}
};

```

## 4.5 Tree Rooting [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

const int N = 2e5 + 5;

vector<int> g[N];
ll sz[N], dist[N], sum[N];

void dfs(int s, int p)
{
    sz[s] = 1;
    dist[s] = 0;
    for (int nxt : g[s])
    {
        if (nxt == p)
            continue;
        dfs(nxt, s);
        sz[s] += sz[nxt];
        dist[s] += (dist[nxt] + sz[nxt]);
    }
}

void dfs1(int s, int p)
{
    if (p != 0)
    {
        ll my_size = sz[s];
        ll my_contrib = (dist[s] + sz[s]);

        sum[s] = sum[p] - my_contrib + sz[1] - sz[s] + dist[s];
    }
    for (int nxt : g[s])
    {
        if (nxt == p)
            continue;
        dfs1(nxt, s);
    }
}

// problem link: https://cses.fi/problemset/task/1133

```

```

int main()
{
    int n;
    cin >> n;

    for (int i = 1, u, v; i < n; i++)
        cin >> u >> v, g[u].push_back(v), g[v].push_back(u);

    dfs(1, 0);

    sum[1] = dist[1];

    dfs1(1, 0);

    for (int i = 1; i <= n; i++)
        cout << sum[i] << " ";
    cout << endl;

    return 0;
}

```

## 5 Range query

### 5.1 BIT [MB]

```

struct BIT
{
private:
    std::vector<long long> mArray;

public:
    BIT(int sz) // Max size of the array
    {
        mArray.resize(sz + 1, 0);
    }

    void build(const std::vector<long long> &list)
    {
        for (int i = 1; i <= list.size(); i++)
        {
            mArray[i] = list[i];
        }

        for (int ind = 1; ind <= mArray.size(); ind++)
        {
            int ind2 = ind + (ind & -ind);
            if (ind2 <= mArray.size())

```

```

        {
            mArray[ind2] += mArray[ind];
        }
    }

    long long prefix_query(int ind)
    {
        int res = 0;
        for (; ind > 0; ind -= (ind & -ind))
        {
            res += mArray[ind];
        }
        return res;
    }

    long long range_query(int from, int to)
    {
        return prefix_query(to) - prefix_query(from - 1);
    }

    void add(int ind, long long add)
    {
        for (; ind < mArray.size(); ind += (ind & -ind))
        {
            mArray[ind] += add;
        }
    }
};

```

### 5.2 Lazy Segment Tree [MB]

```

template <typename T, typename F, T (*op)(T, T), F (*
    lazy_to_lazy)(F, F), T (*lazy_to_seg)(T, F, int, int)>
struct LazySegTree
{
private:
    std::vector<T> segt;
    std::vector<F> lazy;

    int n;
    T neutral;
    F lazyE;

    int left(int si) { return si * 2; }
    int right(int si) { return si * 2 + 1; }
    int midpoint(int ss, int se) { return (ss + (se - ss) / 2); }

    T query(int ss, int se, int si, int qs, int qe)

```

```

{
    // **** //
    if (lazy[si] != lazyE)
    {
        T curr = lazy[si];
        lazy[si] = lazyE;
        segt[si] = lazy_to_seg(segt[si], curr, ss, se);

        if (ss != se)
        {
            lazy[left(si)] = lazy_to_lazy(lazy[left(si)], curr);
            lazy[right(si)] = lazy_to_lazy(lazy[right(si)], curr);
        }
    }

    if (se < qs || qe < ss)
        return neutral;

    if (qs <= ss && qe >= se)
        return segt[si];

    int mid = midpoint(ss, se);

    return op(query(ss, mid, left(si), qs, qe), query(mid + 1,
        se, right(si), qs, qe));
}

void update(int ss, int se, int si, int qs, int qe, F val)
{
    // **** //

    if (lazy[si] != lazyE)
    {
        F curr = lazy[si];
        lazy[si] = lazyE;
        segt[si] = lazy_to_seg(segt[si], curr, ss, se);
        if (ss != se)
        {
            lazy[left(si)] = lazy_to_lazy(lazy[left(si)], curr);
            lazy[right(si)] = lazy_to_lazy(lazy[right(si)], curr);
        }
    }

    if (se < qs || qe < ss)
        return;

    if (qs <= ss && qe >= se)
    {
        // **** //

```

```

        segt[si] = lazy_to_seg(segt[si], val, ss, se);

        if (ss != se)
        {
            lazy[left(si)] = lazy_to_lazy(lazy[left(si)], val);
            lazy[right(si)] = lazy_to_lazy(lazy[right(si)], val);
        }
        return;
    }

    int mid = midpoint(ss, se);

    update(mid + 1, se, si * 2 + 1, qs, qe, val);
    update(ss, mid, left(si), qs, qe, val);

    segt[si] = op(segt[left(si)], segt[right(si)]);
}

public:
LazySegTree() : n(0) {}

LazySegTree(int sz, T ini, T _neutral, F _lazyE)
{
    this->n = sz + 1;
    this->neutral = _neutral;
    this->lazyE = _lazyE;
    segt.resize(n * 4 + 5, ini);
    lazy.resize(n * 4 + 5, _lazyE);
}

LazySegTree(const std::vector<T> &arr, T ini, T _neutral, F
    _lazyE) : LazySegTree((int)arr.size(), ini, _neutral,
    _lazyE)
{
    init(arr);
}

void init(const std::vector<T> &arr)
{
    this->n = (int)arr.size();
    for (int i = 0; i < n; i++)
        set(i, i, arr[i]);
}

T get(int qs, int qe)
{
    return query(0, n - 1, 1, qs, qe);
}

void set(int from, int to, F val)

```

```

{
    update(0, n - 1, 1, from, to, val);
}

};

int op(int a, int b)
{
    return a + b;
}

int lazy_to_seg(int seg, int lazy_v, int l, int r)
{
    return seg + (lazy_v * (r - l + 1));
}

int lazy_to_lazy(int curr_lazy, int input_lazy)
{
    return curr_lazy + input_lazy;
}

```

### 5.3 Lazy Segment Tree [SK]

```

ll v[4*N];
ll add[4*N];
int arr[N];

void push(int cur)
{
    add[cur*2] += add[cur];
    add[cur*2 + 1] += add[cur];
    add[cur] = 0;
}

/*
void build(int cur,int l,int r)
{
    if(l==r)
    {
        v[cur] = arr[l];
        return;
    }

    int mid = l + (r-l)/2;

    build(cur*2,l,mid);
    build(cur*2 + 1,mid+1,r);

    v[cur]= v[cur*2] + v[cur*2 + 1];
}

```

```

    return;
}
*/

ll query(int cur,int l,int r,int x,int y)
{
    if(x>r || y<l)
    {
        return 0;
    }

    if(l==r)
    {
        return v[cur] + add[cur];
    }

    if(l==x && r==y)
    {
        return v[cur] + add[cur]*(r-l+1);
    }

    int mid = 1 + (r-l)/2;

    v[cur] += add[cur]*(r-l+1);
    push(cur);

    ll left = query(cur*2,l,mid,x,min(mid,y));
    ll right = query(cur*2 + 1,mid+1,r,max(mid+1,x),y);

    ll res = 0;

    res = left + right ;

    return res;
}

void update(int cur,int l,int r,int s,int e,int val)
{
    if(l==s && r==e)
    {
        add[cur] += val;
        return;
    }

    if(s>r || e<l)
    {
        return;

```

```

    }

    int mid = 1 + (r-l)/2;

    push(cur);

    update(cur*2,l,mid,s,min(e,mid),val);
    update(cur*2 + 1,mid+1,r,max(s,mid+1),e,val);

    v[cur] = (v[cur*2] + add[cur*2]*(mid-l+1)) + (v[cur*2 + 1] + add[cur*2 + 1]*(r-mid));

    return;
}

```

## 5.4 Mos Algorithm [MB]

```

#include <bits/stdc++.h>

using namespace std;

const int N = 3e4 + 5;
const int blk = sqrt(N) + 1;

struct Query
{
    int l, r, i;
    bool operator<(const Query q) const
    {
        if (this->l / blk == q.l / blk)
            return this->r < q.r;
        return this->l / blk < q.l / blk;
    }
};

vector<int> mos_algorithm(vector<Query> &queries, vector<int> &a)
{
    vector<int> answers(queries.size());
    sort(queries.begin(), queries.end());

    int sza = 1e6 + 5;
    vector<int> freq(sza);

    int cnt = 0;

    auto add = [&](int x) -> void
    {
        freq[x]++;
    }

    if (freq[x] == 1)
        cnt++;
    };

    auto remove = [&](int x) -> void
    {
        freq[x]--;
        if (freq[x] == 0)
            cnt--;
    };

    int l = 0;
    int r = -1;
    for (Query q : queries)
    {
        while (l > q.l)
        {
            l--;
            add(a[l]);
        }
        while (r < q.r)
        {
            r++;
            add(a[r]);
        }
        while (l < q.l)
        {
            remove(a[l]);
            l++;
        }
        while (r > q.r)
        {
            remove(a[r]);
            r--;
        }
        answers[q.i] = cnt;
    }
    return answers;
}

int main()
{
    int n;
    cin >> n;

    vector<int> a(n);
    for (int i = 0; i < n; i++)
        cin >> a[i];

    int q;

```

```

cin >> q;

vector<Query> qr(q);

for (int i = 0; i < q; i++)
{
    int l, r;
    cin >> l >> r;

    l--, r--;
    qr[i].l = l, qr[i].r = r, qr[i].i = i;
}

vector<int> res = mos_algorithm(qr, a);

for (int i = 0; i < q; i++)
    cout << res[i] << endl;

return 0;
}

```

## 5.5 Segment Tree [MB]

## 5.6 Segment Tree [SK]

```

pair<int,int> v[4*N];
int arr[N];

void build(int cur,int l,int r)
{
    if(l==r)
    {
        pair<int,int> tmp = {0,0};
        if(arr[l]==0)
        {
            tmp.second++;
        }
        else if(arr[l]<0)
        {
            tmp.first++;
        }
        v[cur] = tmp;
        return;
    }

    int mid = 1 + (r-l)/2;

```

```

    build(cur*2,l,mid);
    build(cur*2 + 1,mid+1,r);

    v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
    v[cur].second = v[cur*2].second + v[cur*2 + 1].second;
    return;
}

pair<int,int> query(int cur,int l,int r,int x,int y)
{
    if(l==x && r==y)
    {
        return v[cur];
    }

    if(x>r || y<l)
    {
        return {-1,-1};
    }

    int mid = 1 + (r-l)/2;
    pair<int,int> left = query(cur*2,l,mid,x,min(mid,y));
    pair<int,int> right = query(cur*2 + 1,mid+1,r,max(mid+1,x),y);

    pair<int,int> res = {0,0};
    res.first = ((left.first!=-1)?left.first:0) + ((right.first!=-1)?right.first:0);
    res.second = ((left.second!=-1)?left.second:0) + ((right.second!=-1)?right.second:0);

    return res;
}

void update(int cur,int l,int r,int pos,int val)
{
    if(l==r)
    {
        arr[l] = val;
        pair<int,int> tmp = {0,0};
        if(arr[l]==0)
        {
            tmp.second++;
        }
        else if(arr[l]<0)
        {
            tmp.first++;
        }
        v[cur] = tmp;
    }

```

```

        return;
    }

    int mid = 1 + (r-l)/2;
    if(pos<=mid)
    {
        update(cur*2,l,mid,pos,val);
    }
    else
    {
        update(cur*2 + 1,mid+1,r,pos,val);
    }

    v[cur].first = v[cur*2].first + v[cur*2 + 1].first;
    v[cur].second = v[cur*2].second + v[cur*2 + 1].second;
    return;
}

```

## 5.7 Sparse Table [MB]

# 6 String

## 6.1 Hashing [MB]

```

#include <bits/stdc++.h>

using namespace std;

typedef long long ll;

const int PRIMES[] = {2147462393, 2147462419, 2147462587,
2147462633, 2147462747, 2147463167, 2147463203,
2147463569, 2147463727, 2147463863, 2147464211,
2147464549, 2147464751, 2147465153, 2147465563,
2147465599, 2147465743, 2147465953, 2147466457,
2147466463, 2147466521, 2147466721, 2147467009,
2147467057, 2147467067, 2147467261, 2147467379,
2147467463, 2147467669, 2147467747, 2147468003,
2147468317, 2147468591, 2147468651, 2147468779,
2147468801, 2147469017, 2147469041, 2147469173,
2147469229, 2147469593, 2147469881, 2147469983,
2147470027, 2147470081, 2147470177, 2147470673,
2147470823, 2147471057, 2147471327, 2147471581,

```

```

2147472137, 2147472161, 2147472689, 2147472697,
2147472863, 2147473151, 2147473369, 2147473733,
2147473891, 2147473963, 2147474279, 2147474921,
2147474929, 2147475107, 2147475221, 2147475347,
2147475397, 2147475971, 2147476739, 2147476769,
2147476789, 2147476927, 2147477063, 2147477107,
2147477249, 2147477807, 2147477933, 2147478017,
2147478521};

// ll base_pow, base_pow_1;
ll base1 = 43, base2 = 47, mod1 = 1e9 + 7, mod2 = 1e9 + 9;

// **** Enable this function for codeforces
void generateRandomBM()
{
    unsigned int seed = chrono::system_clock::now().
        time_since_epoch().count();
    srand(seed); /// to avoid getting hacked in CF, comment
        this line for easier debugging

    int q_len = (sizeof(PRIMES) / sizeof(PRIMES[0])) / 4;
    base1 = PRIMES[rand() % q_len];
    mod1 = PRIMES[rand() % q_len + q_len];
    base2 = PRIMES[rand() % q_len + 2 * q_len];
    mod2 = PRIMES[rand() % q_len + 3 * q_len];
}

struct Hash
{
public:
    vector<int> base_pow, f_hash, r_hash;
    ll base, mod;

    Hash() {}
    // Update it make it more dynamic like segTree class and
    DSU
    Hash(int mxSize, ll base, ll mod) // Max size
    {
        this->base = base;
        this->mod = mod;
        base_pow.resize(mxSize + 2, 1), f_hash.resize(mxSize + 2,
            0), r_hash.resize(mxSize + 2, 0);

        for (int i = 1; i <= mxSize; i++)
        {
            base_pow[i] = base_pow[i - 1] * base % mod;
        }
    }

    void init(string s)

```

```

{
    int n = s.size();

    for (int i = 1; i <= n; i++)
    {
        f_hash[i] = (f_hash[i - 1] * base + int(s[i - 1])) % mod;
    }

    for (int i = n; i >= 1; i--)
    {
        r_hash[i] = (r_hash[i + 1] * base + int(s[i - 1])) % mod;
    }
}

int forward_hash(int l, int r)
{
    int h = f_hash[r + 1] - (1LL * base_pow[r - l + 1] *
        f_hash[l]) % mod;
    return h < 0 ? mod + h : h;
}

int reverse_hash(int l, int r)
{
    int h = r_hash[l + 1] - (1LL * base_pow[r - l + 1] *
        r_hash[r + 2]) % mod;
    return h < 0 ? mod + h : h;
}

class DHash
{
public:
    Hash sh1, sh2;
    DHash() {}

    DHash(int mx_size)
    {
        sh1 = Hash(mx_size, base1, mod1);
        sh2 = Hash(mx_size, base2, mod2);
    }

    void init(string s)
    {
        sh1.init(s);
        sh2.init(s);
    }

    ll forward_hash(int l, int r)
    {

```

```

        return (ll(sh1.forward_hash(l, r)) << 32) | (sh2.
            forward_hash(l, r));
    }

    ll reverse_hash(int l, int r)
    {
        return ((ll(sh1.reverse_hash(l, r)) << 32) | (sh2.
            reverse_hash(l, r)));
    }
};

```

## 6.2 Hashing [NK]

```

namespace roll_hash_util {
    constexpr int MaxDim = 4;
    constexpr array<int, MaxDim> primes = {257, 263, 269,
        271};
    constexpr array<int, MaxDim> primes_minus1e9 = {7, 9, 21,
        33};
    constexpr int modulus(int dim) { return primes_minus1e9[
        dim] + 1e9; }
    array<vector<int>, MaxDim> p_pow = {};
    void resize(int n) {
        for (int d = 0; d < MaxDim; ++d) {
            auto& pp = p_pow[d];
            if (pp.empty()) {
                pp.push_back(1);
            }
            while (pp.size() < n) {
                pp.push_back((((long long)pp.back() * primes[d
                    ]) % modulus(d));
            }
        }
    }
} // namespace roll_hash_util

template <int Dim = 2>
class Rolling_hash {
private:
    size_t len_;
    array<vector<int>, Dim> pref_hash_;
    array<vector<int>, Dim> suff_hash_;

public:
    template <class InputIter>
    Rolling_hash(InputIter first, InputIter last, bool bidir
        = false) {
        len_ = distance(first, last);
        roll_hash_util::resize(len_);
    }

```

```

for (int d = 0; d < Dim; ++d) {
    vector<int>& ph = pref_hash_[d];
    const int m = roll_hash_util::modulus(d);
    const long long p = roll_hash_util::primes[d];
    ph.resize(len_ + 1);
    ph[0] = 0;
    auto it = first;
    for (int i = 0; i < len_; ++i) {
        ph[i + 1] = ((ph[i] * p) % m) + *it) % m;
        ++it;
    }
}

if (!bidir) return;

for (int d = 0; d < Dim; ++d) {
    vector<int>& sh = suff_hash_[d];
    const int m = roll_hash_util::modulus(d);
    const long long p = roll_hash_util::primes[d];
    sh.resize(len_ + 1);
    sh[len_] = 0;
    auto it = prev(last);
    for (int i = len_; i > 0; --i) {
        sh[i - 1] = ((sh[i] * p) % m + *it) % m;
        --it;
    }
}

array<int, Dim> get(size_t i, size_t n) const {
    array<int, Dim> res;
    for (int d = 0; d < Dim; ++d) {
        const vector<int>& ph = pref_hash_[d];
        const int m = roll_hash_util::modulus(d);
        const long long pp = roll_hash_util::p_pow[d][n];
        res[d] = ((ph[i + n] - (ph[i] * pp) % m) % m + m)
            % m;
    }
    return res;
}

array<int, Dim> getrev(size_t i, size_t n) const {
    assert(!suff_hash_[0].empty());
    array<int, Dim> res;
    for (int d = 0; d < Dim; ++d) {
        const vector<int>& sh = suff_hash_[d];
        const int m = roll_hash_util::modulus(d);
        const long long pp = roll_hash_util::p_pow[d][n];

```

```

        res[d] = ((sh[i] - (sh[i + n] * pp) % m) % m + m)
            % m;
    }
    return res;
}

size_t size() const { return len_; }

array<int, Dim> pref(size_t i) const {
    array<int, Dim> res;
    for (int d = 0; d < Dim; ++d) {
        res[d] = pref_hash_[d][i];
    }
    return res;
}

array<int, Dim> suff(size_t i) const {
    array<int, Dim> res;
    for (int d = 0; d < Dim; ++d) {
        res[d] = suff_hash_[d][i];
    }
    return res;
}
};

```

### 6.3 Hashing [SK]

```

int powhash1[ 1000000 + 10] = {};
int powhash2[ 1000000 + 10] = {};
int f_prefhash1[1000000 + 10];
int f_prefhash2[1000000 + 10];
int r_prefhash1[1000000 + 10];
int r_prefhash2[1000000 + 10];

int add(ll x, ll y, ll mod)
{
    return (x+y>=mod)?(x+y-mod):(x+y);
}

int subtract(ll x, ll y, ll mod)
{
    return (x-y<0)?(x-y+mod):(x-y);
}

int multp(ll x, ll y, ll mod)
{
    return (x*y)%mod;
}

```

```

const int BASE1 = 125;
const int MOD1 = 1e9 + 9;

const int BASE2 = 250;
const int MOD2 = 1e9 + 7;

void f_prefhashcalc(string& s, int base, int mod, int*prefhash)
{
    ll sum = 0;
    int ns = s.size();

    for(int i=0; i<ns; i++)
    {
        sum = add(((ll)sum*base)%mod, s[i], mod);
        prefhash[i]=sum;
    }
}

void r_prefhashcalc(string& s, ll base, ll mod, int*prefhash)
{
    ll sum = 0;
    int ns = s.size();
    prefhash[ns]=0;

    for(int i=ns-1; i>=0; i--)
    {
        sum = add((sum*base)%mod, s[i], mod);
        prefhash[i]=sum;
    }
}

int f_strhash(string& s, int base, int mod)
{
    ll sum = 0;
    int ns = s.size();

    for(int i=0; i<ns; i++)
    {
        sum = add(((ll)sum*base)%mod, s[i], mod);
    }
    return sum;
}

int r_strhash(string& s, ll base, ll mod)
{
    ll sum = 0;
    int ns = s.size();

```

```

    for(int i=ns-1; i>=0; i--)
    {
        sum = add((sum*base)%mod,s[i],mod);
    }
    return sum;
}

void powhashfill(int base,int mod,int*powhash)
{
    for(int i=0; i<1000000 + 10; i++)
    {
        if(i==0)
        {
            powhash[0]=1;
            continue;
        }

        powhash[i] = multp(powhash[i-1],base,mod);
    }
}

```

```

int f_substrhash(int l,int r,ll mod,int*prefhash,int*powhash)
{
    ll x = subtract( prefhash[r], multp(prefhash[l-1],powhash
        [r-l+1],mod), mod );

    return x;
}

int r_substrhash(int l,int r,ll mod,int*prefhash,int*powhash)
{
    ll x = subtract( prefhash[l], multp(prefhash[r+1],powhash
        [r-l+1],mod), mod );

    return x;
}

```

## 6.4 Z-Function [MB]

```

#include<bits/stdc++.h>

/*
tested by ac
submission: https://codeforces.com/contest/432/submission/145953901
problem: https://codeforces.com/contest/432/problem/D
*/
std::vector<int> z_function(const std::string &s)
{
    int n = (int)s.size();
    std::vector<int> z(n, 0);
    for (int i = 1, l = 0, r = 0; i < n; i++)
    {
        if (i <= r)
            z[i] = std::min(r - i + 1, z[i - l]);
        while (i + z[i] < n && s[z[i]] == s[i + z[i]])
            z[i]++;
        if (i + z[i] - 1 > r)
            l = i, r = i + z[i] - 1;
    }
    return z;
}

```