

```
[> with(DifferentialGeometry) : with(LieAlgebras) : with(Library) :
> StructureEquation := [[x,y]=y];
                                StructureEquation := [[x,y]=y] (1)
```

```
> L := LieAlgebraData(StructureEquation, [x,y], Alg1);
                                L := [[e1, e2]=e2] (2)
```

```
> DGsetup(L);
                                Lie algebra: Alg1 (3)
```

```
Alg1 > MultiplicationTable("LieTable");
                                [
                                |'  e1  e2
                                --- --- ---
                                e1 |'  0  e2
                                e2 |' -e2 0
                                ] (4)
```

```
Alg1 > C := Center( )
                                C := [ ] (5)
```

```
Alg1 > A := DerivedAlgebra( )
                                A := [e2] (6)
```

So, $\langle y \rangle$ is the only proper ideal. So every 1-dimensional subspace is $\langle b \rangle$ or $\langle a+kb \rangle$. So adjoint group factorizes as $e^{ad\langle b \rangle} e^{ad\langle a+kb \rangle}$.

Now, we will find the conjugates of $\langle a+kb \rangle$ under e^{tadb} .

```
Alg1 > g := (x,y) -> y + t.LieBracket(x,y)
                                g := (x,y) -> y + t DifferentialGeometry:-LieBracket(x,y) (7)
```

```
Alg1 > g(e2, e1 + k.e2)
                                e1 + k e2 - t e2 (8)
```

Thus, $\langle a+kb \rangle \sim \langle a \rangle$. Hence representatives of 1-dimensional subalgebras are $\langle a \rangle$ and $\langle b \rangle$.