

Class works:

Task 1: Design of FIR filters by frequency sampling.

Code:

```
clc;
close all;
clear all;
Hd=inline('exp(-i*om*(M-1)/2).*(1+abs(om)>(pi/2))','om','M');
M=9;
ok=[0:(M-1)]/M*2*pi;
Hk=Hd(mod(ok+pi,2*pi)-pi,M); %trick: [-pi,pi] specification of
H(\omega)
h=ifft(Hk);
h=fir2(M-1, [0 0.5 .5 1],[1 1 2 2],boxcar(M)); %%high pass like
magnitude
om=linspace(-pi,pi,201);
clf,
pl=230;
subplot(pl+1),plot(om,abs(Hd(om,M)))
hold on,
stem(ok(ok>=0),abs(Hk(ok>=0)),'filled'),
xlabel('\omega');
ylabel('|H_d(\omega)|');
subplot(pl+2),stem(0:(M-1),h,'filled'),title(sprintf('M=%d',M))
xlabel('n');
ylabel('h[n]');
axis([0 M-1 -.5 1.5])
H=freqz(h,1,om);
subplot(pl+3),plot(om,abs(H),'--',om,abs(Hd(om,M)),'--',
'ok',abs(Hk),'o')
xlabel('\omega');ylabel('|H(\omega)|'),
```

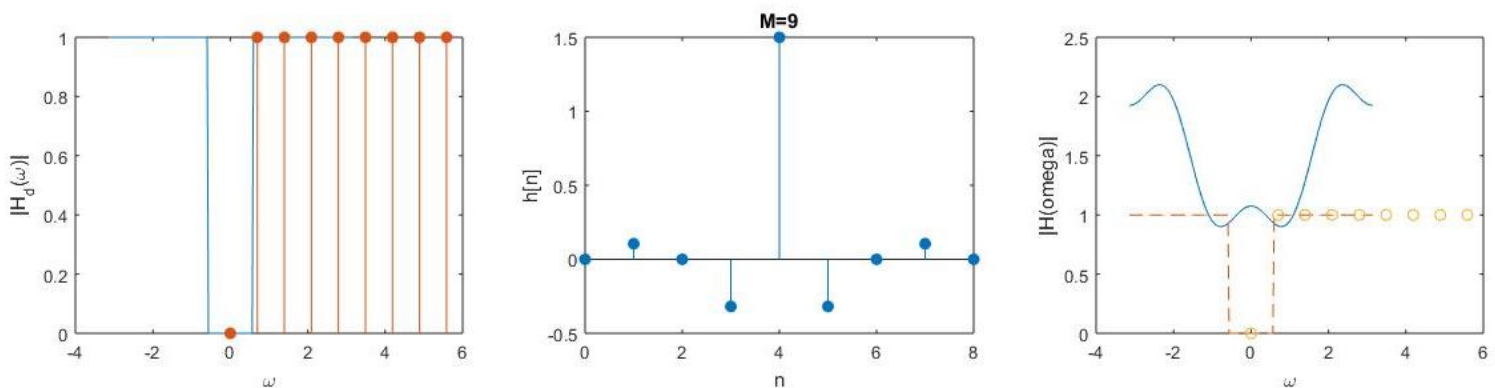


Figure 5.1 : Design of FIR filter by frequency sampling

Task 2: Design of linear phase FIR filters using window

Code:

```
clc;
clear all;
close all;
M=15;
n=[0:(M-1)];
om=linspace(-pi,pi,201); %for displaying freq response
oc=pi/4; %cutoff freq
%desired response:
hd=inline('oc/pi*sinc(oc/pi*(n-(M-1)/2))','n','oc','M');
Hd=inline('1*abs(om)<oc','om','oc');
hn_hann=hd(n,oc,M).*hann(M); %hanning window applied to ideal impulse
hn_rectwin=hd(n,oc,M).*rectwin(M); %rectwin window applied to ideal
impulse response
hn_blackman=hd(n,oc,M).*blackman(M); %blackman window applied to
ideal impulse response
hn_hamming=hd(n,oc,M).*hamming(M); %hamming window applied to ideal
impulse response
hn_kaiser=hd(n,oc,M).*kaiser(M); %kaiser window applied to ideal
impulse response
hn_triang=hd(n,oc,M).*triang(M); %triang window applied to ideal
impulse response

figure(1),subplot(211)
stem(n,hn_hann,'filled'),
axis([0 M-1 -.1 .3]),xlabel('n'), ylabel('h[n]')
title(sprintf('Hanning Lowpass, M=%d',M))
subplot(212)
H=freqz(hn_hann,1,om);
plot(om,20*log10(abs(H)),'-',om,20*log10(max(Hd(om,oc),eps)),'--')
xlabel('\omega');
ylabel('|H(\omega)| (dB)');
title('Magnitude response (Hanning)');

figure(2),subplot(211)
stem(n,hn_hamming,'filled'),
axis([0 M-1 -.1 .3]),xlabel('n'), ylabel('h[n]')
title(sprintf('Hamming Lowpass, M=%d',M))
subplot(212)
H=freqz(hn_hamming,1,om);
plot(om,20*log10(abs(H)),'-',om,20*log10(max(Hd(om,oc),eps)),'--')
xlabel('\omega');
ylabel('|H(\omega)| (dB)');
title('Magnitude response (Hamming)');

figure(3),subplot(211)
stem(n,hn_rectwin,'filled'),
axis([0 M-1 -.1 .3]),xlabel('n'), ylabel('h[n]')
title(sprintf('Rect. window Lowpass, M=%d',M))
```

```

subplot(212)
H=freqz(hn_rectwin,1,om);
plot(om,20*log10(abs(H)),'-',om,20*log10(max(Hd(om,oc),eps)),'--')
xlabel('\omega');
ylabel('|H(\omega)| (dB)');
title('Magnitude response (rect. window)');

figure(4),subplot(211)
stem(n,hn_blackman,'filled'),
axis([0 M-1 -.1 .3]),xlabel('n'), ylabel('h[n]')
title(sprintf('Blackman window Lowpass, M=%d',M))
subplot(212)
H=freqz(hn_blackman,1,om);
plot(om,20*log10(abs(H)),'-',om,20*log10(max(Hd(om,oc),eps)),'--')
xlabel('\omega');
ylabel('|H(\omega)| (dB)');
title('Magnitude response (Blackman window)');

figure(5),subplot(211)
stem(n,hn_kaiser,'filled'),
axis([0 M-1 -.1 .3]),xlabel 'n', ylabel 'h[n]'
title(sprintf('kaiser window Lowpass, M=%d',M))
subplot(212)
H=freqz(hn_kaiser,1,om);
plot(om,20*log10(abs(H)),'-',om,20*log10(max(Hd(om,oc),eps)),'--')
xlabel('\omega');
ylabel('|H(\omega)| (dB)');
title('Magnitude response (kaiser window)');

```

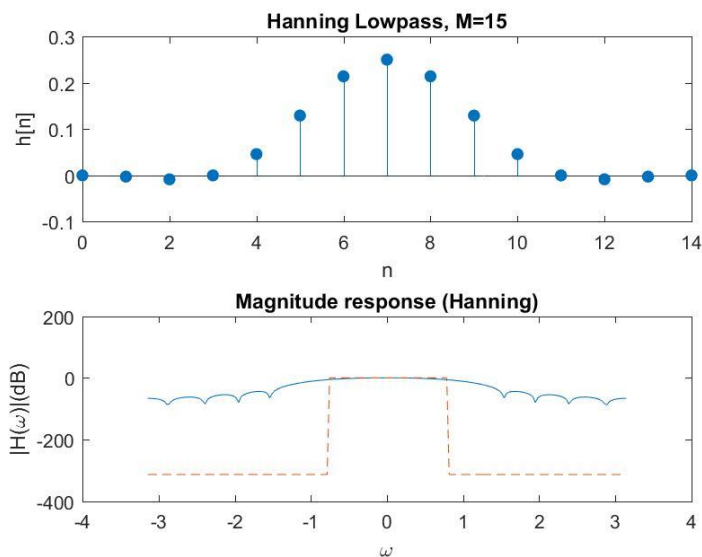


Figure 5.2: Design and magnitude response of hanning window.

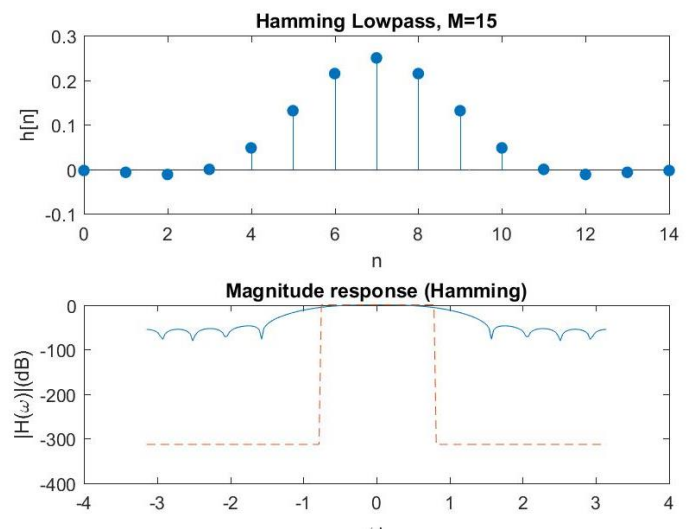


Figure 5.3: Design and magnitude response of hamming window.

Home Work:

Question: A high pass filter has the desired response as given below:

$$H_d(e^{j\omega}) = \begin{cases} 0, & \text{for } 0 \leq \omega \leq \pi/2 \\ e^{-j\omega^3} & \text{for } \pi/2 \leq \omega \leq \pi \end{cases}$$

Determine the filter coefficients $h(n)$ for $M=7$ using type I frequency sampling technique and also plot it.

Code:

```
clc;
close all;
clear all;
Hd=inline('exp(-i*om*3*(M-1)/2).*(1+abs(om)>(pi/2))','om','M');
M=7;
ok=[0:(M-1)]/M*2*pi;
Hk=Hd(mod(ok+pi,2*pi)-pi,M); %trick: [-pi,pi] specification of
H(\omega)
h=ifft(Hk);
h=fir2(M-1, [0 0.5 .5 1],[1 1 2 2],boxcar(M)); %%high pass like
magnitude
om=linspace(-pi,pi,201);
clf,
pl=230;
subplot(pl+1),plot(om,abs(Hd(om,M)))
hold on,

stem(ok(ok>=0),abs(Hk(ok>=0)),'filled'),
xlabel('\omega');
ylabel('|H_d(\omega)|');
subplot(pl+2),stem(0:(M-1),h,'filled'),title(sprintf('M=%d',M))
xlabel('n');
ylabel('h[n]');
axis([0 M-1 -.5 1.5])
H=freqz(h,1,om);
subplot(pl+3),plot(om,abs(H),'-',om,abs(Hd(om,M)),'--',ok,abs(Hk),'o')
xlabel('\omega');ylabel('|H(\omega)|');
```

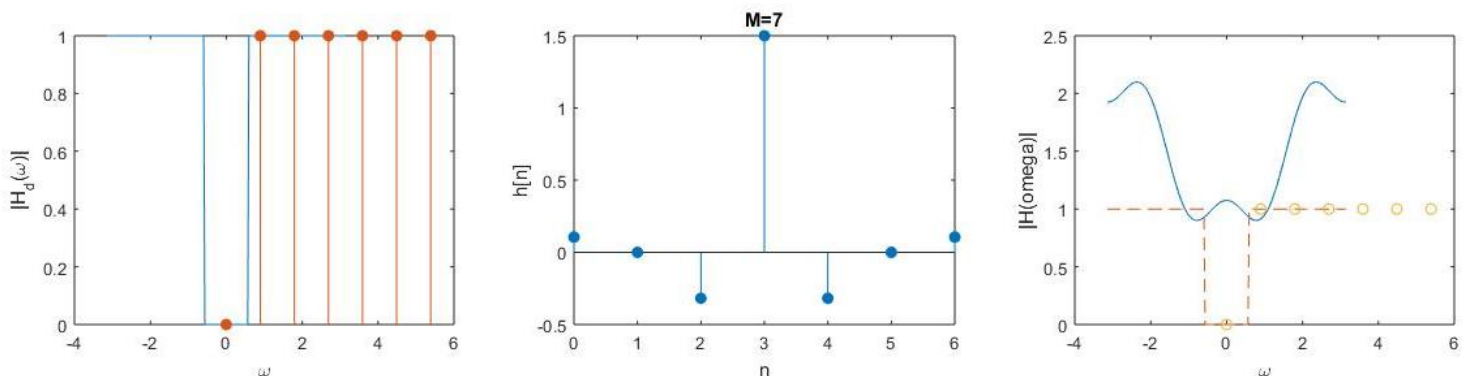


Figure 5.8 : Design of given FIR filter by frequency sampling

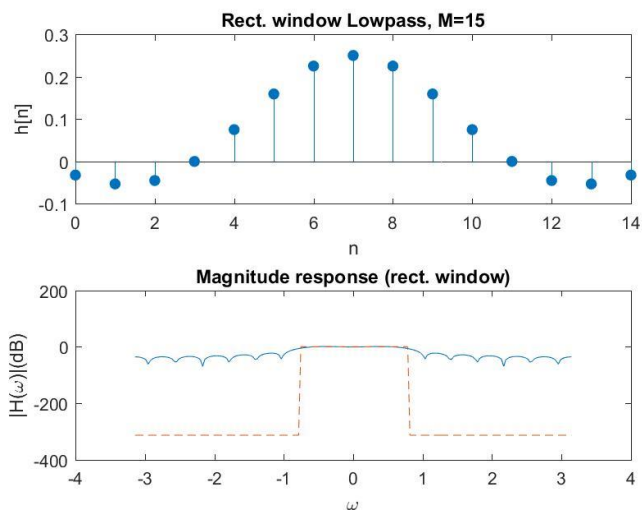


Figure 5.4: Design and magnitude response of rectangular window.

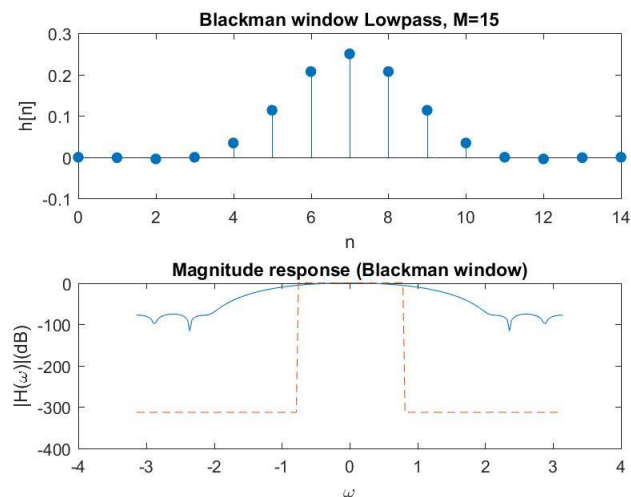


Figure 5.5: Design and magnitude response of blackman window.

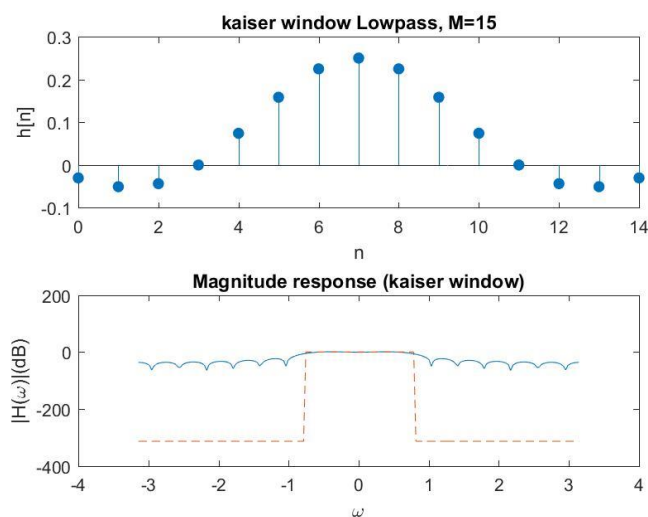


Figure 5.6: Design and magnitude response of kaiser window.

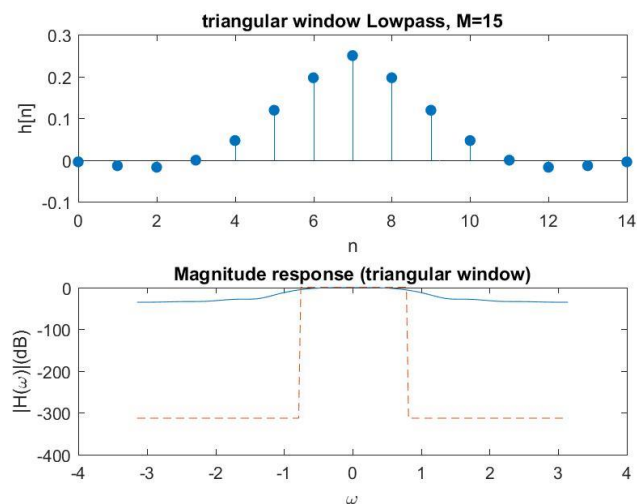


Figure 5.7: Design and magnitude response of triangular window.