

NUMBER SYSTEM

Numbers:

- In Decimal number system, there are ten symbols namely 0,1,2,3,4,5,6,7,8 and 9 called digits. A number is denoted by group of these digits called as numerals.

Face Value:

- Face value of a digit in a numeral is value of the digit itself.
- For example in 321, face value of 1 is 1, face value of 2 is 2 and face value of 3 is 3.

Place Value:

- Place value of a digit in a numeral is value of the digit multiplied by 10^n where n starts from 0.
- For example in 321:

$$\text{Place value of 1} = 1 \times 10^0 = 1 \times 1 = 1$$

$$\text{Place value of 2} = 2 \times 10^1 = 2 \times 10 = 20$$

$$\text{Place value of 3} = 3 \times 10^2 = 3 \times 100 = 300$$

Types of Numbers:

(1) **Natural Numbers** - $n > 0$ where n is counting number; $[1, 2, 3, \dots]$

(2) **Whole Numbers** - $n \geq 0$ where n is counting number; $[0, 1, 2, 3, \dots]$.

0 is the only whole number which is not a natural number.
Every natural number is a whole number.

(3) **Integers** - $n \geq 0$ or $n \leq 0$ where n is counting number; $\dots, -3, -2, -1, 0, 1, 2, 3, \dots$ are integers.

Positive Integers - $n > 0$; $[1, 2, 3, \dots]$

Negative Integers - $n < 0$; $[-1, -2, -3, \dots]$

Non-Positive Integers - $n \leq 0$; $[0, -1, -2, -3, \dots]$

Non-Negative Integers - $n \geq 0$; $[0, 1, 2, 3, \dots]$

- 0 is neither positive nor negative integer.

(4)**Even Numbers** - $n / 2 = 0$ where n is counting number; $[0,2,4,...]$

(5)**Odd Numbers** - $n / 2 \neq 0$ where n is counting number; $[1,3,5,...]$

(6)**Prime Numbers** - Numbers which is divisible by themselves only apart from 1.

- 1 is not a prime number.
- To test a number p to be prime, find a whole number k such that $k > \sqrt{p}$. Get all prime numbers less than or equal to k and divide p with each of these prime numbers. If no number divides p exactly then p is a prime number otherwise it is not a prime number

- Example: 191 is prime number or not?

Solution:

- Step 1 : $14 > \sqrt{191}$
- Step 2 : Prime numbers less than 14 are 2,3,5,7,11 and 13.
- Step 3 : 191 is not divisible by any above prime number.
- Result : 191 is a prime number.

- Example: 187 is prime number or not?

Solution:

- Step 1 : $14 > \sqrt{187}$
- Step 2 : Prime numbers less than 14 are 2,3,5,7,11 and 13.
- Step 3 : 187 is divisible by 11.
- Result : 187 is not a prime number.

(7) Composite Numbers - Non-prime numbers > 1 . For example, 4,6,8,9 etc.

- 1 is neither a prime number nor a composite number.
- 2 is the only even prime number.

(8) Co-Primes Numbers - Two natural numbers are co-primes if their H.C.F. is 1. For example, (2,3), (4,5) are co-primes.

Divisibility

✓ **Divisibility by 2** - A number is divisible by 2 if its unit digit is 0,2,4,6 or 8.

❑ **Example:** 64578 is divisible by 2 or not?

❑ **Solution:**

Step 1 - Unit digit is 8.

Result - 64578 is divisible by 2.

❑ **Example:** 64575 is divisible by 2 or not?

❑ **Solution:**

Step 1 - Unit digit is 5.

Result - 64575 is not divisible by 2.

✓ **Divisibility by 3** - A number is divisible by 3 if sum of its digits is completely divisible by 3

❑ **Example:** 64578 is divisible by 3 or not?

❑ **Solution:** Step 1 - Sum of its digits is $6 + 4 + 5 + 7 + 8 = 30$ which is divisible by 3.

Result - 64578 is divisible by 3.

❑ **Example:** 64576 is divisible by 3 or not?

❑ **Solution:** Step 1 - Sum of its digits is $6 + 4 + 5 + 7 + 6 = 28$ which is not divisible by 3.

Result - 64576 is not divisible by 3.

✓ **Divisibility by 4** - A number is divisible by 4 if number formed using its last two digits is completely divisible by 4.

Example: 64578 is divisible by 4 or not?

Solution:

Step 1 - number formed using its last two digits is 78
which is not divisible by 4.

Result - 64578 is not divisible by 4.

Example: 64580 is divisible by 4 or not?

Solution:

Step 1 - number formed using its last two digits is 80
which is divisible by 4.

Result - 64580 is divisible by 4.

✓ **Divisibility by 5** - A number is divisible by 5 if its unit digit is 0 or 5.

Example: 64578 is divisible by 5 or not?

Solution:

Step 1 - Unit digit is 8.

Result - 64578 is not divisible by 5.

Example: 64575 is divisible by 5 or not?

Solution:

Step 1 - Unit digit is 5.

Result - 64575 is divisible by 5.

✓ **Divisibility by 6** - A number is divisible by 6 if the number is divisible by both 2 and 3.

Example: 64578 is divisible by 6 or not?

Solution:

Step 1 - Unit digit is 8. Number is divisible by 2.

Step 2 - Sum of its digits is $6 + 4 + 5 + 7 + 8 = 30$
which is divisible by 3.

Result - 64578 is divisible by 6.

Example: 64576 is divisible by 6 or not?

Solution:

Step 1 - Unit digit is 6. Number is divisible by 2.

Step 2 - Sum of its digits is $6 + 4 + 5 + 7 + 6 = 28$
which is not divisible by 3.

Result - 64576 is not divisible by 6.

✓ **Divisibility by 8** - A number is divisible by 8 if number formed using its last three digits is completely divisible by 8.

Example: 64578 is divisible by 8 or not?

Solution:

Step 1 - number formed using its last three digits is 578
which is not divisible by 8.

Result - 64578 is not divisible by 8.

Example: 64576 is divisible by 8 or not?

Solution:

Step 1 - number formed using its last three digits is 576
which is divisible by 8.

Result - 64576 is divisible by 8.

✓ **Divisibility by 9** - A number is divisible by 9 if sum of its digits is completely divisible by 9.

Example: 64579 is divisible by 9 or not?

Solution:

Step 1 - Sum of its digits is $6 + 4 + 5 + 7 + 9 = 31$
which is not divisible by 9.

Result - 64579 is not divisible by 9.

Example: 64575 is divisible by 9 or not?

Solution:

Step 1 - Sum of its digits is $6 + 4 + 5 + 7 + 5 = 27$
which is divisible by 9.

Result - 64575 is divisible by 9.

✓ **Divisibility by 10** - A number is divisible by 10 if its unit digit is 0.

Example: 64575 is divisible by 10 or not?

Solution:

Step 1 - Unit digit is 5.

Result - 64575 is not divisible by 10.

Example: 64570 is divisible by 10 or not?

Solution:

Step 1 - Unit digit is 0.

Result - 64570 is divisible by 10.

✓ **Divisibility by 11** - A number is divisible by 11 if difference between sum of digits at odd places and sum of digits at even places is either 0 or is divisible by 11.

Example: 64575 is divisible by 11 or not?

Solution:

Step 1 - difference between sum of digits at odd places and sum of digits at even places = $(6+5+5) - (4+7) = 5$ which is not divisible by 11.

Result - 64575 is not divisible by 11.

Example: 64075 is divisible by 11 or not?

Solution:

Step 1 - difference between sum of digits at odd places and sum of digits at even places = $(6+0+5) - (4+7) = 0$.

Result - 64075 is divisible by 11.

Tips on Division:

If a number n is divisible by two co-primes numbers a , b then n is divisible by ab .

- $(a-b)$ always divides $(a^n - b^n)$ if n is a natural number.
- $(a+b)$ always divides $(a^n - b^n)$ if n is an even number.
- $(a+b)$ always divides $(a^n + b^n)$ if n is an odd number.

Division Algorithm:

When a number is divided by another number then

$$\text{Dividend} = (\text{Divisor} \times \text{Quotient}) + \text{Reminder}$$

Series:

Following are formulaes for basic number series:

- $(1+2+3+\dots+n) = \frac{n(n+1)}{2}$
- $(1^2+2^2+3^2+\dots+n^2) = \frac{n(n+1)(2n+1)}{6}$
- $(1^3+2^3+3^3+\dots+n^3) = \frac{n^2(n+1)^2}{4}$

Basic Formulae

- $(a + b)^2 = a^2 + b^2 + 2ab$
- $(a - b)^2 = a^2 + b^2 - 2ab$
- $(a + b)^2 - (a - b)^2 = 4ab$
- $(a + b)^2 + (a - b)^2 = 2(a^2 + b^2)$
- $(a^2 - b^2) = (a + b)(a - b)$
- $(a + b + c)^2 = a^2 + b^2 + c^2 + 2(ab + bc + ca)$
- $(a^3 + b^3) = (a + b)(a^2 - ab + b^2)$
- $(a^3 - b^3) = (a - b)(a^2 + ab + b^2)$
- $(a^3 + b^3 + c^3 - 3abc) = (a + b + c)(a^2 + b^2 + c^2 - ab - bc - ca)$

PROBLEMS

- Which of the following is a prime number?

A - 187

B - 811

C - 341

D - 437

Solution:

Step 1. Find a whole number k such that $k^2 > n$ for each number.

- $142 > 187$.
- $302 > 811$.
- $192 > 341$.
- $212 > 437$.

Step 2. Get all prime numbers which are $< k$

- 14 - 2, 3, 5, 7, 11, 13
- 30 - 2, 3, 5, 7, 11, 13, 17, 19, 23, 29
- 19 - 2, 3, 5, 7, 11, 13, 17
- 21 - 2, 3, 5, 7, 11, 13, 17, 19

Step 3. Check divisibility of each number

- with prime numbers which are $< k$.
 - 187 is divisible by 11.
 - 811 is not divisible by any prime number.
 - 341 is divisible by 11.
 - 437 is divisible by 19.
-
- Result: 811 is the prime number.

• Which of the following is the output of 6894×99 ?

A - 685506

B - 682506

C - 683506

D - 684506

Answer : B

Solution:

- 6894×99
= $6894 \times (100 - 1)$
= $6894 \times 100 - 6894 \times 1$
= $689400 - 6894$
= 682506

• Which of the following is the output of 685798×125 ?

A - 85724750

B - 8225750

C - 8225950

D - 8224760

- Answer : A

Solution:

- 685798×125
 $= 685798 \times 5^3$
 $= 685798 \times (10/2)^3$
 $= (685798 \times 10^3) / 2^3$
 $= 685798000 / 8$
 $= 85724750$

• Which of the following is the output of $869 \times 738 + 869 \times 262$?

A - 262000

B - 738000

C - 969000

D - 869000

- Answer : D

Solution:

$$869 \times 738 + 869 \times 262$$

$$= 869 \times (738 + 262)$$

$$= 869 \times 1000$$

$$= 869000$$

• Which of the following is the output of 1496×1496 ?

A - 3338016

B - 2238016

C - 2248016

D - 2258016

- Answer : B

Solution:

$$1496 \times 1496$$

$$= (1496)^2$$

$$= (1500-4)^2$$

$$= 1500^2 + 4^2 - 2 \times 1500 \times 4$$

$$= 2250000 + 16 - 12000$$

$$= 2238016$$

- $1000^9 \div 10^{26} = ?$

A - 0

B - 1

C - 10

D - 1000

- Answer : C

Solution:

$$= 1000^9/10^{26}$$

$$= (10^3)^9/10^{26}$$

$$= 10^{27}/10^{26}$$

$$= 10^{(27 - 26)}$$

$$= 10$$

• Which of the following is the output of
 $(578 \times 578 \times 578 + 432 \times 432 \times 432) / (578 \times 578 - 578 \times 432 + 432 \times 432)$

A - 2000

B - 4000

C - 3000

D - 1000

- Answer : D

Solution:

$$(578 \times 578 \times 578 + 432 \times 432 \times 432) / (578 \times 578 - 578 \times 432 + 432 \times 432)$$

Let's have $a = 578$, $b = 432$

Now expression is $(a^3 + b^3) / (a^2 - ab + b^2)$

$$= a + b$$

$$= 578 + 432$$

$$= 1000$$

- Which of the following numbers is completely divisible by 45?

A - 32765

B - 20000

C - 2025

D - 20280

- Answer : C

Solution:

$$45 = 5 \times 9$$

So, co-primes are 5 and 9

For divisibility, the unit digits must be 0 or 5 and sum of digits must be divisible by 9.

The unit digit of 2025 is 5 and sum of digits is divisible by 9

Therefore, 2025 is completely divisible by 45.

• **Which of the following cannot be the square of a natural number?**

A - 75625

B - 143642

C - 30976

D - 28561

• Answer : B

143642 cannot be the square of a natural number because the square of a natural number never ends in 2.

• What will be unit digit in $(3157)^{754}$?

A - 8

B - 9

C - 7

D - 6

Answer : B

- unit digit in $(3157)^{754}$
= unit digit in $(7)^{754}$
= unit digit in $(7^4)^{188} \times 7^2$
= unit digit in (1×49)
= 9
- Thus Unit digit in $(3157)^{754}$ is 9.

- We've used following formulae here:
- Unit digit in $7^1 = 7$
- Unit digit in $7^2 = 9$
- Unit digit in $7^3 = 3$
- Unit digit in $7^4 = 1$
- Unit digit in $7^5 = 7$
- Unit digit in $7^6 = 9$
- Unit digit in $7^7 = 3$
- Unit digit in $7^8 = 1$
- So pattern is 7-9-3-1. This pattern works for all numbers. So Unit digit in $((7)^4)^n$ will be 1.

• **What will be unit digit in $658 \times 539 \times 436 \times 312$?**

A - 8

B - 9

C - 4

D - 6

- Answer : C

Solution:

Multiply unit digits of each number.

Unit digit in $658 \times 539 \times 436 \times 312$

= Unit digit in $8 \times 9 \times 6 \times 2$.

= Unit digit in 864.

= 4.

• What will be unit digit in $3^{57} \times 6^{41} \times 7^{63}$?

A - 8

B - 9

C - 4

D - 6

- Answer : C

Solution:

$$3^{57} = (3^4)^{14} \times 3$$

So Unit digit in 3^{57}

$$= \text{Unit digit in } 1 \times 3$$

$$= 3$$

$$6^{41} = (6^4)^{10} \times 6$$

So Unit digit in 6^{41}

$$= \text{Unit digit in } 6 \times 6$$

$$= 6$$

$$7^{63} = (7^4)^{15} \times 7^3$$

So Unit digit in 7^{63}

$$= \text{Unit digit in } 1 \times 343$$

$$= 3$$

So Unit digit in $3^{57} \times 6^{41} \times 7^{63}$

$$= \text{Unit digit in } 3 \times 6 \times 3$$

$$= 4$$

- We've used following formulae here:

Unit digit in $3^4 = 1$

Unit digit in $6^4 = 6$

Unit digit in $7^4 = 1$

So Unit digit

- in $((3)^4)^n$ will be 1.

- in $((6)^4)^n$ will be 6.

- in $((7)^4)^n$ will be 1.

• Which of the following is the output of 43986×625 ?

A - 27491450

B - 27491350

C - 27491250

D - 27491750

- Answer : C

Solution:

$$43986 \times 625$$

$$= 43986 \times 5^4$$

$$= 43986 \times (10/2)^4$$

$$= (43986 \times 10^4) / 2^4$$

$$= 439860000 / 16$$

$$= 27491250$$

• If $5358 \times 51 = y$, then what is y ?

A - 273268

B - 273258

C - 273248

D - 273368

- Answer : B

Solution:

$$\begin{aligned}y &= 5358 \times 51 \\&= 5358 \times (50 + 1) \\&= 5358 \times 50 + 5358 \\&= 267900 + 5358 \\&= 273258\end{aligned}$$

- If $a - b = 5$ and $a^2 + b^2 = 41$, what is ab ?

A - 5

B - 7

C - 8

D - 16

- Answer : C

Solution:

Using formulae $(a-b)^2 = a^2 + b^2 - 2ab$

$$\Rightarrow ab = (a^2 + b^2 - (a-b)^2) / 2$$

$$\Rightarrow ab = [41 - 25] / 2 = 8$$

A number is as much greater than 36 as is less than 86. Find the number

- A. 61**
- B. 56**
- C. 63**
- D. 52**

ANSWER: A

Sol: Let x be the required number.

Given, x is as much greater than 36 as is less than 86.

$$x - 36 = 86 - x$$

$$x + x = 86 + 36$$

$$2x = 122$$

$$x = 122/2 = 61$$

The sum of two numbers is 184. If one-third of the one exceeds one-seventh of the other by 8, find the smaller number.

- A. 61
- B. 32
- C. 72
- D. 52

ANSWER: C

Let the numbers be x and (184-x)

$$\Rightarrow \frac{1}{3}x - \frac{184-x}{7} = 8$$

$\Rightarrow x=72$ Thus the numbers are 72 and 112 Hence the smaller number is 72

The average of four consecutive even numbers is 27. Find the largest of these numbers.

- A. 24
- B. 30
- C. 27
- D. 31

ANSWER: B

Sol: Given that the average of four consecutive even numbers is 27

Let the four consecutive even numbers be $x-2, x, x+2, x+4$

$$\text{The average} = \frac{(x-2) + x + (x+2) + (x+4)}{4}$$

$$\text{Therefore, } 27 = \frac{4x+4}{4}$$

$$\Rightarrow 27 = x+1$$

$$\Rightarrow x = 26$$

The largest number is $x+4 = 26+4 = 30$

If three numbers are added in pairs, the sums equal 10, 19 and 21. Find the least number.

- A. 6
- B. 15
- C. 10
- D. 4

ANSWER: D

Sol: let the numbers be x, y & z

According to question

$$x + y = 10 \dots\dots(1)$$

$$y + z = 19 \dots\dots(2)$$

$$z + x = 21 \dots\dots(3)$$

Subtracting (1) from (2)

$$\text{we get } z - x = 9 \dots\dots(4)$$

Subtracting (3) from (2)

$$\text{we get } x - y = 2 \dots\dots(5)$$

Adding (5) & (1)

$$\text{we get } 2x = 12 \text{ implies}$$

$$x = 6$$

Substituting $x = 6$ in (1) we get

$$y = 4$$

Substituting $y = 4$ in (2) we get

$$z = 15$$

Therefore the numbers are 6, 4 & 15

The least number is 4.

The difference between a number and its three-fifth is 50. What is the number?

- A. 75
- B. 100
- C. 125
- D. None of these

ANSWER: C

Sol: Let the number be 'x'

According to the question,

$$\Rightarrow x - \frac{3}{5}x = 50$$

$$\Rightarrow \frac{2}{5}x = 50$$

$$\Rightarrow x = 125$$

A number is doubled and 9 is added. If resultant is trebled, it becomes 75. What is that number

- A. 8
- B. 10
- C. 12
- D. 14

Answer: A

Explanation:

$$\Rightarrow 3(2x+9) = 75$$

$$\Rightarrow 2x+9 = 25$$

$$\Rightarrow x = 8$$

If the sum of a number and its square is 182, what is the number ?

A. 15

B. 26

C. 13

D. 91

Answer: C

Let the number be x

Then,

$$\Rightarrow x + x^2 = 182$$

$$\Rightarrow x + x^2 - 182 = 0$$

$$\Rightarrow (x + 14)(x - 13) = 0$$

$$\Rightarrow x = 13$$

Twenty times a positive integer is less than its square by 96. What is the integer?

- A. 20
- B. 24
- C. 30
- D. Cannot be determined

ANSWER: B

Sol: Let the positive integer be x , then

$$\Rightarrow x^2 - 96 = 20x$$

$$\Rightarrow x^2 - 20x - 96 = 0$$

$$\Rightarrow x^2 - 24x + 4x - 96 = 0$$

$$\Rightarrow x(x - 24) + 4(x - 24) = 0$$

$$\Rightarrow (x - 24)(x + 4) = 0$$

$$\Rightarrow x = 24 \text{ and } x = -4$$

$$\because x > 0 \quad \therefore x = 24$$

Find a positive number which when increased by 17 is equal to 60 times the reciprocal of the number.

- A. 3
- B. 10
- C. 17
- D. 20

Answer: A

Sol: Let the number be 'x'.

$$\text{Then, } \Rightarrow x+17=(60/x)$$

$$\Rightarrow x^2+17x-60=0$$

$$\Rightarrow (x+20)(x-3)=0$$

$$\Rightarrow x=3$$

The sum of two numbers is 22. Five times one number is equal to 6 times the other. The bigger of the two numbers is:

- A. 10
- B. 12
- C. 15
- D. 16

ANSWER: B

Sol: The sum of two numbers is 22,

$$x+y=22 \quad \text{.....(1)}$$

Five times one number is equal to 6 times the other,

$$5x=6y \quad \text{.....(2)}$$

From equation 1st,

$$5(22-y)=6y$$

$$110-5y=6y$$

$$11y=110$$

$$y=10$$

Put, the value of y in equation 1st,

$$10+x=22$$

$$x=12$$

∴ Bigger of two numbers is 12

One-fifth of a number is equal to $\frac{5}{8}$ of another number. If 35 is added to the first number, it becomes four times of the second number. The second number is:

- A. 25
- B. 40
- C. 70
- D. 125

ANSWER: B

Sol: Let the first number be x and the second number be y .

$$\text{Given : } (1/5)x = (5/8)y$$

$$x = (25/8)y$$

It is also given that, $x + 35 = 4y$

Replacing the value of x we had previously obtained,

$$(25/8)y + 35 = 4y$$

$$(25/8)y - 4y = -35$$

$$(25y - 32y)/8 = -35$$

$$-7y = -280$$

$y = 40$ and replacing this value in the first equation,

$$x = 125$$

Therefore, the first number is 125 and the second number is 40

If the sum of two numbers is 33 and their difference is 15, the smaller number is:

- A. 9
- B. 12
- C. 15
- D. 18

ANSWER: A

Sol: Let the numbers be x and y.

Since,

$$\mathbf{x+y=33 \quad \text{.....(1)}}$$

$$\mathbf{x-y=15 \quad \text{.....(2)}}$$

On solving equation (1) and (2), we get

$$\mathbf{x=24,y=9}$$

Hence, the smallest number is 9.

The sum of two numbers is 40 and their difference is 4. The ratio of the numbers is:

- A. 22:9
- B. 11:18
- C. 21:19
- D. 11:9

ANSWER: D

Sol: Let the two numbers be x and y :

$$x+y=40 \quad (1)$$

$$x-y=4 \quad (2)$$

$$(1)+(2): 2x=44, x=22$$

Substitute $x=22$ into (1):

$$y+22=40, y=18$$

$$\text{Ratio: } \frac{x}{y} = \frac{22}{18} = \frac{11}{9} \Rightarrow x:y = 11:9$$

Two numbers differ by 5. If their product is 336, then the sum of the two numbers is:

A. 39

B. 37

C. 15

D. 18

ANSWER: B

Sol: Let numbers are x and y

$$\Rightarrow x - y = 5 \text{ and } xy = 336$$

Now using identity

$$(x + y)^2 = (x - y)^2 + 4xy$$

$$= 25 + 4(336)$$

$$= 25 + 1344$$

$$= 1369$$

$$\Rightarrow x + y = 37$$

The sum of three consecutive odd numbers is 20 more than the first of these numbers. What is the middle number?

A. 7

B. 9

C. 11

D. Data inadequate

ANSWER: B

Sol: Let the numbers are $x, (x+2)$ & $(x+4)$

$$\Rightarrow x+x+2+x+4=x+20$$

$$\Rightarrow 2x=14$$

$$\Rightarrow x=7$$

$$\text{Middle number} = x+2=7+2=9$$

The sum of three consecutive multiples of 3 is 72. What is the largest number?

A. 21

B. 24

C. 27

D. 36

ANSWER: C

Sol: Let the numbers be $3x$, $3x + 3$ and $3x + 6$.

Then,

$$3x + (3x + 3) + (3x + 6) = 72$$

$$9x = 63$$

$$x = 7$$

$$\text{Largest number} = 3x + 6 = 27.$$

$$\Rightarrow \text{Second largest number} = 27 - 3 = 24$$

In a two-digit number, the digit in the unit's place is four times the digit in the ten's place and sum of the digits is equal to 10. What is the number?

- A. 14
- B. 41
- C. 82
- D. None of these

ANSWER: D

Sol: Let's take number as $10x+y$

As per question,

$y=4x$, and

$x+y=10$

So, $x+4x=10$

$5x=10$

$x=2$

$y=2 \times 4=8$

So, number is $10x+y=10 \times 2+8=28$

The denominator of a fraction is 3 more than the numerator. If the numerator as well as the denominator is increased by 4, the fraction becomes $\frac{4}{5}$. What was the original fraction?

A. $\frac{8}{11}$

B. $\frac{5}{8}$

C. $\frac{10}{13}$

D. $\frac{7}{10}$

ANSWER: A

Sol: Let the numerator be x Then, denominator = $x + 3$.

$$\text{Now. } (x + 4)/(x + 3) + 4 = 4/5$$

$$\Rightarrow 5(x + 4) = 4(x + 7)$$

$$\Rightarrow x = 8.$$

The fraction is $8/11$.

50 is divided into two parts such that the sum of their reciprocals is $\frac{1}{12}$. Find the greatest part?

- A. 20
- B. 10
- C. 30
- D. 40

ANSWER: C

Sol: Now according to given conditions,

$$X+Y=50, \text{---(1)}$$

And

$$1/X+1/Y=1/12 \text{---(2)}$$

Solving equation(2),we get,

$$(X+Y)/XY=1/12$$

$$50/XY=1/12 \text{---(from eq(1))}$$

$$XY=600 \text{---(3)}$$

Now solving eq(1) and (3) we get

$$X = 30 \text{ and } Y = 20.$$

Therefore the two parts in which 50 is divided are 30 and 20.

Which of the following numbers is divisibility by 3 ?

A. 541326

B. 5967013

C. 15689

D. 3578

ANSWER: A

Sol:

That is 541326 is the only one coz divisibility rule of 3 is such that if the sum of digits of a number is divisible by 3 the number is also divisible by 3. And sum of digits of 541326 is 21 which is divisible by 3 hence number is also divisible by 3.

What least value must be assigned to * so that the number $197*5462$ is divisible by 9 ?

- A. 6
- B. 3
- C. 5
- D. 2

ANSWER: D

Sol: First keep in mind that we can calculate this by easy method

just add all those numbers

i.e., $1+9+7+5+4+6+2=70$

So 70 will not divided by 9

So we can add the number So that can divided easily

for that add 1 now 71 not possible

add 2 now 72 so $72/9=8$ now possible

So put 2 in * position

Which of the following numbers is divisibility by 4 ?

A. 67920594

B. 618703572

C. 15000689

D. 3517398

ANSWER: B

Divisibility by 4 - A number is divisible by 4 if number formed using its last two digits is completely divisible by 4.

Here 72 is divisible by 4

Which digits should come in place of * and # if the number 62684*# is divisible by both 8 and 5 ?

- A. 6268450
- B. 6268440
- C. 6268430
- D. 6268460

ANSWER: B

Divisibility by 5 - A number is divisible by 5 if its unit digit is 0 or 5.

Divisibility by 8 - A number is divisible by 8 if number formed using its last three digits is completely divisible by 8.

Which of the following number is divisible by 24 ?

A. 35718

B. 63810

C. 537804

D. 3125736

Answer: D

Sol:

$24 = 3 \times 8$, where 3 and 8 co-prime

Clearly, 35718 is not divisible by 8, as 718 is not divisible by 8

Similarly, 63810 is not divisible by 8 and 537804 is not divisible by 8

Consider option (D),

Sum of digits = $(3 + 1 + 2 + 5 + 7 + 3 + 6) = 27$, which is divisible by 3

Also, 736 is divisible by 8

\therefore 3125736 is divisible by (3×8) , i.e., 24

THANK YOU