

MISCELLANEOUS (Sets, Relations, Statistics & Mathematical Reasoning)

Section-A

JEE Advanced/ IIT-JEE

Fill in the Blanks

A variable takes value x with frequency $^{n+x-1}C_{x}$, x = 0, 1, 2, ...n. The mode of the variable is....

(1982 - 2 Marks)

True / False

For real numbers x and y, we write x * y if $x - y + \sqrt{2}$ is an irrational number. Then, the relation* is an equivalence relation. (1981 - 2 Marks)

MCQs with One Correct Answer

- If X and Y are two sets, then $X \cap (X \cup Y)^c$ equals. (1979)
 - (a) X (c) ¢

- (d) None of these.
- The expression $\frac{12}{3+\sqrt{5}+2\sqrt{2}}$ is equal to
 - (a) $1 \sqrt{5} + \sqrt{2} + \sqrt{10}$ (b) $1 + \sqrt{5} + \sqrt{2} \sqrt{10}$
 - (c) $1 + \sqrt{5} \sqrt{2} + \sqrt{10}$ (d) $1 \sqrt{5} \sqrt{2} + \sqrt{10}$
- Select the correct alternative in each of the following. Indicate your choice by the appropriate letter only.
 - Let S be the standard deviation of n observations. Each of the n observations is multiplied by a constant c. Then the standard deviation of the resulting number is
 - (a) s

- (c) $s\sqrt{c}$
- (d) none of these
- The standard deviation of 17 numbers is zero. Then (1980)
 - (a) the numbers are in geometric progression with common ratio not equal to one.
 - (b) eight numbers are positive, eight are negative and one is zero.
 - (c) either (a) or (b)
- (d) none of these
- Consider any set of 201 observations $x_1, x_2, x_{200}, x_{201}$. It is given that $x_1 < x_2 < < x_{200} < x_{201}$. Then the mean deviation of this set of observations about a point k is (1981 - 2 Marks) minimum when k equals
 - (a) $(x_1 + x_2 + ... + x_{200} + x_{201})/201$

- If x_1, x_2, \dots, x_n are any real numbers and n is any (1982 - 2 Marks) postive integer, then
 - (a) $n \sum_{i=1}^{n} x_i^2 < \left(\sum_{i=1}^{n} x_i\right)^2$ (b) $\sum_{i=1}^{n} x_i^2 \ge \left(\sum_{i=1}^{n} x_i\right)^2$
 - (c) $\sum_{i=1}^{n} x_i^2 \ge n \left(\sum_{i=1}^{n} x_i\right)^2$ (d) none of these
- Let $S=\{1, 2, 3, 4\}$. The total number of unordered pairs of disjoint subsets of S is equal to
- (b) 34
- (d) 41
- Let $P = \{\theta : \sin \theta \cos \theta = \sqrt{2} \cos \theta\}$ and
 - $Q = \{\theta : \sin \theta + \cos \theta = \sqrt{2} \sin \theta\}$ be two sets. Then (2011)
 - (a) $P \subset Q$ and $Q P \neq \emptyset$ (b) $Q \not\subset P$
 - (c) P ⊄ Q
- (d) P = Q

MCQs with One or More than One Correct

- In a college of 300 students every student reads 5 newspapers and every newspaper is read by 60 students. (1998 - 2 Marks) The number of newpapers is
 - (a) at least 30
- (b) at most 20
- (c) exactly 25
- (d) none of these
- Let S_1, S_2, \ldots be squares such that for each $n \ge 1$, the length of a side of S_n equals the length of a diagonal of S_{n+1} . If the length of a side of S_1 is 10 cm, then for which of the following values of n is the area of S_n less than 1 sq. cm? (1999 - 3 Marks)

(a) 210

- (d) 10
- Let $S = \{1, 2, 3, ..., 9\}$. For k = 1, 2, ..., 5, let N_k be the number of subsets of S, each containing five elements out of which exactly k are odd. Then $N_1 + \bar{N_2} + N_3 + N_4 + N_5 =$

(Jee Adv. 2017) (d) 126

E Subjective Problems

(b) 252

An investigator interviewed 100 students to determine their preferences for the three drinks: milk (M), coffee (C) and tea (T). He reported the following: 10 students had all the three drinks M, C and T; 20 had M and C; 30 had C and T; 25 had M and T; 12 had M only; 5 had C only; and 8 had T only. Using a Venn diagram find how many did not take any of the three drinks (1978)

- Construct a triangle with base 9 cm and altitude 4 cm, 2. the ratio of the other two sides being 2:1.
 - (b) Construct a triangle in which the sum of the three sides is 15 cm with base angles 60° and 45°. Justify your (1979)steps.
- A tent is made in the form of a frustrum A of a right circular cone surmounted by another right circular cone B. The diameter of the ends of the frustrum A are 8 m and 4 m, its height is 3 m and the height of the cone B is 2 m. Find the area of the canvas required.
- In calculating the mean and variance of 10 readings, a student wrongly used the figure 52 for the correct figure of 25. He obtained the mean and variance as 45.0 and 16.0 respectively. Determine the correct mean and variance.

- The diameter PQ of a semicircle is 6 cm. Construct a square 5. ABCD with points A, B on the circumference, and the side CD on the diameter PQ. Describe briefly the method of construction.
- C and D are any two points on the same side of a line L. 6. Show how to find a point P on the line L such that PC and PD are equally inclined to the line L. Justify your steps.

- Set A has 3 elements, and set B has 6 elements. What 7. can be the minimum number of elements in the set $A \cup B$?
 - (ii) P, Q, R are subsets of a set A. Is the following equality true? $R \times (P^c \cup Q^c)^c = (R \times P) \cap (R \times Q)$? (1980)

(iii) For any two subset X and Y of a set A define $X \circ Y = (X^c \cap Y) \cup (X \cap Y^c)$

Then for any three subsets X, Y and Z of the set A, is the following equality true.

 $(X \circ Y) \circ Z = X \circ (Y \circ Z)$? Suppose A_1 , A_2 , A_{30} are thirty sets each with five elements and B_1 , B_2 , B_n are n sets each with three

elements. Let $\bigcup_{i=1}^{30} A_i = \bigcup_{j=1}^{n} B_j = S$. Assume that each

element of S belongs to exactly ten of the Ai's and to exactly (1981 - 2 Marks) nine of the Bj's. Find n.

The mean square deviations of a set of observations

 x_1, x_2, \dots, x_n about a points c is defined to be $\frac{1}{n} \sum_{i=1}^{n} (x_1 - c)^2$. The mean sugare deviations about -1 and +1 of a set of

observatons are 7 and 3 respectively. Find the standard deviation of this set of observations. (1981 - 2 Marks) The marks obtained by 40 students are grouped in a frequency table in class intervals of 10 maks each. The mean and the variance obtained from this distribution are found to be 40 and 49 respectively. It was later discovered that two observations belonging to the class interval (21-30) were included in the class interval (31-40) by mistake. Find the

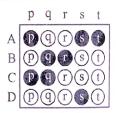
mean and the variance after correcting the error. (1982 - 3 Marks)

A relation R on the set of complex numbers is defined by $z_1 R z_2$ if and only if $\frac{z_1 - z_2}{z_1 + z_2}$ is real. Show that R is an (1982 - 2 Marks) equivalence relation.

Match the Following

Each question contains statements given in two columns, which have to be matched. The statements in Column-I are labelled A, B, C and D, while the statements in Column-II are labelled p, q, r, s and t. Any given statement in Column-I can have correct matching with ONE OR MORE statement(s) in Column-II. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A-p, s and t; B-q and r; C-p and q; and D-s then the correct darkening of bubbles will look like the given.



(2011)

Match the statements given in Column-I with the intervals/union of intervals given in Column-II. 1.

Column-II

(A) The set
$$\left\{ \text{Re}\left(\frac{2iz}{1-z^2}\right) : z \text{ is a complex number, } |z| = 1 \ z \neq \pm 1 \right\} \text{ is}$$

(p)
$$(-\infty, -1) \cup (1, \infty)$$

(B) The domain of the function
$$f(x) = \sin^{-1}\left(\frac{8(3)^{x-2}}{1-3^{2(x-1)}}\right)$$
 is

(q)
$$(-\infty, -0) \cup (0, \infty)$$

(C) If
$$f(\theta) = \begin{vmatrix} 1 & \tan \theta & 1 \\ -\tan \theta & 1 & \tan \theta \\ -1 & -\tan \theta & 1 \end{vmatrix}$$
, then the set $\left\{ f(\theta) : 0 \le \theta < \frac{\pi}{2} \right\}$ is (r) $[2, \infty)$

(s)
$$(-\infty, -1] \cup [1, \infty)$$

(D) If
$$f(x) = x^{3/2} (3x - 10)$$
, $x \ge 0$ then $f(x)$ is increasing in

(t)
$$(-\infty,0] \cup [2,\infty)$$

Integer Value Correct Type

The value of $6 + \log_{\frac{3}{2}} \left(\frac{1}{3\sqrt{2}} \sqrt{4 - \frac{1}{3\sqrt{2}}} \sqrt{4 - \frac{1}{3\sqrt{2}}} \sqrt{4 - \frac{1}{3\sqrt{2}}} \dots \right)$ is (2012)

Section-B JEE Main / AIEEE

- In a class of 100 students there are 70 boys whose average marks in a subject are 75. If the average marks of the complete class is 72, then what is the average of the girls?
 - (a) 73
- (b) 65
- (c) 68
- (d) 74
- The sum of two forces is 18 N and resultant whose direction is at right angles to the smaller force is 12 N. The magnitude of the two forces are [2002]
 - (a) 13,5
- (b) 12,6
- (c) 14,4
- (d) 11,7
- A bead of weight w can slide on smooth circular wire in a 3. vertical plane. The bead is attached by a light thread to the highest point of the wire and in equilibrium, the thread is taut and make an angle θ with the vertical then tension of the thread and reaction of the wire on the bead are
 - (a) $T = w \cos \theta$
- $R = w \tan A$
- [2002]

- (b) $T = 2w \cos \theta$
- R = w
- (c) T = w
- $R = w \sin \theta$
- (d) $T = w \sin \theta$
- $R = w \cot \theta$
- The median of a set of 9 distinct observations is 20.5. If each of the largest 4 observations of the set is increased by 2, then the median of the new set 120031
 - (a) remains the same as that of the original set
 - (b) is increased by 2
 - (c) is decreased by 2
 - (d) is two times the original median.
- A couple is of moment \vec{G} and the force forming the couple is \vec{P} . If \vec{P} is turned through a right angle the moment of the couple thus formed is \vec{H} . If instead , the force \vec{P} are turned through an angle a, then the moment of couple [2003] becomes

 - (a) $\vec{H} \sin \alpha \vec{G} \cos \alpha$ (b) $\vec{G} \sin \alpha \vec{H} \cos \alpha$
 - (c) $\vec{H} \sin \alpha + \vec{G} \cos \alpha$ (d) $\vec{G} \sin \alpha + \vec{H} \cos \alpha$.
- The resultant of forces \vec{P} and \vec{Q} is \vec{R} . If \vec{Q} is doubled then \vec{R} is doubled. If the direction of \vec{Q} is reversed, then \vec{R} is again doubled. Then $P^2: Q^2: R^2$ is
 - [2003]

- (a) 2:3:1 (b) 3:1:1 (c) 2:3:2
- (d) 1:2:3
- A body travels a distance s in t seconds. It starts from rest and ends at rest. In the first part of the journey, it moves

with constant acceleration f and in the second part with constant retardation r. The value of t is given by

(a)
$$\sqrt{2s\left(\frac{1}{f} + \frac{1}{r}\right)}$$

(b) $2s \left(\frac{1}{f} + \frac{1}{r} \right)$

[2003]

(c)
$$\frac{2s}{\frac{1}{f} + \frac{1}{r}}$$

- (d) $\sqrt{2}$
- Two stones are projected from the top of a cliff h metres high, with the same speed u, so as to hit the same spot. If one of the stones is projected. izontally and the other is projected horizonally and are other is projected at an angle θ to the proportion tan θ equals

(a)
$$u\sqrt{\frac{2}{gh}}$$
 (b) $\sqrt{\frac{2u}{gh}}$ (c) $2g\sqrt{\frac{u}{h}}$ (d) $2h\sqrt{\frac{u}{g}}$

- Two particles start simultaneously from the same point and move along two straight lines, one with uniform velocity \vec{u} and the other from rest with uniform acceleration

 \vec{f} . Let α be the angle between their directions of motion. The relative velocity of the second particle w.r.t. the first is least after a time [2003]

- (a) $\frac{u\cos\alpha}{f}$ (b) $\frac{u\sin\alpha}{f}$ (c) $\frac{f\cos\alpha}{u}$ (d) $u\sin\alpha$

- 10. The upper $\frac{3}{4}$ th portion of a vertical pole subtends an

angle $\tan^{-1} \frac{3}{5}$ at a point in the horizontal plane through its

foot and at a distance 40 m from the foot. A possible height of the vertical pole is [2003]

- (a) 80 m
- (b) 20 m
- (c) 40 m
- (d) 60 m.
- Let R_1 and R_2 respectively be the maximum ranges up and down an inclined plane and R be the maximum range on the horizontal plane. Then R_1, R, R_2 are in [2003]
 - (a) H.P
- (b) A.G.P
- (c) A.P
- (d) G.P.

In an experiment with 15 observations on x, the following results were available:

$$\Sigma x^2 = 2830, \ \Sigma x = 170$$

One observation that was 20 was found to be wrong and was replaced by the correct value 30. The corrected [2003] variance is

(a) 8.33

- (b) 78.00
- (c) 188.66
- (d) 177.33
- Let $R = \{(1,3),(4,2),(2,4),(2,3),(3,1)\}$ be a relation on the 120041 set $A = \{1, 2, 3, 4\}$.. The relation R is
 - (a) reflexive
- (b) transitive
- (c) not symmetric
- (d) a function
- Consider the following statements:
 - (A) Mode can be computed from histogram
 - (B) Median is not independent of change of scale
 - (C) Variance is independent of change of origin and scale. Which of these is / are correct?
 - (a) (A), (B) and (C)
- (b) only (B)
- (c) only (A) and (B)
- (d) only (A)
- In a series of 2 n observations, half of them equal a and remaining half equal -a. If the standard deviation of the observations is 2, then |a| equals.
 - (a) $\frac{\sqrt{2}}{}$
- (b) $\sqrt{2}$

(c) 2

- (d) $\frac{1}{}$
- With two forces acting at point, the maximum affect is obtained when their resultant is 4N. If they act at right angles, then their resultant is 3N. Then the forces are
 - (a) $\left(2+\frac{1}{2}\sqrt{3}\right)N$ and $\left(2-\frac{1}{2}\sqrt{3}\right)N$

[2004]

- (b) $(2+\sqrt{3})N$ and $(2-\sqrt{3})N$
- (c) $\left(2+\frac{1}{2}\sqrt{2}\right)N$ and $\left(2-\frac{1}{2}\sqrt{2}\right)N$
- (d) $(2+\sqrt{2})N$ and $(2-\sqrt{2})N$
- In a right angle $\triangle ABC$, $\angle A = 90^{\circ}$ and sides a, b, c are respectively, 5 cm, 4 cm and 3 cm. If a force \vec{F} has moments 0, 9 and 16 in N cm. units respectively about vertices A, B and C, then magnitude of \vec{F} is [2004]
 - (a) 9

(c) 5

(d) 3

- Three forces \vec{P}, \vec{Q} and \vec{R} acting along IA, IB and IC, where I is the incentre of a $\triangle ABC$ are in equilibrium. Then $\vec{P}: \vec{Q}: \vec{R}$
 - (a) $\cos ec \frac{A}{2} : \csc \frac{B}{2} : \csc \frac{C}{2}$
 - (b) $\sin \frac{A}{2} : \sin \frac{B}{2} : \sin \frac{C}{2}$
 - (c) $\sec \frac{A}{2} : \sec \frac{B}{2} : \sec \frac{C}{2}$
 - (d) $\cos \frac{A}{2} : \cos \frac{B}{2} : \cos \frac{C}{2}$
- 19. A paticle moves towards east from a point A to a point B at the rate of 4 km/h and then towards north from B to C at the rate of 5km/hr. If AB = 12 km and BC = 5 km, then its average speed for its journey from A to C and resultant average velocity direct from A to C are respectively
 - (a) $\frac{13}{9}$ km/h and $\frac{17}{9}$ km/h
 - (b) $\frac{13}{4}$ km/h and $\frac{17}{4}$ km/h
 - (c) $\frac{17}{9}$ km/h and $\frac{13}{9}$ km/h
 - (d) $\frac{17}{4}$ km/h and $\frac{13}{4}$ km/h
- 20. A velocity $\frac{1}{4}$ m/s is resolved into two components along OA and OB making angles 30° and 45° respectively with the given velocity. Then the component along OB is
 - (a) $\frac{1}{9}(\sqrt{6}-\sqrt{2})$ m/s (b) $\frac{1}{4}(\sqrt{3}-1)$ m/s
 - (c) $\frac{1}{4}$ m/s
- (d) $\frac{1}{9}$ m/s
- 21. If t_1 and t_2 are the times of flight of two particles having the same initial velocity u and range R on the horizontal, then $t_1^2 + t_2^2$ is equal to
 - (a) 1

- (b) $4u^2/g^2$
- (c) $u^2/2g$
- (d) u^2/g

MISCELLANEOUS (Sets, Relations, Statistics & Mathematical Reasoning)

- 22. Let $R = \{(3, 3), (6, 6), (9, 9), (12, 12), (6, 12), (3, 9), (12, 12), (12, 12), (13, 12), (14, 12), (15, 12),$ (3, 12), (3, 6)} be a relation on the set $A = \{3, 6, 9, 12\}$. The relation is [2005]
 - (a) reflexive and transitive only
 - (b) reflexive only
 - (c) an equivalence relation
 - (d) reflexive and symmetric only
- 23. ABC is a triangle. Forces \overrightarrow{P} , \overrightarrow{Q} , \overrightarrow{R} acting along IA, IB, and IC respectively are in equilibrium, where I is the incentre of $\triangle ABC$. Then P: O: R is
 - (a) $\sin A : \sin B : \sin C$ (b) $\sin \frac{A}{2} : \sin \frac{B}{2} : \sin \frac{C}{2}$
 - (c) $\cos \frac{A}{2}$: $\cos \frac{B}{2}$: $\cos \frac{C}{2}$ (d) $\cos A$: $\cos B$: $\cos C$
- 24. If in a frequency distribution, the mean and median are 21 and 22 respectively, then its mode is approximately [2005]
 - (a) 22.0
- (b) 20.5
- (c) 25.5
- A lizard, at an initial distance of 21 cm behind an insect, moves from rest with an acceleration of $2 cm/s^2$ and pursues the insect which is crawling uniformly along a straight line at a speed of 20 cm/s. Then the lizard will catch the insect after [2005]
 - (a) 20 s
- (b) 1 s
- (c) 21s
- (d) 24s
- Two points A and B move from rest along a straight line with constant acceleration f and f' respectively. If A takes m sec. more than B and describes 'n'units more than B in acquiring the same speed then
 - (a) $(f f')m^2 = ff'n$ (b) $(f + f')m^2 = ff'n$
 - (c) $\frac{1}{2}(f+f')m = ff'n^2$ (d) $(f'-f)n = \frac{1}{2}ff'm^2$
- A and B are two like parallel forces. A couple of moment H lies in the plane of A and B and is contained with them. The resultant of A and B after combining is displaced through a distance
 - (a) $\frac{2H}{A-B}$
- (b) $\frac{H}{A+B}$
- [2005]
- (c) $\frac{H}{2(A+B)}$ (d) $\frac{H}{A-B}$
- 28. Let x_1, x_2, \dots, x_n be n observations such that $\sum x_i^2$ = 400 and $\sum x_i$ = 80. Then the possible value of n among the following is [2005]
 - (a) 15
- (b) 18
- (c) 9
- (d) 12

- A particle is projected from a point O with velocity u at an angle of 60° with the horizontal. When it is moving in a direction at right angles to its direction at O, its velocity then is given by

- $\frac{u}{3}$ (b) $\frac{u}{2}$ (c) $\frac{2u}{3}$ (d) $\frac{u}{\sqrt{3}}$

M-183

- The resultant R of two forces acting on a particle is at right angles to one of them and its magnitude is one third of the other force. The ratio of larger force to the smaller one is [2005]
 - (a) 2:1
- (b) $3:\sqrt{2}$ (c) 3:2
- (d) $3:2\sqrt{2}$
- 31. ABC is a triangle, right angled at A. The resultant of the

forces acting along \overline{AB} , \overline{BC} with magnitudes $\frac{1}{AB}$ and $\frac{1}{AC}$

respectively is the force along \overline{AD} , where D is the foot of the perpedicular from A onto BC. The magnitude of the resultant is

- (a) $\frac{AB^2 + AC^2}{(AB)^2 (AC)^2}$ (b) $\frac{(AB)(AC)}{AB + AC}$
- (c) $\frac{1}{AB} + \frac{1}{AC}$
- Let W denote the words in the English dictionary. Define the relation R by $R = \{(x, y) \in W \times W | \text{ the words } x \text{ and } y \text{ have} \}$ at least one letter in common.} Then R is
 - (a) not reflexive, symmetric and transitive [2006]
 - (b) relexive, symmetric and not transitive
 - (c) reflexive, symmetric and transitive
 - (d) reflexive, not symmetric and transitive
- Suppose a population A has 100 observations 101, 102,, 200 and another population B has 100 obsevrations

of the two populations, respectively then $\frac{V_A}{V_B}$ is [2006]

- (b) $\frac{9}{4}$ (c) $\frac{4}{9}$ (d) $\frac{2}{3}$
- A particle has two velocities of equal magnitude inclined to each other at an angle θ . If one of them is halved, the angle between the other and the original resultant velocity is bisected by the new resultant. Then θ is [2006]
- (b) 120°
- (c) 45°
- A body falling from rest under gravity passes a certain point P. It was at a distance of 400 m from P, 4s prior to passing through P. If $g = 10m/s^2$, then the height above the point

P from where the body began to fall is [2006]

- (a) 720m (b) 900m
- (c) 320m (d) 680m

	for a first of the
26	The resultant of two forces Pn and $3n$ is a force of $7n$. If the
36.	The resultant of the state of t
	direction of $3n$ force were reversed, the resultant would be
	direction of sit

 $\sqrt{19} n$. The value of P is

[2007]

- (a) 3n
- (b) 4 n
- (c) 5 n
- (d) 6 n.
- A particle just clears a wall of height b at a distance a and strikes the ground at a distance c from the point of projection. The angle of projection is
 - (a) $\tan^{-1} \frac{bc}{a(c-a)}$ (b) $\tan^{-1} \frac{bc}{a}$
 - (c) $\tan^{-1} \frac{b}{a}$
- The average marks of boys in class is 52 and that of girls is 42. The average marks of boys and girls combined is 50. The [2007] percentage of boys in the class is
 - (a) 80
- (b) 60
- (c) 40
- (d) 20.
- A body weighing 13 kg is suspended by two strings 5m and 39. 12m long, their other ends being fastened to the extremities of a rod 13m long. If the rod be so held that the body hangs immediately below the middle point, then tensions in the strings are
 - (a) 5 kg and 12 kg
- (b) 5 kg and 13 kg
- (c) 12 kg and 13 kg
- (d) 5 kg and 5 kg
- The mean of the numbers a, b, 8, 5, 10 is 6 and the variance is 6.80. Then which one of the following gives possible [2008] values of a and b?
 - (a) a = 0, b = 7
- (b) a = 5, b = 2
- (c) a=1, b=6
- (d) a = 3, b = 4
- 41. Let p be the statement "x is an irrational number", q be the statement "y is a transcendental number", and r be the statement "x is a rational number if fy is a transcendental number".

Statement-1: r is equivalent to either q or p

Statement-2: r is equivalent to $\sim (p \leftrightarrow \sim q)$.

- (a) Statement -1 is false, Statement-2 is true
- (b) Statement -1 is true, Statement -2 is true; Statement -2 is a correct explanation for Statement-1
- (c) Statement -1 is true, Statement -2 is true; Statement -2 is not a correct explanation for Statement-1
- (d) Statement -1 is true, Statement-2 is false
- The statement $p \rightarrow (q \rightarrow p)$ is equivalent to [2008]

 - (a) $p \to (p \to q)$ (b) $p \to (p \lor q)$
 - (c) $p \rightarrow (p \land q)$
- (d) $p \rightarrow (p \leftrightarrow q)$
- Statement-1: $\sim (p \leftrightarrow \sim q)$ is equivalent to $p \leftrightarrow q$.

Statement-2: $\sim (p \leftrightarrow \sim q)$ is a tautology

[2009]

- (a) Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-1.
- (b) Statement-1 is true, Statement-2 is false.
- (c) Statement-1 is false, Statement-2 is true.
- (d) Statement-1 is true, Statement-2 is true. Statement-2 is a correct explanation for statement-1

Statement-1: The variance of first n even natural numbers

is
$$\frac{n^2 - 1}{4}$$
.

Statement-2: The sum of first *n* natural numbers is $\frac{n(n+1)}{n}$

and the sum of squares of first n natural numbers j_s

$$\frac{n(n+1)(2n+1)}{6}.$$
 [2009]

- (a) Statement-1 is true, Statement-2 is true Statement-2 is not a correct explanation for Statement-
- (b) Statement-1 is true, Statement-2 is false.
- (c) Statement-1 is false, Statement-2 is true.
- (d) Statement-1 is true, Statement-2 is true. Statement-2 is a correct explanation for Statement-1.
- If A, B and C are three sets such that $A \cap B = A \cap C$ and $A \cup B = A \cup C$, then [2009]
 - (a) A = C
- (b) B = C
- (c) $A \cap B = \emptyset$
- (d) A = B
- 46. If the mean deviation of the numbers 1, 1 + d, 1 + 2d, ...1 + 100d from their mean is 255, then d is equal to: [2009]
 - (a) 20.0
- (b) 10.1
- (c) 20.2
- (d) 10.0
- 47. Let S be a non-empty subset of R. Consider the following statement:

P: There is a rational number $x \in S$ such that x > 0.

Which of the following statements is the negation of the statement P?

- (a) There is no rational number $x \in S$ such than x < 0.
- (b) Every rational number $x \in S$ satisfies x < 0.
- (c) $x \in S$ and $x \le 0 \implies x$ is not rational.
- (d) There is a rational number $x \in S$ such that $x \le 0$.
- Consider the following relations: $R = \{(x, y) | x, y \text{ are real numbers and } x = wy \text{ for some rational } x = xy \text{ for some$

number w};

$$S = \left\{ \left(\frac{m}{n}, \frac{p}{q} \right) \mid m, n, p \text{ and } q \text{ are integers such that } n, q \neq 0 \right\}$$

and qm = pn.

Then

[2010]

- (a) Neither R nor S is an equivalence relation
- (b) S is an equivalence relation but R is not an equivalence
- (c) R and S both are equivalence relations
- (d) R is an equivalence relation but S is not an equivalence relation

Let A and B two sets containing 2 elements and 4 elements

The mean of the data set comprising of 16 observations is

16. If one of the observation valued 16 is deleted and three new observations valued 3, 4 and 5 are added to the data,

(c) 16.8

IJEE M 2015

(d) 16.0

then the mean of the resultant data, is:

(b) 14.0

(a) 15.8

be 4 and 5 and the corresponding means are given to be 2

(d) Statement-1 is true, statement-2 is false.

empty is:

(a) 5^2

55. Let $X = \{1,2,3,4,5\}$. The number of different ordered pairs

(b) 3^5 (c) 2^5

(Y,Z) that can formed such that $Y \subseteq X$, $Z \subseteq X$ and $Y \cap Z$ is

respectively. The number of subsets of A × B having 3 or and 4, respectively. The variance of the combined data set [JEE M 2013] more elements is is (d) 211 (a) 256 (b) 220 57. Consider (b) 6 (a) (d) **Statement-1**: $(p \land \sim q) \land (\sim p \land q)$ is a fallacy. 50. Let R be the set of real numbers. **Statement-2**: $(p \rightarrow q) \leftrightarrow (\sim q \rightarrow \sim p)$ is a tautology. Statement-1: $A = \{(x, y) \in R \times R : y - x \text{ is an integer} \}$ is an [JEE M 2013] equivalence relation on R. (a) Statement-1 is true; Statement-2 is true; Statement-2: $B = \{(x, y) \in R \times R : x = \alpha y \text{ for some rational } \}$ Statement-2 is a correct explanation for Statement-1. number α } is an equivalence relation on R. (b) Statement-1 is true; Statement-2 is true; Statement-2 is Statement-1 is true, Statement-2 is true; Statement-2 is not a correct explanation for Statement-L not a correct explanation for Statement-1. (c) Statement-1 is true; Statement-2 is false. (b) Statement-1 is true, Statement-2 is false. (d) Statement-1 is false; Statement-2 is true. (c) Statement-1 is false, Statement-2 is true. All the students of a class performed poorly in (d) Statement-1 is true, Statement-2 is true; Statement-2 is Mathematics. The teacher decided to give grace marks of 10 a correct explanation for Statement-1. to each of the students. Which of the following statistical 51. Consider the following statements [2011] measures will not change even after the grace marks were P: Suman is brilliant [JEE M 2013] given? O: Suman is rich (b) median (a) mean R: Suman is honest (d) variance (c) mode The negation of the statement "Suman is brilliant and **59.** If $X = \{4^n - 3n - 1 : n \in N\}$ and $Y = \{9(n-1) : n \in N\}$, dishonest if and only if Suman is rich" can be expressed as (a) $\sim (O \leftrightarrow (P \land \sim R))$ (b) $\sim O \leftrightarrow \sim P \land R$ where N is the set of natural numbers, then $X \cup Y$ is equal [JEE M 2014] to: (c) $\sim (P \land \sim R) \leftrightarrow Q$ (d) $\sim P \land (Q \leftrightarrow \sim R)$ (d) Y - X(a) *X* (b) Y (c) N 52. If the mean deviation about the median of the numbers a, 60. The variance of first 50 even natural numbers is [2011] $2a,\ldots,50a$ is 50, then |a| equals [JEE M 2014] (d) 2 (c) 5 (a) 3 (b) 4 53. The negation of the statement [2012] (b) $\frac{437}{4}$ (c) $\frac{833}{4}$ (a) 437 (d) 833 "If I become a teacher, then I will open a school", is: (a) I will become a teacher and I will not open a school. **61.** The statement $\sim (p \leftrightarrow \sim q)$ is: (b) Either I will not become a teacher or I will not open a [JEE M 2014] school. (a) a tautology (b) a fallacy (c) Neither I will become a teacher nor I will open a school. (c) eqivalent to $p \leftrightarrow q$ (d) equivalent to $\sim p \leftrightarrow q$ (d) I will not become a teacher or I will open a school. 62. Let A and B be two sets containing four and two elements 54. Let x_1 , x_2 ,..., x_n be n observations, and let \overline{x} be their arithmetic mean and σ^2 be the variance. [2012] respectively. Then the number of subsets of the set A × B, each having at least three elements is: [JEE M 2015] Statement-1: Variance of $2x_1, 2x_2, ..., 2x_n$ is $4\sigma^2$. (a) 275 (b) 510 (c) 219 (d) 256 Statement-2: Arithmetic mean $2x_1, 2x_2, ..., 2x_n$ is $4\overline{x}$. The negation of $\sim s \vee (\sim r \wedge s)$ is equivalent to: (a) Statement-1 is false, Statement-2 is true. [JEE M 2015] (b) Statement-1 is true, statement-2 is true; statement-2 is a correct explanation for Statement-1. (a) $s \vee (r \vee \sim s)$ (b) s \ r (c) Statement-1 is true, statement-2 is true; statement-2 is (c) $s \wedge \sim r$ (d) $s \wedge (r \wedge \sim s)$ not a correct explanation for Statement-1.

[2012]

(d) 5^3

65. If
$$f(x) + 2f\left(\frac{1}{x}\right) = 3x$$
, $x \ne 0$ and

 $S = \{x \mid R : f(x) = f(-x)\}; \text{ then } S:$

[JEE M 2016]

- (a) contains exactly two elements.
- (b) contains more than two elements.
- (c) is an empty set.
- (d) contains exactly one element.
- The Boolean Expression $(p \land \sim q) \lor q \lor (\sim p \land q)$ is equivalent to: [JEE M 2016]
 - (a) pUq
- (b) $p \lor \sim q$ (c) $\sim p \land q$
- (d) pUq
- If the standard deviation of the numbers 2, 3, a and 11 is 3.5, then which of the following is true? [JEE M 2016]
 - (a) $3a^2 34a + 91 = 0$
- (b) $3a^2 23a + 44 = 0$
- (c) $3a^2 26a + 55 = 0$
- (d) $3a^2 32a + 84 = 0$
- A man is walking towards a vertical pillar in a straight path, at a uniform speed. At a certain point A on the path, he observes that the angle of elevation of the top of the pillar is 30°. After walking for 10 minutes from A in the same direction, at a point B, he observes that the angle of elevation of the top of the pillar is 60°. Then the time taken (in minutes) by [JEE M 2016] him, from B to reach the pillar, is:
 - (a) 20
- (b) 5
- (d) 10

69. The following statement

 $(p \rightarrow q) \rightarrow [(\sim p \rightarrow q) \rightarrow q]$ is:

[JEE M 2017]

- (a) a fallacy
- (b) a tautology
- (c) equivalent to $\sim p \rightarrow q$ (d) equivalent to $p \rightarrow \sim q$
- If $\sum_{i=1}^{9} (x_i 5) = 9$ and $\sum_{i=1}^{9} (x_i 5)^2 = 45$, then the standard

deviation of the 9 items $x_1, x_2, ..., x_9$ is:

- (a) 4
- (b) 2
- (c) 3
- (d) 9

The Boolean expression

 $\sim (p \lor q) \lor (\sim p \land q)$ is equivalent to:

[JEE M 2018]

- (a) p
- (b) q
- (c) ~q
- (d) ~p

Let $S = \{x \in R : x \ge 0 \text{ and }$

$$2|\sqrt{x}-3|+\sqrt{x}(\sqrt{x}-6)+6=0$$
. Then S: $|JEE_{M20]}$

- (a) contains exactly one element.
- (b) contains exactly two elements.
- (c) contains exactly four elements.
- (d) is an empty set.
- If the Boolean expression

$$(p \oplus q) \wedge (\sim p \odot q)$$
 is equivalent to

$$p \wedge q$$
 , where $\oplus, \odot \in \{\wedge\,, \vee\}$ then the

ordered pair (\oplus, \odot) is:

[JEE M 2019 - 9 Jan (Ma

- (a) (\vee, \wedge)
- (b) (v,v)
- (c) (\land, \lor)
- (d) (\wedge, \wedge)
- 5 students of a class have an average height 150 cm $_{\rm and}$ variance 18 cm². A new student, whose height is 156 cm joined them. The variance (in cm²) of the height of these six JEE M 2019 - 9 Jan (Ma students is:
 - (a) 16

(b) 22

(c) 20

- (d) 18
- If the standard deviation of the numbers -1, 0, 1, k is \sqrt{s} where k > 0, then k is equal to: [JEEM 2019-9 April(M)]
 - (a) $2\sqrt{6}$
- (b) $2\sqrt{\frac{10}{3}}$
- (c) $4\sqrt{\frac{5}{2}}$
- For any two statements p and q, the negation of the JEE M 2019-9 April (M) expression $p \lor (\sim p \land q)$ is:
 - (a) $\sim p \land \sim q$
- (b) $p \wedge q$
- (c) $p \leftrightarrow q$
- (d) $\sim p \vee \sim q$