# **Mathematical Induction** and Binomial Theorem

## Section-A

# JEE Advanced/ IIT-JEE

#### Fill in the Blanks

- The larger of  $99^{50} + 100^{50}$  and  $101^{50}$  is .....
  - (1982 2 Marks)
- 2. The sum of the coefficients of the plynomial  $(1 + x - 3x^2)^{2163}$ (1982 - 2 Marks)
- 3. If  $(1 + ax)^n = 1 + 8x + 24x^2 + \dots$  then  $a = \dots$  and  $n = \dots$ (1983 - 2 Marks)
- Let n be positive integer. If the coefficients of 2nd, 3rd, and 4th terms in the expansion of  $(1 + x)^n$  are in A.P., then the value of n is ..... (1994 - 2 Marks)
- The sum of the rational terms in the expansion of 5.  $(\sqrt{2} + 3^{1/5})^{10}$  is ..... (1997 - 2 Marks)

## **MCQs with One Correct Answer**

- 1. Given positive integers r > 1, n > 2 and that the coefficient of (3r)th and (r + 2)th terms in the binomial expansion of  $(1+x)^{2n}$  are equal. Then (1983 - 1 Mark)
  - (a) n=2r
- (c) n = 2r + 1
- (c) n=3r
- (d) none of these
- The coefficient of  $x^4$  in  $\left(\frac{x}{2} \frac{3}{x^2}\right)^{10}$  is (1983 1 Mark)

- (d) none of these
- The expression  $\left(x + (x^3 1)^{\frac{1}{2}}\right)^5 + \left(x (x^3 1)^{\frac{1}{2}}\right)^5$  is a
  - (1992 2 Marks) polynomial of degree (c) 7 (a) 5 (b) 6 (d) 8
- If in the expansion of  $(1+x)^m (1-x)^n$ , the coefficients of x and  $x^2$  are 3 and – 6 respectively, then m is (1999 - 2 Marks)
- For  $2 \le r \le n$ ,  $\binom{n}{r} + 2 \binom{n}{r-1} + \binom{n}{r-2} =$ (2000S)
  - (a)  $\binom{n+1}{r-1}$  (b)  $2\binom{n+1}{r+1}$  (c)  $2\binom{n+2}{r}$  (d)  $\binom{n+2}{r}$
- In the binomial expansion of  $(a-b)^n$ ,  $n \ge 5$ , the sum of the 5<sup>th</sup> and  $6^{th}$  terms is zero. Then a/b equals

- (a) (n-5)/6
- (b) (n-4)/5
- (c) 5/(n-4)
- (d) 6/(n-5)
- The sum  $\sum_{i=1}^{m} {10 \choose i} {20 \choose m-i}$ , (where  ${p \choose q} = 0$  if p < q) is
  - (2002S)maximum when m is (c) 15 (d) 20
- (b) 10 (a) 5 Coefficient of  $t^{24}$  in  $(1+t^2)^{12}(1+t^{12})(1+t^{24})$  is
- (a)  $^{12}C_6 + 3$  (b)  $^{12}C_6 + 1$  (c)  $^{12}C_6$  (d)  $^{12}C_6 + 2$  If  $^{n-1}C_r = (k^2 3) \, ^nC_{r+1}$ , then  $k \in (2004S)$
- (a)  $(-\infty, -2]$  (b)  $[2, \infty)$  (c)  $[-\sqrt{3}, \sqrt{3}]$  (d)  $(\sqrt{3}, 2]$
- The value of
  - $\binom{30}{0}\binom{30}{10} \binom{30}{1}\binom{30}{11} + \binom{30}{2}\binom{30}{12} + \dots + \binom{30}{20}\binom{30}{30}$  is where
  - $\binom{n}{r} = {}^{n}C_{r}$ (2005S)
  - (a)  $\begin{pmatrix} 30 \\ 10 \end{pmatrix}$  (b)  $\begin{pmatrix} 30 \\ 15 \end{pmatrix}$  (c)  $\begin{pmatrix} 60 \\ 30 \end{pmatrix}$  (d)  $\begin{pmatrix} 31 \\ 10 \end{pmatrix}$
- 11. For r = 0, 1, ..., 10, let  $A_r$ ,  $B_r$  and  $C_r$  denote, respectively, the coefficient of x<sup>r</sup> in the expansions of  $(1+x)^{10}$ , (2010)
  - $(1+x)^{20}$  and  $(1+x)^{30}$ . Then  $\sum_{r=1}^{10} A_r (B_{10}B_r C_{10}A_r)$  is equal to
  - (a)  $B_{10} C_{10}$ (c) 0
- (b)  $A_{10}(B^2_{10}C_{10}A_{10})$ (d)  $C_{10}-B_{10}$
- 12. Coefficient of  $x^{11}$  in the expansion of
  - $(1+x^2)^4(1+x^3)^7(1+x^4)^{12}$  is
    - (JEE Adv. 2014)
  - (a) 1051 (b) 1106
- (c) 1113
- (d) 1120

## D MCQs with One or More than One Correct

If  $C_r$  stands for  ${}^nC_r$ , then the sum of the series

$$\frac{2\left(\frac{n}{2}\right)!\left(\frac{n}{2}\right)!}{n!}\left[C_0^2 - 2C_1^2 + 3C_2^2 - \dots + (-1)^n(n+1)C_n^2\right],$$

where n is an even positive integer, is equal to

(1986 - 2 Marks)

(a) 0

- (b)  $(-1)^{n/2}(n+1)$
- (c)  $(-1)^{n/2}(n+2)$
- (d)  $(-1)^n n$
- (e) none of these.

- If  $a_n = \sum_{r=0}^n \frac{1}{{}^nC_r}$ , then  $\sum_{r=0}^n \frac{r}{{}^nC_r}$  equals (1998 2 Marks)
- (c)  $\frac{1}{2} na$
- (d) None of the above

# **Subjective Problems**

- $C_1 + 2C_2x + 3C_3x^2 + \dots + 2nC_{2n}x^{2n-1} = 2n(1+x)^{2n-1}$ 
  - where  $C_r = \frac{(2n)!}{r!(2n-r)!}$   $r = 0, 1, 2, \dots, 2n$

- Prove that  $C_1^2 2C_2^2 + 3C_3^2 \dots 2nC_{2n}^2 = (-1)^n n C_n$ . Prove that  $7^{2n} + (2^{3n-3})(3^{n-1})$  is divisible by 25 for any
- If  $(1+x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$  then show that the sum of the products of the  $C_1$ 's taken two at a time,
  - represented by  $\sum_{0 \le i < j \le n} \sum_{j \le n} C_i C_j$  is equal to  $2^{2n-1} \frac{(2n)!}{2(n!)^2}$

Use mathematical Induction to prove: If n is any odd

- positive integer, then  $n(n^2 1)$  is divisible by 24. If p be a natural number then prove that  $p^{n+1} + (p+1)^{2n-1}$
- is divisible by  $p^2 + p + 1$  for every positive integer n. (1984 - 4 Marks)
- Given  $s_n = 1 + q + q^2 + \dots + q^n$ :
  - $S_n = 1 + \frac{q+1}{2} + \left(\frac{q+1}{2}\right)^2 + \dots + \left(\frac{q+1}{2}\right)^n, q \neq 1$  Prove that
  - $^{n+1}C_1 + ^{n+1}C_2s_1 + ^{n+1}C_3s_2 + \dots + ^{n+1}C_ns_n = 2^nS_n$

Use method of mathematical induction  $2.7^n + 3.5^n - 5$  is

- divisible by 24 for all n > 0
- Prove by mathematical induction that (1987 3 Marks)
  - $\frac{(2n)!}{2^{2n}(n!)^2} \le \frac{1}{(3n+1)^{1/2}} \text{ for all positive Integers n.}$
- Let  $R = (5\sqrt{5} + 11)^{2n+1}$  and f = R [R], where [ ] denotes the greatest integer function. Prove that  $Rf = 4^{2n+4}$

Using mathematical induction, prove that (1989 - 3 Marks)  ${}^{m}C_{0}{}^{n}C_{k} + {}^{m}C_{1}{}^{n}C_{k-1} + \dots {}^{m}C_{k}{}^{n}C_{0} = {}^{(m+n)}C_{k},$ 

where m, n, k are positive integers, and  ${}^{p}C_{q} = 0$  for p < q.

Prove that

 $C_0 - 2^2 C_1 + 3^2 C_2 - \dots + (-1)^n (n+1)^2 C_n = 0$ n > 2, where  $C_{\nu} = {}^{n}C_{\nu}$ .

12. Prove that  $\frac{n^7}{7} + \frac{n^5}{5} + \frac{2n^3}{3} - \frac{n}{105}$  is an integer for every positive integer n.

Using induction or otherwise, prove that for any non-

$$\sum_{m=0}^{k} (n-m) \frac{(r+m)!}{m!} = \frac{(r+k+1)!}{k!} \left[ \frac{n}{r+1} - \frac{k}{r+2} \right]$$

14. If  $\sum_{r=0}^{2n} a_r (x-2)^r = \sum_{r=0}^{2n} b_r (x-3)^r$  and  $a_k = 1$  for all

 $k \ge n$ , then show that  $b_n = {}^{2n+1}C_{n+1}$  (1992 - 6 Marks)

- 15. Let  $p \ge 3$  be an integer and  $\alpha$ ,  $\beta$  be the roots of  $x^2 - (p+1)x + 1 = 0$  using mathematical induction show that  $\alpha^n + \beta^n$ .
  - (i) is an integer and
- (ii) is not divisible by p
- Using mathematical induction, prove that  $\tan^{-1}(1/3) + \tan^{-1}(1/7) + \dots + \tan^{-1}\{1/(n^2 + n + 1)\}\$  $= \tan^{-1} \{n/(n+2)\}\$
- 17. Prove that  $\sum_{r=1}^{k} (-3)^{r-1-3n} C_{2r-1} = 0$ , where k = (3n)/2 and

If x is not an integral multiple of  $2\pi$  use mathematical induction to prove that:

$$\cos x + \cos 2x + \dots + \cos nx = \cos \frac{n+1}{2} x \sin \frac{nx}{2} \csc \frac{x}{2}$$

Let n be a positive integer and  $(1+x+x^2)^n = a_0 + a_1 x + \dots + a_{2n} x^{2n}$ Show that  $a_0^2 - a_1^2 + a_2^2 + \dots + a_{2n}^2 = a_n$ Using mathematical induction prove that for every integer

 $n \ge 1$ ,  $(3^{2n}-1)$  is divisible by  $2^{n+2}$  but not by  $2^{n+3}$ 

(1996 - 3 Marks)

Let  $0 < A_i < \pi$  for i = 1, 2, ..., n. Use mathematical induction to prove that

$$\sin A_1 + \sin A_2 \dots + \sin A_n \le n \sin \left( \frac{A_1 + A_2 + \dots + A_n}{n} \right)$$

where  $\geq 1$  is a natural number.

{You may use the fact that

$$p\sin x + (1-p)\sin y \le \sin [px + (1-p)y],$$

where  $0 \le p \le 1$  and  $0 \le x, y \le \pi$ . (1997 - 5 Marks)

Let p be a prime and m a positive integer. By mathematical induction on m, or otherwise, prove that whenever r is an integer such that p does not divide r, p divides  $mpC_p$ ,

[**Hint:** You may use the fact that  $(1+x)^{(m+1)p} = (1+x)^p (1+x)^{mp}$ ] Let n be any positive integer. Prove that

$$\sum_{k=0}^{m} \frac{\binom{2n-k}{k}}{\binom{2n-k}{n}} \cdot \frac{(2n-4k+1)}{(2n-2k+1)} 2^{n-2k} = \frac{\binom{n}{m}}{\binom{2n-2m}{n-m}} 2^{n-2m}$$

for each non-be gatuve integer  $m \le n$ .  $\left( \operatorname{Here} \begin{pmatrix} p \\ q \end{pmatrix} = {}^{p}C_{q} \right)$ .

- 24. For any positive integer m, n (with  $n \ge m$ ), let  $\binom{n}{m} = {}^{n}C_{m}$ . Prove that  $\binom{n}{m} + \binom{n-1}{m} + \binom{n-2}{m} + \dots + \binom{m}{m} = \binom{n+1}{m+2}$  $\binom{n}{m} + 2\binom{n-1}{m} + 3\binom{n-2}{m} + \dots + (n-m+1)\binom{m}{m} = \binom{n+2}{m+2}.$
- 25. For every positive integer n, prove that  $\sqrt{(4n+1)} < \sqrt{n} + \sqrt{n+1} < \sqrt{4n+2}$ . Hence or otherwise, prove that  $[\sqrt{n} + \sqrt{(n+1)}] = [\sqrt{4n+1}]$ , where [x] denotes the greatest integer not exceeding x. (2000 - 6 Marks) 26. Let a, b, c be positive real numbers such that  $b^2 - 4ac > 0$
- and let  $\alpha_1 = c$ . Prove by induction that  $\alpha_{n+1} = \frac{a\alpha_n^2}{\left(b^2 - 2a(\alpha_1 + \alpha_2 + ... + \alpha_n)\right)}$  is well – defined and  $\alpha_{n+1} < \frac{\alpha_n}{2}$  for all n = 1, 2, ... (Here, 'well – defined' means that the denominator in the expression for  $\alpha_{n+1}$  is not zero.)
- Use mathematical induction to show that  $(25)^{n+1} - 24n + 5735$  is divisible by  $(24)^2$  for all  $n = 1, 2, \dots$ (2002 - 5 Marks) (2003 - 2 Marks) 28. Prove that
  - $2^{k} \binom{n}{0} \binom{n}{k} 2^{k-1} \binom{n}{2} \binom{n}{1} \binom{n-1}{k-1}$  $+2^{k-2}\binom{n-2}{k-2}-\dots(-1)^k\binom{n}{k}\binom{n-k}{0}=\binom{n}{k}$

- 29. A coin has probability p of showing head when tossed. It is tossed n times. Let  $p_n$  denote the probability that no two (or more) consecutive heads occur. Prove that  $p_1=1$ ,  $p_2=1-p^2$ and  $p_n = (1-p)$ .  $p_{n-1} + p(1-p) p_{n-2}$  for all  $n \ge 3$ .
  - Prove by induction on n, that  $p_n = A\alpha^n + B\beta^n$  for all  $n \ge 1$ , where  $\alpha$  and  $\beta$  are the roots of quadratic equation
  - $x^{2}$  (1-p)x-p(1-p)=0 and  $A = \frac{p^{2} + \beta 1}{\alpha\beta \alpha^{2}}$ ,  $B = \frac{p^{2} + \alpha 1}{\alpha\beta \beta^{2}}$ .

    (2000 5 Marks)

#### Integer Value Correct Type

- The coefficients of three consecutive terms of  $(1+x)^{n+5}$  are in the ratio 5:10:14. Then n =(JEE Adv. 2013)
  - Let m be the smallest positive integer such that the coefficient of  $x^2$  in the expansion of  $(1+x)^2 + (1+x)^3 + ... + (1+x)^{49} + (1+mx)^{50}$  is  $(3n+1)^{51}C_3$  for some positive integer n. Then the value of n is integer n. Then the value of n is
- $X = ({}^{10}C_1)^2 + 2({}^{10}C_2)^2 + 3({}^{10}C_3)^2 + \dots + 10({}^{10}C_{10})^2,$ where  ${}^{10}C_r$ ,  $r \in \{1, 2, \dots, 10\}$  denote binomial coefficients.
- Then, the value of  $\frac{1}{1430}$  X is \_\_\_\_\_. (JEE Adv. 2018) Suppose
  - $\det \begin{vmatrix} \sum_{k=0}^{n} k & \sum_{k=0}^{n} {}^{n}C_{k}k^{2} \\ \sum_{k=0}^{n} {}^{n}C_{k}k & \sum_{k=0}^{n} {}^{n}C_{k}3^{k} \end{vmatrix} = 0$

holds for some positive integer n. The  $\sum_{k=0}^{n} {n \choose k}$  equals (JEE Adv. 2019)

# Section-B

- The coefficients of  $x^p$  and  $x^q$  in the expansion of  $(1+x)^{p+q}$ 
  - (a) equal
  - (b) equal with opposite signs
  - (c) reciprocals of each other
  - (d) none of these
- If the sum of the coefficients in the expansion of  $(a + b)^n$  is 4096, then the greatest coeficient in the expansion is
- (a) 1594 (b) 792 (c) 924 (d) 2924The positive integer just greater than  $(1 + 0.0001)^{10000}$  is
- (c) 2 r and n are positive integers r > 1, n > 2 and coefficient of r and n are positive integers r > 1, n = 2 and n = n = n are (r+2)<sup>th</sup> term and 3r<sup>th</sup> term in the expansion of  $(1+x)^{2n}$  are [2002]
- equal, then n equals (a) 3r (b) 3r+1 (c) 2r
- If  $a_n = \sqrt{7 + \sqrt{7 + \sqrt{7 + \dots}}}$  haing n radical signs then by methods of mathematical induction which is true [2002]
  - (a)  $a_n > 7 \forall n \ge 1$
- (b)  $a_n < 7 \ \forall \ n \ge 1$
- (d)  $a_n < 3 \ \forall \ n \ge 1$
- (c)  $a_n < 4 \ \forall \ n \ge 1$  (d)  $a_n < 3 \ \forall \ n \ge 1$ If x is positive, the first negative term in the expansion of
  - 120031  $(1+x)^{27/5}$  is
  - (a) 6th term (b) 7th term (c) 5th term (d) 8th term.

- The number of integral terms in the expansion of
  - $(\sqrt{3} + \sqrt[8]{5})^{256}$  is (a) 35 (b) 32
- (c) 33 (d) 34
- Let  $S(K) = 1 + 3 + 5... + (2K 1) = 3 + K^2$ . Then which of the following is true
  - Principle of mathematical induction can be used to prove the formula
  - (b)  $S(K) \Rightarrow S(K+1)$
  - (c)  $S(K) \Rightarrow S(K+1)$
  - (d) S(1) is correct
- The coefficient of the middle term in the binomial expansion in powers of x of  $(1 + \alpha x)^4$  and of  $(1 - \alpha x)^6$  is the same if  $\alpha$ equals

- (a)  $\frac{3}{5}$  (b)  $\frac{10}{3}$  (c)  $\frac{-3}{10}$  (d)  $\frac{-5}{3}$ 10. The coefficient of  $x^n$  in expansion of  $(1+x)(1-x)^n$  is
  - (a)  $(-1)^{n-1}n$
- (b)  $(-1)^n (1-n)$
- (c)  $(-1)^{n-1}(n-1)^2$  (d) (n-1)
- 11. The value of  ${}^{50}C_4 + \sum_{10}^{6} {}^{56}C_{10} = 0$  is The value of  ${}^{50}C_4 + \sum_{r=1}^{56} {}^{56}C_r C_3$  is [20]
  (a)  ${}^{55}C_4$  (b)  ${}^{55}C_3$  (c)  ${}^{56}C_3$  (d)  ${}^{56}C_4$

- If  $A = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix}$  and  $I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ , then which one of the following holds for all  $n \ge 1$ , by the principle of mathematical induction
- (b)  $A^n = 2^{n-1}A (n-1)I$
- (c)  $A^n = nA + (n-1)I$
- (d)  $A^n = 2^{n-1} A + (n-1) I$
- If the coefficient of  $x^7$  in  $\left[ax^2 + \left(\frac{1}{bx}\right)\right]^{11}$  equals the

coefficient of  $x^{-7}$  in  $\left[ax - \left(\frac{1}{bx^2}\right)\right]^{11}$ , then a and b satisfy

- (a) a b = 1
- (b) a+b=1

- If x is so small that  $x^3$  and higher powers of x may be

neglected, then  $\frac{(1+x)^{\frac{3}{2}} - \left(1 + \frac{1}{2}x\right)^3}{(1-x)^{\frac{1}{2}}}$  may be approximated as

(a)  $1 - \frac{3}{2}x^2$  (b)  $3x + \frac{3}{8}x^2$  [2005]

- (c)  $-\frac{3}{9}x^2$
- If the expansion in powers of x of the function  $\frac{1}{(1-ax)(1-bx)}$  is  $a_0 + a_1x + a_2x^2 + a_3x^3$ ..... then  $a_n$  is
  - (a)  $\frac{b^n a^n}{b a}$
- (b)  $\frac{a^n b^n}{b a}$ [2006]

- For natural numbers m, n if  $(1-y)^m (1+y)^n = 1 + a_1 y + a_2 y^2 + \dots$  and  $a_1 = a_2 = 10$ , then (m, n) is (a) (20, 45) (b) (35, 20)
  - (c) (45,35)
- (d) (35,45)
- In the binomial expansion of  $(a-b)^n$ ,  $n \ge 5$ , the sum of  $5^{th}$ and 6th terms is zero, then a/b equals
  - (a)  $\frac{n-5}{6}$  (b)  $\frac{n-4}{5}$  (c)  $\frac{5}{n-4}$  (d)  $\frac{6}{n-5}$ .
- The sum of the series  $^{20}C_0 - ^{20}C_1 + ^{20}C_2 - ^{20}C_3 + \dots + ^{20}C_{10}$  is

  - (a) 0 (b)  ${}^{20}C_{10}$  (c)  ${}^{-20}C_{10}$  (d)  $\frac{1}{2}{}^{20}C_{10}$
- Statement -1:  $\sum_{r=0}^{n} (r+1)^{-n} C_r = (n+2)2^{n-1}$ .

Statement-2:  $\sum_{r=0}^{n} (r+1)^{-n} C_r x^r = (1+x)^n + nx(1+x)^{n-1}$ 

- (a) Statement -1 is false, Statement-2 is true
- (b) Statement -1 is true, Statement-2 is true; Statement -2 is a correct explanation for Statement-1
- Statement -1 is true, Statement-2 is true; Statement -2 is not a correct explanation for Statement-1
- (d) Statement -1 is true, Statement-2 is false

- The remainder left out when  $8^{2n} (62)^{2n+1}$  is divided by 9
  - (b) 7 (a) 2

- 21. Let  $S_1 = \sum_{j=1}^{10} j(j-1)^{10} C_j$ ,  $S_2 = \sum_{j=1}^{10} j^{10} C_j$  and  $S_3 = \sum_{j=1}^{10} j^{2} {}^{10} C_j$ .

Statement-1:  $S_3 = 55 \times 2^9$ . Statement-2:  $S_1 = 90 \times 2^8$  and  $S_2 = 10 \times 2^8$ . [2010] (a) Statement -1 is true, Statement -2 is true; Statement -2

- is not a correct explanation for Statement -1.
- Statement -1 is true, Statement -2 is false.
- Statement -1 is false, Statement -2 is true
- Statement 1 is true, Statement 2 is true; Statement -2 is a correct explanation for Statement -1.
- The coefficient of  $\hat{x}^7$  in the expansion of  $(1-x-x^2+x^3)^6$  is
  - (a) -132 (b) -144
- (c) 132
- If *n* is a positive integer, then  $(\sqrt{3}+1)^{2n}-(\sqrt{3}-1)^{2n}$  is:
  - (a) an irrational number
  - (b) an odd positive integer
  - (c) an even positive integer
  - (d) a rational number other than positive integers
- The term independent of x in expansion of

- $(1+ax+bx^2)(1-2x)^{18}$  in powers of x are both zero, then (a, b) is equal to:
  - (a)  $\left(14, \frac{272}{3}\right)$  (b)  $\left(16, \frac{272}{3}\right)$  (c)  $\left(16, \frac{251}{3}\right)$  (d)  $\left(14, \frac{251}{3}\right)$
- The sum of coefficients of integral power of x in the binomial expansion  $(1-2\sqrt{x})^{50}$  is: [JEE M 2015]
  - (a)  $\frac{1}{2}(3^{50}-1)$
- (b)  $\frac{1}{2}(2^{50}+1)$
- (c)  $\frac{1}{2}(3^{50}+1)$
- (d)  $\frac{1}{2}(3^{50})$
- If the number of terms in the expansion of  $\left(1 \frac{2}{x} + \frac{4}{\sqrt{2}}\right)^n$ ,  $x \neq 0$ , is 28, then the sum of the coefficients of all the terms in this expansion, is: [JEEM 2016] (a) 243 (c) 64
- (b) 729 28. The value of
  - $({}^{21}C_1 {}^{10}C_1) + ({}^{21}C_2 {}^{10}C_2) + ({}^{21}C_3 {}^{10}C_3) + ({}^{21}C_4 {}^{10}C_4)$
- - +....+ $(^{21}C_{10} ^{10}C_{10})$  is: (a)  $2^{20} - 2^{10}$ (c)  $2^{21} - 2^{10}$
- (b)  $2^{21} 2^{11}$ (d)  $2^{20} 2^9$

- 29. The sum of the co-efficients of all odd degree terms in the expansion of

 $(x+\sqrt{x^3-1})^5+(x-\sqrt{x^3-1})^5, (x>1)$  is: [JEE M 2018]

- If the fourth term in the Binomial expansion of  $\left(\frac{2}{x} + x^{\log 8x}\right)^6$ (x > 0) is  $20 \times 8^7$ , then a value of x is: [JEE M 2019 - 9 April (M)]
  - (a)  $8^3$ (b)  $8^2$ 
    - (c) 8
- (d)  $8^{-2}$