

1. Simplify the following expression to sum of product using Tabulation Method

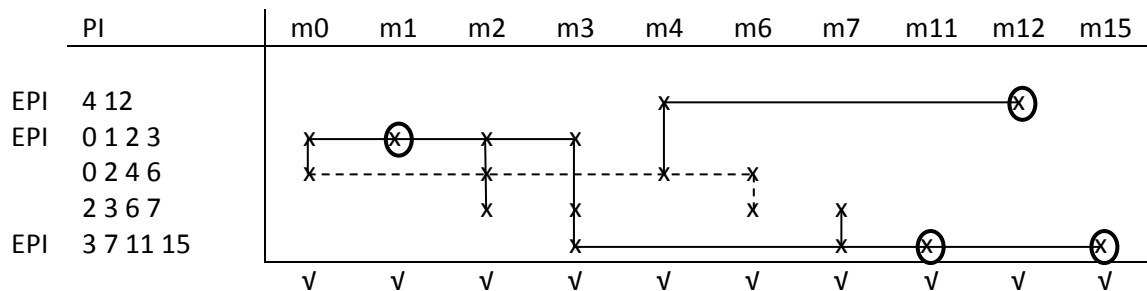
$$F(a, b, c, d) = \sum (0, 1, 2, 3, 4, 6, 7, 11, 12, 15)$$

Solution:

**a. Determination of Prime Implicants**

<b>Group 0</b>	m0: 0000	✓	(0,1) 000-	✓	<b>(0,1,2,3) 00--</b>
			(0,2) 00-0	✓	<b>(0,2,4,6) 0--0</b>
			(0,4) 0-00	✓	(0,2,1,3) 00-- redundant
					(0,4,2,6) 0--0 redundant
<b>Group 1</b>	m1: 0001	✓	(1,3) 00-1	✓	<b>(2,3,6,7) 0-1-</b>
	m2: 0010	✓	(2,3) 001-	✓	(2,6,3,7) 0-1-
	m4: 0100	✓	(2,6) 0-10	✓	
			(4,6) 01-0	✓	
			<b>(4,12) -100</b>		
<b>Group 2</b>	m3: 0011	✓	(3,7) 0-11	✓	<b>(3,7,11,15) --11</b>
	m6: 0110	✓	(3,11) -011	✓	(3,11,7,15) --11 redundant
	m12: 1100	✓	(6,7) 011-	✓	
<b>Group 3</b>	m7: 0111	✓	(7,15) -111	✓	
	m11: 1011	✓	(11,15) 1-11	✓	
<b>Group 4</b>	m15: 1111	✓			

**b. Prime Implicant Chart:**



$$f(a, b, c, d) = bc'd' + a'b' + cd + a'd'$$

2. Simplify the following expression to sum of product using Tabulation Method

$$F(a, b, c, d) = m(0,4,8,10,12,13,15) + d(1,2)$$

Solution:

**a. Determination of Prime Implicants**

Group 0	m0: 0000	✓	(0,4) 0-00	✓	<b>(0,4,8,12) -00</b>
			(0,8) -000	✓	(0,8,4,12) --00 redundant
			(0,d1) 000-		<b>(0,8,d2,10) -0-0</b>
			(0,d2) 00-0	✓	(0,d2,8,10) -0-0 redundant
<hr/>					
Group 1	m4: 0100	✓	(4,12) -100	✓	
	m8: 1000	✓	(8,10) 10-0	✓	
	d1: 0001	✓	(8,12) 1-00	✓	
	d2: 0010	✓	(d2,10) -010	✓	
<hr/>					
Group 2	m10: 1010	✓	<b>(12,13) 110-</b>		
	m12: 1100	✓			
<hr/>					
Group 3	m13: 1101	✓	<b>(13,15) 11-1</b>		
		✓			
Group 4	m15: 1111	✓			

**b. Prime Implicant Chart:**

PI	m0	m4	m8	m10	m12	m13	m15
12 13					x	x	
EPI 13 15						x	x
EPI 0 4 8 12	x	x	x		x		
EPI 0 8 d2 10	x		x	x			
	✓	✓	✓	✓	✓	✓	✓

$$f(a, b, c, d) = abd + c'd' + b'd'$$

3. Simplify the following expression to product of sum using Tabulation Method

$$F(a, b, c, d) = \prod (1, 3, 5, 7, 13, 15)$$

Solution:

**a. Determination of Prime Implicants**

Group 0					
Group 1	M1: 0001	✓	(1,3) 00-1	✓	<b>(1,3,5,7) 0--1</b>
			(1,5) 0-01	✓	(1,5,3,7) 0--1 redundant
Group 2	M3: 0011	✓	(3,7) 0-11	✓	<b>(5,7,13,15) -1-1</b>
	M5: 0101	✓	(5,7) 01-1	✓	(5,13,7,15) -1-1 redundant
			(5,13) -101	✓	
Group 3	M7: 0111	✓	(7,15) -111	✓	
	M13: 1101	✓	(13,15) 11-1	✓	
Group 4	M15: 1111	✓			

**b. Prime Implicant Chart:**

PI	M1	M3	M5	M7	M13	M15
EPI 1 3 5 7	⊗	⊗	x	x		
EPI 5 7 13 15			x	x	⊗	⊗
	✓	✓	✓	✓	✓	✓

$$f(a, b, c, d) = (a + d')(b' + d')$$

4. Simplify the following expression to product of sum using Tabulation Method

$$F(a, b, c, d) = \prod (0,8,10,12,13,15) \cdot d(1,2,3)$$

Solution:

**a. Determination of Prime Implicants**

Group 0	M0: 0000	✓	(0,8) -000	✓	<b>(0,8,d2,10) -0-0</b>
			(0,d1) 000-	✓	<b>(0,d1,d2,d3) 00--</b>
			(0,d2) 00-0	✓	(0,d2,8,10) -0-0 redundant
					(0,d2,d1,d3) 00-- redundant
Group 1	M8: 1000	✓	(8,10) 10-0	✓	
	d1: 0001	✓	<b>(8,12) 1-00</b>		
	d2: 0010	✓	(d1,d3) 00-1	✓	
			(d2,10) -010	✓	
			(d2,d3) 001-	✓	
Group 2	M10: 1010	✓	<b>(12,13) 110-</b>		
	M12: 1100	✓			
	d3: 0011	✓			
Group 3	M13: 1101	✓	<b>(13,15) 11-1</b>		
Group 4	M15: 1111	✓			

**b. Prime Implicant Chart:**

PI	M0	M8	M10	M12	M13	M15
8 12		x		x		
12 13				x	x	
EPI 13 15					x	x
EPI 0 8 d2 10	x	x	x			
0 d1 d2 d3	x					
	✓	✓	✓	✓	✓	✓

$$f(a, b, c, d) = (a' + b' + d')(b + d)(a' + b' + c)$$