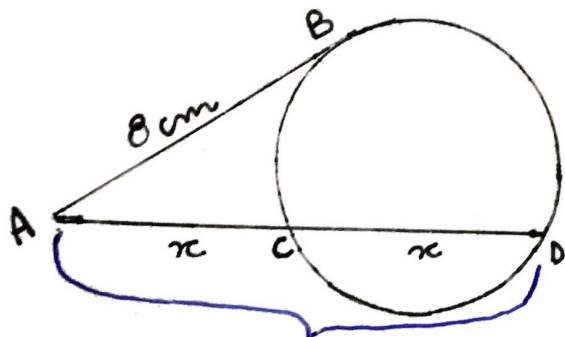


Potência de Ponto

Naihara Barboza- 317

①



$$AD = (AC + CD)$$

$$\begin{array}{r|l} 32 & 2 \\ 16 & 2 > 2 \\ 8 & 2 \\ 4 & 2 > 2 \\ 2 & 2 \\ \hline 1 & 4\sqrt{2} \end{array}$$

Pela equação da potência de ponto:

$$AB^2 = AC \cdot AD$$

$$AB = 8 \text{ cm}$$

$$AC = CD = x \quad AD = AC + CD$$

$$8^2 = x \cdot (x + x)$$

$$64 = x \cdot 2 \cdot x$$

$$64 = 2 \cdot x^2$$

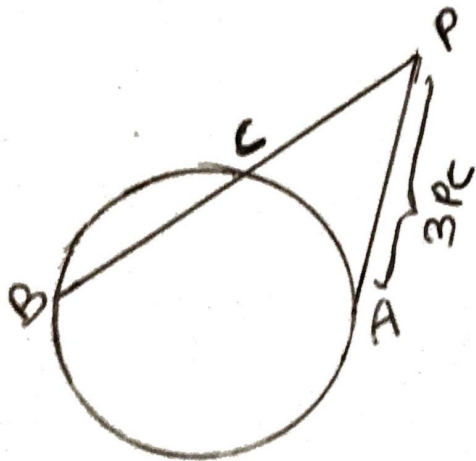
$$\frac{64}{2} = x^2$$

$$x^2 = 32$$

$$x = \sqrt{32}$$

$$x = 4\sqrt{2} \text{ cm}$$

(2)



$$AP^2 = PC * PB$$

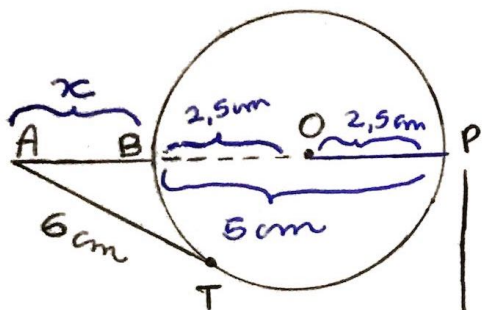
$$AP = 3PC$$

$$(3PC)^2 = PC * PB$$

$$\frac{9PC^2}{PC} = PC * PB$$

$$= 9PC = PB$$

③



O raio foi duplicado (diâmetro), para achar o segmento da secante.

$$AT^2 = AB \cdot AP$$

$$AB = x$$

$$AP = x + 5$$

$$AT^2 = x \cdot (x + 5)$$

$$6^2 = x \cdot (x + 5)$$

$$36 = x \cdot (x + 5)$$

$$36 = x^2 + 5x$$

$$x^2 + 5x - 36 = 0$$

$$\Delta = b^2 - 4a \cdot c$$

$$\Delta = 5^2 + 4 \cdot 1 \cdot (-36)$$

$$\Delta = 25 + 144$$

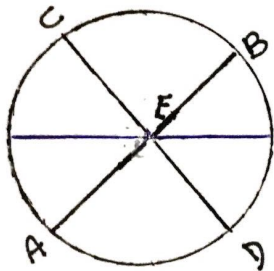
$$\Delta = 169$$

$$x = \frac{-5 \pm \sqrt{169}}{2 \cdot 1} \quad \begin{cases} x' = \frac{-5 + 13}{2} = \frac{8}{2} = 4 \\ x'' = \frac{-5 - 13}{2} = \frac{-18}{2} = -9 \end{cases}$$

↳ medida geométrica é positiva, então:

$$x = AB = 4 \text{ cm}$$

4



↳ Como o diâmetro divide a corda ao meio,
 $CE = DE$

$$CE = DE \rightarrow$$

$$AE \cdot EB = CE \cdot DE$$

$$AE \cdot EB = CE^2 \rightarrow$$

$$3 = CE^2$$

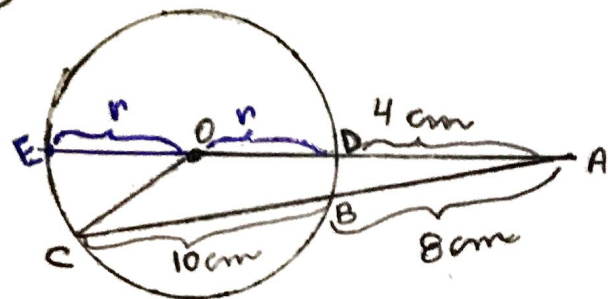
$$CE = \sqrt{3}$$

$$CD = 2CE$$

$$CD = 2\sqrt{3}$$

\overline{DE} por ser congruente foi substituído.

5



\overline{EO} = segmento para
Somar à secante.

$$DO = EO = r \quad / \quad AE = 4 + 2r \quad / \quad AC = 10 + 8 = 18$$

$$AE * AD = AC * AB$$

$$(4 + 2r) * 4 = 18 * 8$$

$$16 + 8r = 144$$

$$8r = 144 - 16$$

$$8r = 128$$

$$r = \frac{128}{8}$$

$$r = 16 \text{ cm}$$

$$OC = r = 16 \text{ cm}$$

$$AC = AB + BC = 10 + 8 = 18 \text{ cm}$$

$$OA = AD + r = 4 + 16 = 20 \text{ cm}$$

$$\text{Perímetro} = OC + AC + OA$$

$$= 16 + 18 + 20 = 54 \text{ cm}$$