

## Trasporto tronchi (alberi)

The preparations for the building of the OII<sup>1</sup> commemorative monument are starting. To free the area some trees have been cut and now they have to be loaded on a lorry to be transported to the carpentry.



Figure 1: The trees that have been cut down.

Initially the  $i$ -th tree is in position  $A_i$  and the lorry is in position 0.

Before starting the loading some trees can be pruned: pruning<sup>2</sup> a tree has a cost of  $K$  and makes the trunk smooth so that it can roll on other smooth trunks.

The trees can be moved in two ways:

- Any tree can be moved by one position towards the lorry at a cost of 1, given that the position in which it is being moved is empty.
- If immediately to the left of a pruned tree there are one or more consecutive pruned trees followed by an empty position the tree can be rolled on those (but not on non-pruned trees or the ground) until the first empty position at a cost of 1.

The lorry is always to be considered as an empty position.

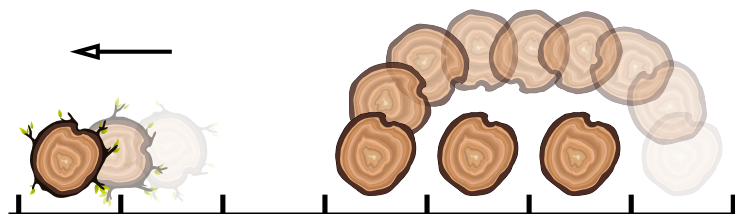


Figure 2: The two ways of moving trees.

Help the organizers determine the minimum cost to load all trees on the lorry!

<sup>1</sup>Italian Olympiads in Informatics

<sup>2</sup>Removing all branches

## Implementation

You must submit a single file with the extension `.cpp`.



Among the attachments of this task you will find a template file `alberi.cpp` with a sample implementation.

You will have to implement the following function:

C++	<code>long long carica(int N, int K, vector&lt;int&gt; A);</code>
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- The integer  $N$  represents the number of trees.
- The integer  $K$  represents the cost of pruning a tree.
- The array  $A$ , indexed from  $0$  to  $N - 1$ , contains the initial positions of the trees.
- The function must return the minimum cost to bring all trees in position  $0$ .

## Sample Grader

Among this task's attachments you will find a simplified version of the grader used during evaluation, which you can use to test your solutions locally. The sample grader reads data from `stdin`, calls the function you have to implement and writes back on `stdout` using the following format.

The input file contains 2 lines:

- Line 1: the integers  $N$  e  $K$ .
- Line 2: the integers  $A_0, \dots, A_{N-1}$ .

The output file contains one single line with the value returned by the `carica` function.

## Constraints

- $1 \leq N \leq 500\,000$
- $0 \leq K \leq 10^9$
- $1 \leq A_i \leq 10^9$  for each  $0 \leq i < N$
- $A_i < A_{i+1}$  for each  $0 \leq i < N - 1$

## Scoring

Your program will be tested against several test cases grouped in subtasks. In order to obtain the full score of a subtask, your program needs to correctly solve all of its test cases.

- **Subtask 0 [ 0 points]:** Examples.
- **Subtask 1 [11 points]:**  $K = 10^9$ .
- **Subtask 2 [17 points]:**  $K = 0$ ,  $N \leq 500$  and  $1 \leq A_i \leq 2000$  for each  $0 \leq i < N$ .
- **Subtask 3 [22 points]:**  $K = 0$ .
- **Subtask 4 [23 points]:**  $K \leq 2000$ ,  $N \leq 500$  and  $1 \leq A_i \leq 2000$  for each  $0 \leq i < N$ .
- **Subtask 5 [27 points]:** No additional limitations.

## Examples

stdin	stdout
3 2 1 5 6	11
6 3 1 4 5 10 12 14	30

## Explanation

In the **first sample case** it is optimal to prune the trees in positions 5 and 6.

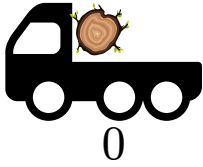


Initial situation

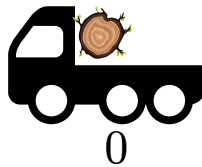


Two trees are pruned

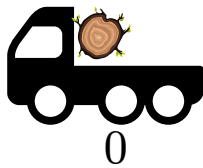
After pruning the two trees 7 moves are enough: the total cost is  $7 + 2 \cdot 2 = 11$ .



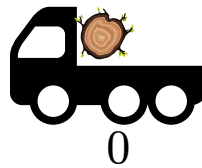
Move 1



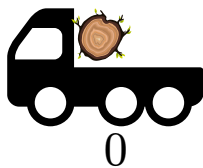
Move 2



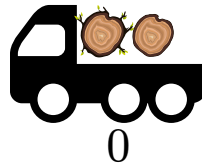
Move 3



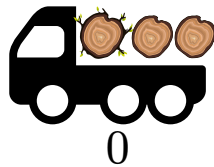
Move 4



Move 5



Move 6



Move 7 - final situation

In the **second sample case** it is optimal to prune all trees except for the first.