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%%Homework
%STUID 15307130224
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The answer is shown in paper attached in the same directory
%%Code For Question1
clear all
sigma = 1.5;
area_x =
[10+5*rand(100,1),20+5*rand(100,1),30+5*rand(100,1),40+5*rand(100,1)];
area_y =
 [10*rand(100,1),10*rand(100,1),10*rand(100,1),10*rand(100,1)];
figure(1)
plot(area_x, area_y, '.')
hold on
W=zeros(400,400);
for i = 1:400
for j = 1:400
 W(i,j) = \exp((-((area_x(i)-area_x(j))^2+(area_y(i)-area_x(j))^2))
area_y(j))^2)^0.5)/(2*sigma*sigma));
 end
end
D = zeros(400, 400);
for i = 1:400
D(i,i) = sum(W(i,:));
end
L = D - W;
L_sys = D^{(-0.5)*L*D^{(-0.5)}};
L_rw = D^(-1);
[V_{tras}, S, V] = eig(L_{sys});
value1 = S(400,400)
value2 = S(399,399)
value3 = S(398,398)
value4 = S(397,397)
U = V(:,1:4);
H = D^{(-0.5)}U;
```

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figure(2)
subplot(2,2,1); plot(H(:,1),'.');
subplot(2,2,2); plot(H(:,2),'.');
subplot(2,2,3); plot(H(:,3),'.');
subplot(2,2,4);plot(H(:,4),'.');
hold on
%%Code For Question2
clear all
sigma = 1.5;
area x =
[10+5*rand(100,1),20+5*rand(100,1),30+5*rand(100,1),40+5*rand(100,1)];
 [10*rand(100,1),10*rand(100,1),10*rand(100,1),10*rand(100,1)];
W=zeros(400,400);
for i = 1:400
 for j = 1:400
  %%Judge whether two points are in the same area
  if (i>0 && i<101 && j>0 && j<101) || (i>100 && i<201 && j>100 &&
 j<201) ||(i>200 && i<301 && j>200 && j<301)||(i>300 && i<401 && j>300
 && j<401)
   W(i,j) = \exp((-((area_x(i)-area_x(j))^2+(area_y(i)-area_x(j))^2))
area_y(j))^2)^0.5/(2*sigma*sigma));
  end
 end
end
D = zeros(400,400);
for i = 1:400
D(i,i) = sum(W(i,:));
end
L = D - W;
L_sys = D^{(-0.5)*L*D^{(-0.5)}};
L rw = D^{(-1)};
[V,S] = eig(L_sys);
[k, index] = sort(sum(S,1));
U = V(:, index(1:4));
H = D^{(-0.5)}U;
figure(3)
subplot(2,2,1); plot(H(:,1),'.')
subplot(2,2,2); plot(H(:,2),'.')
```

```
subplot(2,2,3);plot(H(:,3),'.')
subplot(2,2,4);plot(H(:,4),'.')
hold on

value1 =
    0.9990

value2 =
    0.9987

value3 =
    0.9987
```

0.9987





