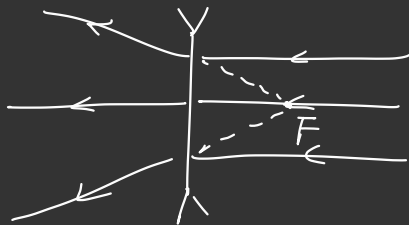


凸透镜—会聚

converging lenses

凹透镜—发散

diverging lenses

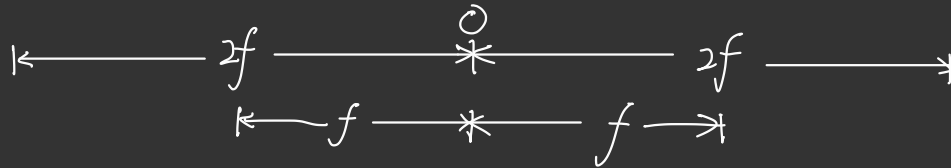


光心 optical center

主轴
principal axis

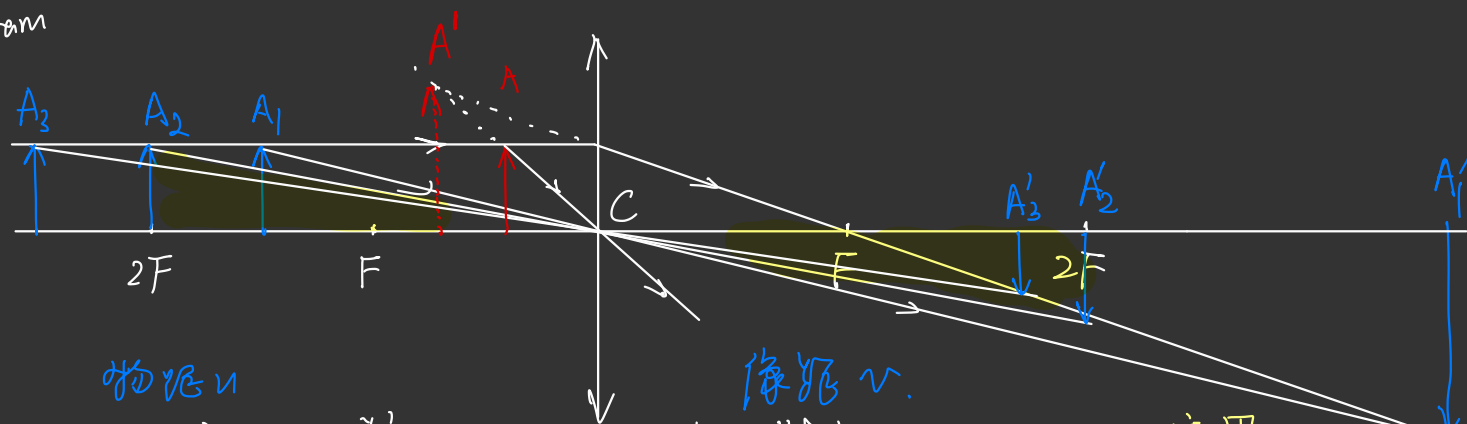
焦点
focal point

focal length
焦距



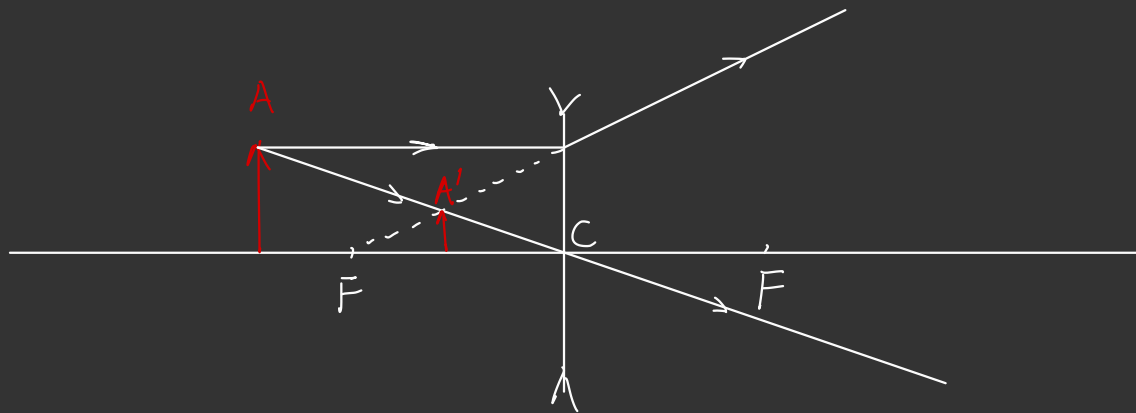
image

光路图
ray diagram



1
2
3
4
5

Object position	image position	像的特点			应用
1 $u > 2f$	$f < v < 2f$	倒立 inverted	缩小 smaller	实像 real image	照相机, 眼睛
2 $u = 2f$	$v = 2f$	倒立	等大 of same size	实像	测焦距
3 $f < u < 2f$	$v > 2f$	倒立	放大 larger	实像	幻灯机, 投影仪原理
4 $u = f$	不成像				测焦距
5 $u < f$	$v > u$	正立 upright	放大 larger	虚像 virtual	放大镜, 老花镜



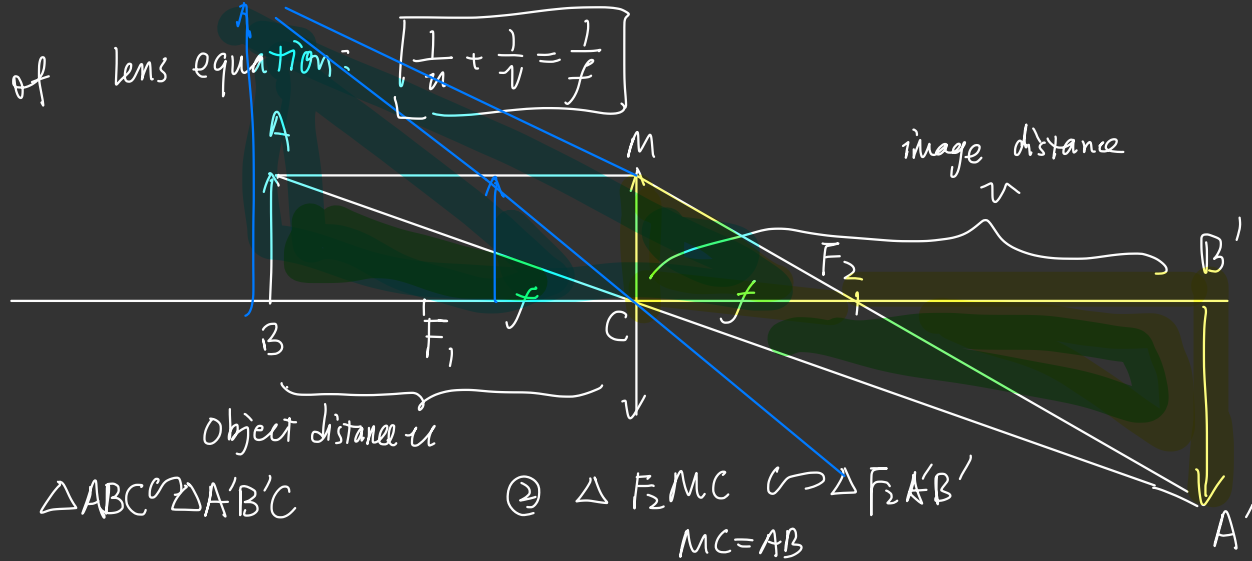
四:

$$u > v$$

正立 缩小 虚像

近视镜

Proof of lens equation: $\boxed{\frac{1}{u} + \frac{1}{v} = \frac{1}{f}}$



Proof:

①

$$\triangle ABC \sim \triangle A'B'C$$

$$\frac{BC}{AB} = \frac{B'C}{A'B'}$$

$$\frac{u}{AB} = \frac{v}{A'B'} \quad (1)$$

$$\frac{u}{v} = \frac{AB}{A'B'}$$

② $\triangle F_2MC \sim \triangle F_2A'B'$
 $MC = AB$

$$\frac{MC}{CF_2} = \frac{A'B'}{F_2B'}$$

$$\frac{AB}{f} = \frac{A'B'}{v-f} \quad (2)$$

$$\frac{AB}{A'B'} = \frac{f}{v-f}$$

$$\frac{u}{v} = \frac{f}{v-f} \Rightarrow u(v-f) = vf \Rightarrow uv - uf = vf$$

$$uv = uf + vf$$

$$\frac{uv}{f} = (u+v)$$

$$\frac{1}{f} = \frac{u+v}{uv} = \frac{u}{uv} + \frac{v}{uv} = \frac{1}{v} + \frac{1}{u} \quad \square$$

$$\boxed{\frac{1}{u} + \frac{1}{v} = \frac{1}{f}}$$

Object: image:

$$u = 2f, v = 2f$$

$$u > 2f$$

$$\frac{1}{2f} + \frac{1}{2f} = \frac{1}{f} \quad \checkmark \quad \frac{1}{2} + \frac{1}{2} = 1$$

$$\frac{1}{3f} + \frac{1}{2f} = \frac{1}{f} \quad \checkmark \quad \frac{1}{3} + \frac{1}{2} = \frac{5}{6} \neq 1$$

$$\frac{1}{4f} + \frac{1}{5f} = \frac{1}{f} \quad \checkmark \quad \frac{1}{4} + \frac{1}{5} = \frac{9}{20} \neq 1$$

$$\frac{4}{5} + \frac{1}{5} = 1$$

