Solutions — Example 5 Practice

Problem A (easier)

Ciphertext: URYYB JBEYQ; shift k = 13 (ROT13). Decrypt by $p \equiv c - 13 \pmod{26}$ (or apply ROT13 again):

HELLO WORLD

Problem B (similar)

Ciphertext: ZHOFRPH WR FODVV, unknown k.

Guess that WR is T0. Then W=22 should map to T=19, so $k\equiv 22-19\equiv 3$ and decryption uses $p\equiv c-3\pmod{26}$. Check also that FODVV becomes CLASS:

$$F(5) \to C(2), \ O(14) \to L(11), \ D(3) \to A(0), \ V(21) \to S(18), \ V(21) \to S(18).$$

Hence k = 3 and

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Problem C (harder)

 $\label{thm:conditional} {\it Ciphertext:} \ {\tt YMJ} \ {\tt VZNHP} \ {\tt GWTBS} \ {\tt KTC} \ {\tt OZRUX} \ {\tt TAJW} \ {\tt YMJ} \ {\tt QFED} \ {\tt ITL}.$

The trigram YMJ repeats and often corresponds to THE. If so,

$$Y(24) \to T(19) \Rightarrow k \equiv 24 - 19 \equiv 5$$
, so decrypt with $p \equiv c - 5 \pmod{26}$.

Applying k = 5 across the text yields:

THE QUICK BROWN FOX JUMPS OVER THE LAZY DOG

Takeaways.

- Shift ciphers preserve frequency shape; a good guess (E, T, A, O) usually cracks k.
- Decryption rule: $p \equiv c k \pmod{26}$; verify the guess by reading for sensible English.
- Longer texts make frequency clues stronger; short texts can be ambiguous, so test multiple hypotheses.