

ADVANCED DIGITAL SIGNAL PROCESSING Chapter 2: Wireless Channel

20/02/2017



Content

- Review
- Wireless Channel Overview
- Large-scale fading
 - □ Path loss
 - Shadowing
- Small-scale fading
 - Multi-path fading
 - ☐ Time variance



Frequency and Wavelength

- $= c = \lambda f$
 - c: speed of light
 - □λ: wavelength
 - ☐f: frequency
- Example:
- AM radio with frequency 1710 kHz
- What's the wavelength? Ans: 175m
- What's the period? Ans: 584 ns





Decibels

- $\square 10 \log_{10}(x)$
- Power in decibels
 - dB
 - \blacksquare Y dB=10 log₁₀ (x Watt)
- □ Power ratio in decibels
 - dB
 - Power P1, P2 in Watt
 - 10 log₁₀ (P1/P2)
- ■Example:
 - Input power 100W and output power 1W
 - What's the power ratio in decibel? Ans: 20dB





- dBm
 - Reference power is 1 mW
 - $\square 10 \log_{10} (Watts/10^{-3})$
- **Example:**
 - $\square 0 dB = 30dBm = 1 Watt$
- Summary
 - $\square P (dBW) = 10 \log (P/1 Watt)$
 - $\square P (dBm) = 10 \log (P/1 \text{ mWatt})$



Gain and Attenuation in dB or dBm

- Gain/attenuation in dB
 - $\square 10\log_{10}$ (output power/input power)
 - \blacksquare Gain(dB)=Pout(dB)-Pin(dB)
 - ☐ Gain: Pout > Pin
 - ☐ Attenuation Pout<Pin
- Gain/attenuation in dBm
 - \square X(dBm)+Y(dB) =??(dB)=??(dBm)
 - \square X(dBm)-Y(dB) =??(dB)=??(dBm)
 - □Example:
 - Input power is 2dBm, system gain is 5dB
 - What s output power? Ans: 7dBm
 - Notice: is it dB or dBm?



Wireless communication system

- Antenna gain
 - ☐ Transmitter antenna
 - Receiver antenna
- Wireless channel attenuation



- Questions: how do you represent the relationships between P_{tx} and P_{rx} ?
 - □In dB
 - ☐ In Watt



Signal-to-Noise ratio

■ S/N

- ■SNR= signal power(Watt)/noise power(Watt)
- ☐ Signal-to-Noise power ratio
- Relate to the performance of communications systems
 - Bit-error probability
 - Shannon capacity

■ SNR in dB

- \square S/N(dB)= 10 log₁₀ (S/N power ratio)
- □ 10 log₁₀ (signal power(Watt)/noise power(Watt))



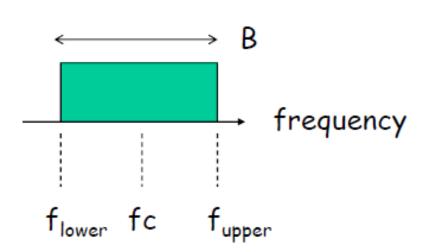
Noise, Interference, SNR

- SNR
 - □(signal power)/(noise power)
 - Noise: thermal noise
- SIR
 - ☐ Signal-to-Interference
 - Sometimes known as C/I (carrier-to-interference ratio)
 - □(signal power)/(interference power)
 - ■Interference: signals from other simultaneous communications
- SINR
 - Signal-to-Interference-Plus-Noise ratio
 - □(signal power)/(interference power + noise power)



Bandwidth

- \blacksquare B=f_{upper}-f_{lower}
- Carrier frequency: fc
- Example:
 - ■802.11 2.4GHz ISM band (channel 1)
 - \blacksquare f_{upper}=2434 MHz
 - \blacksquare f_{lower}=2412 MHz
 - fc=2423 MHz
 - B=22 MHz



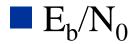


Thermal Noise

- Thermal noise power
 - \square N= kT_NB
 - ■N: power in Watt
 - □k: Boltzman's constant= 1.38*10⁻²³
 - $\square T_N$: temperature (degree Kelvin)
 - ■B: bandwidth of channel (Hz)



Bit Energy to Noise Ratio



- Energy per bit over the noise power spectral density
- Related to SNR power ratio
- ☐ Independent of bandwidth



Relate E_b/N_0 to SNR

- SNR=S/N (Watt/Watt)
- \blacksquare $E_b = St_b$
 - $\square E_b$: energy per bit (J)
 - ■S: signal power (carrier power) (W)
 - $\square t_h$: duration of a bit (s)
- $\blacksquare E_b/N_0 = (S/N_0)*t_b = (S/N_0)*(1/f_b)$
- $N_0 = N/B$
- N: total noise power (W)
- B: bandwidth (Hz)
- $\blacksquare E_b/N_0 = (S/N)(B/f_b)$



S/N (or E_b/N_0)

- To compare systems, generally they should have the same transmitted S/N (or E_b/N_0)
- The S/N (or E_b/N_0) at the input to the receiver will determine the system performance



- Find the Eb/N0 for a system operating at 2Mbps in a bandwidth of 1MHz. The carrier power is 0.1pW. The system noise temperature is 120K.
- Ans:



Capture model

- SNR_{received} ≥ SNR_{threshold}
 - Minimum SNR requirement, given a target bit error-rate (or frame-error-rate)



Shannon Capacity

- Theoretical (upper) bound of communication systems
- \blacksquare C=B*log₂ (1+S/N)
 - □C: capacity (bits/s)
 - ■B: bandwidth (Hz)
 - ■S/N: linear Signal-to-Noise ratio
- How to evaluate the performance of a communication scheme?
 - How close to Shannon bound?
 - Spectral efficiency
 - □bit/s/Hz



Concepts Related to Channel Capacity

- Data rate
 - □rate at which data can be communicated (bps)
- Bandwidth
 - □ the bandwidth of the transmitted signal as constrained by the transmitter and the nature of the transmission medium (Hertz)
- Noise
 - □ average level of noise over the communications path
- Error rate rate at which errors occur
 - ■Error
 - transmit 1 and receive 0
 - transmit 0 and receive 1



Shannon Capacity Formula

Equation:

$$C = B \log_2(1 + SNR)$$

- Represents theoretical maximum that can be achieved in AWGN channel)
- In practice, only much lower rates achieved
 - ☐ Formula assumes white noise (thermal noise)
 - ☐ Impulse noise is not accounted for
 - Attenuation distortion or delay distortion not accounted for



Nyquist Bandwidth

- For binary signals (two voltage levels)
 - $\square C = 2B$
- With multilevel signaling
 - $\square C = 2B \log_2 M$
 - M = number of discrete signal or voltage levels



Example of Nyquist and Shannon Formulations

- Spectrum of a channel between 3 MHz and 4 MHz; $SNR_{dB} = 24 dB$
 - $\square B = 4MHz 3MHz = 1MHz$
 - $\square SNR_{dB} = 24 \text{ dB} = 10\log_{10}(SNR)$
 - \square SNR = 251
- Using Shannon's formula
 - \Box C = 10⁶ x log₂(1 + 251) ~ 10⁶ x 8 = 8Mbps



Example of Nyquist and Shannon Formulations

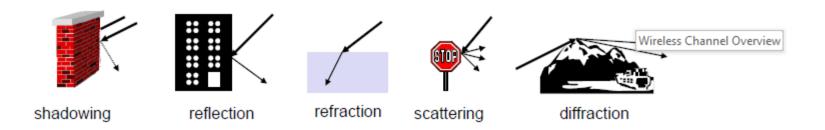
■ How many signaling levels are required?

- $\square C = 2B\log_2 M$
- $8x10^6 = 2x10^6 x \log_2 M$
- $\square 4 = \log_2 M$
- \square M = 16



Signal propagation

- Propagation in free space always like light (straight line)
- Receiving power proportional to 1/d² in free-space
- Receiving power additionally influenced by
 - ☐ fading (frequency dependent)
 - shadowing
 - □ reflection at large obstacles
 - refraction depending on the density of a medium
 - scattering at small obstacles
 - □ diffraction at edges

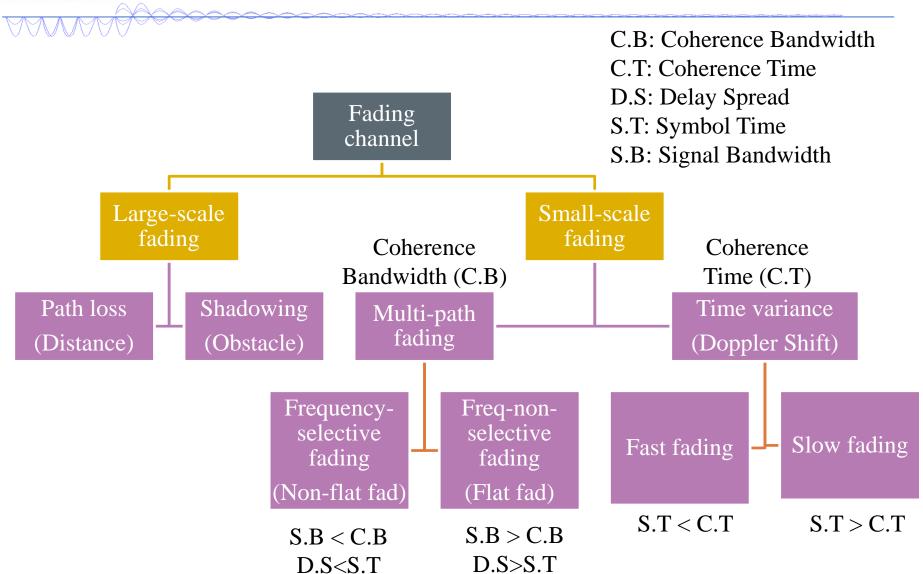




Wireless Channel Overview



Wireless Channel Overview





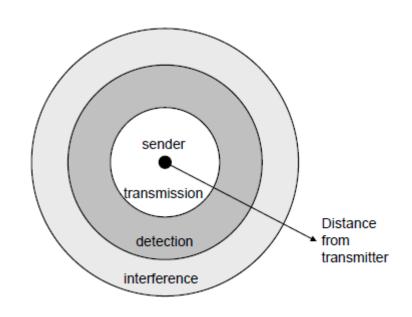
The Effects of Multipath Propagation

- Multiple copies of a signal may arrive at different phases
 - ☐ If phases add destructively, the signal level relative to noise declines, making detection more difficult
- Inter-symbol interference (ISI)
 - □ One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit



Signal Propagation Ranges

- Transmission range
 - communication possible
 - □low error rate
- Detection range
 - detection of the signal possible but communication may not be possible due to high error rate
- Interference range
 - □ signal may not be detected
 - □ signal adds to the background noise





Radio Propagation Models

- Three components
 - □ Path-loss
 - Radio signal attenuation due to transmission over a certain distance
 - Free-space path loss model
- Shadowing
 - Signal attenuation due to penetration of buildings and walls.
 - □Log-normal distribution model
- Fading
 - □ Due to multi-path transmission (reflection creates multiple radio paths) and Doppler Shift
 - Rayleigh distribution model, Ricean distribution model



Radio Propagation Models

- Signal power at receiver: $G_{channel}$ includes 3 components
 - □Path-loss (g1)
 - □Log-normal shadowing (g2)
 - □ Rayleigh fading (g3)



$$P_{rx} = G_{channel} \times G_{ant,tx} \times G_{ant,rx} \times P_{tx}$$

$$G_{channel} = g1 \times g2 \times g3$$



Path-loss model

■ Free-space path-loss model



Log-normal shadowing model



Rayleigh distribution model



Summary of radio propagation and mitigations

- Shadowing
 - ☐ Problem: received signal strength
 - ☐ Mitigation:
 - increase transmit power
 - reduce cell size
- Fast fading
 - Problem: error rate (BER, FER, PER)
 - Mitigation:
 - Interleaving
 - Error correction coding
 - Frequency hopping
 - Diversity techniques

- Delay spread
 - ☐ Problem: ISI and error rates
 - ☐ Mitigation:
 - Equalization
 - Spread spectrum
 - OFDM
 - Directional antenna



END