



COMPUTER ENGINEERING

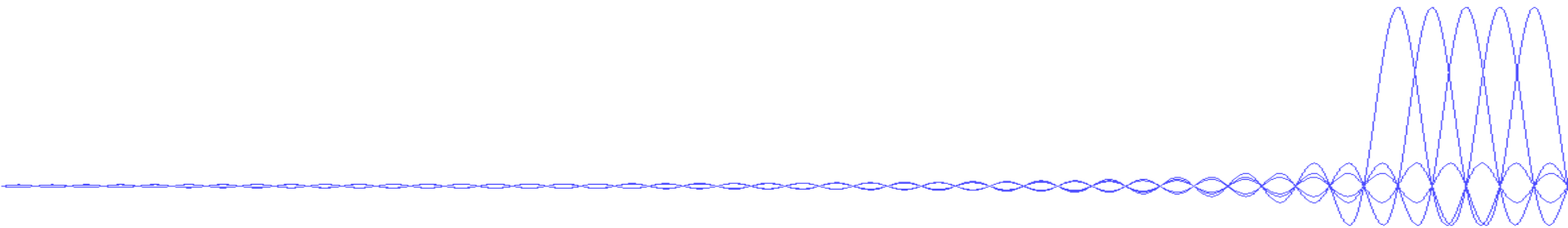


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ADVANCED DIGITAL SIGNAL PROCESSING

Chapter 4: OFDM Modulation/Demodulation

28/10/2017





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- Orthogonality
- Orthogonality – CDMA
- Orthogonality - OFDM
- OFDM Modulation - IFFT
- OFDM Demodulation - FFT



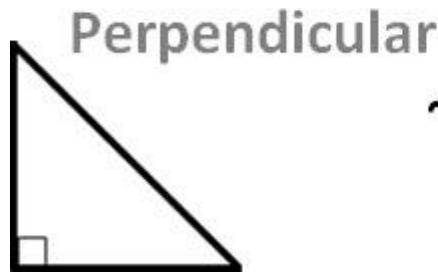
Orthogonality

- Orthogonality is property that allows multiple information signals to be transmitted perfectly over a common channel with the successful detection
- Two functions or signals are said to be orthogonal if they are mutually independent of each other
- Two vectors are said to be orthogonal if dot product is zero. Sine and cosine are best example of orthogonal signal and integration of product of the two orthogonal is zero.



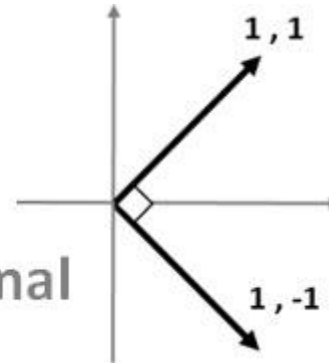
Orthogonality

■ Perpendicular Vs Orthogonality



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Orthogonal



□ $u = (1, 1) \quad v = (1, -1)$

□ $u \cdot v = u_1 \cdot v_1 + u_2 \cdot v_2 = 1 \cdot 1 + 1 \cdot (-1) = 0$

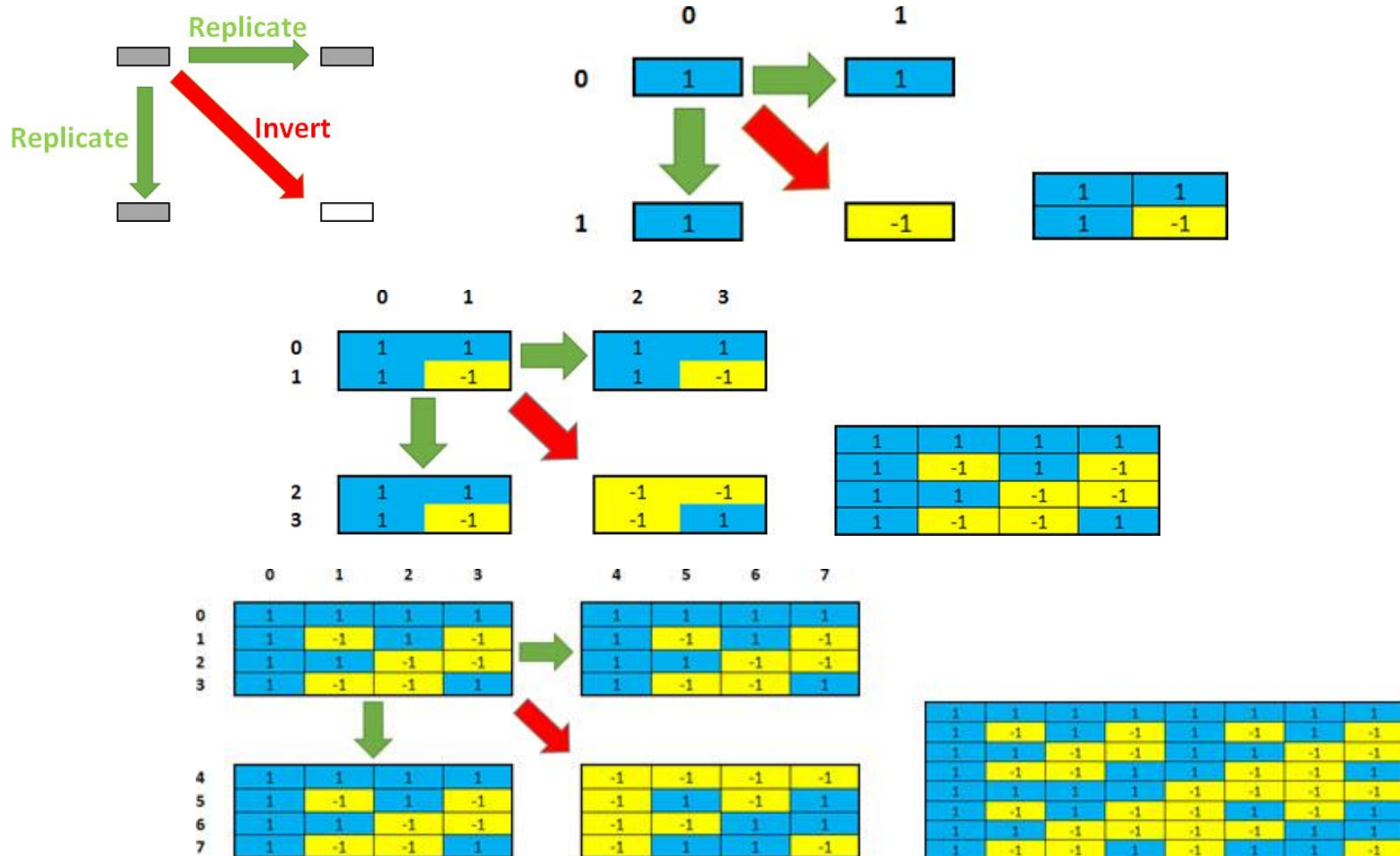
□ Then, u and v are orthogonal

■ Hence, if two vectors has an angle X of 90 degrees to each other - ie they are orthogonal - their Dot Product is equal to zero



Orthogonality - CDMA

■ CDMA: Code-division multiple access





Orthogonality - CDMA

i.e. code 2

1	1	-1	-1	1	1	-1	-1
X	X	X	X	X	X	X	X

i.e. code 5

1	-1	1	-1	-1	1	-1	1
=	=	=	=	=	=	=	=
1	-1	-1	1	-1	1	1	-1

$\Sigma = 0$



Orthogonality - CDMA

■ Orthogonal code matrix

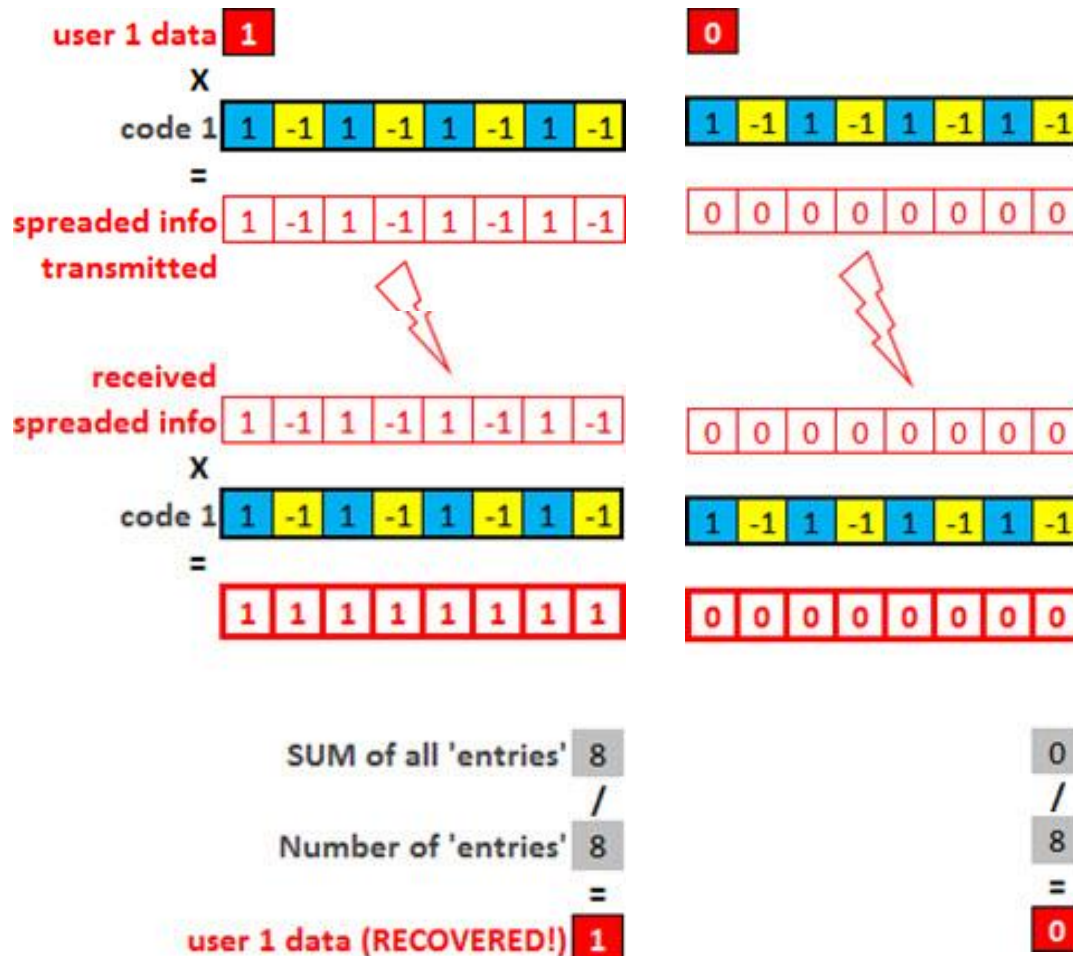
8 x 8

	0	1	2	3	4	5	6	7
0	1	1	1	1	1	1	1	1
1	1	-1	1	-1	1	-1	1	-1
2	1	1	-1	-1	1	1	-1	-1
3	1	-1	-1	1	1	-1	-1	1
4	1	1	1	1	-1	-1	-1	-1
5	1	-1	1	-1	-1	1	-1	1
6	1	1	-1	-1	-1	-1	1	1
7	1	-1	-1	1	-1	1	1	-1



Orthogonality - CDMA

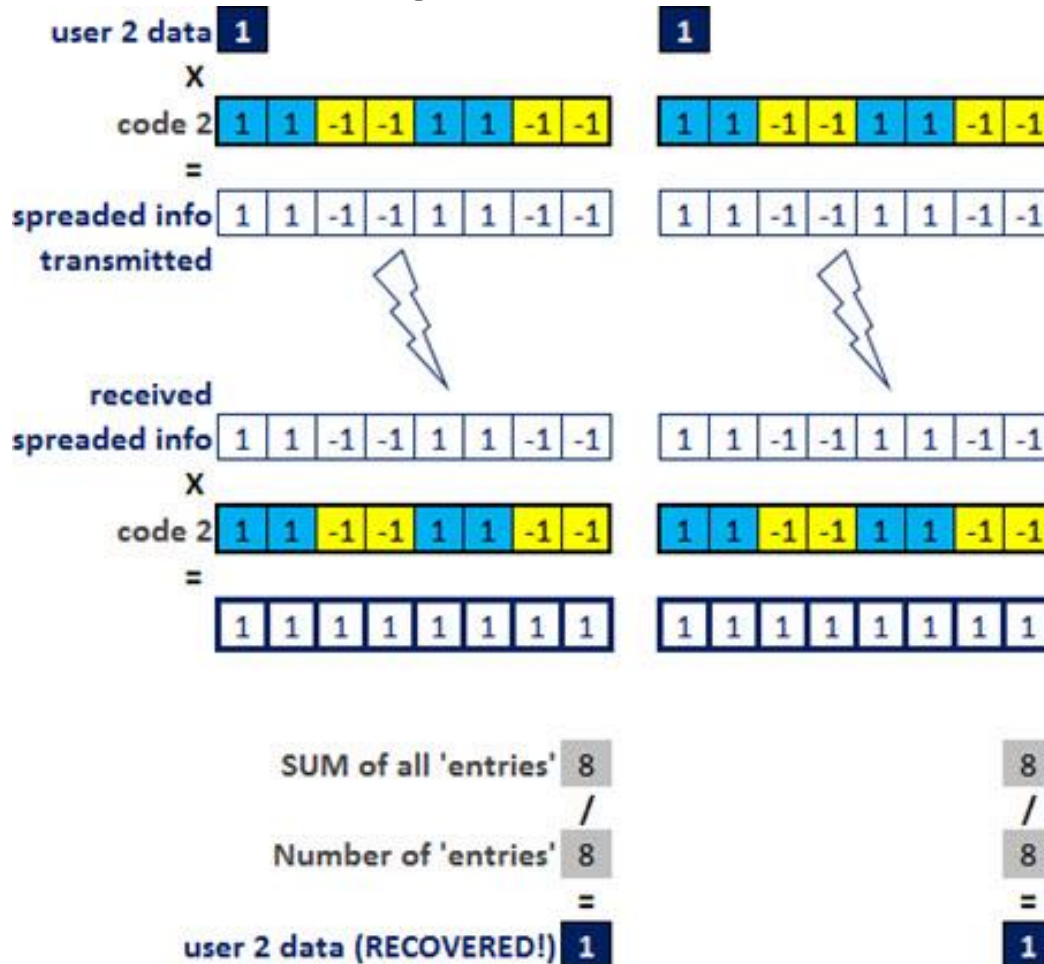
■ Spreaded code – Single User1





Orthogonality - CDMA

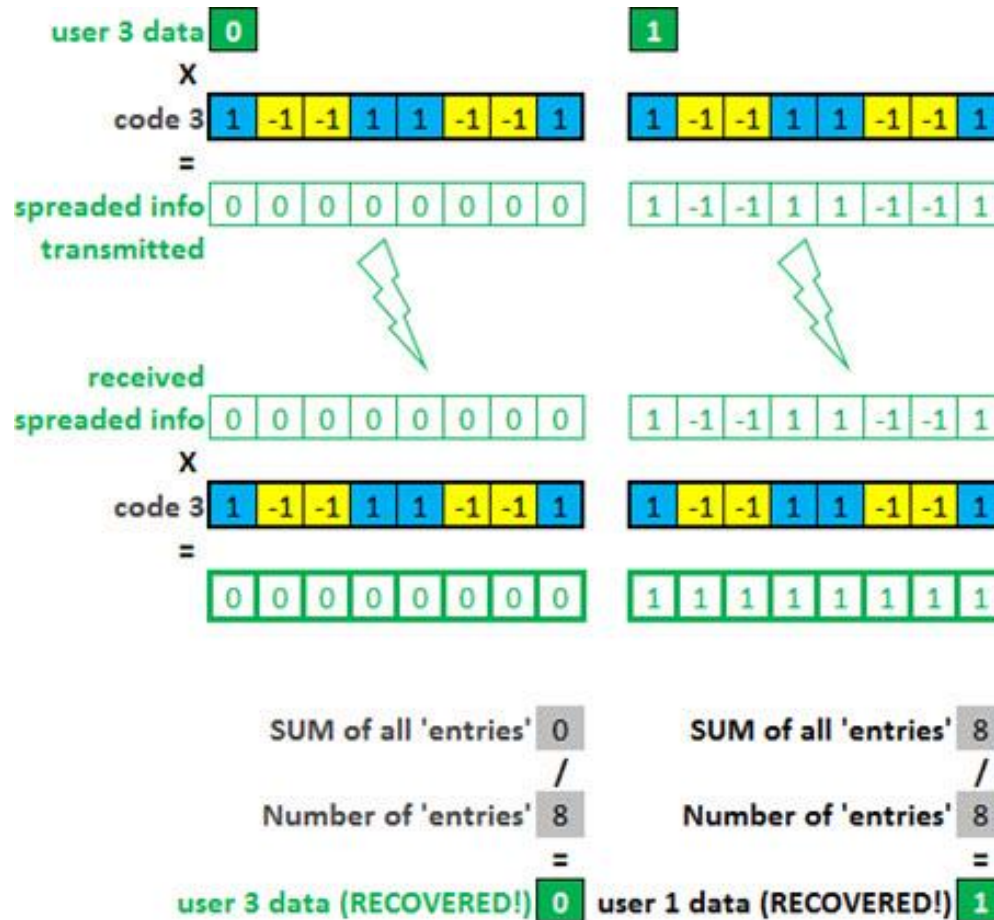
■ Spreaded code – Single User2





Orthogonality - CDMA

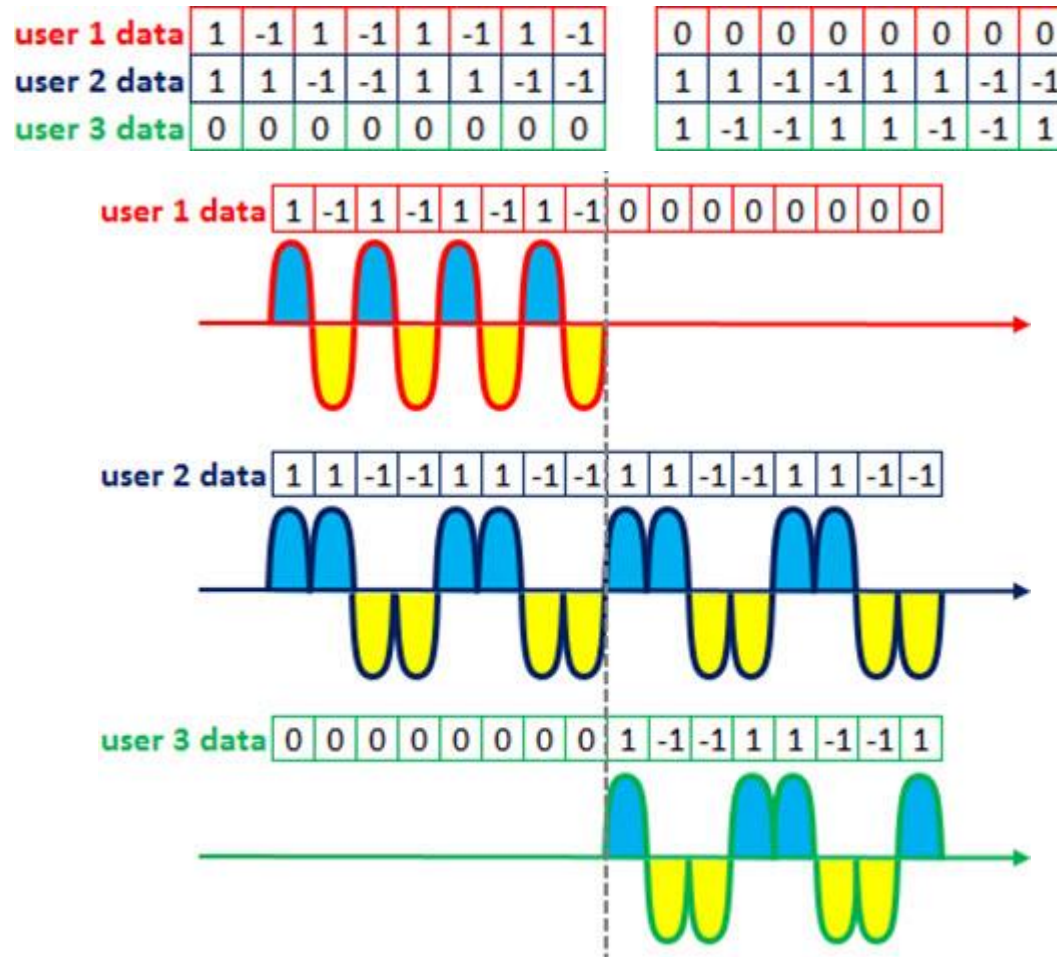
■ Spreaded code – Single User3





Orthogonality - CDMA

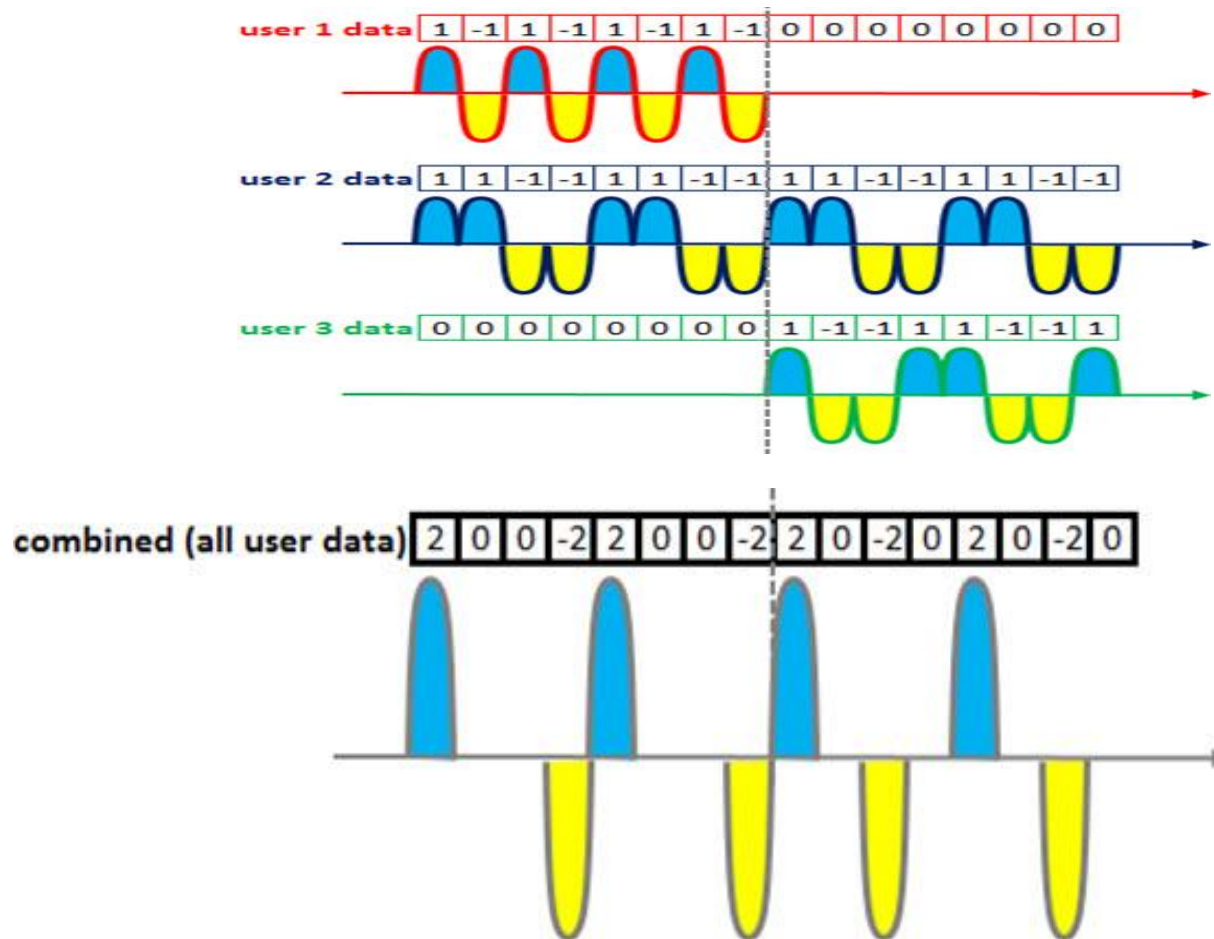
■ Spreaded code – Multiple User {1, 2, 3}





Orthogonality - CDMA

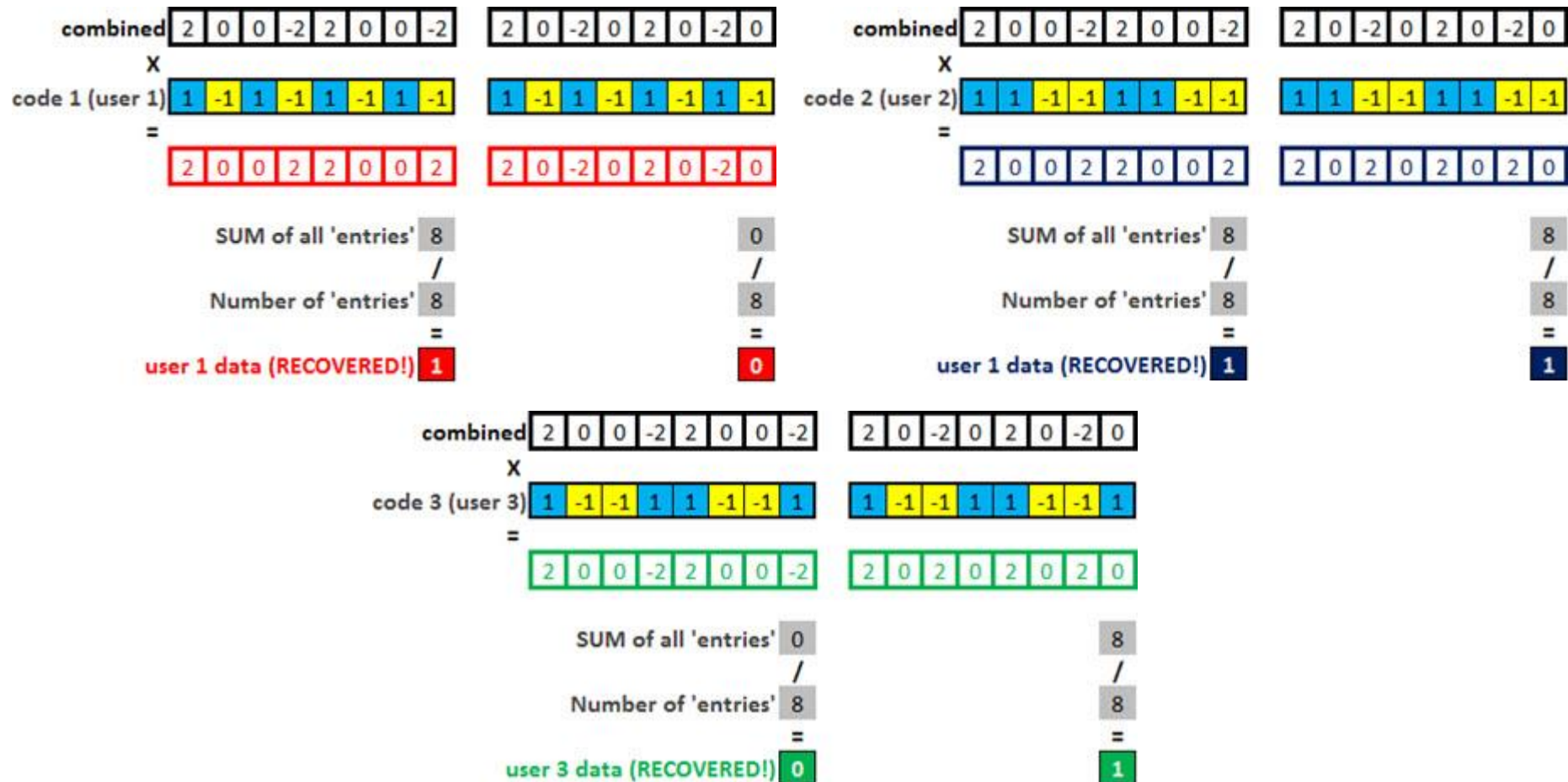
■ Spreaded code – Multiple User {1, 2, 3}





Orthogonality - CDMA

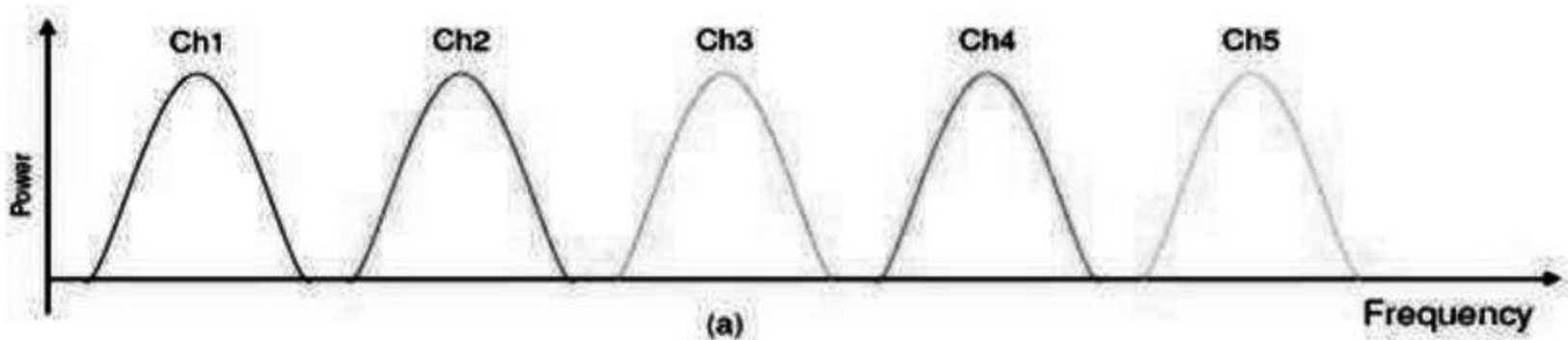
■ Spreaded code – Multiple User { 1, 2, 3 }



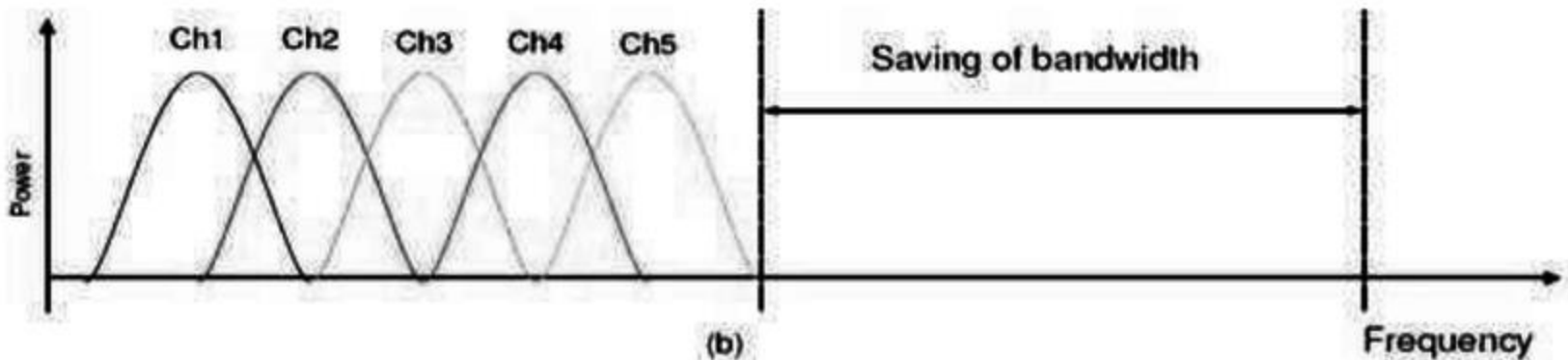


Orthogonality - OFDM

■ Conventional FDM



■ Orthogonal FDM





Orthogonality - OFDM



■ OFDM: Orthogonal Frequency Division Multiplexing

$$x(t) = \sum_{k=0}^{N-1} X_k e^{j2\pi f_k t}$$

□ where,

- X_k , $k=0:N-1$, transmitted data (complex number I, Q) is given constellation modulation (Mapper)
- f_k , $k=0:N-1$, carrier frequency
- N : Number of subcarriers, Number of samples per OFDM symbol duration



Orthogonality - OFDM



$$x(t) = \sum_{k=0}^{N-1} X_k e^{j2\pi k f_s t}$$

□ where,

■ f_s : frequency spacing

■ To keep orthogonality among signals on different frequency, the minimum frequency spacing must be:

$$f_s = \frac{1}{T_s}$$

□ where,

■ T_s : OFDM symbol duration



Orthogonality - OFDM

■ Proven:

$$x_q(t) = X_q e^{j2\pi q f_s t}$$

$$x_p(t) = X_p e^{j2\pi p f_s t}$$

$$\langle x_p(t), x_q(t) \rangle$$

$$= \int_0^{T_s} X_q e^{j2\pi q f_s t} \cdot X_p e^{j2\pi p f_s t} dt$$

$$= \frac{X_q \cdot X_p}{e^{j2\pi(q+p)f_s T_s} - 1} (e^{j2\pi(q+p)f_s T_s} - 1)$$

$$= 0 \quad \text{if } f_s = 1/T_s$$



Reminder: IDFT/DFT – IFFT/FFT

- IDFT: The mathematical computation is used to convert frequency domain signal into a same-length time domain signal

$$x_n = \sum_{k=0}^{N-1} X_k e^{j2\pi kn/N}, \quad k = 0, \dots, N-1$$

- IFFT: An algorithm to rapidly compute and reduce the complexity of IDFT if N is power of 2

- DFT: The mathematical computation is used to convert time domain signal into a same-length frequency domain signal

$$X_k = \sum_{n=0}^{N-1} x_n e^{-j2\pi kn/N}, \quad k = 0, \dots, N-1$$

- FFT: An algorithm to rapidly compute and reduce the complexity of DFT if N is power of 2



OFDM Modulation/Demodulation



■ OFDM Modulation

$$x_n = \sum_{k=0}^{N-1} X_k e^{j2\pi k f_s n T_s / N} \quad n = 0, \dots, N-1 \text{ (IFFT)}$$

$$= \sum_{k=0}^{N-1} X_k e^{j2\pi k n / N}$$

■ OFDM Demodulation

$$X_k = \sum_{n=0}^{N-1} x_n e^{-j2\pi k f_s n T_s / N} \quad k = 0, \dots, N-1 \text{ (FFT)}$$

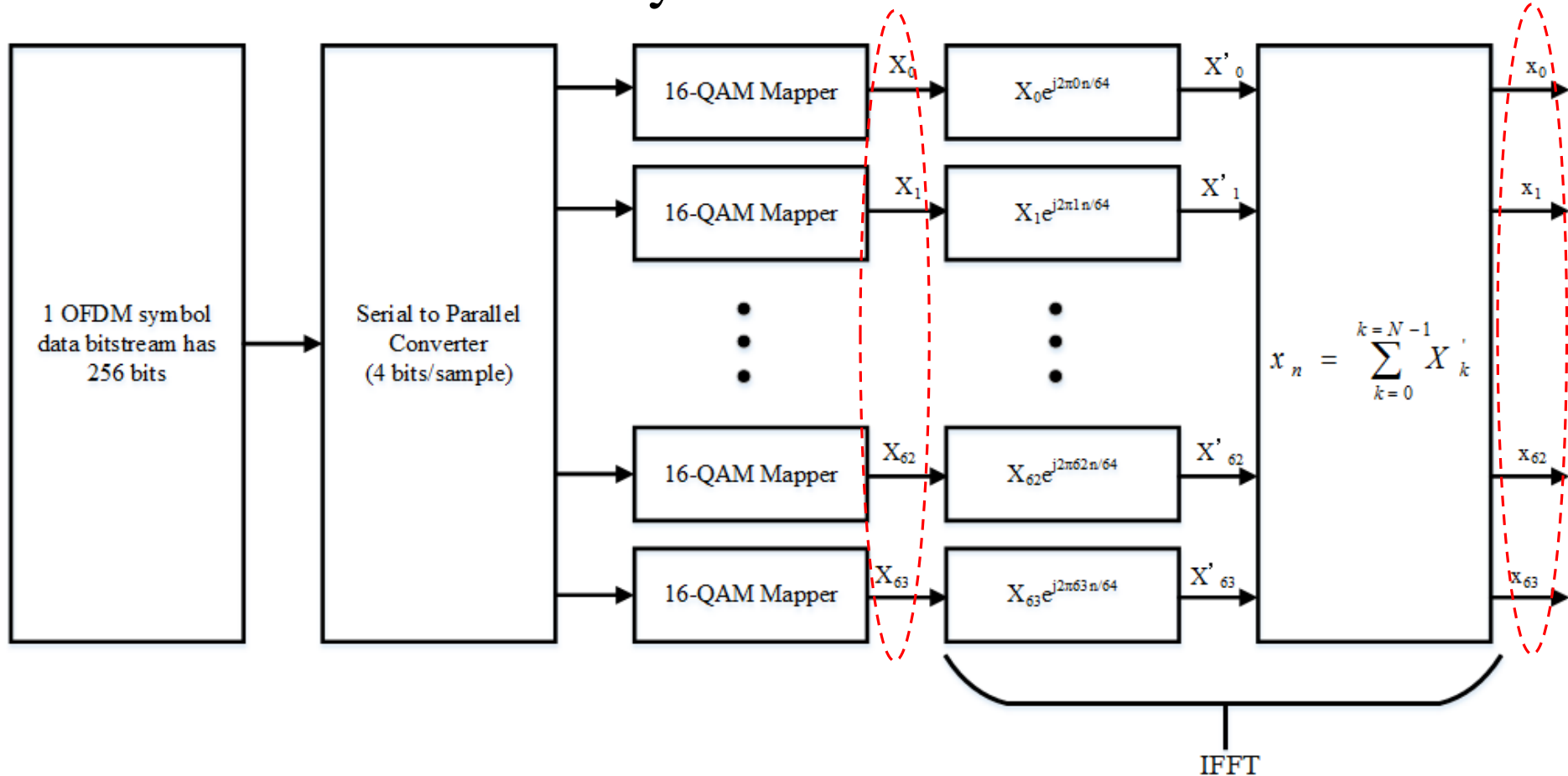
$$= \sum_{n=0}^{N-1} x_n e^{-j2\pi k n / N}$$



OFDM Modulation System

■ OFDM Modulation System

Number of samples
per OFDM symbol





END

