



COMPUTER ENGINEERING

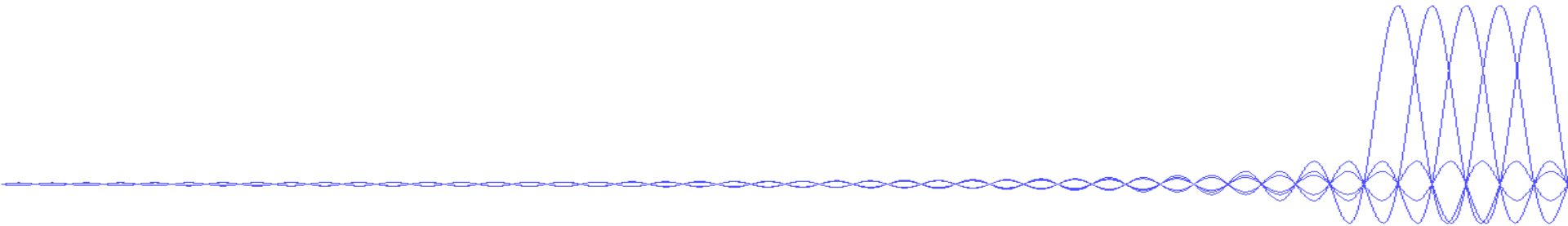


UIT
TRƯỜNG ĐẠI HỌC
CÔNG NGHỆ THÔNG TIN

ADVANCED DIGITAL SIGNAL PROCESSING

Chapter 3: Modulation/Demodulation

28/10/2017





■ PSK

- BPSK

- QPSK (4-QAM)

■ ASK

- BASK

- 4-ASK

■ QAM

- 16-QAM

- Mapper

- De-Mapper

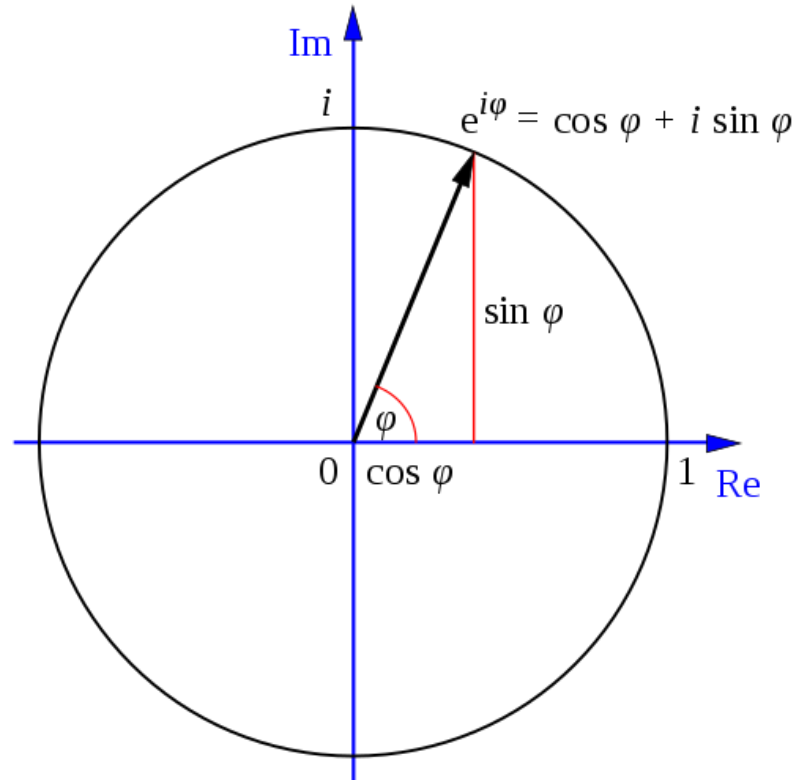
 - Hard De-Mapper

 - Soft De-Mapper



■ Remind

$$e^{i\varphi} = \cos \varphi + i \sin \varphi$$





Phase Shift Keying (PSK)

- In PSK, the modulation signal set is

$$s_i(t) = A \cos(2\pi f_c t + \phi_i(t)), i = 1, \dots, M; 0 \leq t \leq T_s$$

- T_s is symbol period, A is carrier amplitude (constant), “phase” $\phi_i(t)$ carries symbol information, and $\log_2 M$ bits per symbol
- BPSK: 1 bit per symbol - minimum phase separation 180°
- QPSK: 2 bits per symbol - minimum phase separation 90°
- 8-PSK: 3 bits per symbol - minimum phase separation 45°
- Etc...



Binary Phase Shift Keying (BPSK)

- BPSK: $M = 2$. It is convention to use $m_1 = 1$ for bit 0, and $m_2 = -1$ for bit 1

$$s_i(t) = A \cos(2\pi f_c t + (i - 1)\pi + \theta_c), i = 1, 2; 0 \leq t \leq T_b$$

- T_b : bit period

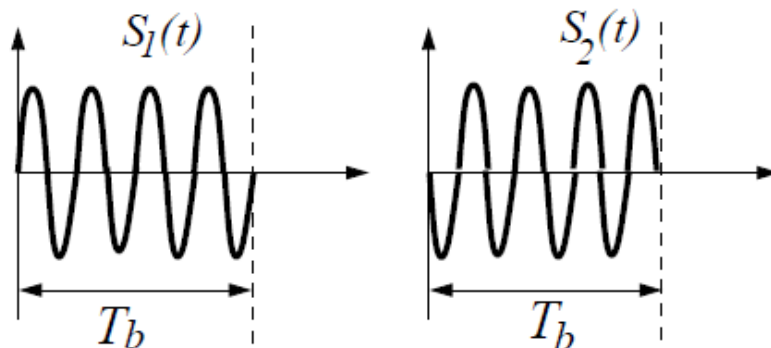
- $T_s = T_b$

- θ_c : an initial phase

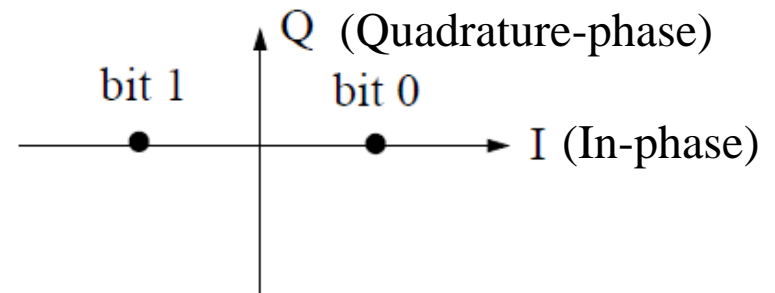
- $A = \sqrt{\frac{2E_b}{T_b}}$

- E_b : Energy per bit

Phase separation: π (90°)



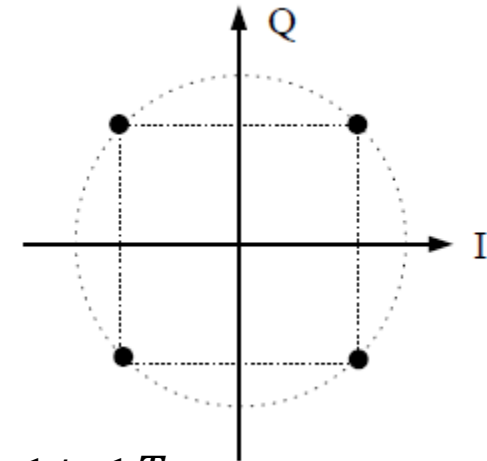
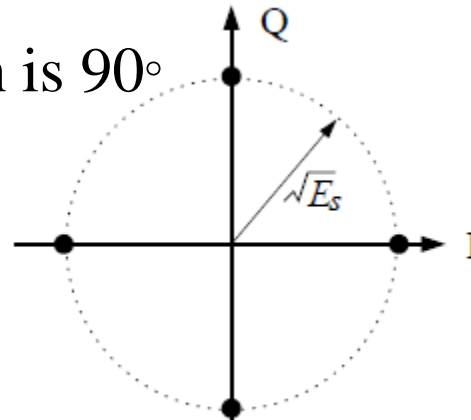
BPSK constellation diagram





Quadrature Phase Shift Keying (QPSK)

- QPSK: $M = 4$, 2 bits per symbol, symbol period $T_s = 2T_b$, energy per symbol $E_s = 2E_b$
- QPSK signal constellation:
- Minimum phase separation is 90°



- QPSK signal set:

$$s_i(t) = \sqrt{\frac{2E_s}{T_s}} \cos\left(2\pi f_c t + (i-1)\frac{\pi}{2}\right), 1 \leq i \leq 4; \quad 0 \leq t \leq T_s$$

- The transmitted QPSK RF signal can also be written as:

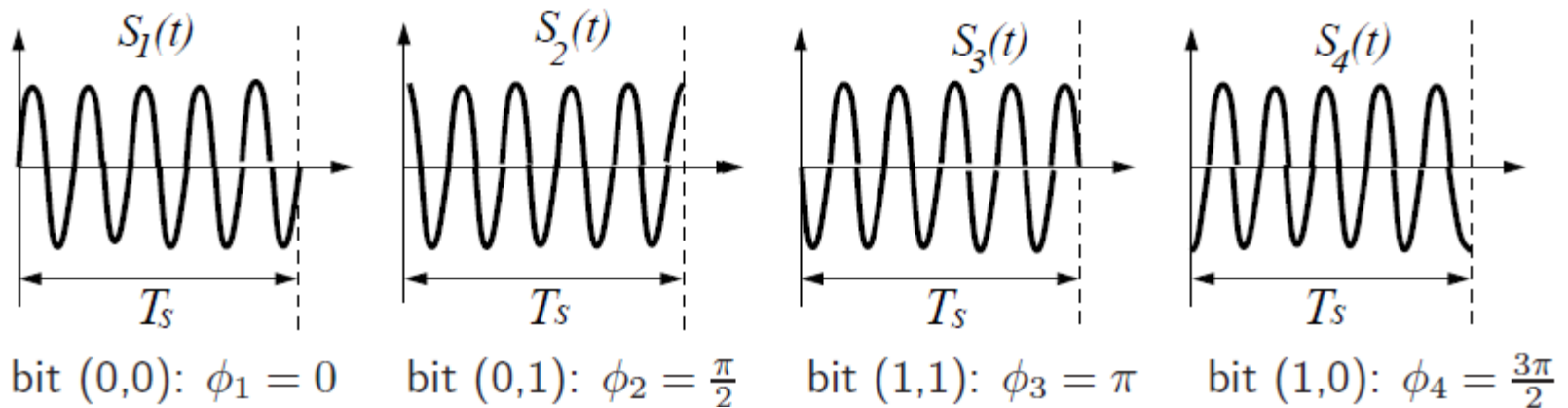
$$s_i(t) = \sqrt{\frac{2E_s}{T_s}} \cos\left((i-1)\frac{\pi}{2}\right) \cos(2\pi f_c t) - \sqrt{\frac{2E_s}{T_s}} \sin\left((i-1)\frac{\pi}{2}\right) \sin(2\pi f_c t)$$



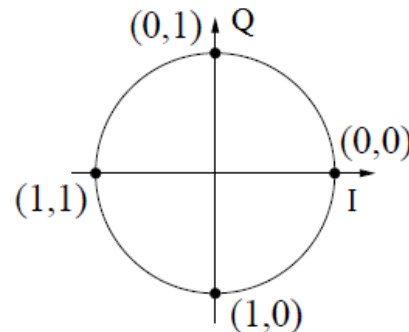
Quadrature Phase Shift Keying (QPSK)

■ QPSK signal set:

$$s_i(t) = \sqrt{\frac{2E_s}{T_s}} \cos(2\pi f_c t + \phi_i), 1 \leq i \leq 4; 0 \leq t \leq T_s; \phi_i = (i - 1) \frac{\pi}{2}$$



■ QPSK constellation diagram





Binary Amplitude Shift Keying (BASK)

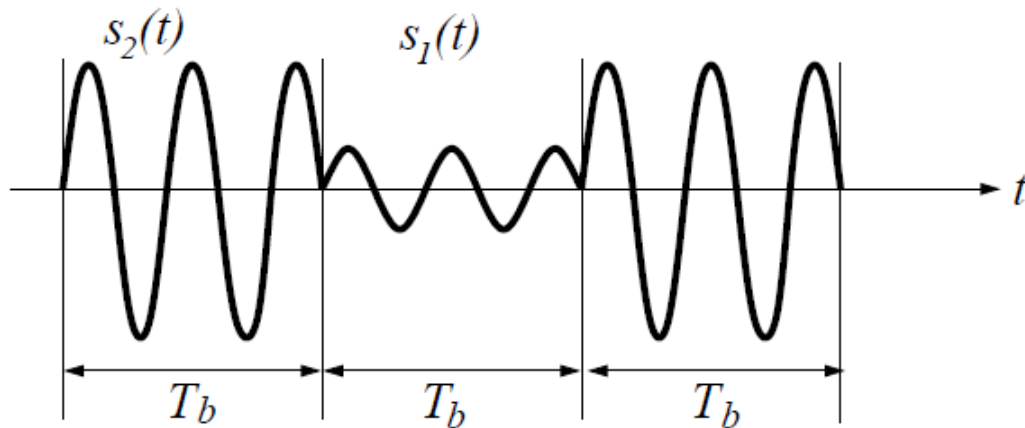
- ASK: Carrier amplitude A_i carries symbol information

$$s_i(t) = A_i \cos(2\pi f_c t + \theta), \quad 1 \leq i \leq M; 0 \leq t \leq T_s$$

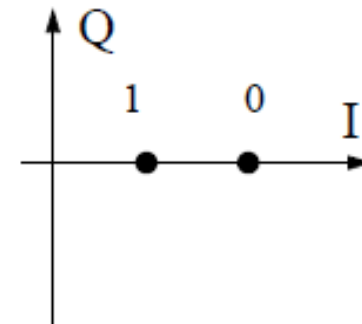
- BASK: $M = 2$, bit 0: $A_1 = A$, bit 1: $A_2 = 3A$

$$s_1(t) = A \cos(2\pi f_c t + \theta)$$

$$s_2(t) = 3A \cos(2\pi f_c t + \theta)$$



BASK constellation diagram





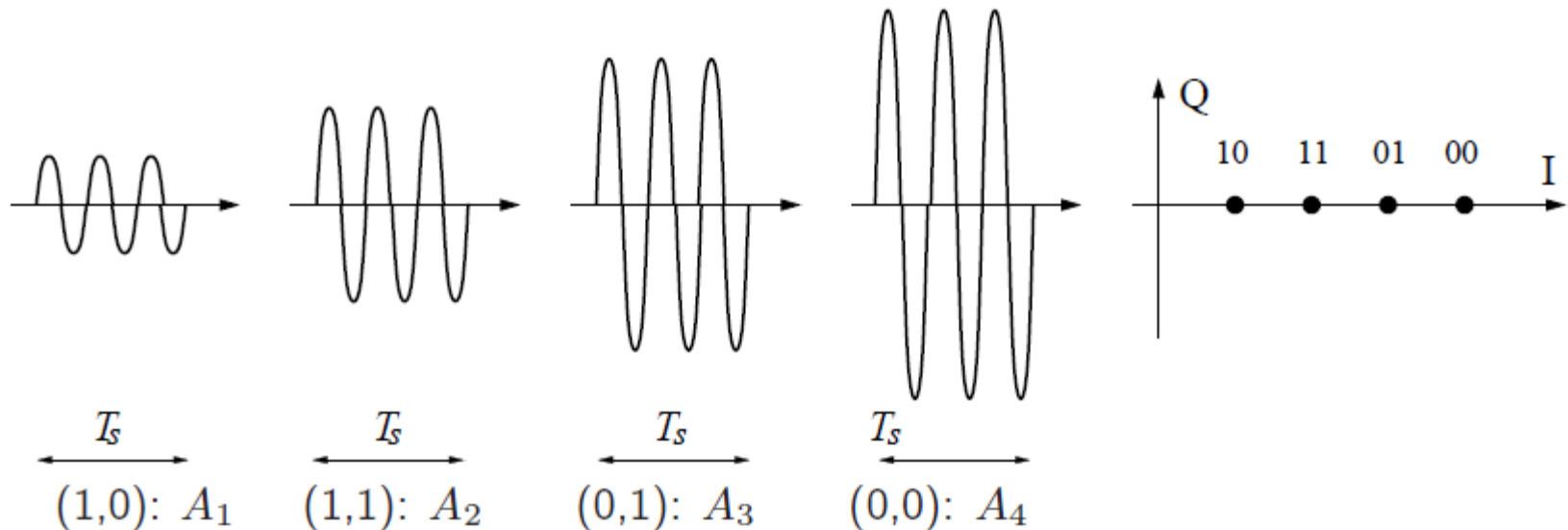
4-Amplitude Shift Keying (4-ASK)

■ 4-ASK: $M = 4$

■ Signal set:

$$s_i(t) = A_i \cos(2\pi f_c t + \theta), \quad 1 \leq i \leq 4; 0 \leq t \leq T_s$$

4-ASK constellation diagram



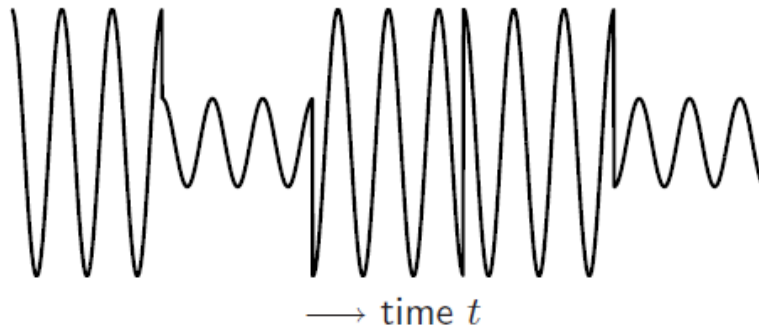


Combined ASK/PSK

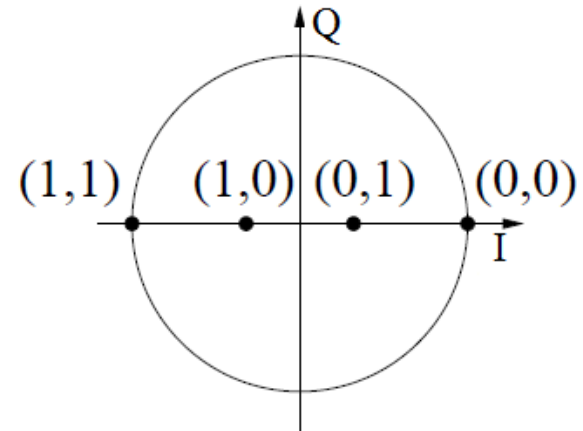
- PSK and ASK can be combined.
- Here is an example of 4-ary or 4-PAM (pulse amplitude modulation) of 2 amplitude levels and phase shift of π are combined to represent 4-ary symbols

Transmitted signal $s(t)$

(00) (01) (11) (00) (10)



Constellation diagram



- Note in \sqrt{M} -ary or \sqrt{M} -PAM, quadrature component is not used, a more generic scheme of combining PSK/ASK is QAM, which uses both I and Q branches



Quadrature Amplitude Modulation

- QAM: combines features of PSK and ASK, uses both I and Q components, and is bandwidth very efficient

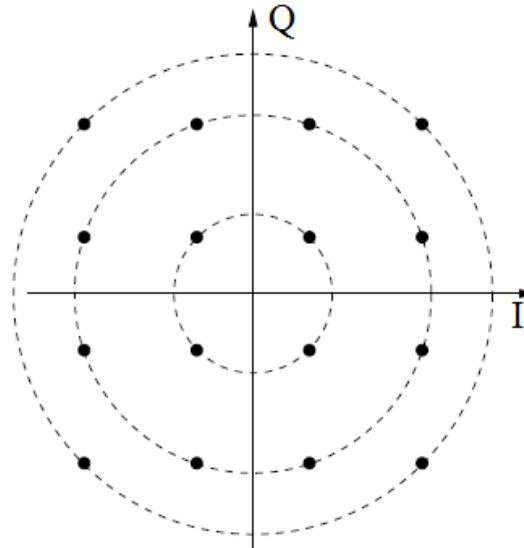
$$s_i(t) = A_i \cos(2\pi f_c t + \phi_i(t)), 0 \leq t \leq T_s, 1 \leq i \leq M$$

- T_s being symbol period, as both amplitude and phase are used to carry symbol information, it is very bandwidth efficient
- symbol set size M : $2^1 \times 2^1 = 4$, $2^2 \times 2^2 = 16$, $2^3 \times 2^3 = 64$, etc → 4QAM, 16QAM, 64QAM, etc
- The larger M is, the better bandwidth efficiency but lower robustness against noise and fading



Quadrature Amplitude Modulation (QAM)

- An example of (squared) 16-QAM:

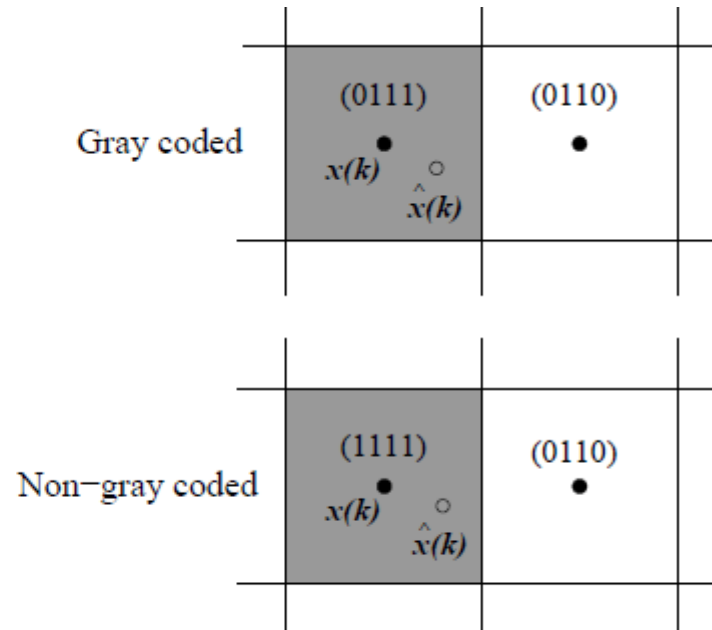
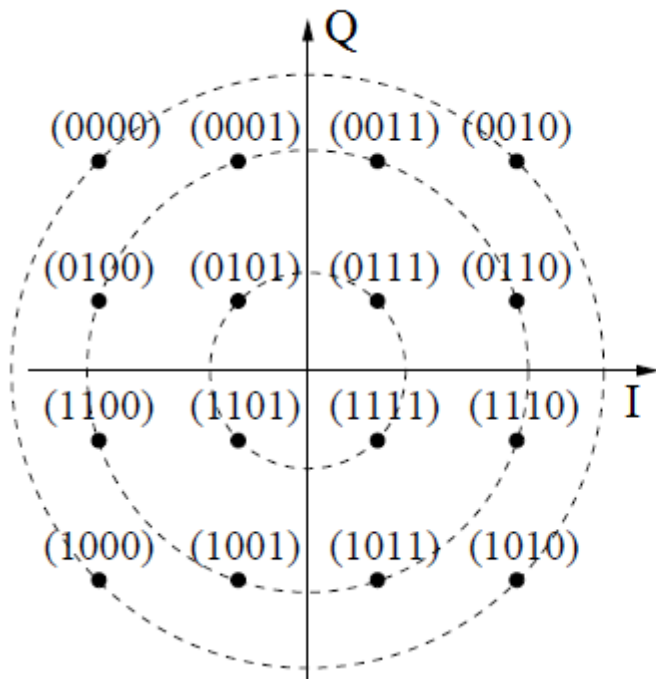


- Note for squared M-QAM, I and Q branches are both pM -ary (of previous slide)
- Depending on the channel quality, 64-QAM, 128-QAM, or 256-QAM are possible
- Why high-order QAM particularly bandwidth efficient? and what is penalty paid?



Quadrature Amplitude Modulation (QAM)

- Gray Mapping: adjacent constellation points only differ in a single bit (minimum Hamming distance)

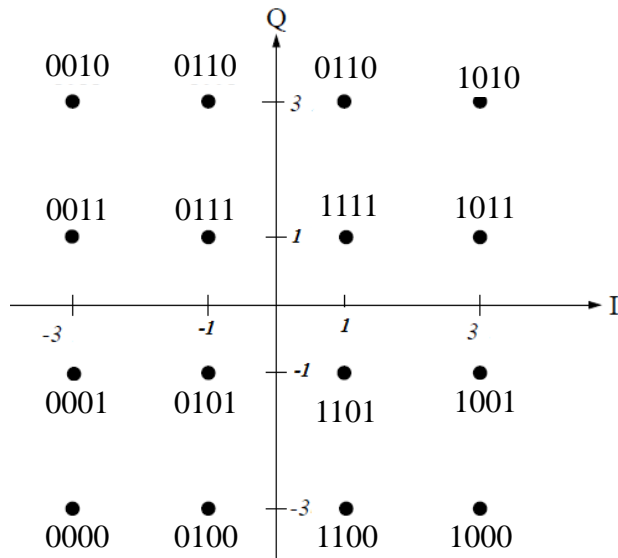


Transmitted symbol $x(k)$ was sent, but received symbol $\hat{x}(k)$ in neighbor region due to noise.

- If noise or distortions cause misclassification in the receiver, Gray coding can minimize the bit error rate



■ 16-QAM Mapper

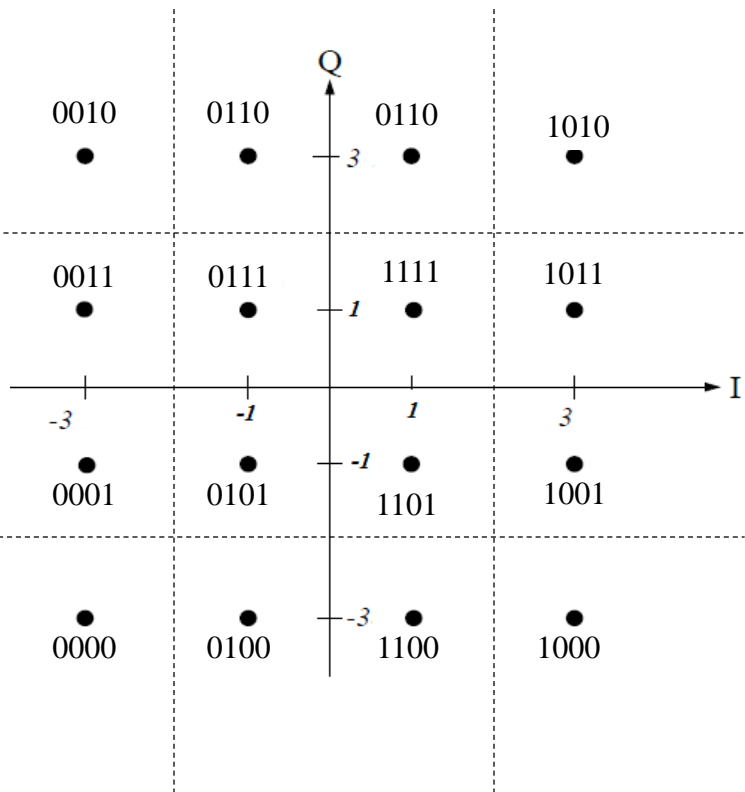


Input	$I + jQ$
0000	$-3-3j$
0001	$-3-j$
0010	$-3+3j$
0011	$-3+j$
0100	$-1-3j$
0101	$-1-j$
0110	$-1+3j$
0111	$-1+j$

Input	$I + jQ$
1000	$3-3j$
1001	$3-j$
1010	$3+3j$
1011	$3+j$
1100	$1-3j$
1101	$1-j$
1110	$1+3j$
1111	$1+j$



■ Hard-Decision



Input (I, Q)	Output
$-2 \geq I$ & $-2 \geq Q$	0000
	0001
	0010
	0011
	0100
	0101
	0110
	0111

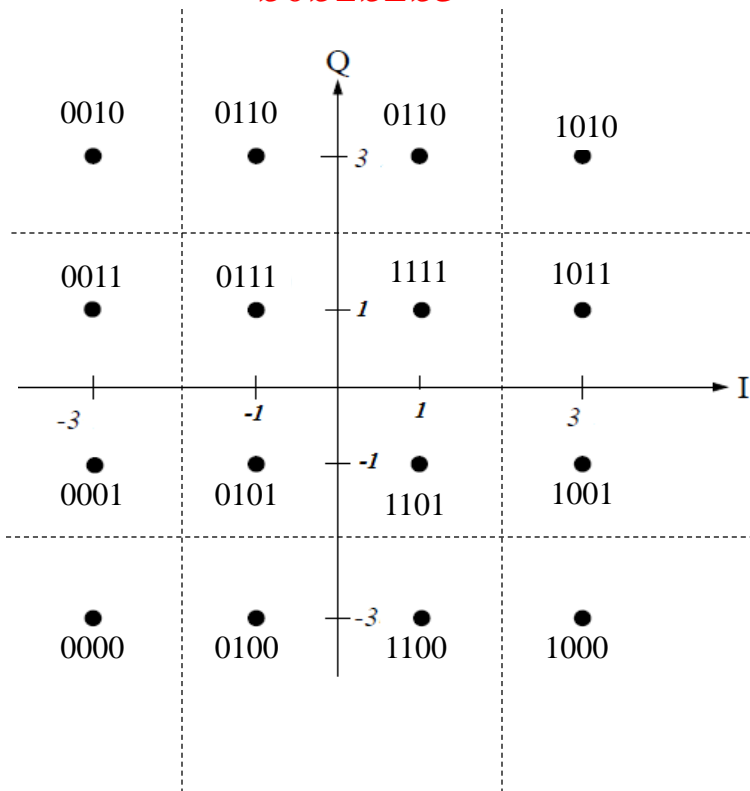
Input	Output
	1000
	1001
	1010
	1011
	1100
	1101
	1110
	1111



■ Soft-Decision

<http://www.dsblog.com/2009/07/05/softbit-16qam/>

b0b1b2b3



$$sb(b0) = \begin{cases} 2(Y_{re} + 1) & Y_{re} < -2 \\ Y_{re} & -2 \leq Y_{re} < 2 \\ 2(Y_{re} - 1) & Y_{re} > 2 \end{cases}$$

$$sb(b1) = -|Y_{re}| + 2 \quad \text{for all } Y_{re}$$

$$sb(b2) = \begin{cases} 2(Y_{im} + 1) & Y_{im} < -2 \\ Y_{im} & -2 \leq Y_{im} < 2 \\ 2(Y_{im} - 1) & Y_{im} > 2 \end{cases}$$

$$sb(b3) = -|Y_{im}| + 2 \quad \text{for all } Y_{im}$$

$$DeMap \text{ Bit} = (sign(sb) + 1)/2$$



END

