Evaluation of Diagnostic Models

Welcome to the second assignment of course 1. In this assignment, we will be working with the results of the X-ray classification model we developed in the previous assignment. In order to make the data processing a bit more manageable, we will be working with a subset of our training, and validation datasets. We will also use our manually labeled test dataset of 420 X-rays.

As a reminder, our dataset contains X-rays from 14 different conditions diagnosable from an X-ray. We'll evaluate our performance on each of these classes using the classification metrics we learned in lecture.

Outline

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 - 3.1 True Positives, False Positives, True Negatives, and False Negatives
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 - 3.6 ROC Curve
- 4. Confidence Intervals
- <u>5. Precision-Recall Curve</u>
- 6. F1 Score
- 7. Calibration

By the end of this assignment you will learn about:

- 1. Accuracy
- 2. Prevalence
- 3. Specificity & Sensitivity
- 4. PPV and NPV
- 5. ROC curve and AUCROC (c-statistic)
- 6. Confidence Intervals

1. Packages

In this assignment, we'll make use of the following packages:

- <u>numpy (https://docs.scipy.org/doc/numpy/)</u> is a popular library for scientific computing
- matplotlib (https://matplotlib.org/3.1.1/contents.html) is a plotting library compatible with numpy
- pandas (https://pandas.pydata.org/docs/) is what we'll use to manipulate our data
- sklearn (https://scikit-learn.org/stable/index.html) will be used to measure the performance of our model

Run the next cell to import all the necessary packages as well as custom util functions.

```
In [3]: import numpy as np
   import matplotlib.pyplot as plt
   import pandas as pd
   import util
```

2. Overview

We'll go through our evaluation metrics in the following order.

- Metrics
 - TP, TN, FP, FN
 - Accuracy
 - Prevalence
 - Sensitivity and Specificity
 - PPV and NPV
 - AUC
- Confidence Intervals

Let's take a quick peek at our dataset. The data is stored in two CSV files called train_preds.csv and valid_preds.csv. We have precomputed the model outputs for our test cases. We'll work with these predictions and the true class labels throughout the assignment.

```
In [4]: train results = pd.read csv("train preds.csv")
        valid results = pd.read csv("valid preds.csv")
        # the labels in our dataset
        class labels = ['Cardiomegaly',
          'Emphysema',
         'Effusion',
          'Hernia',
          'Infiltration',
          'Mass',
          'Nodule',
         'Atelectasis',
          'Pneumothorax',
          'Pleural Thickening',
          'Pneumonia',
          'Fibrosis',
         'Edema',
          'Consolidation'
        # the labels for prediction values in our dataset
        pred_labels = [l + "_pred" for l in class_labels]
```

Extract the labels (y) and the predictions (pred).

```
In [5]: y = valid_results[class_labels].values
    pred = valid_results[pred_labels].values
```

Run the next cell to view them side by side.

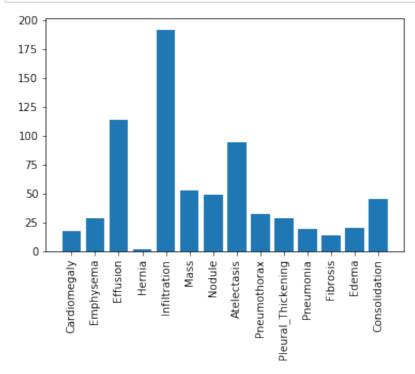
```
In [6]: # let's take a peek at our dataset
    valid_results[np.concatenate([class_labels, pred_labels])].head()
```

Out[6]:

	Cardiomegaly	Emphysema	Effusion	Hernia	Infiltration	Mass	Nodule	Atelecta
0	0	0	0	0	0	0	0	0
1	0	0	0	0	1	0	1	0
2	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0

5 rows × 28 columns

To further understand our dataset details, here's a histogram of the number of samples for each label in the validation dataset:



It seem like our dataset has an imbalanced population of samples. Specifically, our dataset has a small number of patients diagnosed with a Hernia.

3 Metrics

3.1 True Positives, False Positives, True Negatives, and False Negatives

The most basic statistics to compute from the model predictions are the true positives, true negatives, false positives, and false negatives.

As the name suggests

- true positive (TP): The model classifies the example as positive, and the actual label also positive.
- false positive (FP): The model classifies the example as positive, **but** the actual label is negative.
- true negative (TN): The model classifies the example as negative, and the actual label is also negative.
- false negative (FN): The model classifies the example as negative, but the label is actually
 positive.

We will count the number of TP, FP, TN and FN in the given data. All of our metrics can be built off of these four statistics.

Recall that the model outputs real numbers between 0 and 1.

- To compute binary class predictions, we need to convert these to either 0 or 1.
- We'll do this using a threshold value th.
- Any model outputs above th are set to 1, and below th are set to 0.

All of our metrics (except for AUC at the end) will depend on the choice of this threshold.

Fill in the functions to compute the TP, FP, TN, and FN for a given threshold below.

The first one has been done for you.

```
In [8]: # UNQ_C1 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
def true_positives(y, pred, th=0.5):
    """
    Count true positives.

Args:
    y (np.array): ground truth, size (n_examples)
    pred (np.array): model output, size (n_examples)
    th (float): cutoff value for positive prediction from model
    Returns:
        TP (int): true positives
    """
    TP = 0

# get thresholded predictions
    thresholded_preds = pred >= th
```

```
# compute TP
   TP = np.sum((y == 1) & (thresholded preds == 1))
   return TP
def true negatives(y, pred, th=0.5):
   Count true negatives.
   Args:
        y (np.array): ground truth, size (n examples)
        pred (np.array): model output, size (n examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        TN (int): true negatives
    .....
   TN = 0
   # get thresholded predictions
   thresholded preds = pred >= th
   ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
   # compute TN
   TN = np.sum((y == 0) & (thresholded preds == 0))
   ### END CODE HERE ###
   return TN
def false positives(y, pred, th=0.5):
   Count false positives.
   Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n examples)
        th (float): cutoff value for positive prediction from model
       FP (int): false positives
   FP = 0
   # get thresholded predictions
   thresholded preds = pred >= th
   ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
   # compute FP
   FP = np.sum((y == 0) & (thresholded preds == 1))
```

```
### END CODE HERE ###
    return FP
def false negatives(y, pred, th=0.5):
    Count false positives.
    Args:
        y (np.array): ground truth, size (n examples)
        pred (np.array): model output, size (n examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        FN (int): false negatives
    FN = 0
    # get thresholded predictions
    thresholded preds = pred >= th
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
    # compute FN
    FN = np.sum((y == 1) & (thresholded preds == 0))
    ### END CODE HERE ###
    return FN
```

In [9]: # Note: we must explicity import 'display' in order for the autogra der to compile the submitted code # Even though we could use this function without importing it, keep this import in order to allow the grader to work from IPython.display import display # Test $df = pd.DataFrame(\{'y test': [1,1,0,0,0,0,0,0,0,1,1,1,1,1,1],$ 'preds test': [0.8,0.7,0.4,0.3,0.2,0.5,0.6,0.7,0 .8,0.1,0.2,0.3,0.4,0], 'category': ['TP','TP','TN','TN','TN','FP','FP', 'FP', 'FP', 'FN', 'FN', 'FN', 'FN', 'FN'] display(df) #y test = np.array([1, 0, 0, 1, 1])y_test = df['y_test'] #preds test = np.array([0.8, 0.8, 0.4, 0.6, 0.3]) preds test = df['preds test'] threshold = 0.5print(f"threshold: {threshold}\n") print(f"""Our functions calculated: TP: {true positives(y test, preds test, threshold)} TN: {true negatives(y test, preds test, threshold)} FP: {false positives(y test, preds test, threshold)} FN: {false negatives(y test, preds test, threshold)} """) print("Expected results") print(f"There are {sum(df['category'] == 'TP')} TP") print(f"There are {sum(df['category'] == 'TN')} TN") print(f"There are {sum(df['category'] == 'FP')} FP") print(f"There are {sum(df['category'] == 'FN')} FN")

	y_test	preds_test	category
0	1	0.8	TP
1	1	0.7	TP
2	0	0.4	TN
3	0	0.3	TN
4	0	0.2	TN
5	0	0.5	FP
6	0	0.6	FP
7	0	0.7	FP
8	0	0.8	FP
9	1	0.1	FN
10	1	0.2	FN
11	1	0.3	FN
12	1	0.4	FN
13	1	0.0	FN

threshold: 0.5

Our functions calculated:

TP: 2 TN: 3 FP: 4 FN: 5

Expected results

There are 2 TP

There are 3 TN

There are 4 FP

There are 5 FN

Run the next cell to see a summary of evaluative metrics for the model predictions for each class.

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In [10]: util.get_performance_metrics(y, pred, class_labels)

Out[10]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	Not Defined	Not Defined	Not Defined	Not Defined
Emphysema	20	869	103	8	Not Defined	Not Defined	Not Defined	Not Defined
Effusion	99	690	196	15	Not Defined	Not Defined	Not Defined	Not Defined
Hernia	1	743	255	1	Not Defined	Not Defined	Not Defined	Not Defined
Infiltration	114	543	265	78	Not Defined	Not Defined	Not Defined	Not Defined
Mass	40	789	158	13	Not Defined	Not Defined	Not Defined	Not Defined
Nodule	28	731	220	21	Not Defined	Not Defined	Not Defined	Not Defined
Atelectasis	64	657	249	30	Not Defined	Not Defined	Not Defined	Not Defined
Pneumothorax	24	785	183	8	Not Defined	Not Defined	Not Defined	Not Defined
Pleural_Thickening	24	713	259	4	Not Defined	Not Defined	Not Defined	Not Defined
Pneumonia	14	661	320	5	Not Defined	Not Defined	Not Defined	Not Defined
Fibrosis	10	725	261	4	Not Defined	Not Defined	Not Defined	Not Defined
Edema	15	767	213	5	Not Defined	Not Defined	Not Defined	Not Defined
Consolidation	36	658	297	9	Not Defined	Not Defined	Not Defined	Not Defined

Right now it only has TP, TN, FP, FN. Throughout this assignment we'll fill in all the other metrics to learn more about our model performance.

3.2 Accuracy

Let's use a threshold of .5 for the probability cutoff for our predictions for all classes and calculate our model's accuracy as we would normally do in a machine learning problem.

```
accuracy = \frac{\text{true positives} + \text{true negatives}}{\text{true positives} + \text{true negatives} + \text{false positives} + \text{false negatives}}
```

Use this formula to compute accuracy below:

▶ Hints

```
In [11]: # UNQ C2 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get_accuracy(y, pred, th=0.5):
             Compute accuracy of predictions at threshold.
             Args:
                 y (np.array): ground truth, size (n examples)
                 pred (np.array): model output, size (n examples)
                 th (float): cutoff value for positive prediction from model
             Returns:
                 accuracy (float): accuracy of predictions at threshold
             accuracy = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
         ) ###
             # get TP, FP, TN, FN using our previously defined functions
             TP = true positives(y, pred, th)
             FP = false_positives(y, pred, th)
             TN = true negatives(y, pred, th)
             FN = false_negatives(y, pred, th)
             # Compute accuracy using TP, FP, TN, FN
             accuracy = (TP+TN)/(TP+TN+FP+FN)
             ### END CODE HERE ###
             return accuracy
```

```
In [12]: # Test
    print("Test case:")

y_test = np.array([1, 0, 0, 1, 1])
    print('test labels: {y_test}')

preds_test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
    print(f'test predictions: {preds_test}')

threshold = 0.5
    print(f"threshold: {threshold}")

print(f"computed accuracy: {get_accuracy(y_test, preds_test, threshold)}")

Test case:
```

```
Test case:
test labels: {y_test}
test predictions: [0.8 0.8 0.4 0.6 0.3]
threshold: 0.5
computed accuracy: 0.6
```

Expected output:

```
test labels: {y_test}
test predictions: [0.8 0.8 0.4 0.6 0.3]
threshold: 0.5
computed accuracy: 0.6
```

Run the next cell to see the accuracy of the model output for each class, as well as the number of true positives, true negatives, false positives, and false negatives.

```
In [13]: util.get_performance_metrics(y, pred, class_labels, acc=get_accurac
y)
```

Out[13]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	Not Defined	Not Defined	Not Defined
Emphysema	20	869	103	8	0.889	Not Defined	Not Defined	Not Defined
Effusion	99	690	196	15	0.789	Not Defined	Not Defined	Not Defined
Hernia	1	743	255	1	0.744	Not Defined	Not Defined	Not Defined
Infiltration	114	543	265	78	0.657	Not Defined	Not Defined	Not Defined
Mass	40	789	158	13	0.829	Not Defined	Not Defined	Not Defined
Nodule	28	731	220	21	0.759	Not Defined	Not Defined	Not Defined
Atelectasis	64	657	249	30	0.721	Not Defined	Not Defined	Not Defined
Pneumothorax	24	785	183	8	0.809	Not Defined	Not Defined	Not Defined
Pleural_Thickening	24	713	259	4	0.737	Not Defined	Not Defined	Not Defined
Pneumonia	14	661	320	5	0.675	Not Defined	Not Defined	Not Defined
Fibrosis	10	725	261	4	0.735	Not Defined	Not Defined	Not Defined
Edema	15	767	213	5	0.782	Not Defined	Not Defined	Not Defined
Consolidation	36	658	297	9	0.694	Not Defined	Not Defined	Not Defined

If we were to judge our model's performance based on the accuracy metric, we would say that our model is not very accurate for detecting the Infiltration cases (accuracy of 0.657) but pretty accurate for detecting Emphysema (accuracy of 0.889).

But is that really the case?...

Let's imagine a model that simply predicts that any patient does **Not** have Emphysema, regardless of patient's measurements. Let's calculate the accuracy for such a model.

```
In [14]: get_accuracy(valid_results["Emphysema"].values, np.zeros(len(valid_results)))
Out[14]: 0.972
```

As you can see above, such a model would be 97% accurate! Even better than our deep learning based model.

But is this really a good model? Wouldn't this model be wrong 100% of the time if the patient actually had this condition?

In the following sections, we will address this concern with more advanced model measures - **sensitivity** and **specificity** - that evaluate how well the model predicts positives for patients with the condition and negatives for cases that actually do not have the condition.

3.3 Prevalence

Another important concept is **prevalence**.

- In a medical context, prevalence is the proportion of people in the population who have the disease (or condition, etc).
- In machine learning terms, this is the proportion of positive examples. The expression for prevalence is:

$$prevalence = \frac{1}{N} \sum_{i} y_{i}$$

where $y_i = 1$ when the example is 'positive' (has the disease).

Let's measure prevalence for each disease:

▶ Hints

```
In [15]: # UNQ C3 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get prevalence(y):
             Compute prevalence.
             Args:
                 y (np.array): ground truth, size (n examples)
             Returns:
                 prevalence (float): prevalence of positive cases
             prevalence = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
         ) ###
             prevalence = np.mean(y)
             ### END CODE HERE ###
             return prevalence
In [16]: # Test
         print("Test case:\n")
         y_{test} = np.array([1, 0, 0, 1, 1, 0, 0, 0, 0, 1])
         print(f'test labels: {y_test}')
```

Test case:

test labels: [1 0 0 1 1 0 0 0 0 1] computed prevalence: 0.4

In [17]: util.get_performance_metrics(y, pred, class_labels, acc=get_accurac
y, prevalence=get_prevalence)

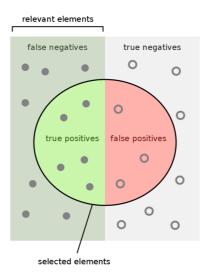
print(f"computed prevalence: {get prevalence(y test)}")

Out[17]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	0.017	Not Defined	Not Defined
Emphysema	20	869	103	8	0.889	0.028	Not Defined	Not Defined
Effusion	99	690	196	15	0.789	0.114	Not Defined	Not Defined
Hernia	1	743	255	1	0.744	0.002	Not Defined	Not Defined
Infiltration	114	543	265	78	0.657	0.192	Not Defined	Not Defined
Mass	40	789	158	13	0.829	0.053	Not Defined	Not Defined
Nodule	28	731	220	21	0.759	0.049	Not Defined	Not Defined
Atelectasis	64	657	249	30	0.721	0.094	Not Defined	Not Defined
Pneumothorax	24	785	183	8	0.809	0.032	Not Defined	Not Defined
Pleural_Thickening	24	713	259	4	0.737	0.028	Not Defined	Not Defined
Pneumonia	14	661	320	5	0.675	0.019	Not Defined	Not Defined
Fibrosis	10	725	261	4	0.735	0.014	Not Defined	Not Defined
Edema	15	767	213	5	0.782	0.02	Not Defined	Not Defined
Consolidation	36	658	297	9	0.694	0.045	Not Defined	Not Defined

Hernia has a prevalence 0.002, which is the rarest among the studied conditions in our dataset.

3.4 Sensitivity and Specificity



Sensitivity and specificity are two of the most prominent numbers that are used to measure diagnostics tests.

- Sensitivity is the probability that our test outputs positive given that the case is actually positive.
- Specificity is the probability that the test outputs negative given that the case is actually negative.

We can phrase this easily in terms of true positives, true negatives, false positives, and false negatives:

$$sensitivity = \frac{\text{true positives}}{\text{true positives} + \text{false negatives}}$$
$$specificity = \frac{\text{true negatives}}{\text{true negatives} + \text{false positives}}$$

Let's calculate sensitivity and specificity for our model:

```
### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
   # get TP and FN using our previously defined functions
   TP = true positives(y, pred, th)
   FN = false negatives(y, pred, th)
   # use TP and FN to compute sensitivity
   sensitivity = TP/(TP+FN)
   ### END CODE HERE ###
   return sensitivity
def get specificity(y, pred, th=0.5):
   Compute specificity of predictions at threshold.
   Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n examples)
        th (float): cutoff value for positive prediction from model
   Returns:
        specificity (float): probability that the test outputs nega
tive given that the case is actually negative
   specificity = 0.0
   ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
   # get TN and FP using our previously defined functions
   TN = true negatives(y, pred, th)
   FP = false positives(y, pred, th)
   # use TN and FP to compute specificity
   specificity = TN/(TN+FP)
   ### END CODE HERE ###
   return specificity
```

```
In [21]: # Test
         print("Test case")
         y_test = np.array([1, 0, 0, 1, 1])
         print(f'test labels: {y_test}\n')
         preds test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
         print(f'test predictions: {preds_test}\n')
         threshold = 0.5
         print(f"threshold: {threshold}\n")
         print(f"computed sensitivity: {get sensitivity(y test, preds test,
         threshold):.2f}")
         print(f"computed specificity: {get_specificity(y_test, preds_test,
         threshold):.2f}")
         Test case
         test labels: [1 0 0 1 1]
         test predictions: [0.8 0.8 0.4 0.6 0.3]
         threshold: 0.5
         computed sensitivity: 0.67
```

Expected output:

```
Test case
test labels: [1 0 0 1 1]

test predictions: [0.8 0.8 0.4 0.6 0.3]

threshold: 0.5

computed sensitivity: 0.67
computed specificity: 0.50
```

computed specificity: 0.50

Out[22]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	0.017	0.941	0.828
Emphysema	20	869	103	8	0.889	0.028	0.714	0.894
Effusion	99	690	196	15	0.789	0.114	0.868	0.779
Hernia	1	743	255	1	0.744	0.002	0.5	0.744
Infiltration	114	543	265	78	0.657	0.192	0.594	0.672
Mass	40	789	158	13	0.829	0.053	0.755	0.833
Nodule	28	731	220	21	0.759	0.049	0.571	0.769
Atelectasis	64	657	249	30	0.721	0.094	0.681	0.725
Pneumothorax	24	785	183	8	0.809	0.032	0.75	0.811
Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	0.734
Pneumonia	14	661	320	5	0.675	0.019	0.737	0.674
Fibrosis	10	725	261	4	0.735	0.014	0.714	0.735
Edema	15	767	213	5	0.782	0.02	0.75	0.783
Consolidation	36	658	297	9	0.694	0.045	0.8	0.689

Note that specificity and sensitivity do not depend on the prevalence of the positive class in the dataset.

- This is because the statistics are only computed within people of the same class
- Sensitivity only considers output on people in the positive class
- Similarly, specificity only considers output on people in the negative class.

3.5 PPV and NPV

Diagnostically, however, sensitivity and specificity are not helpful. Sensitivity, for example, tells us the probability our test outputs positive given that the person already has the condition. Here, we are conditioning on the thing we would like to find out (whether the patient has the condition)!

What would be more helpful is the probability that the person has the disease given that our test outputs positive. That brings us to positive predictive value (PPV) and negative predictive value (NPV).

- Positive predictive value (PPV) is the probability that subjects with a positive screening test truly have the disease.
- Negative predictive value (NPV) is the probability that subjects with a negative screening test truly don't have the disease.

Again, we can formulate these in terms of true positives, true negatives, false positives, and false negatives:

$$PPV = \frac{\text{true positives}}{\text{true positives} + \text{false positives}}$$

$$NPV = \frac{\text{true negatives}}{\text{true negatives} + \text{false negatives}}$$

Let's calculate PPV & NPV for our model:

```
In [23]: # UNQ_C5 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
         def get ppv(y, pred, th=0.5):
             Compute PPV of predictions at threshold.
             Args:
                 y (np.array): ground truth, size (n examples)
                 pred (np.array): model output, size (n examples)
                 th (float): cutoff value for positive prediction from model
             Returns:
                 PPV (float): positive predictive value of predictions at th
         reshold
             PPV = 0.0
             ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
         ) ###
             # get TP and FP using our previously defined functions
             TP = true positives(y, pred, th)
             FP = false positives(y, pred, th)
             # use TP and FP to compute PPV
```

```
PPV = TP/(TP+FP)
    ### END CODE HERE ###
    return PPV
def get_npv(y, pred, th=0.5):
    Compute NPV of predictions at threshold.
    Args:
        y (np.array): ground truth, size (n_examples)
        pred (np.array): model output, size (n examples)
        th (float): cutoff value for positive prediction from model
    Returns:
        NPV (float): negative predictive value of predictions at th
reshold
   NPV = 0.0
    ### START CODE HERE (REPLACE INSTANCES OF 'None' with your code
) ###
    # get TN and FN using our previously defined functions
    TN = true_negatives(y, pred, th)
    FN = false negatives(y, pred, th)
    # use TN and FN to compute NPV
   NPV = TN/(TN+FN)
    ### END CODE HERE ###
    return NPV
```

```
In [24]: # Test
         print("Test case:\n")
         y_test = np.array([1, 0, 0, 1, 1])
         print(f'test labels: {y_test}')
         preds test = np.array([0.8, 0.8, 0.4, 0.6, 0.3])
         print(f'test predictions: {preds_test}\n')
         threshold = 0.5
         print(f"threshold: {threshold}\n")
         print(f"computed ppv: {get_ppv(y_test, preds_test, threshold):.2f}"
         print(f"computed npv: {get_npv(y_test, preds_test, threshold):.2f}"
         Test case:
         test labels: [1 0 0 1 1]
         test predictions: [0.8 0.8 0.4 0.6 0.3]
         threshold: 0.5
         computed ppv: 0.67
         computed npv: 0.50
```

Expected output:

Test case:

ppv=get ppv, npv=get npv)

Out[25]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	0.017	0.941	0.828
Emphysema	20	869	103	8	0.889	0.028	0.714	0.894
Effusion	99	690	196	15	0.789	0.114	0.868	0.779
Hernia	1	743	255	1	0.744	0.002	0.5	0.744
Infiltration	114	543	265	78	0.657	0.192	0.594	0.672
Mass	40	789	158	13	0.829	0.053	0.755	0.833
Nodule	28	731	220	21	0.759	0.049	0.571	0.769
Atelectasis	64	657	249	30	0.721	0.094	0.681	0.725
Pneumothorax	24	785	183	8	0.809	0.032	0.75	0.811
Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	0.734
Pneumonia	14	661	320	5	0.675	0.019	0.737	0.674
Fibrosis	10	725	261	4	0.735	0.014	0.714	0.735
Edema	15	767	213	5	0.782	0.02	0.75	0.783
Consolidation	36	658	297	9	0.694	0.045	0.8	0.689

Notice that despite having very high sensitivity and accuracy, the PPV of the predictions could still be very low.

This is the case with Edema, for example.

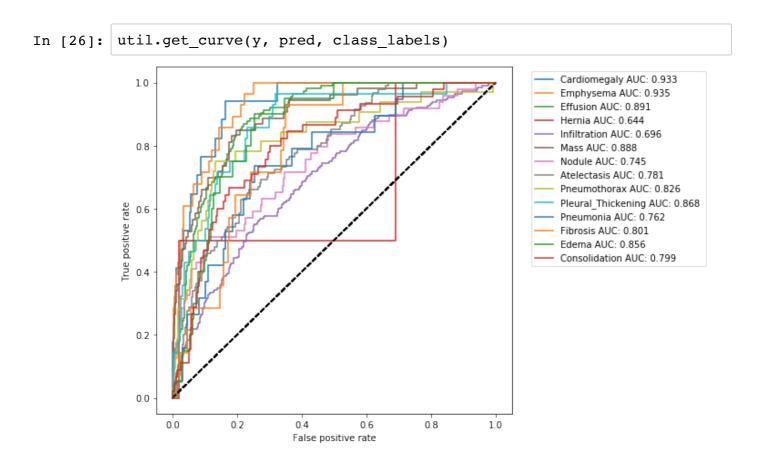
- The sensitivity for Edema is 0.75.
- However, given that the model predicted positive, the probability that a person has Edema (its PPV) is only 0.066!

3.6 ROC Curve

So far we have been operating under the assumption that our model's prediction of 0.5 and above should be treated as positive and otherwise it should be treated as negative. This however was a rather arbitrary choice. One way to see this, is to look at a very informative visualization called the receiver operating characteristic (ROC) curve.

The ROC curve is created by plotting the true positive rate (TPR) against the false positive rate (FPR) at various threshold settings. The ideal point is at the top left, with a true positive rate of 1 and a false positive rate of 0. The various points on the curve are generated by gradually changing the threshold.

Let's look at this curve for our model:



The area under the ROC curve is also called AUCROC or C-statistic and is a measure of goodness of fit. In medical literature this number also gives the probability that a randomly selected patient who experienced a condition had a higher risk score than a patient who had not experienced the event. This summarizes the model output across all thresholds, and provides a good sense of the discriminative power of a given model.

Let's use the sklearn metric function of roc auc score to add this score to our metrics table.

Out[27]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	0.017	0.941	0.828
Emphysema	20	869	103	8	0.889	0.028	0.714	0.894
Effusion	99	690	196	15	0.789	0.114	0.868	0.779
Hernia	1	743	255	1	0.744	0.002	0.5	0.744
Infiltration	114	543	265	78	0.657	0.192	0.594	0.672
Mass	40	789	158	13	0.829	0.053	0.755	0.833
Nodule	28	731	220	21	0.759	0.049	0.571	0.769
Atelectasis	64	657	249	30	0.721	0.094	0.681	0.725
Pneumothorax	24	785	183	8	0.809	0.032	0.75	0.811
Pleural_Thickening	24	713	259	4	0.737	0.028	0.857	0.734
Pneumonia	14	661	320	5	0.675	0.019	0.737	0.674
Fibrosis	10	725	261	4	0.735	0.014	0.714	0.735
Edema	15	767	213	5	0.782	0.02	0.75	0.783
Consolidation	36	658	297	9	0.694	0.045	0.8	0.689

4. Confidence Intervals

Of course our dataset is only a sample of the real world, and our calculated values for all above metrics is an estimate of the real world values. It would be good to quantify this uncertainty due to the sampling of our dataset. We'll do this through the use of confidence intervals. A 95\% confidence interval for an estimate s of a parameter s is an interval I=(a,b) such that 95\% of the time when the experiment is run, the true value s is contained in s. More concretely, if we were to run the experiment many times, then the fraction of those experiments for which s contains the true parameter would tend towards 95\%.

While some estimates come with methods for computing the confidence interval analytically, more complicated statistics, such as the AUC for example, are difficult. For these we can use a method called the *bootstrap*. The bootstrap estimates the uncertainty by resampling the dataset with replacement. For each resampling i, we will get a new estimate, s_i . We can then estimate the distribution of s by using the distribution of s_i for our bootstrap samples.

In the code below, we create bootstrap samples and compute sample AUCs from those samples. Note that we use stratified random sampling (sampling from the positive and negative classes separately) to make sure that members of each class are represented.

```
In [28]: def bootstrap_auc(y, pred, classes, bootstraps = 100, fold_size = 1
             statistics = np.zeros((len(classes), bootstraps))
             for c in range(len(classes)):
                 df = pd.DataFrame(columns=['y', 'pred'])
                 df.loc[:, 'y'] = y[:, c]
                 df.loc[:, 'pred'] = pred[:, c]
                 # get positive examples for stratified sampling
                 df_pos = df[df.y == 1]
                 df neg = df[df.y == 0]
                 prevalence = len(df pos) / len(df)
                 for i in range(bootstraps):
                     # stratified sampling of positive and negative examples
                     pos_sample = df_pos.sample(n = int(fold_size * prevalen
         ce), replace=True)
                     neg sample = df neg.sample(n = int(fold size * (1-preva
         lence)), replace=True)
                     y sample = np.concatenate([pos sample.y.values, neg sam
         ple.y.values])
                     pred_sample = np.concatenate([pos_sample.pred.values, n
         eg sample.pred.values])
                     score = roc auc score(y sample, pred sample)
                     statistics[c][i] = score
             return statistics
         statistics = bootstrap auc(y, pred, class labels)
```

Now we can compute confidence intervals from the sample statistics that we computed.

In [29]: util.print_confidence_intervals(class_labels, statistics)

Out[29]:

	Mean AUC (CI 5%-95%)
Cardiomegaly	0.93 (0.90-0.96)
Emphysema	0.93 (0.91-0.96)
Effusion	0.89 (0.87-0.91)
Hernia	0.63 (0.30-0.98)
Infiltration	0.70 (0.67-0.73)
Mass	0.89 (0.85-0.92)
Nodule	0.75 (0.66-0.81)
Atelectasis	0.78 (0.75-0.82)
Pneumothorax	0.83 (0.74-0.91)
Pleural_Thickening	0.87 (0.81-0.92)
Pneumonia	0.75 (0.68-0.83)
Fibrosis	0.80 (0.74-0.86)
Edema	0.85 (0.80-0.89)
Consolidation	0.81 (0.75-0.86)

As you can see, our confidence intervals are much wider for some classes than for others. Hernia, for example, has an interval around (0.30 - 0.98), indicating that we can't be certain it is better than chance (at 0.5).

5. Precision-Recall Curve

Precision-Recall is a useful measure of success of prediction when the classes are very imbalanced.

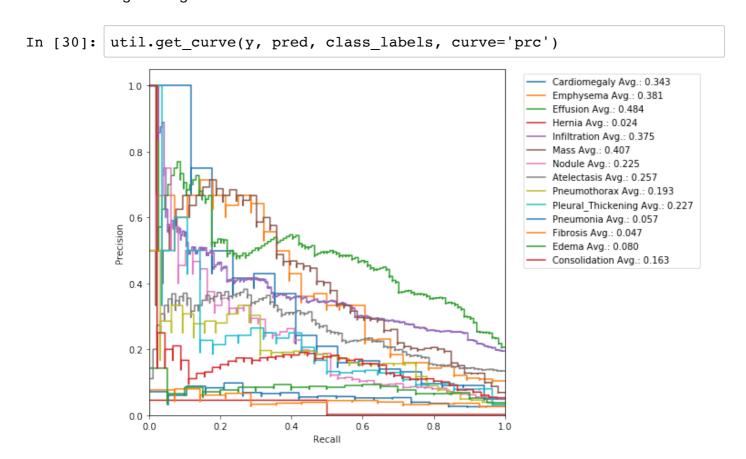
In information retrieval

- Precision is a measure of result relevancy and that is equivalent to our previously defined PPV.
- Recall is a measure of how many truly relevant results are returned and that is equivalent to our previously defined sensitivity measure.

The precision-recall curve (PRC) shows the trade-off between precision and recall for different thresholds. A high area under the curve represents both high recall and high precision, where high precision relates to a low false positive rate, and high recall relates to a low false negative rate.

High scores for both show that the classifier is returning accurate results (high precision), as well as returning a majority of all positive results (high recall).

Run the following cell to generate a PRC:



6. F1 Score

F1 score is the harmonic mean of the precision and recall, where an F1 score reaches its best value at 1 (perfect precision and recall) and worst at 0.

Again, we can simply use sklearn's utility metric function of f1_score to add this measure to our performance table.

In [31]: from sklearn.metrics import f1_score
 util.get_performance_metrics(y, pred, class_labels, acc=get_accurac
 y, prevalence=get prevalence,

sens=get_sensitivity, spec=get_specificity,
ppv=get ppv, npv=get npv, auc=roc auc score,f1=f1 score)

Out[31]:

	TP	TN	FP	FN	Accuracy	Prevalence	Sensitivity	Specificity
Cardiomegaly	16	814	169	1	0.83	0.017	0.941	0.828
Emphysema	20	869	103	8	0.889	0.028	0.714	0.894
Effusion	99	690	196	15	0.789	0.114	0.868	0.779
Hernia	1	743	255	1	0.744	0.002	0.5	0.744
Infiltration	114	543	265	78	0.657	0.192	0.594	0.672
Mass	40	789	158	13	0.829	0.053	0.755	0.833
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Edema	15	767	213	5	0.782	0.02	0.75	0.783
Consolidation	36	658	297	9	0.694	0.045	0.8	0.689

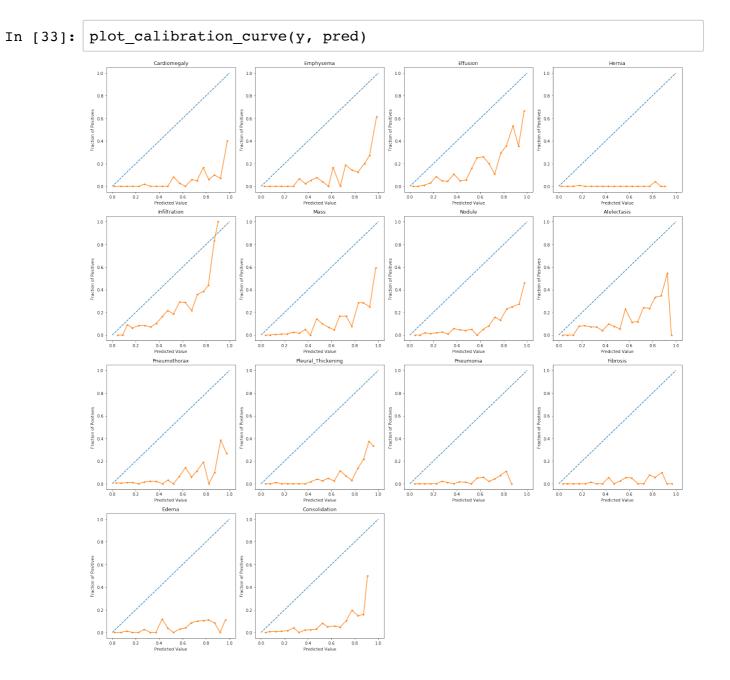
7. Calibration

When performing classification we often want not only to predict the class label, but also obtain a probability of each label. This probability would ideally give us some kind of confidence on the prediction. In order to observe how our model's generated probabilities are aligned with the real probabilities, we can plot what's called a *calibration curve*.

In order to generate a calibration plot, we first bucketize our predictions to a fixed number of separate bins (e.g. 5) between 0 and 1. We then calculate a point for each bin: the x-value for each point is the mean for the probability that our model has assigned to these points and the y-value for each point fraction of true positives in that bin. We then plot these points in a linear plot. A well-calibrated model has a calibration curve that almost aligns with the y=x line.

The sklearn library has a utility calibration_curve for generating a calibration plot. Let's use it and take a look at our model's calibration:

```
In [32]:
         from sklearn.calibration import calibration curve
         def plot calibration curve(y, pred):
             plt.figure(figsize=(20, 20))
             for i in range(len(class labels)):
                 plt.subplot(4, 4, i + 1)
                 fraction of positives, mean predicted value = calibration c
         urve(y[:,i], pred[:,i], n bins=20)
                 plt.plot([0, 1], [0, 1], linestyle='--')
                 plt.plot(mean_predicted_value, fraction_of_positives, marke
         r='.')
                 plt.xlabel("Predicted Value")
                 plt.ylabel("Fraction of Positives")
                 plt.title(class labels[i])
             plt.tight layout()
             plt.show()
```

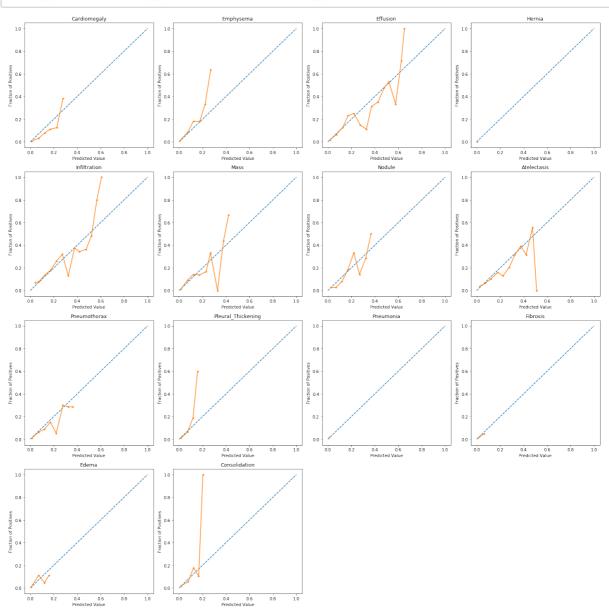


As the above plots show, for most predictions our model's calibration plot does not resemble a well calibrated plot. How can we fix that?...

Thankfully, there is a very useful method called <u>Platt scaling (https://en.wikipedia.org/wiki/Platt_scaling)</u> which works by fitting a logistic regression model to our model's scores. To build this model, we will be using the training portion of our dataset to generate the linear model and then will use the model to calibrate the predictions for our test portion.

In [34]: from sklearn.linear_model import LogisticRegression as LR y_train = train_results[class_labels].values pred_train = train_results[pred_labels].values pred_calibrated = np.zeros_like(pred) for i in range(len(class_labels)): lr = LR(solver='liblinear', max_iter=10000) lr.fit(pred_train[:, i].reshape(-1, 1), y_train[:, i]) pred_calibrated[:, i] = lr.predict_proba(pred[:, i].reshape(-1, 1))[:,1]

In [35]: plot_calibration_curve(y[:,], pred_calibrated)



That's it!

Congratulations! That was a lot of metrics to get familiarized with. We hope that you feel a lot more confident in your understanding of medical diagnostic evaluation and test your models correctly in your future work :)