



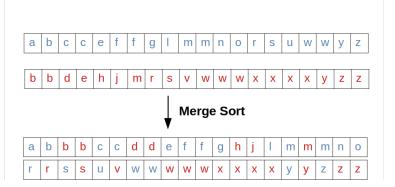
1 Introduction

Introduction

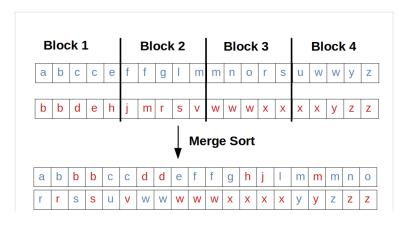
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- 3 Batch merge
- 4 Application in Cryptanalysis

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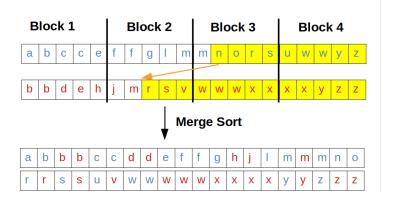




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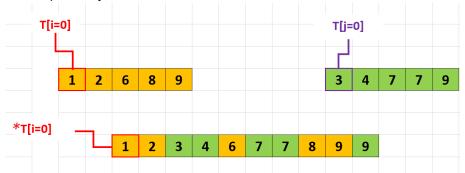


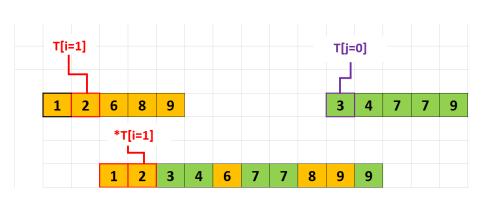
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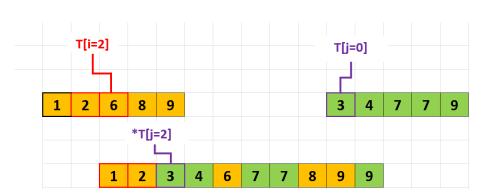
Merge Path and Sort Sorbonne Université

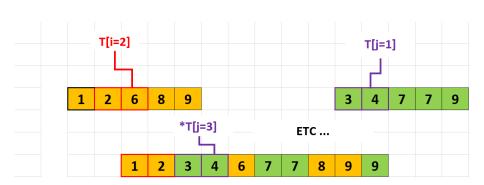
The most common idea is to use two pointers and increment one of them whenever it has the lowest value among both, while copying its value to the output array:











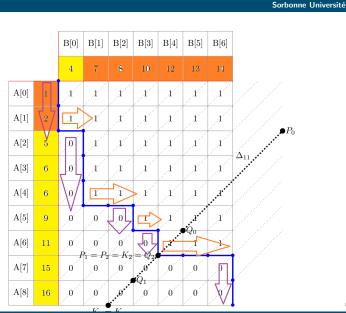


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A[i] < B[j]



1 marked

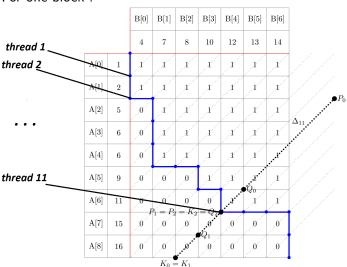




- It is simple to implement
- It has always the same linear complexity $\Theta(|A| + |B|)$: no bad surprise
- In its original form, it is impossible to parallelize the algorithm.
- An average linear complexity is not optimal

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For one block:



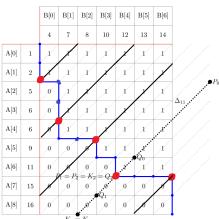


- Parallel Partition
 - ⇒ Map exactly the necessary inputs into each tile.
- Merge Path
 - ⇒ Cross diagonal binary search GLOBAL MEMORY
- MergeSort of the Merge Path ⇒ Placing the Merge Path on the SHARED MEMORY ⇒ Blocksort



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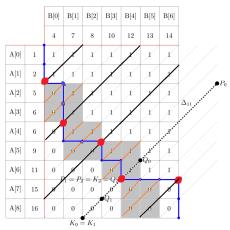
Diagonals divide the work among the blocks. Points of intersection using binary searches on the cross diagonals by comparing elements from A and B on **GLOBAL MEMORY**.





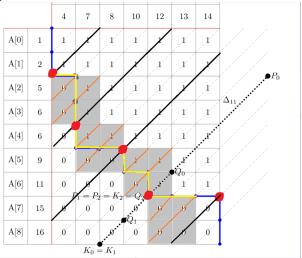
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Take a window consisting of the Z largest elements of each of the partitions and place them in local **SHARED MEMORY**.



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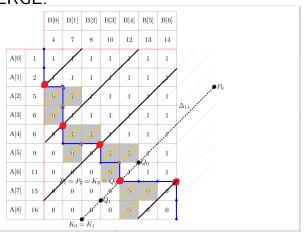
Write the Merge Path found on GLOBAL MEMORY.





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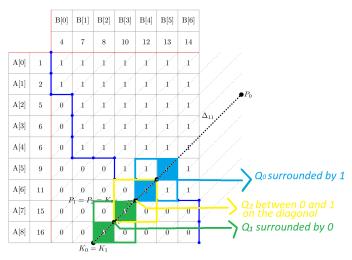
Several cycles in parallel and Place the Merge Path on the **SHARED MEMORY** \Rightarrow MERGE.



Merge Path and Sort

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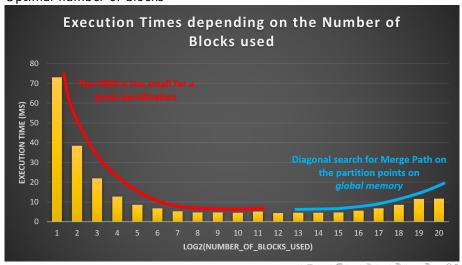
3 different cases illustration:



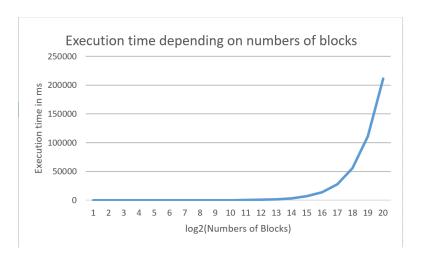


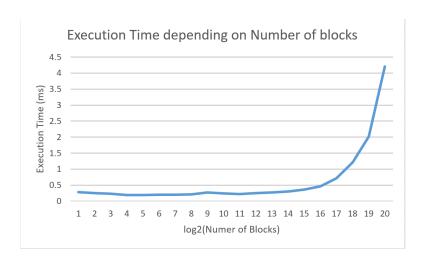
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Optimal number of blocks











- We decided to compare the wall-clock time of merging randomly generated vectors of integers for the three algorithms. For the GPU algorithm, we also monitored the wall-clock time for sort initialization ⇒CUDA EVEN TIMER
- Sanity check We implemented a sanity check (on CPU for the three versions) to check if the array is really sorted in the end of the program.



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We ran 100 simulations of the three algorithms, gathering the average wall-clock time of the merge part only. The task consisted in merging 2^{20} = 1,048,576 arrays of size 2

Algorithm	Wall-clock time (ms)	
Merge path (CPU)	50 032	
Sequential merge path	1 650	~
Merge path (GPU)	70	~

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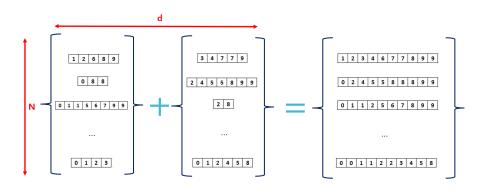
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Batch merge

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d: number of elements in a pair of array m: number of pairs of array mergesorted in a single block

- I int tidx = threadIdx.x%d ⇒ Enumeration from 0 to d-1 of the elements of each of the m pairs of arrays which are going to be sorted in a single block
- 2 int Qt = (threadIdx.x-tidx)/d \Rightarrow Local enumeration from 0 to m-1 of the pairs of arrays in a single block
- 3 int gbx = Qt + blockldx.x*(blockDim.x/d) \Rightarrow Global enumeration from 0 to N-1 of the pairs of arrays in all the blocks



	thread.ldx.x	tidx	Qt	Blockldx.x	gbx
A0	0	0	0	0	0
A1	1	1	0	0	0
A2	2	2	0	0	0
В0	3	3	0	0	0
B1	4	4	0	0	0
A0	5	0	1	0	1
A1	6	1	1	0	1
A2	7	2	1	0	1
A3	8	3	1	0	1
B0	9	4	1	0	1
A0	10	0	2	0	2
В0	11	1	2	0	2
B1	12	2	2	0	2
B2	13	3	2	0	2
В3	14	4	2	0	2
A0	0	0	0	1	1 2 2 2 2 2 2 3 3 3 3 3 3
B0	1	1	0	1	3
B1	2	2	0	1	3
B2	3	3	0	1	3
B3	4	4	0	1	3

Figure: Indices for d=5, N=4, BlockDim.x =15

Batch merge

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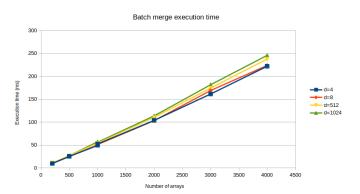


Figure: Batch merge execution times in function of N with various values of d

Batch merge

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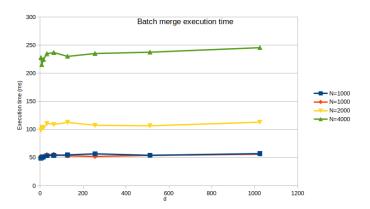


Figure: Batch merge execution times in function of d with various values of N



Figure: Batch merge execution times in function of ${\it N}=10^4$ with various values of ${\it d}$

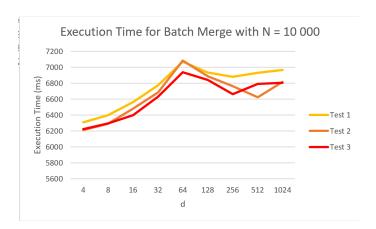


Figure: Batch merge execution times in function of ${\it N}=10^5$ with various values of ${\it d}$



Figure: Batch merge execution times in function of ${\it N}=10^6$ with various values of ${\it d}$

Batch merge

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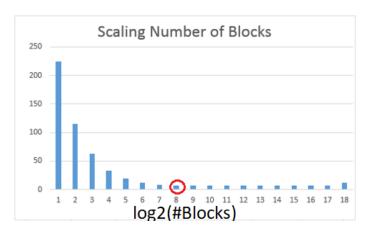


Figure: Scaling Numbers of blocks depending on the execution time in ms

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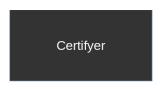




Figure: Alice and Bob wan't to get access to the certifyer



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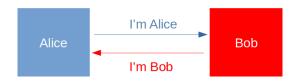


Figure: Alice and Bob recognise each other



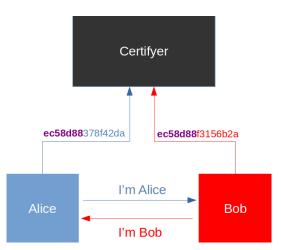


Figure: Alice and Bob send their hashed message



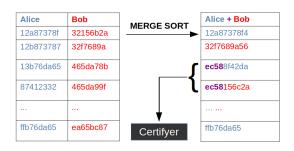


Figure: Merge sort and find keys to get access

```
./main
Initialize and sort every possible vectors ... Ok.
Alice and bob arrive ! Merge sort Alice's and Bob's vectors
dim: 80000
-13507636 -13507255 -13506814 -13506804 -13506753 -13506653
End. Execution time: 0.760576 ms
Try to find 2 chains with the same first bits
Begining of the search... End of the search.
2 keys are:
ff36e7fe
ff36e707
```

Figure: Output

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THANK YOU FOR YOUR ATTENTION! ANY QUESTIONS?

Reference: O. Green, R. McColl and D. A. Bader «GPU Merge Path, A GPU Merging Algorithm» 26th ACM International Conference on Supercomputing (ICS), San Servolo Islan, Venice, Italy, June 25-29, 2012

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