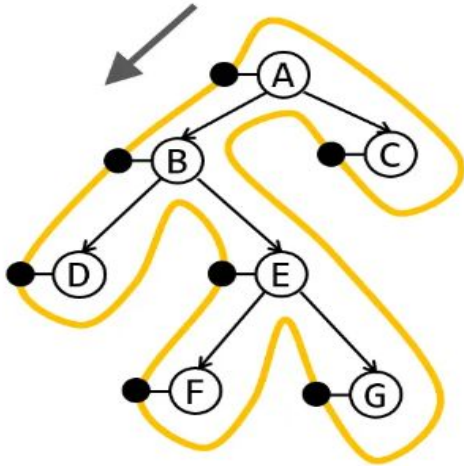


Depth First Search(DFS) on Trees

Naren Doraiswamy

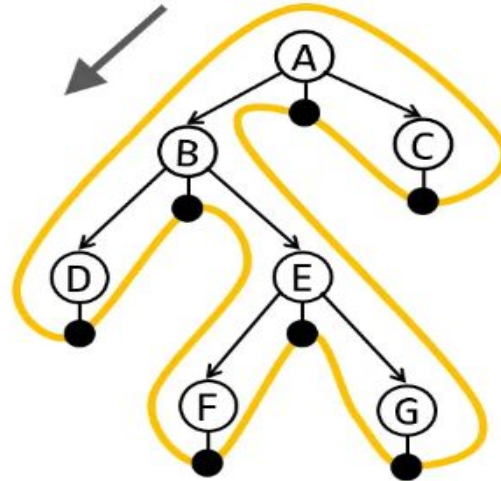
Tree Traversals

Node, Node.left, Node.right



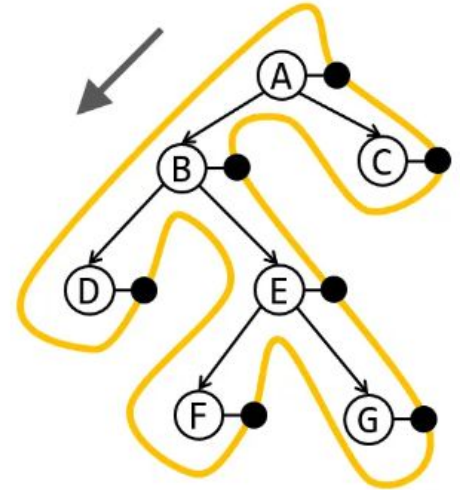
Pre-order traversal **[A, B, D, E, F, G, C]**

Node.left, Node, Node.right

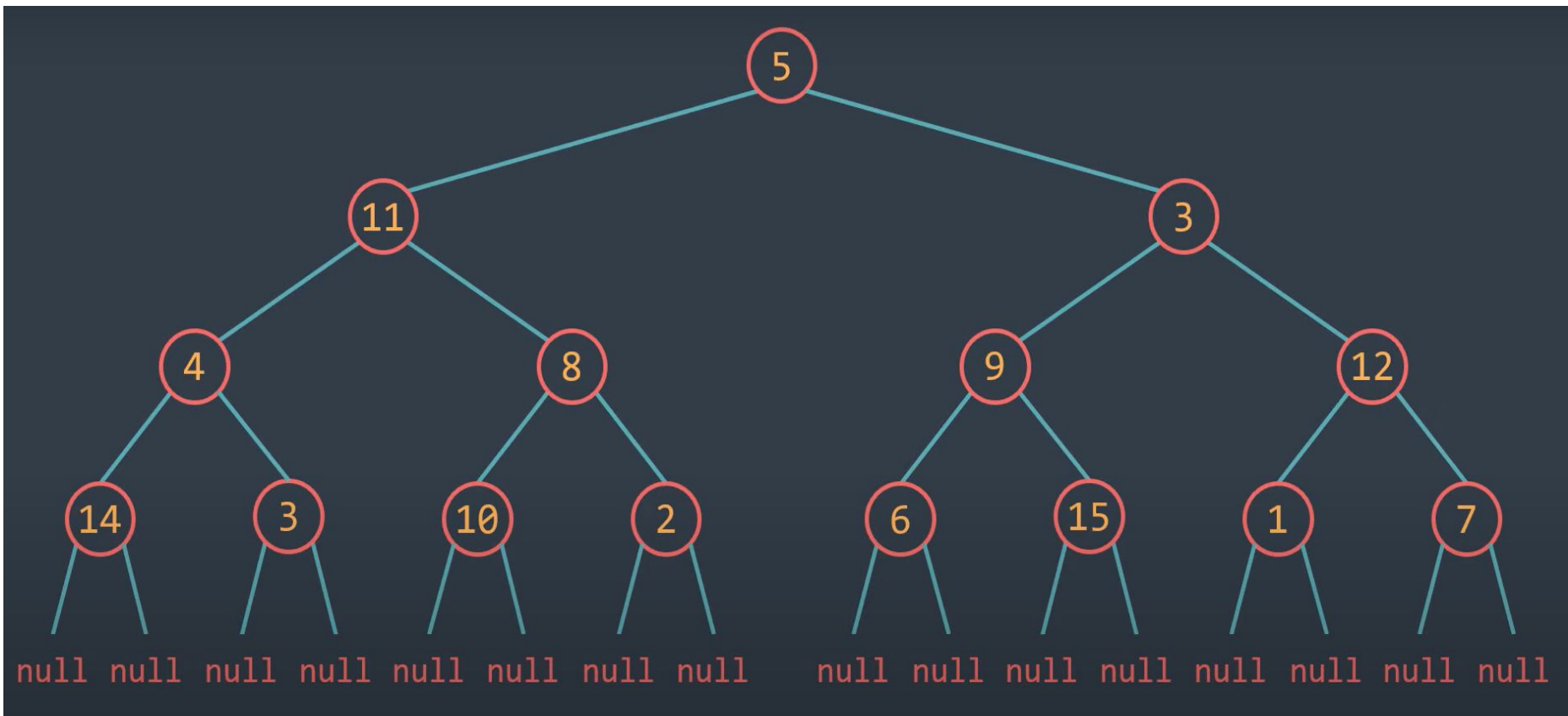


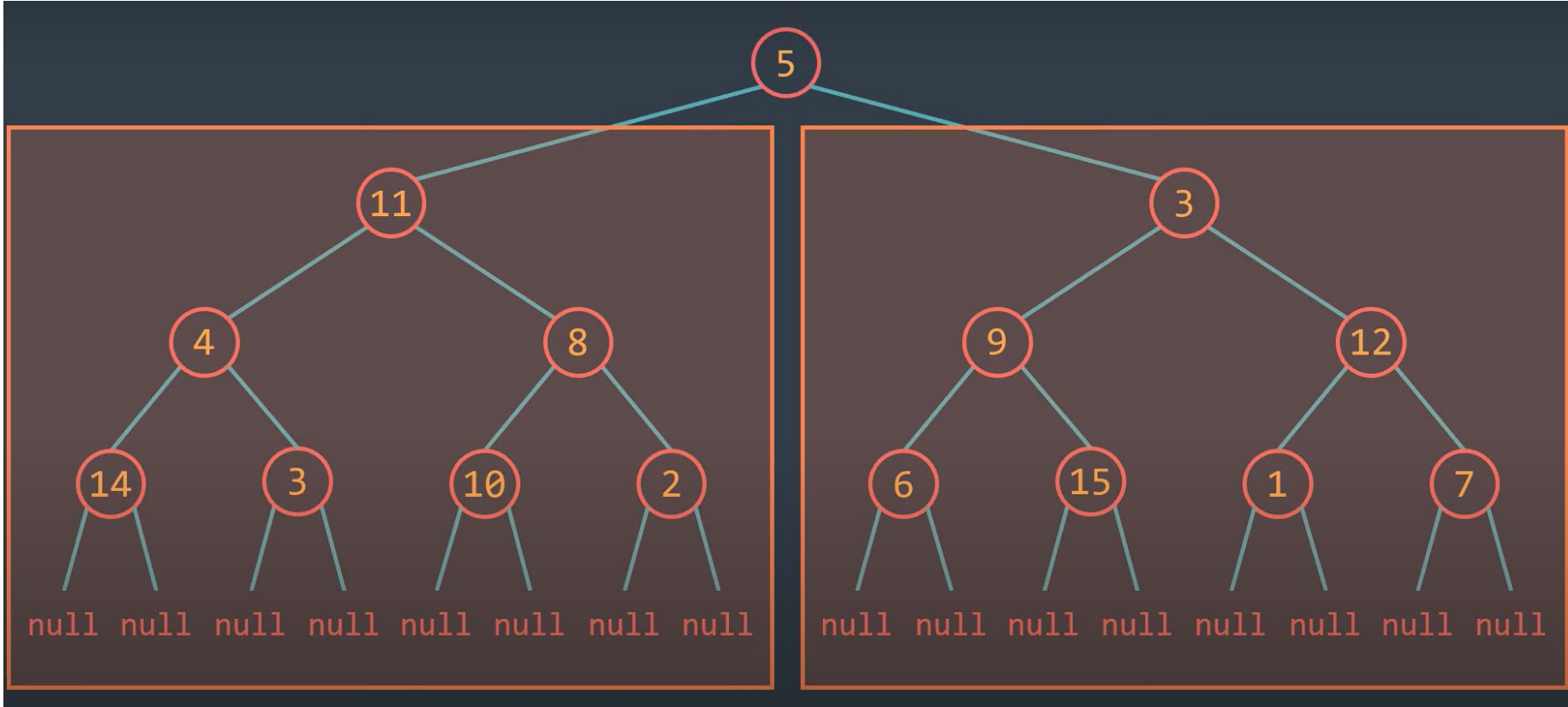
In-Order Traversal **[D, B, F, E, G, A, C]**

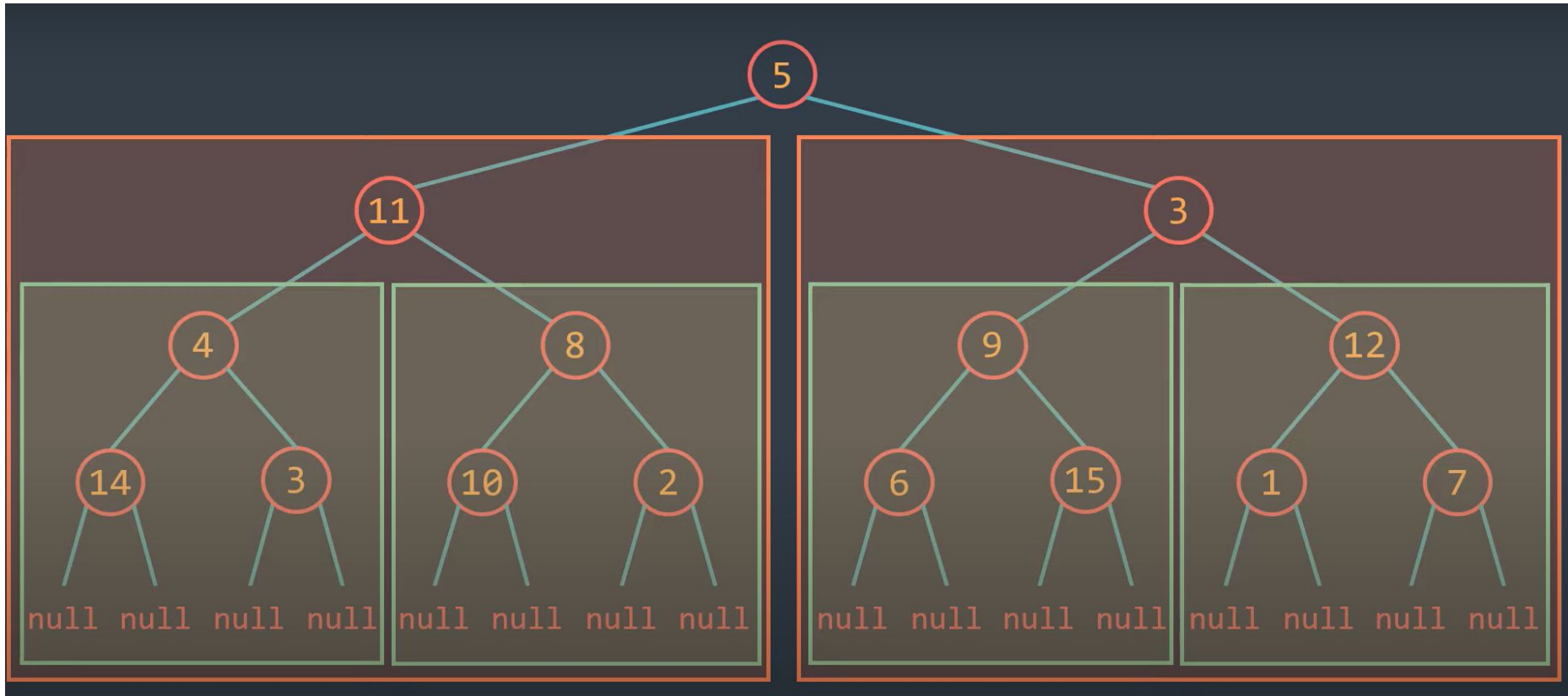
Node.left, Node.right, Node

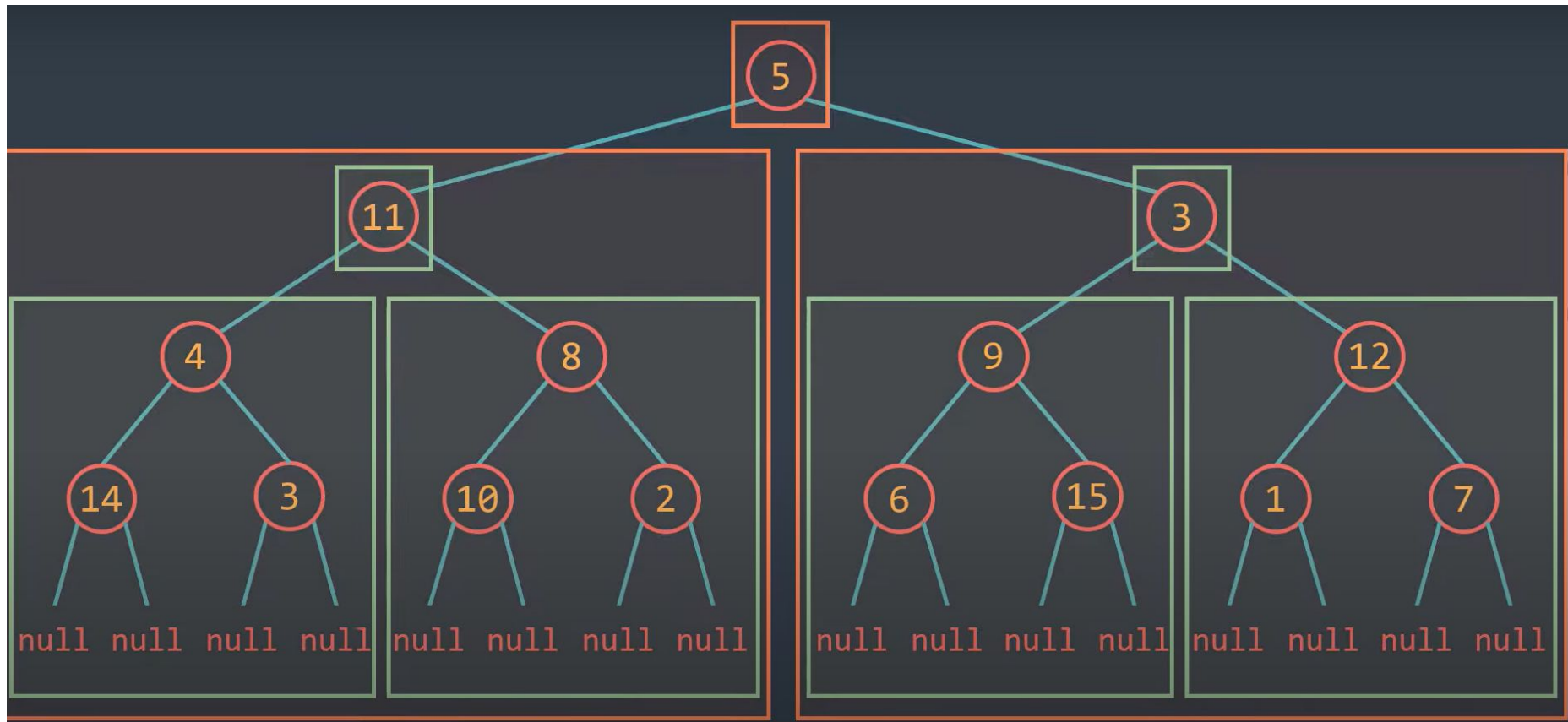


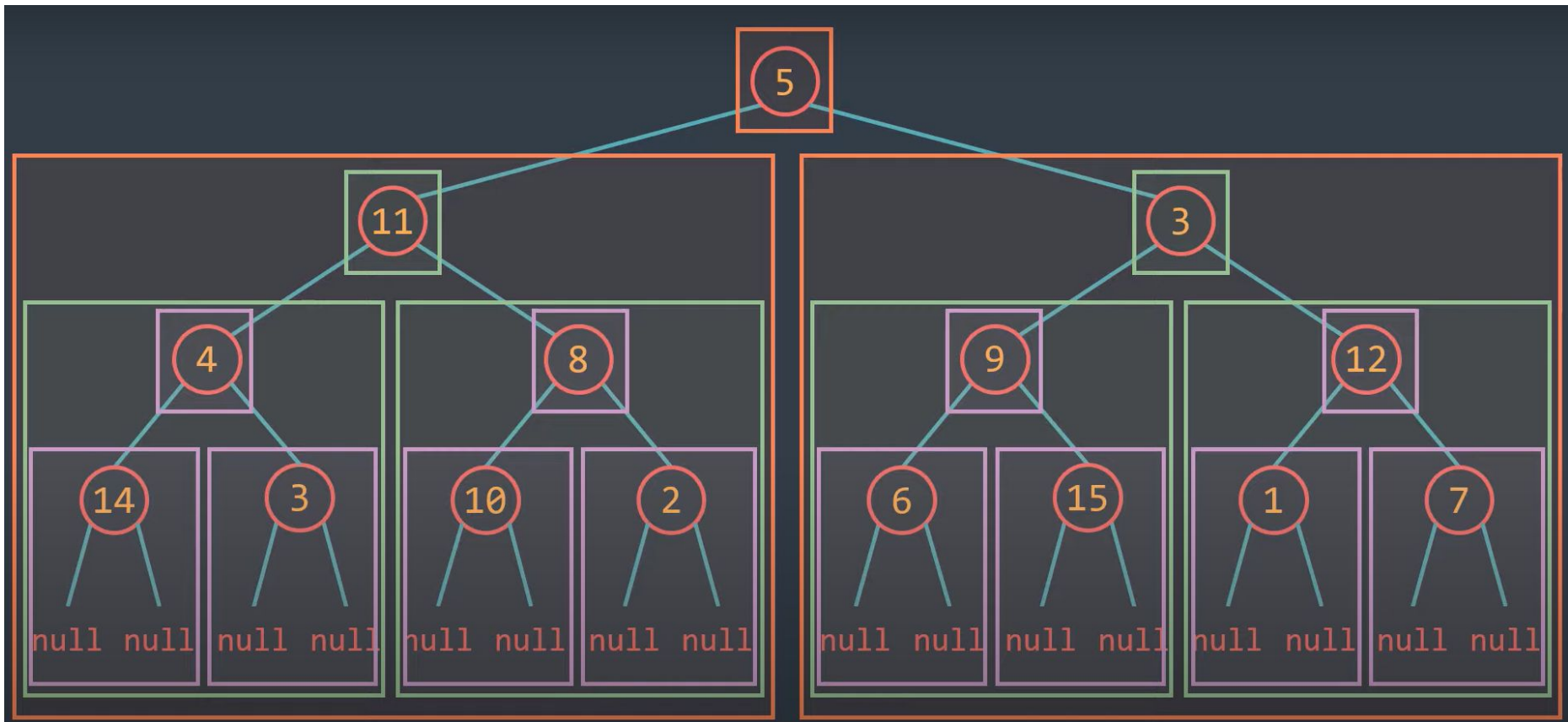
Post-Order Traversal **[D, F, G, E, B, C, A]**

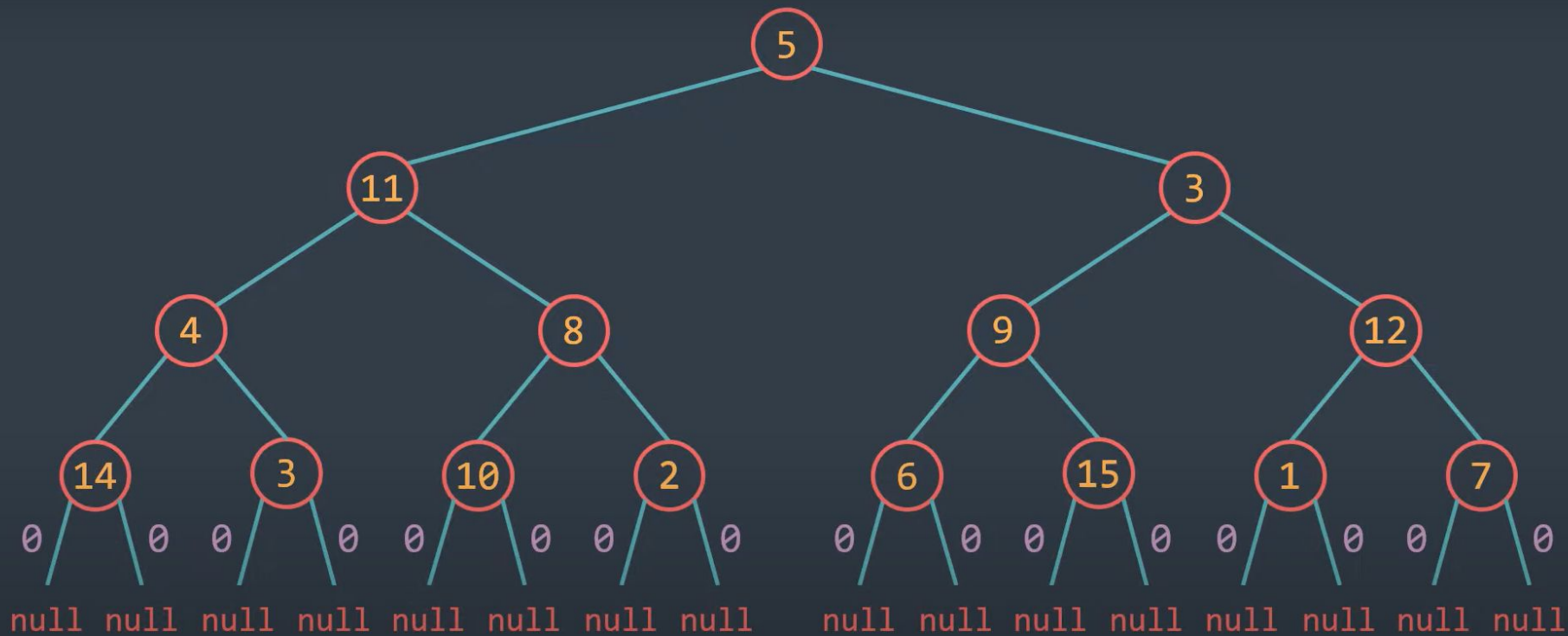


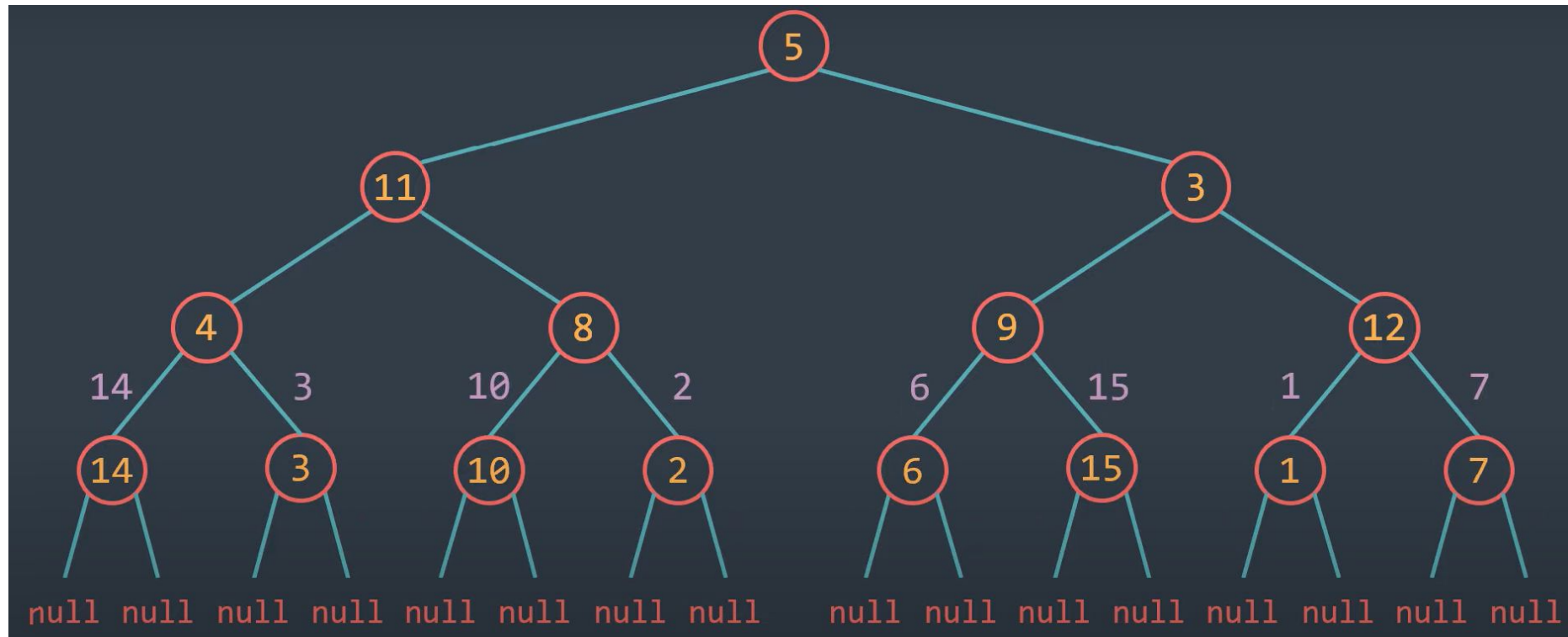


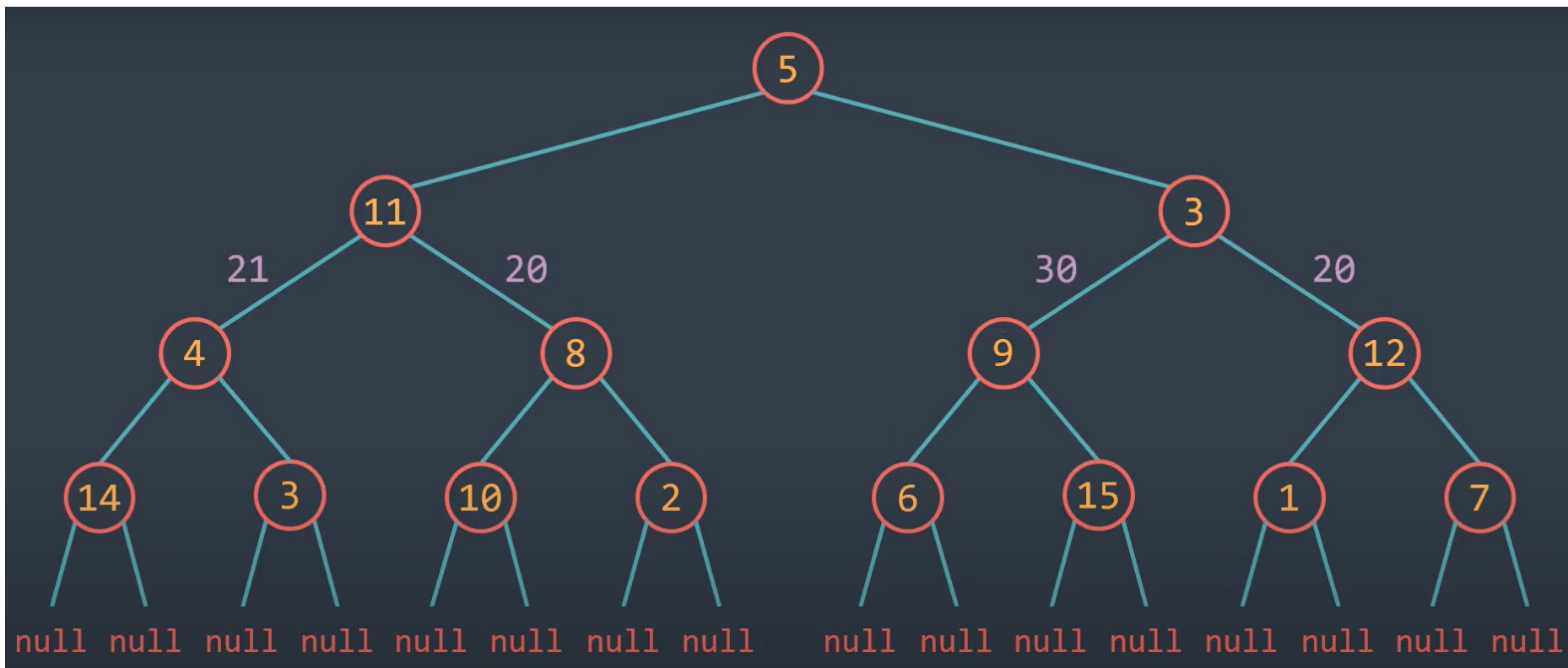


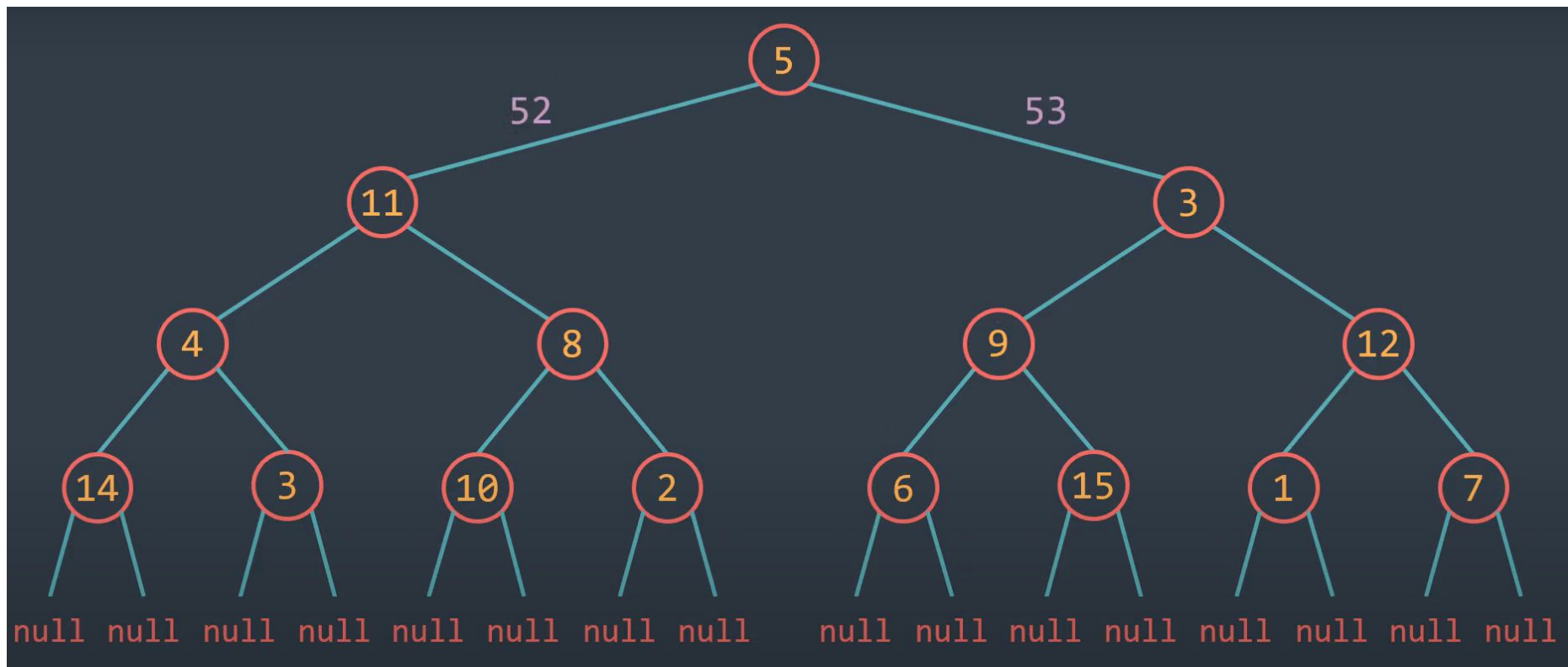












110

5

11

3

4

8

9

12

14

3

10

2

6

15

1

7

null null null null null null null null

null null null null null null null null

Steps in solving most DFS based Tree problems.

1. Figure out the Base conditions.
2. Call the recursive function on left sub-tree.
3. Call the recursive function on right sub-tree.
4. Combine to get the required results.

```
def sum_tree(root):
```

```
    # Base condition
```

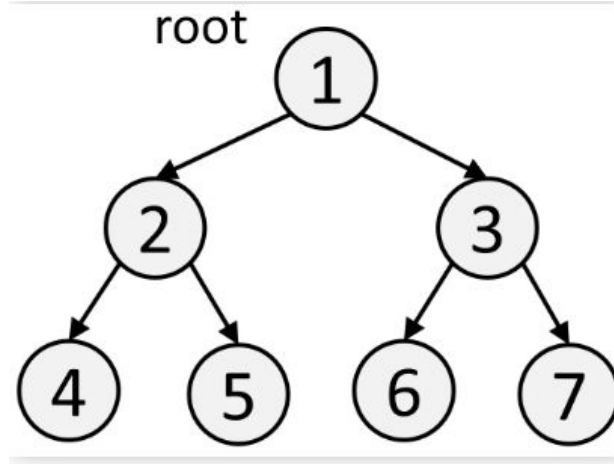
```
    If root is None:
```

```
        return 0
```

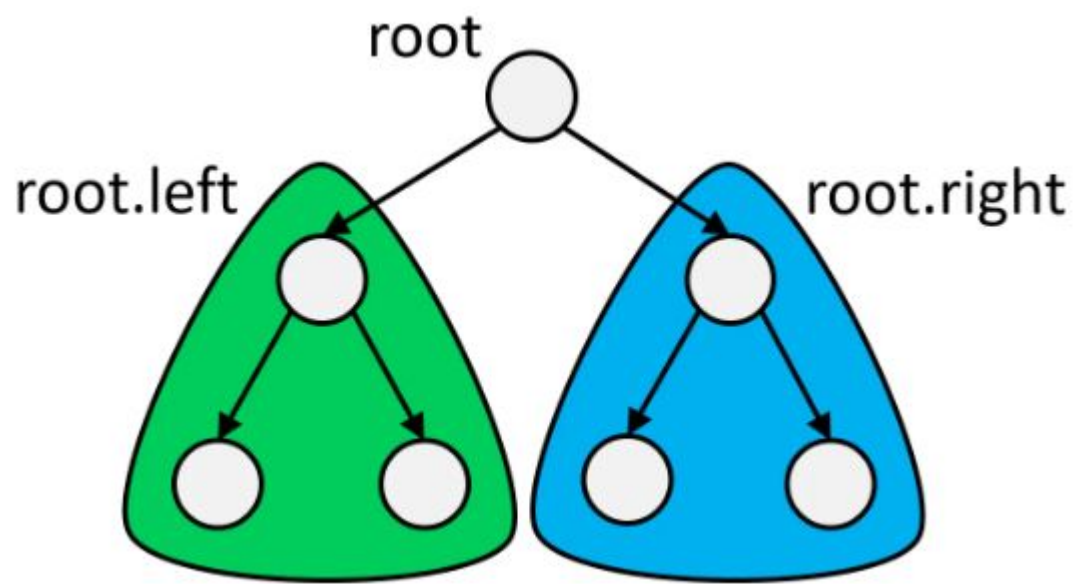
```
    # Recursive condition
```

```
    return root.val + sum_tree(root.left) +  
    sum_tree(root.right)
```

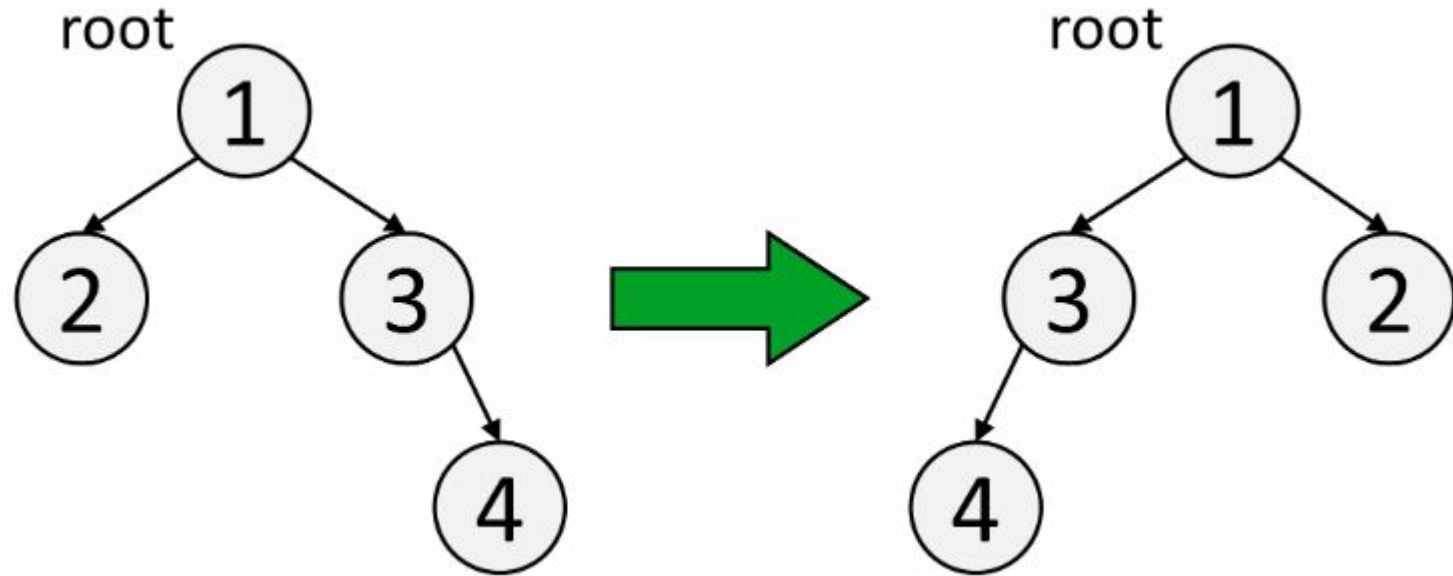
Question 1: Sum of number of nodes

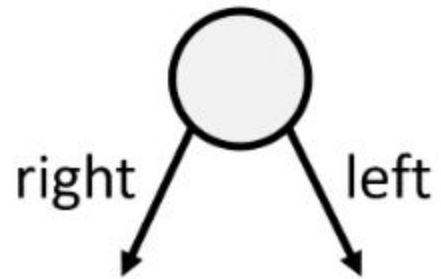
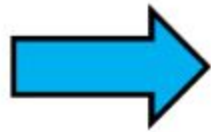
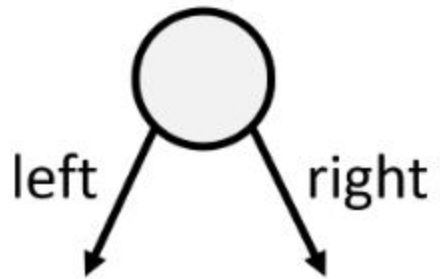


=> returns 7

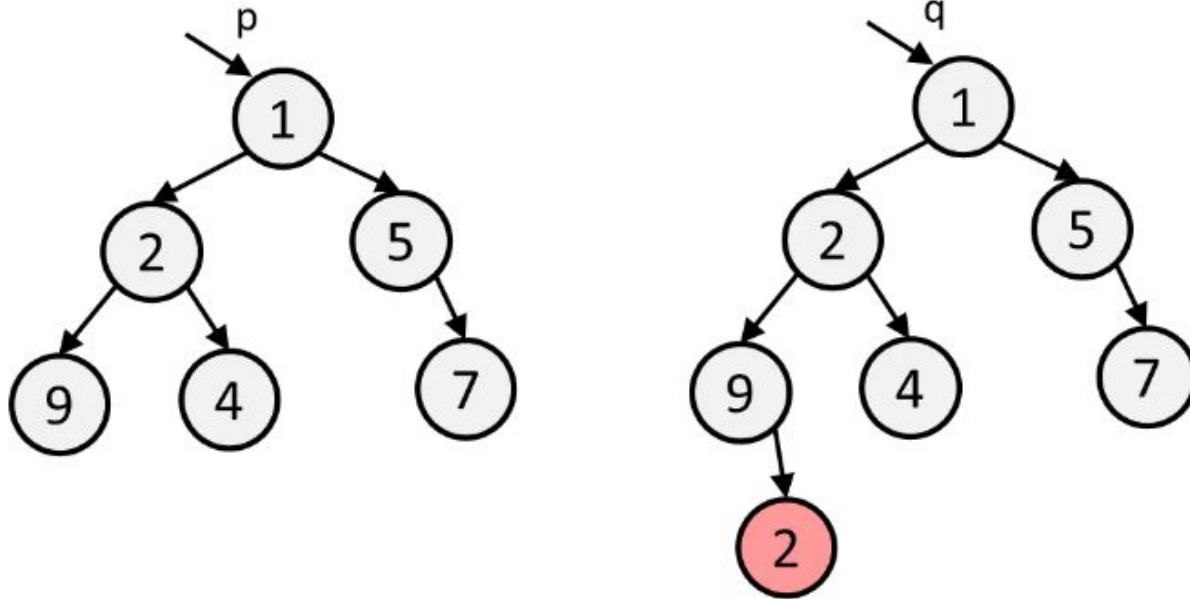


Question 2 : Mirror Tree





Question 3: Equal Trees?

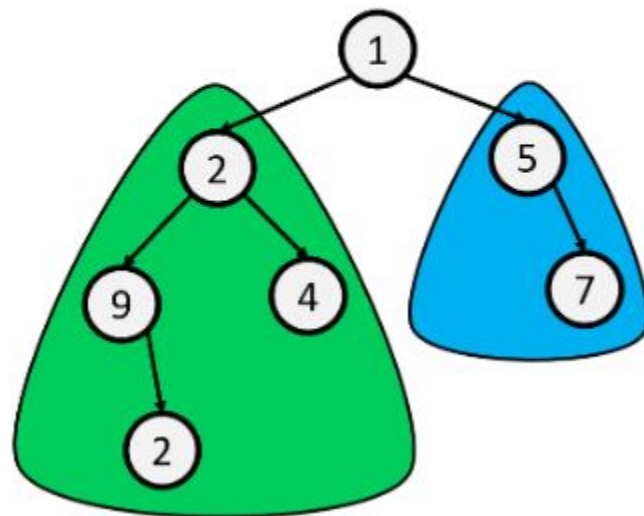
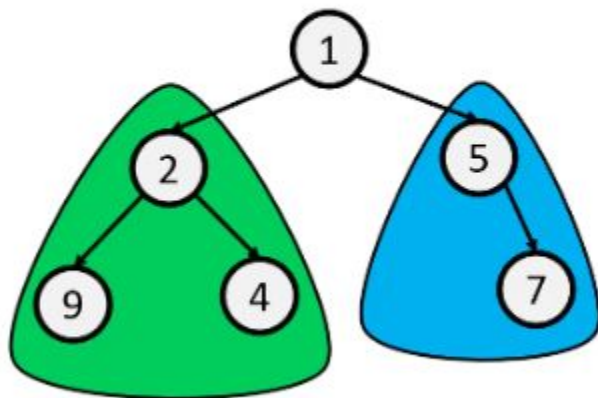


=> returns false

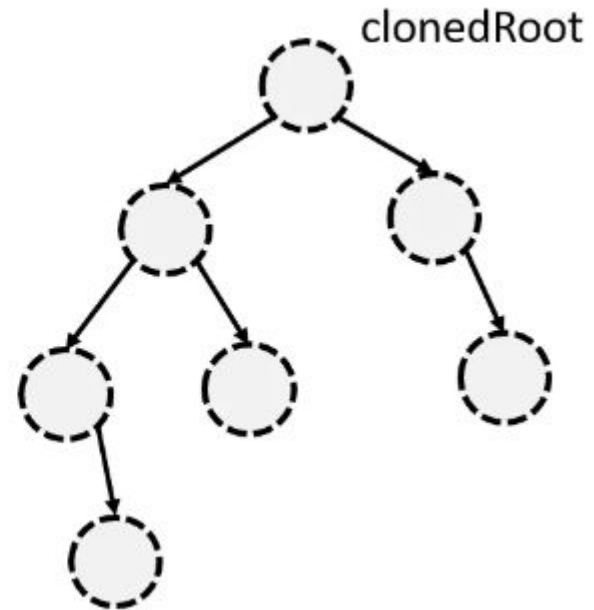
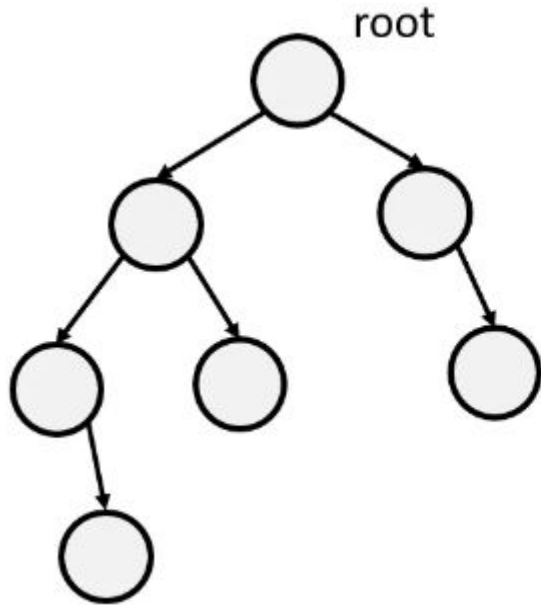
Values are equal?

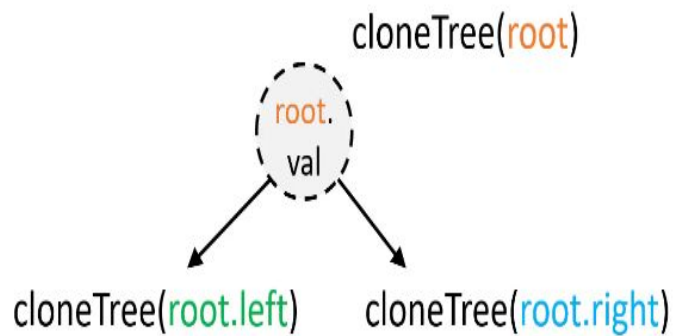
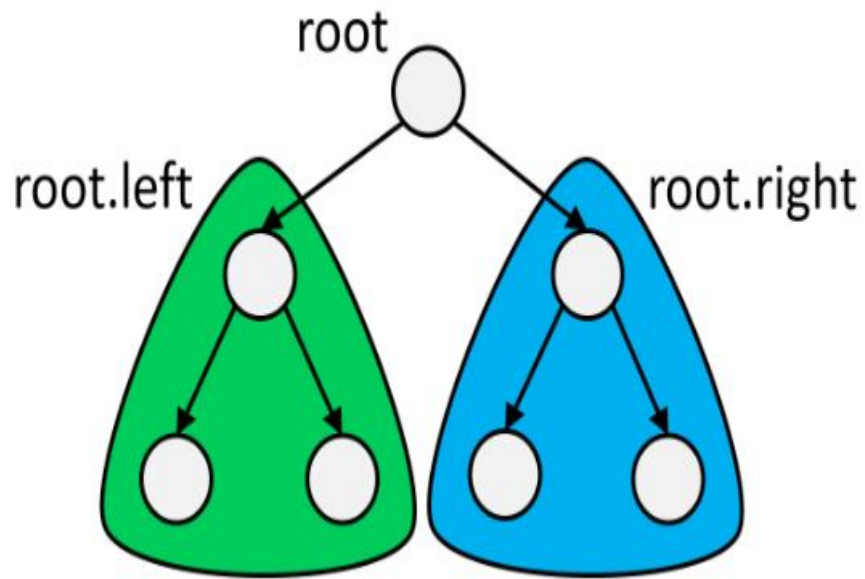
Left subtrees are the same?

Right subtrees are the same?

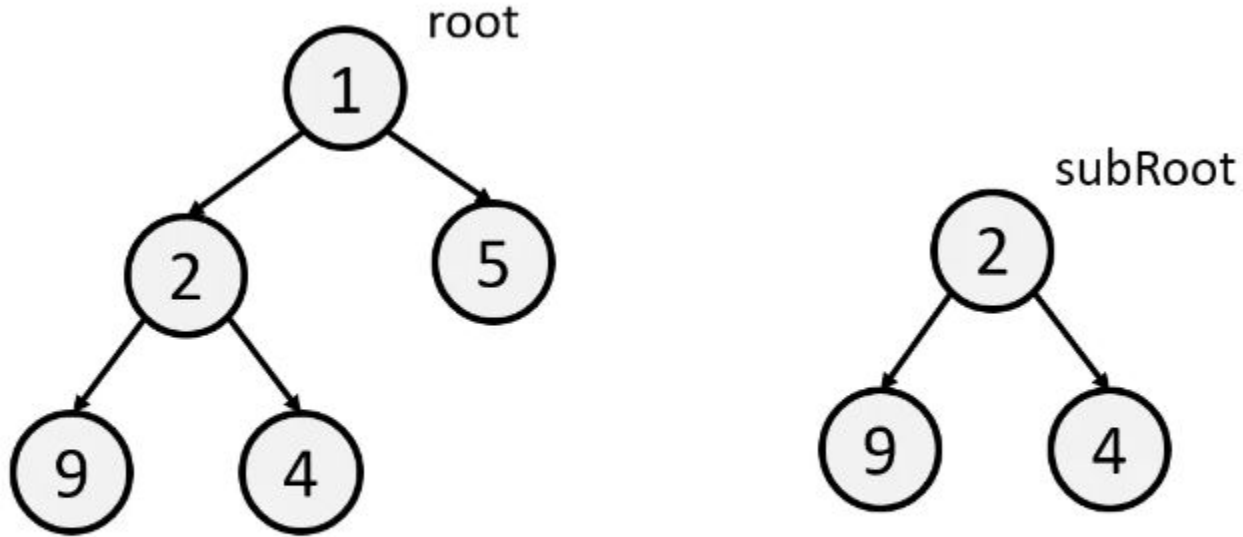


Question 4: Clone tree



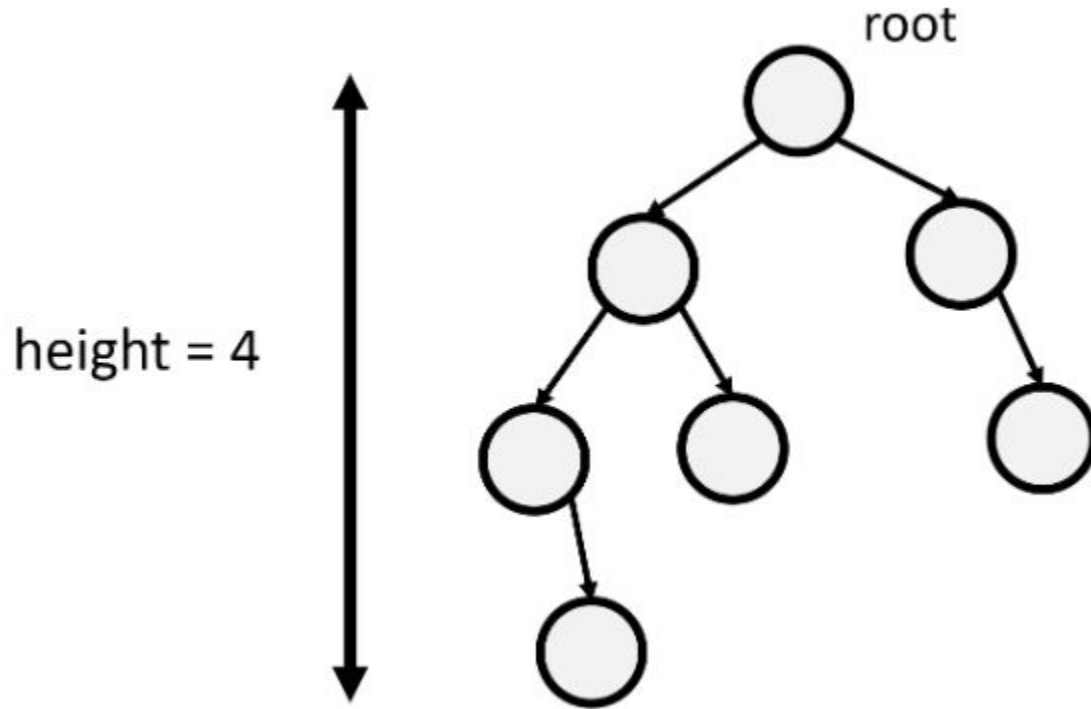


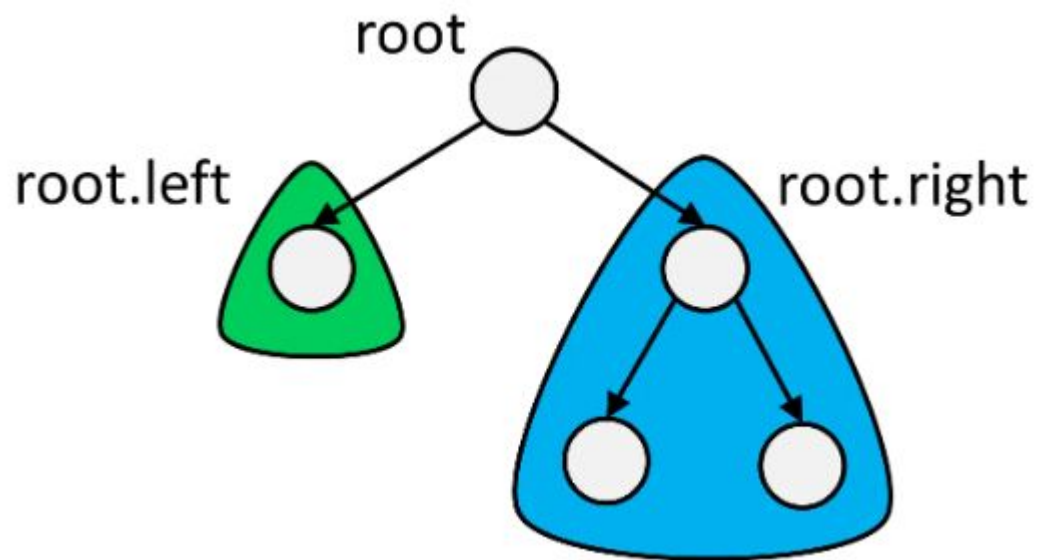
Question 5: Tree contains Sub-Tree



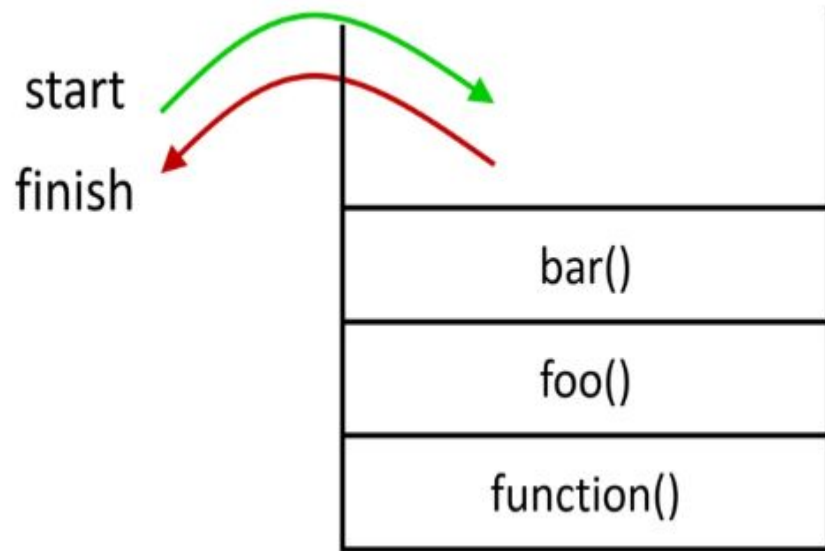
=> returns True

Question 6: Height of a tree

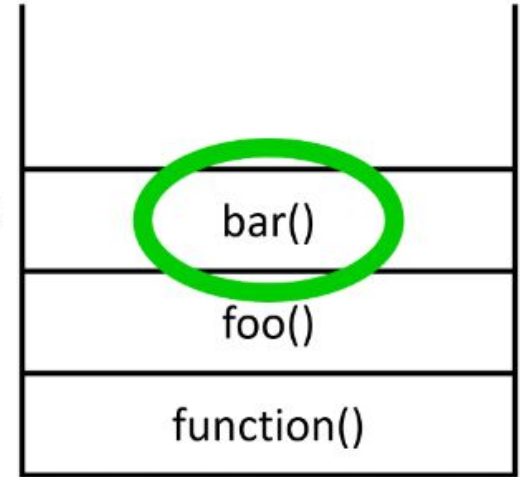




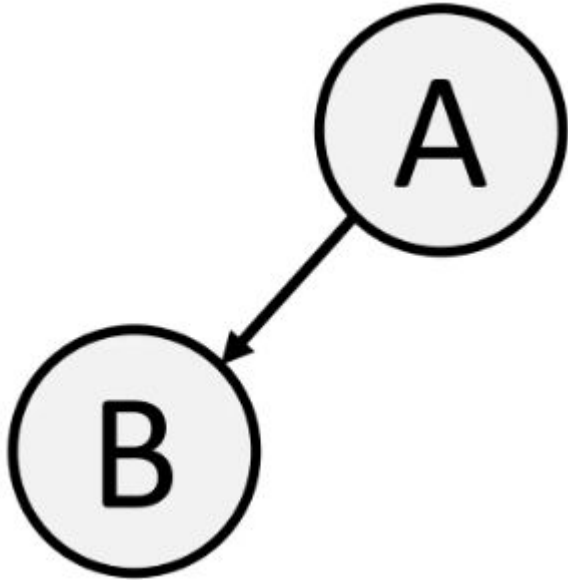
Call Stack: Stack of function calls.



Run top function

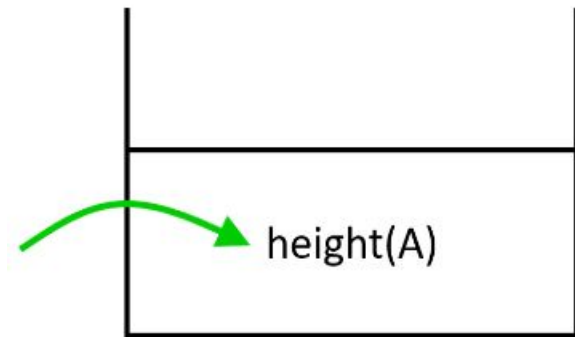


Calculate the height of the tree



```
def height(node):  
    if node == None:  
        return 0  
    heightL = height(node.left)  
    heightR = height(node.right)  
    return max(heightL, heightR) + 1
```

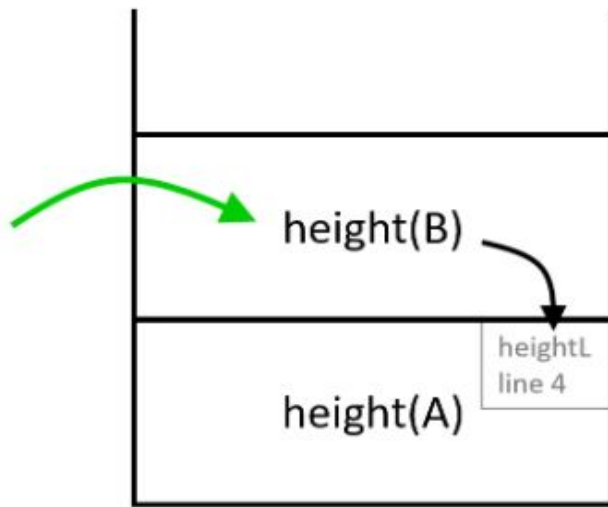
The very first thing that happens when we call `height(A)` is that the computer adds it to the Call Stack.



The computer then sees that `height(A)` is at the top of the Call Stack, so it starts computing `height(A)`. Eventually, the computer gets to line 4, and has to make *another* function call `height(B)`.

```
def height(Aroot):  
    if root == None:  
        return 0  
    heightL = height(Broot.left)  
    heightR = height(root.right)  
    return max(heightL, heightR) + 1
```

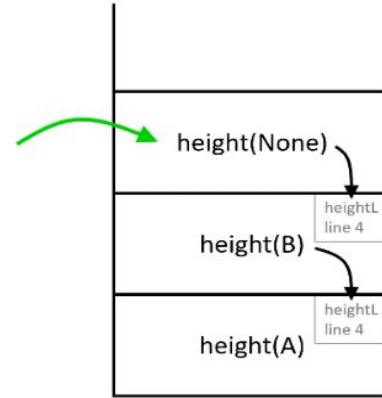
The computer adds `height(B)` it to the Call Stack. It saves information on how to resume `height(A)` when `height(B)` finishes:



Now `height(B)` is on top of the Call Stack, so the computer starts running it. It eventually reaches another function call `height(None)`:

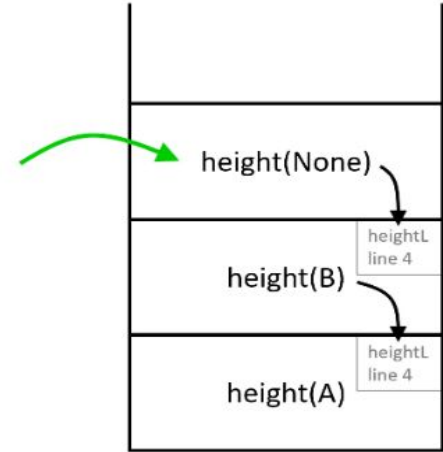
```
1  def height(Broot):
2      if root == None:
3          return 0
4      heightL = height(Noneroot.left)
5      heightR = height(root.right)
6      return max(heightL, heightR) + 1
```

So it adds it to the Call Stack:



Now the function call `height(None)` is on top of the Call Stack, so the computer runs it. It gets to the base case, and returns `0`

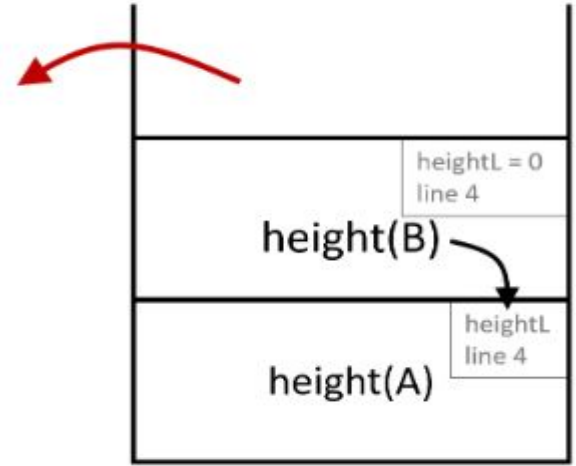
Now `height(None)` finished, so the computer removes it from the Call Stack. It updates the variables inside of the `height(B)` function accordingly.



Now the function call `height(None)` is on top of the Call Stack, so the computer runs it. It gets to the base case, and returns `0`.

```
1  def height(None root):  
2      if root == None:  
3          return 0  
4      heightL = height(root.left)  
5      heightR = height(root.right)  
6      return max(heightL, heightR) + 1
```

Now `height(None)` finished, so the computer removes it from the Call Stack. It updates the variables inside of the `height(B)` function accordingly.



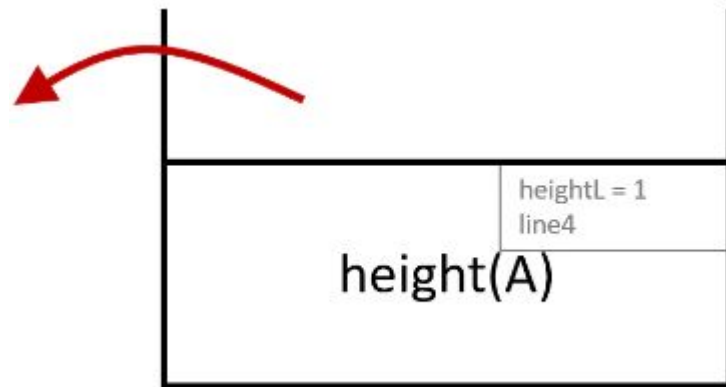
The Call Stack now has `height(B)` on top, so it resumes this function where it left off. Now it knows that `heightL = 0`.

So the computer resumes at line 5:

```
def height(Broot):  
    if root == None:  
        return 0  
    heightL = height(root.left)0  
    heightR = height(0root.right)  
    return max(heightL, heightR) + 1
```

The computer finds that `heightR = 0`. The computer then returns `max(0, 0) + 1`, which is `1`. Since the computer finished `height(B)`, it removes it from the Call Stack. It updates the variables in `height(A)` accordingly.

It now resumes `height(A)` on line 4, and knows that `heightL = 1`.



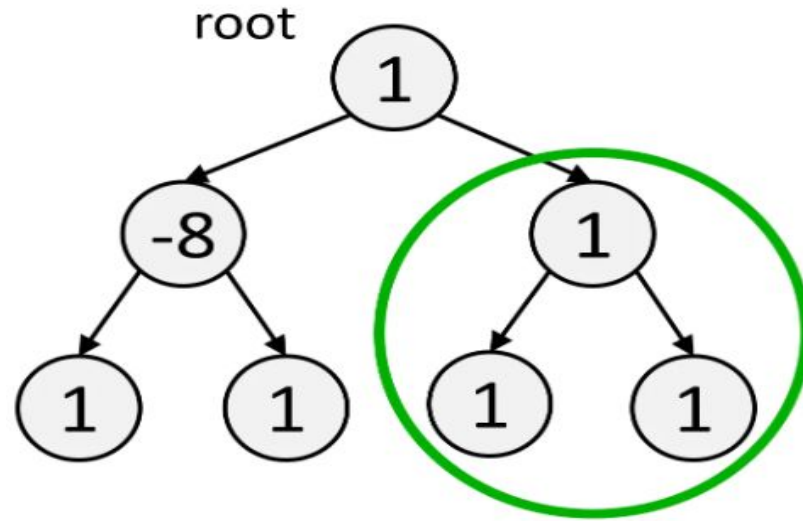
```
1  def height(Aroot):
2      if root == None:
3          return 0
4      heightL = height(root.left)
5      heightR = height(root.right)
6      return max(heightL, heightR) + 1
```

```
1  def height(Aroot):
2      if root == None:
3          return 0
4      heightL = height(root.left)
5      heightR = height(root.right)
6      return max(heightL, heightR) + 1
```

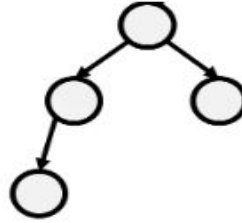
Annotations in the second code block: A red '1' is above line 3. A red '0' is to the right of line 5. A red '2' is to the right of line 6.

Recursion Hijacking

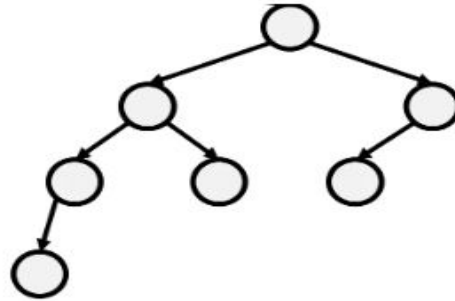
Max sub-tree sum:



Height balanced tree

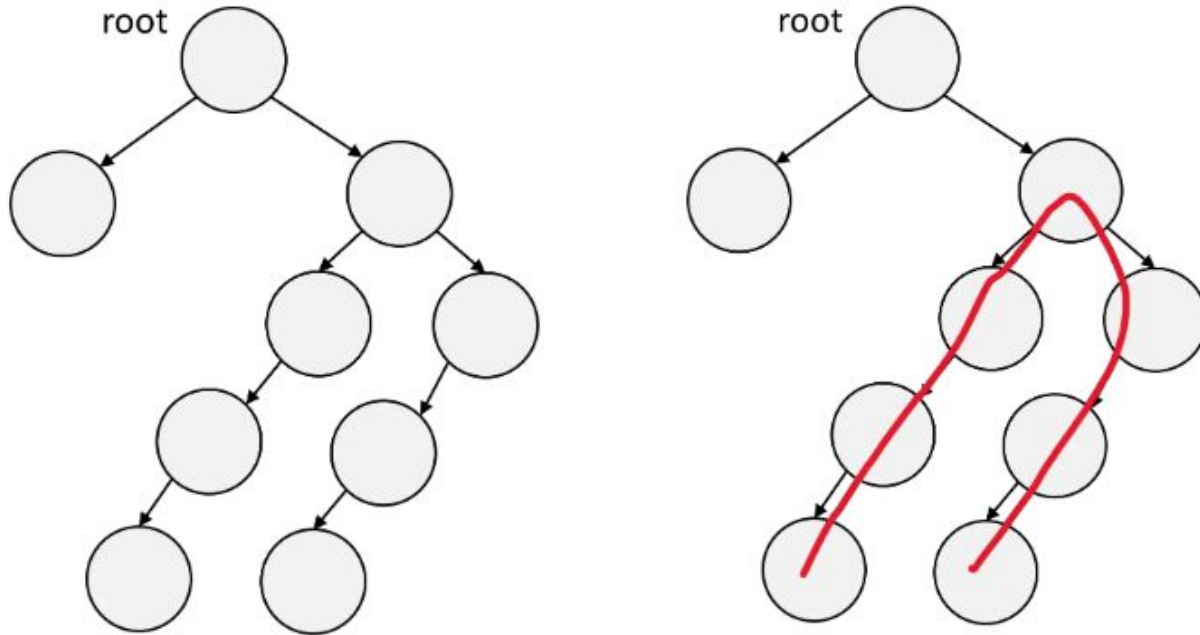


=> returns True



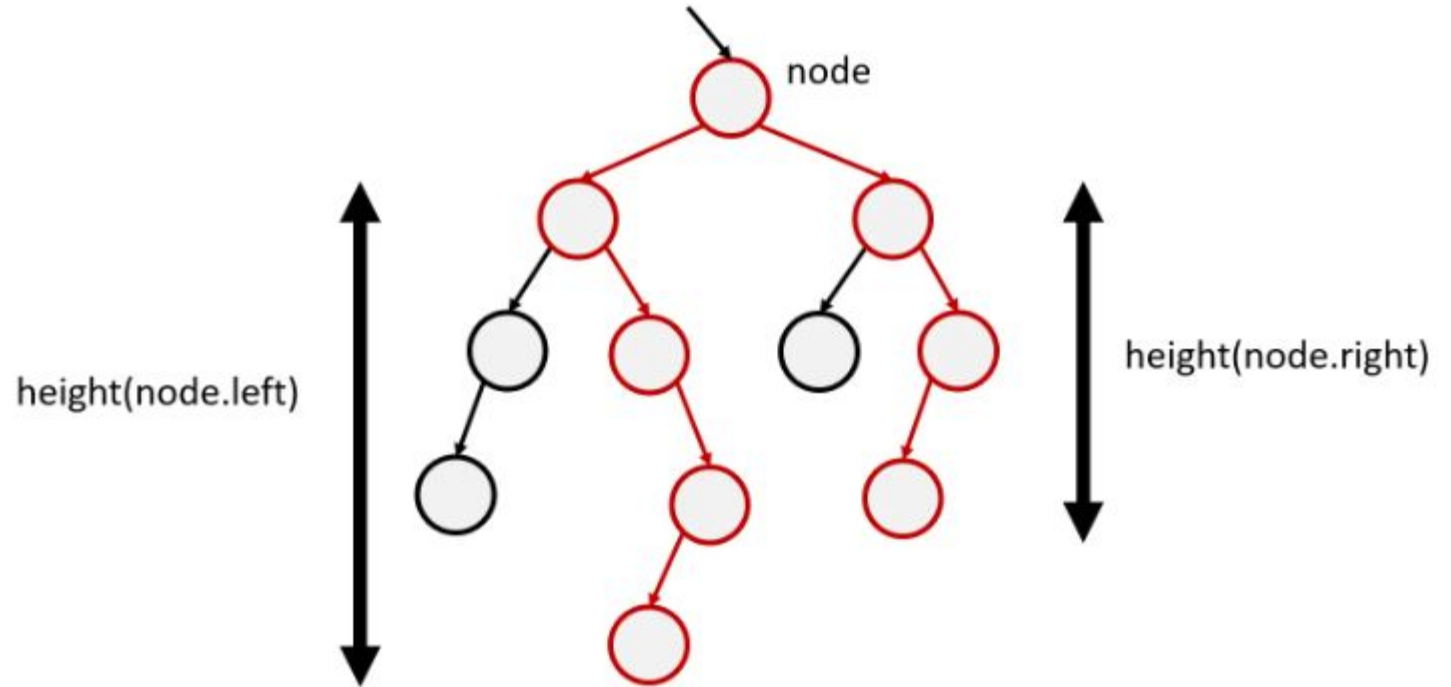
=> returns True

Diameter of a tree

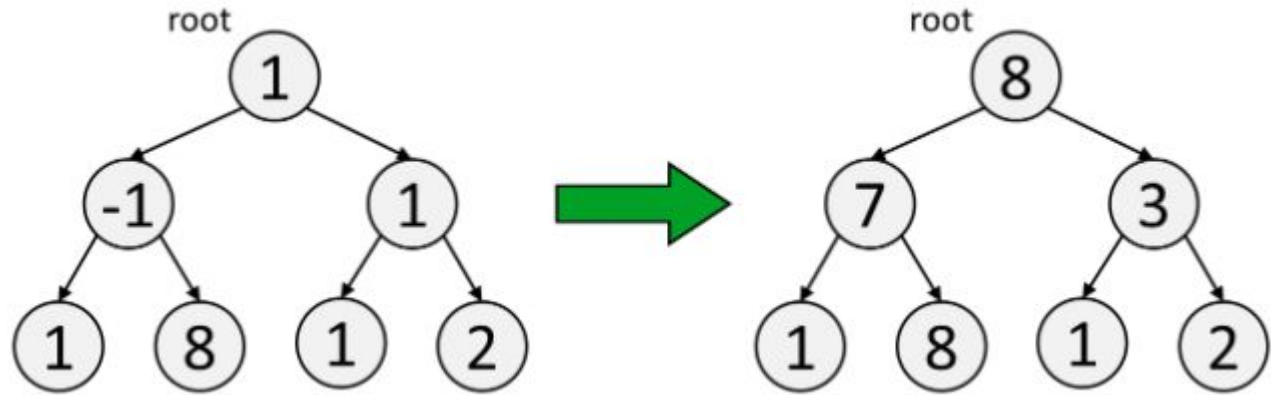


=> returns 6 (red path)

Diameter of a tree

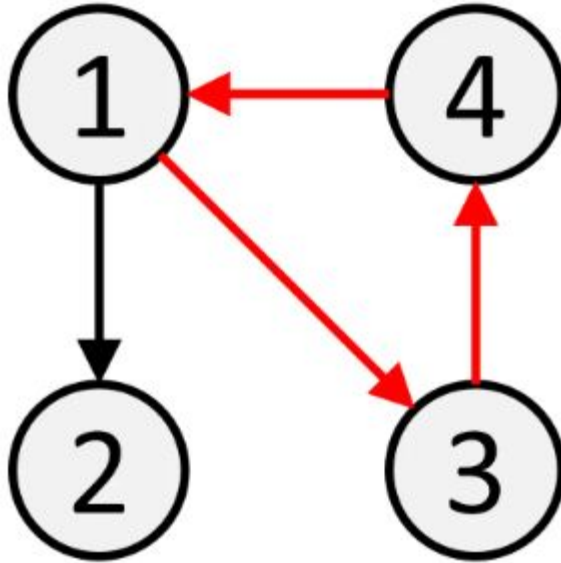


Max node to leaf sum



Graphs

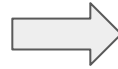
Number of nodes in the graph



Returns 4

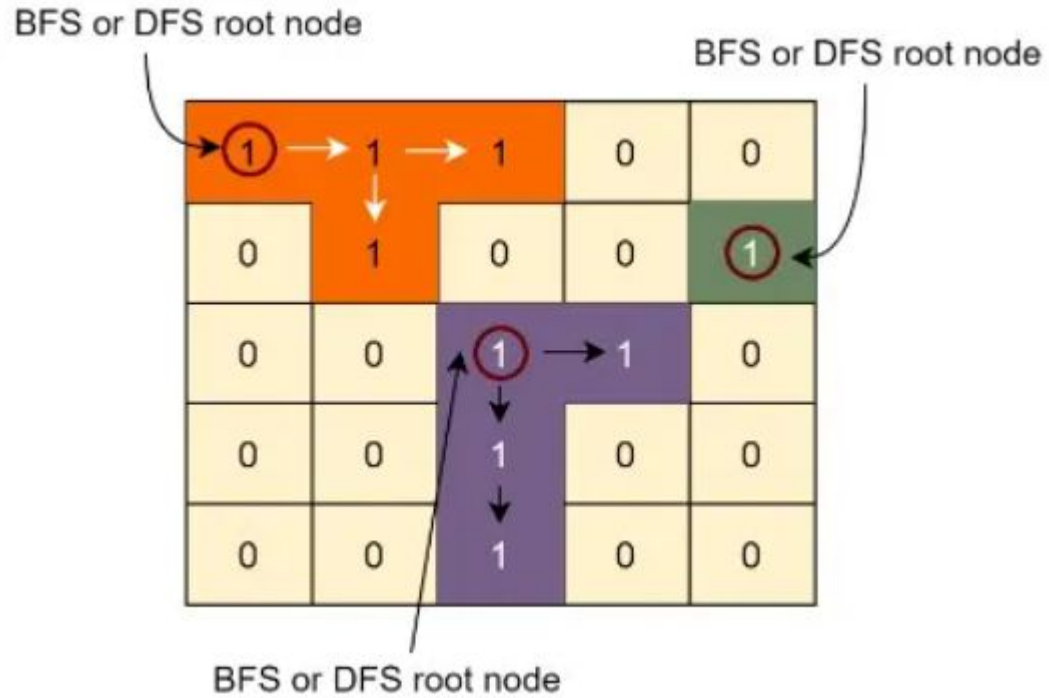
Calculate the number of islands

1	1	1	0	0
0	1	0	0	1
0	0	1	1	0
0	0	1	0	0
0	0	1	0	0



1	1	1	0	0
0	1	0	0	1
0	0	1	1	0
0	0	1	0	0
0	0	1	0	0

Calculate the number of islands

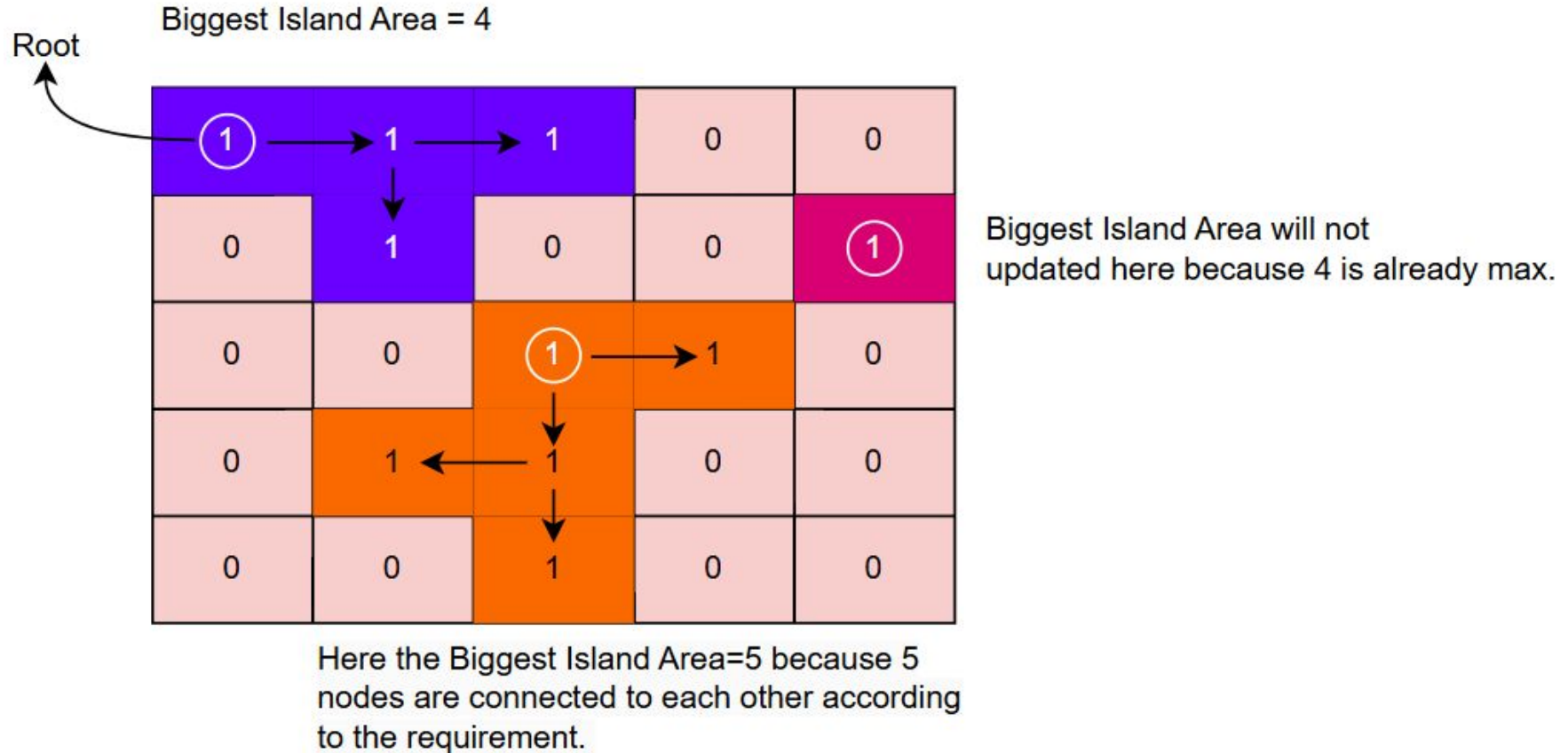


Biggest island among the different islands

1	1	1	0	0
0	1	0	0	1
0	0	1	1	0
0	1	1	0	0
0	0	1	0	0

1	1	1	0	0
0	1	0	0	1
0	0	1	1	0
0	1	1	0	0
0	0	1	0	0

Biggest island among the different islands



Flood fill

Starting cell

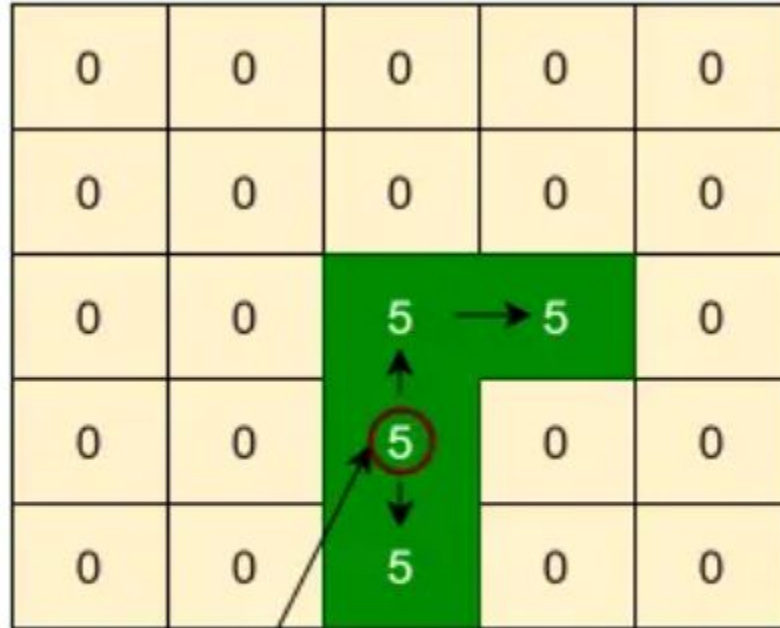
0	1	1	1	0
0	0	0	1	1
0	1	1	1	0
0	1	1	0	0
0	0	0	0	0

0	2	2	2	0
0	0	0	2	2
0	2	2	2	0
0	2	2	0	0
0	0	0	0	0

starting cell = (1, 3)

new color = 2

Flood fill



BFS or DFS root node

