

ACM International Collegiate Programming Contest
Thirteenth Arab Collegiate Programming Contest
Lebanese American University
Beirut, Lebanon, November 2010

[B] Sum the Square

Program: distance.(c|cpp|java)
Input: distance.in

Balloon Color: Yellow

Description

Take any positive number, find the sum of the squares of its digits, repeat! You'll end up with an infinite sequence with an interesting property that we would like to investigate further. Starting with the number 5, the sequence is:

$$(5, 25, 29, 85, 89, 145, 42, 20, 4, 16, 37, 58, \ldots)$$

The interesting part is in what comes after 58: $5^2 + 8^2 = 89$ which is a number that's already been seen in the sequence. In other words, after 58, the sequence will fall into the repeating cycle: 89, 145, 42, 20, 4, 16, 37, 58.

What's amazing is that this cycle will appear for many other numbers: 3, 18, 36, and 64 just to name a few. (see figure on the following page.)

For some numbers, the sequence will fall into another repeating cycle by reaching 1. (see second figure on the following page) For example, starting with 19, you'll end up with the sequence:

$$(19, 82, 68, 100, 1, \ldots)$$

And that's about it. Any number you choose will end up falling into a repeating cycle: Either the 89, 145, . . . cycle or the 1, . . . cycle.

Given two numbers, your objective is to generate as few numbers in their sequences for the two sequences to intersect at one common number. For example, given 61 and 29, we can achieve what's required by generating the sequences: (61, 37, 58, 89) and (29, 85, 89). Similarly, for 19 and 100, the sequences would be (19, 82, 68, 100) and (100).

Input Format

Your program will be tested on one or more test cases. Each test case is specified on a single line having two integers $(0 < A, B < 10^9)$.

The last case is followed by a dummy line made of two zeros.

Output Format

For each test case, print the following line:

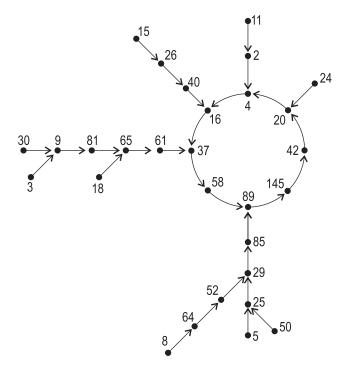
 $A \sqcup B \sqcup S$

Where A, B are as in the input and S is the (minimum) sum of the lengths of the two sequences. If the sequences starting at A and B do not intersect, then S = 0.

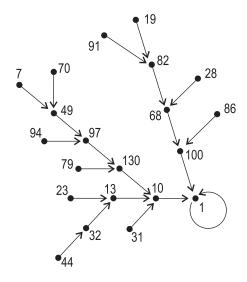
Sample Input/Output

	distance.in
89 89	
19 100	
61 19	
0 0	
ſ	

		 OUTPUT	
89	89 2		
19	100 5		
61	19 0		



Few numbers falling into the 89, 145, 42, 20, 4, 16, 37, 58 cycle



Few numbers falling into the 1 cycle.

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