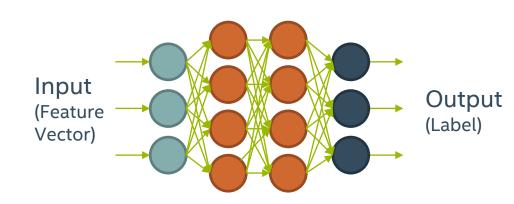


#### **HOW TO TRAIN A NEURAL NET?**

- Put in training inputs, get the output
- Compare output to correct answers: look at loss function J
- Adjust and repeat!
- Backpropagation tells us how to make a single adjustment using calculus.

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#### **HOW HAVE WE TRAINED BEFORE?**

#### **Gradient Descent!**

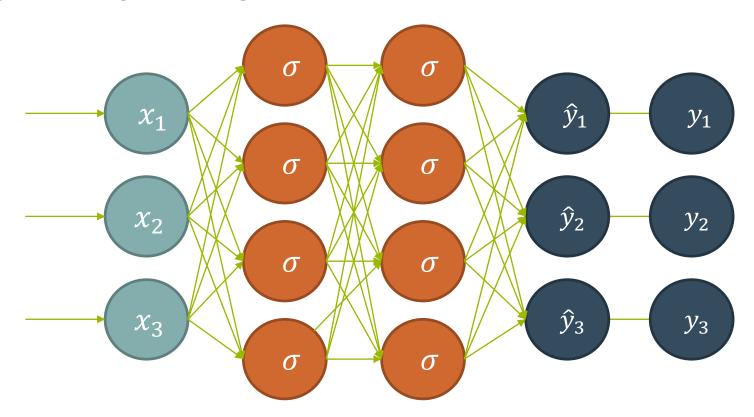
- 1. Make prediction
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- 3. Calculate gradient of the loss function w.r.t. parameters
- 4. Update parameters by taking a step in the opposite direction
- 5. Iterate

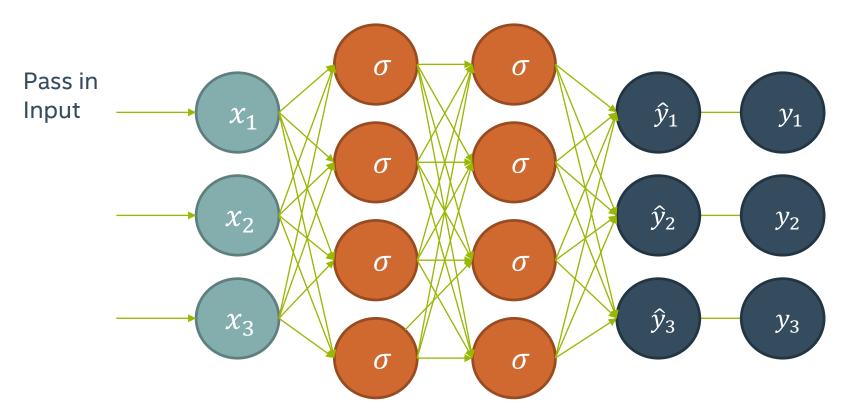
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#### **Gradient Descent!**

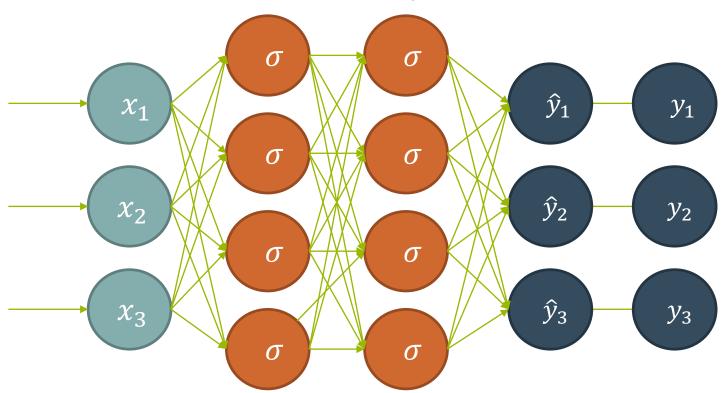
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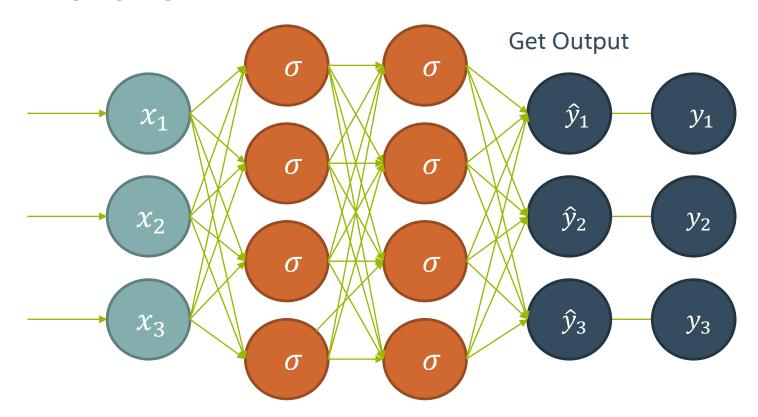
## FEEDFORWARD NEURAL NETWORK

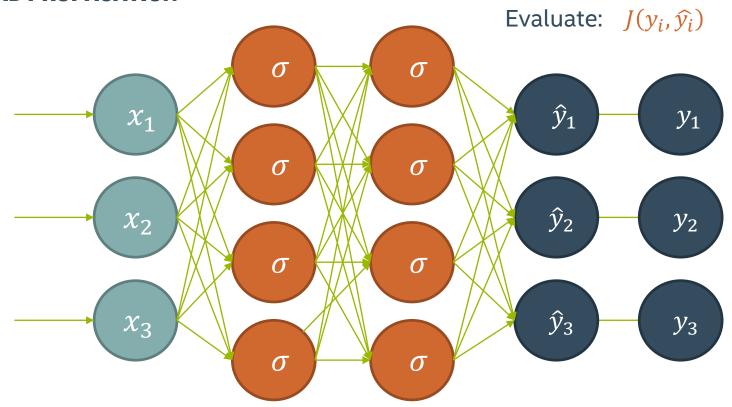




#### Calculate each Layer







#### **HOW HAVE WE TRAINED BEFORE?**

#### **Gradient Descent!**

- 1. Make prediction
- 2. Calculate Loss
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## **HOW TO CALCULATE GRADIENT?**

Chain rule

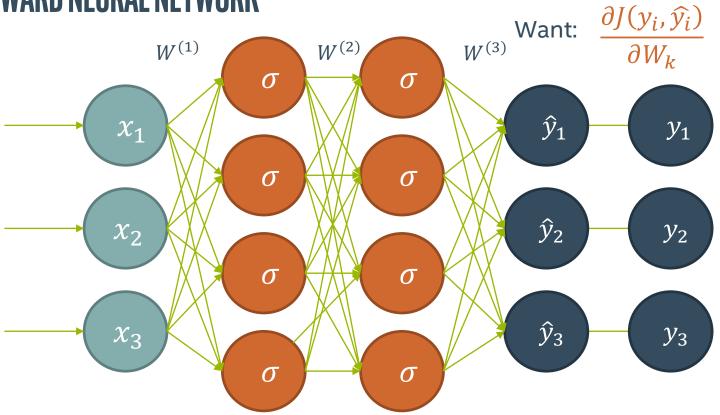
#### **HOW TO TRAIN A NEURAL NET?**

- How could we change the weights to make our Loss Function lower?
- Think of neural net as a function F: X -> Y
- F is a complex computation involving many weights W\_k
- Given the structure, the weights "define" the function F (and therefore define our model)
- Loss Function is J(y,F(x))

#### **HOW TO TRAIN A NEURAL NET?**

- Get  $\frac{\partial J}{\partial W_k}$  for every weight in the network.
- This tells us what direction to adjust each Wk if we want to lower our loss function.
- Make an adjustment and repeat!

#### FEEDFORWARD NEURAL NETWORK



#### CALCULUS TO THE RESCUE

- Use calculus, chain rule, etc. etc.
- Functions are chosen to have "nice" derivatives
- Numerical issues to be considered

#### **PUNCHLINE**

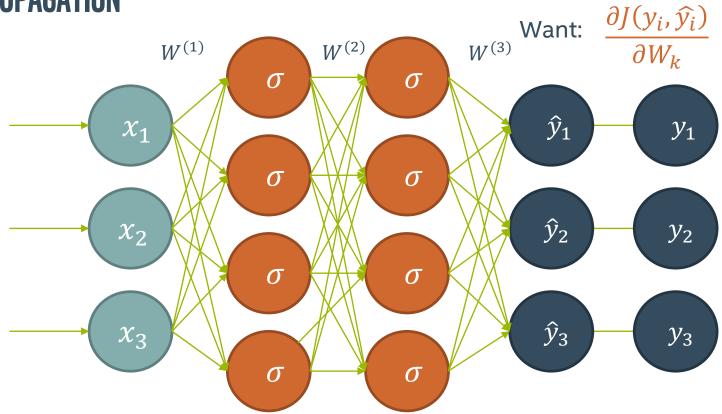
$$\frac{\partial J}{\partial W^{(3)}} = (\hat{y} - y) \cdot a^{(3)}$$

$$\frac{\partial J}{\partial W^{(2)}} = (\hat{y} - y) \cdot W^{(3)} \cdot \sigma'(z^{(3)}) \cdot a^{(2)}$$

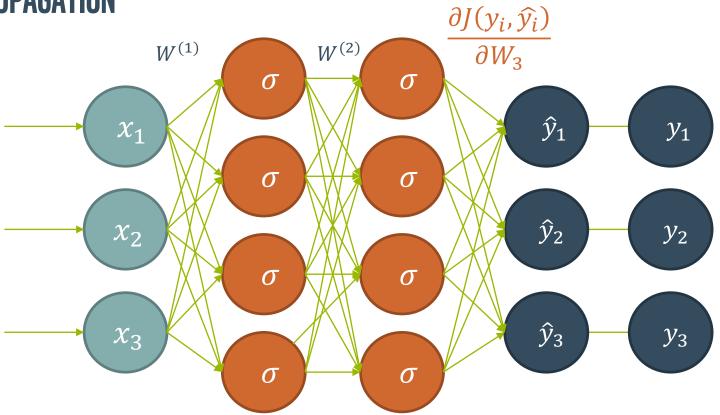
$$\frac{\partial J}{\partial W^{(1)}} = (\hat{y} - y) \cdot W^{(3)} \cdot \sigma'(z^{(3)}) \cdot W^{(2)} \cdot \sigma'(z^{(2)}) \cdot X$$

- Recall that:  $\sigma'(z) = \sigma(z)(1 \sigma(z))$
- Though they appear complex, above are easy to compute!

#### **BACKPROPAGATION**

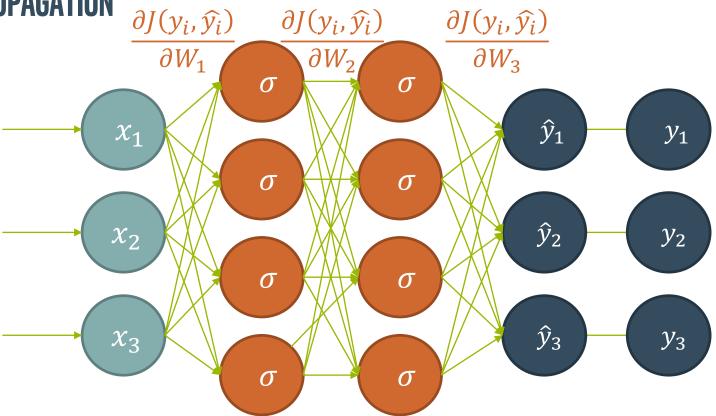


### **BACKPROPAGATION**



#### **BACKPROPAGATION** $\partial J(y_i, \widehat{y_i})$ $\partial J(y_i, \widehat{y_i})$ $W^{(1)}$ $\partial W_3$ $\partial W_2$ $\sigma$ $\sigma$ $\hat{y}_1$ $\chi_1$ $y_1$ $\sigma$ $\hat{y}_2$ $\chi_2$ $y_2$ $\sigma$ σ $\hat{y}_3$ $\chi_3$ $y_3$ $\sigma$ $\sigma$

# **BACKPROPAGATION**



#### **HOW HAVE WE TRAINED BEFORE?**

#### **Gradient Descent!**

- 1. Make prediction
- 2. Calculate Loss
- 3. Calculate gradient of the loss function w.r.t. parameters
- 4. Update parameters by taking a step in the opposite direction
- 5. Iterate

#### **VANISHING GRADIENTS**

#### **Recall that:**

$$\frac{\partial J}{\partial W^{(1)}} = (\hat{y} - y) \cdot W^{(3)} \cdot \sigma'(z^{(3)}) \cdot W^{(2)} \cdot \sigma'(z^{(2)}) \cdot X$$

- Remember:  $\sigma'(z) = \sigma(z)(1-\sigma(z)) \le .25$
- As we have more layers, the gradient gets very small at the early layers.
- This is known as the "vanishing gradient" problem.
- For this reason, other activations (such as ReLU) have become more common.

# OTHER ACTIVATION FUNCTIONS

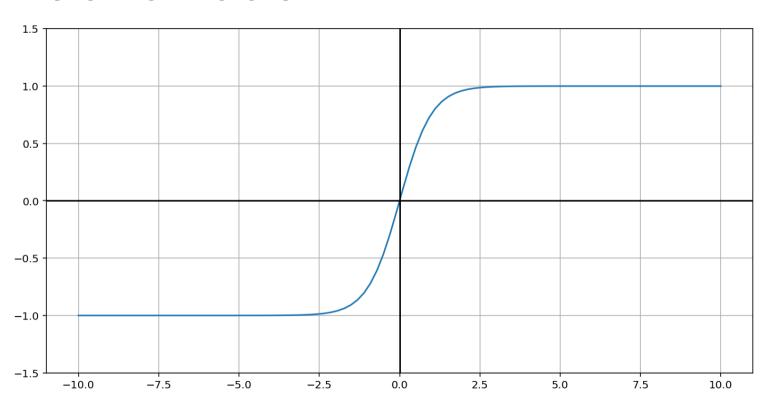
#### HYPERBOLIC TANGENT FUNCTION

- Hyperbolic tangent function
- Pronounced "tanch"

$$tanh(z) = \frac{\sinh(z)}{\cosh(z)} = \frac{e^{2x} - 1}{e^{2x} + 1}$$

$$tanh(0) = 0$$
$$tanh(\infty) = 1$$
$$tanh(-\infty) = -1$$

## HYPERBOLIC TANGENT FUNCTION



## **RECTIFIED LINEAR UNIT (RELU)**

$$ReLU(z) = \begin{cases} 0, & z < 0 \\ z, & z \ge 0 \end{cases}$$
$$= \max(0, z)$$

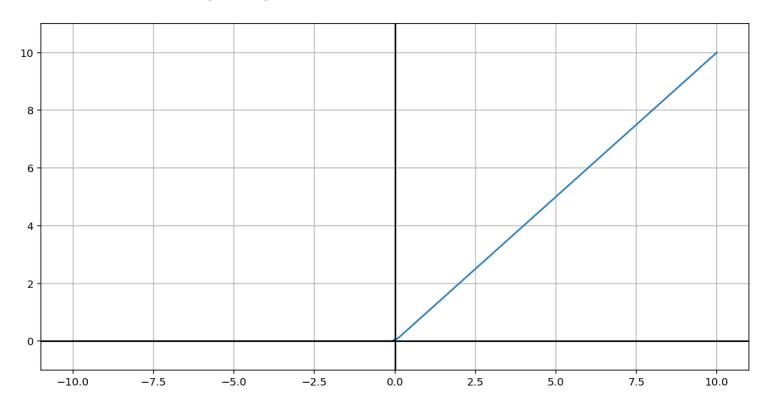
$$ReLU(0) = 0$$

$$ReLU(z) = z$$

$$ReLU(-z) = 0$$

for  $(z \gg 0)$ 

# RECTIFIED LINEAR UNIT (RELU)



## "LEAKY" RECTIFIED LINEAR UNIT (RELU)

$$LReLU(z) = \begin{cases} \alpha z, & z < 0 \\ z, & z \ge 0 \end{cases}$$

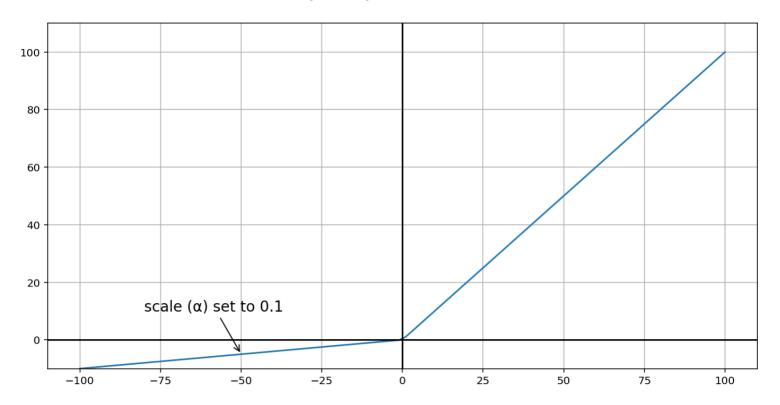
$$= \max(\alpha z, z) \qquad \text{for } (\alpha < 1)$$

$$LReLU(0) = 0$$

$$LReLU(z) = z \qquad \text{for } (z \gg 0)$$

$$LReLU(-z) = -\alpha z$$

# "LEAKY" RECTIFIED LINEAR UNIT (RELU)



#### WHAT NEXT?

We now know how to make a single update to a model given some data.

But how do we do the full training?

We will dive into these details in the next lecture.

