

15/10/2024

Lab-03

Program title: For 8-puzzle A\* implementation, to calculate,  $f(n)$ , consider two cases,  
2.  $g(n)$ : Depth of the node,  $h(n)$ : Manhattan Distance

Code:

```
import heapq
```

```
goal_state = [  
    [1, 2, 3],  
    [8, 0, 4],  
    [7, 6, 5]  
]
```

```
def flatten(puzzle):  
    return [item for row in puzzle for item in row]
```

```
def find_blank(puzzle):  
    for i in range(3):  
        for j in range(3):  
            if puzzle[i][j] == 0:  
                return i, j
```

```
def manhattan_distance(puzzle):  
    distance = 0  
  
    # Define target positions based on the goal state  
    target_positions = {  
        1: (0, 0), 2: (0, 1), 3: (0, 2),  
        4: (1, 2), 5: (2, 2), 6: (2, 1),  
        7: (2, 0), 8: (1, 0), 0: (1, 1) # Blank space  
    }
```

```

for i in range(3):
    for j in range(3):
        value = puzzle[i][j]
        if value != 0: # Skip the blank tile
            target_x, target_y = target_positions[value]
            distance += abs(i - target_x) + abs(j - target_y)
return distance

```

```

def generate_neighbors(puzzle):
    x, y = find_blank(puzzle)
    neighbors = []
    moves = [(-1, 0), (1, 0), (0, -1), (0, 1)]

    for dx, dy in moves:
        nx, ny = x + dx, y + dy
        if 0 <= nx < 3 and 0 <= ny < 3:
            new_puzzle = [row[:] for row in puzzle]
            new_puzzle[x][y], new_puzzle[nx][ny] = new_puzzle[nx][ny], new_puzzle[x][y]
            neighbors.append(new_puzzle)
    return neighbors

```

```

def is_goal(puzzle):
    return puzzle == goal_state

```

```

def print_puzzle(puzzle):
    for row in puzzle:
        print(row)
    print()

```

```

def a_star_manhattan_distance(initial_state):
    frontier = []

```

```
heapq.heappush(frontier, (manhattan_distance(initial_state), 0, initial_state, []))
```

```
visited = set()
```

```
while frontier:
```

```
    f, g, current_state, path = heapq.heappop(frontier)
```

```
    print("Current State:")
```

```
    print_puzzle(current_state)
```

```
    h = manhattan_distance(current_state)
```

```
    print(f"g(n) = {g}, h(n) = {h}, f(n) = {g + h}")
```

```
    print("-" * 20)
```

```
    if is_goal(current_state):
```

```
        print("Goal reached!")
```

```
        return path
```

```
    visited.add(tuple(flatten(current_state)))
```

```
    for neighbor in generate_neighbors(current_state):
```

```
        if tuple(flatten(neighbor)) not in visited:
```

```
            h = manhattan_distance(neighbor)
```

```
            heapq.heappush(frontier, (g + 1 + h, g + 1, neighbor, path + [neighbor]))
```

```
    return None # No solution found
```

```
# Initial puzzle state
```

```
initial_state = [
```

```
    [2, 8, 3],
```

```
    [1, 6, 4],
```

```
    [7, 0, 5]
```

```
]
```

```
solution = a_star_manhattan_distance(initial_state)
```

```
if solution:
```

```
    print("Solution found!")
```

```
else:
```

```
    print("No solution found.")
```

Algorithm:

program title: A\* search algorithm with manhattan value algorithm:

1. initialize:

- (i) start with the initial state of the puzzle
- (ii) set the goal state

2. priority queue:

- (i) use a priority queue (or min-heap) to store states of the puzzle prioritized by  $f(n) = g(n) + h(n)$

- (i)  $g(n)$ : the number of moves (steps) taken from the start
- (ii)  $h(n)$ : the manhattan distance ~~heuristic~~ heuristic which sums the distances of each tile from its correct position

3. explore states:

- (i) remove the state with smallest  $f(n)$  from the queue
- (ii) if this state is the goal state stop and return the solution
- (iii) otherwise generate all possible new states by moving the blank tile left, up, down (or) right

4. evaluate new states:

- (i) for each new state
  - (a) calculate  $g(n)$  (number of steps taken so far)
  - (b) calculate  $h(n)$  (the manhattan distance)
  - (c) add this new state to the priority queue with its  $f(n) = g(n) + h(n)$

5. repeat:

- (i) continue exploring states from the queue until the goal state is reached

6. goal reached:

- (i) once the goal state is reached the algorithm terminates and outputs the solution

*Pen*  
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	2	3
1	8	4
7	6	5

1	2	3
8		4
7	6	5

$$g(n)=4 \quad h(n)=1 \\ f(n)=5$$

2		3
1	8	4
7	6	5

$$g(n)=4 \quad h(n)=3 \\ f(n)=7$$

1	2	3
8		4
7	6	5

$$g(n)=5 \quad h(n)=0 \\ f(n)=5$$

~~implement A\*~~  
mon

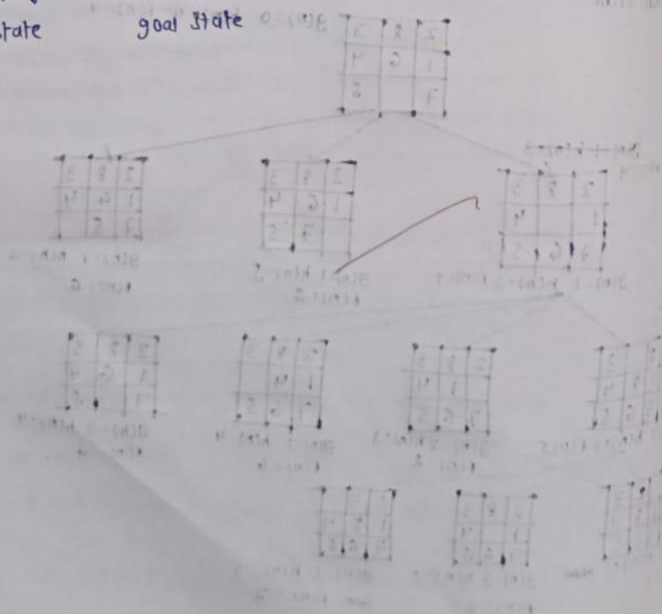
implement A\* search algorithm with manhattan distance

2	8	3
1	6	4
7		5

initial state

1	2	3
8		4
7	6	5

goal state



2	8	3
1		4
7	6	5

$$g(n)=1 \quad h(n)=4 \\ f(n)=5$$

2		3
1	8	4
7	6	5

$$g(n)=2 \quad h(n)=3 \\ f(n)=5$$

2	3
1	8
7	6

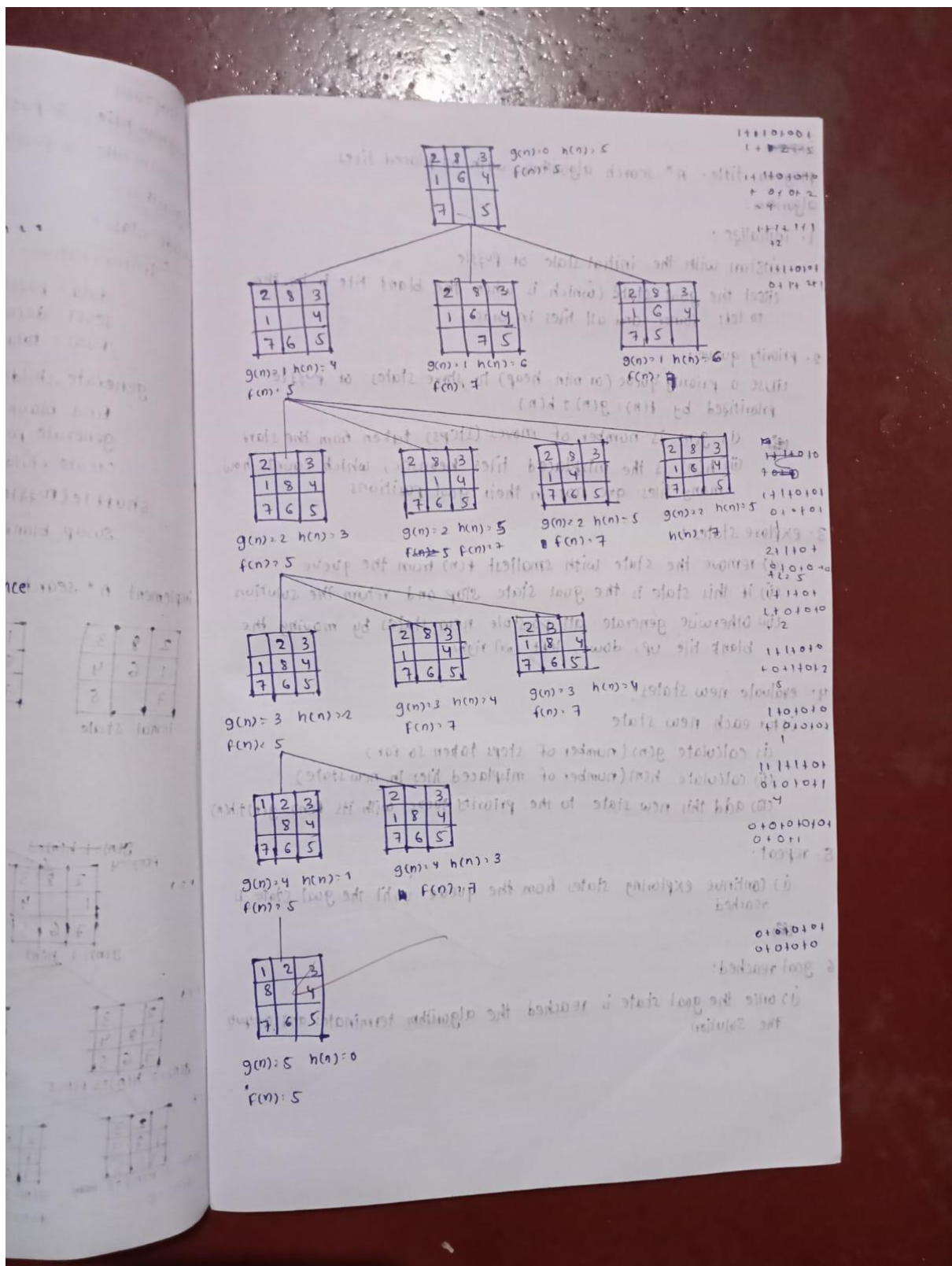
$$g(n)=3 \quad h(n)=2 \\ f(n)=5$$

1	2	3
8		4
7	6	5

$$g(n)=4 \quad h(n)=1 \\ f(n)=5$$

1	2	3
8		4
7	6	5

$$g(n)=5 \quad h(n)=0 \\ f(n)=5$$



Output:

Current State:

[2, 8, 3]

[1, 6, 4]

[7, 0, 5]

$g(n) = 0, h(n) = 5, f(n) = 5$

-----

Current State:

[2, 8, 3]

[1, 0, 4]

[7, 6, 5]

$g(n) = 1, h(n) = 4, f(n) = 5$

-----

Current State:

[2, 0, 3]

[1, 8, 4]

[7, 6, 5]

$g(n) = 2, h(n) = 3, f(n) = 5$

-----

Current State:

[0, 2, 3]

[1, 8, 4]

[7, 6, 5]

$g(n) = 3, h(n) = 2, f(n) = 5$

-----

Current State:

[1, 2, 3]

[0, 8, 4]

[7, 6, 5]

$g(n) = 4, h(n) = 1, f(n) = 5$



-----  
Current State:

[1, 2, 3]

[8, 0, 4]

[7, 6, 5]

$g(n) = 5$ ,  $h(n) = 0$ ,  $f(n) = 5$

-----  
Goal reached!

Solution found!