# Feature Selection and Classification of Diffraction Images

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Abstract — We present to you our latest research work on diffraction images captured using flow cytometer. In flow cytometry, the investigation of 3D morphological features of biological cells can provide the basis to deeply study the biochemical processes that a cell undergoes during various activities such as apoptosis and mitosis. Also, automatic classification of biological cells is highly desired, as in most of the cases, manual analysis of image data is often necessary to study the underlying morphological processes due to the complex cell structure. In previous studies, we have already shown the potential to automatically classify diffraction images using GLCM and SVM. In this paper, our primary objective is to select the most discriminating GLCM features, and deeply investigate the quantization and displacement factors of GLCM on the performance of two classifiers, Support Vector Machine (SVM) and Logistic Model Trees (LMT) for diffraction images. We computed a total of 20 GLCM textural features for 6 types of cultured cells (100 samples per cell). Without any feature selection the maximum classification accuracy was 90.8%, 86.83% with stratified 10 fold cross validation (10FCV) using SVM and LMT respectively. An optimal subset of features was selected using 2 different approaches. In approach 1, feature selection was done using Extensive Feature Correlation Study (EFCS) resulting in 7 GLCM textural features. In approach 2, feature selection was done using correlation based feature selection algorithm resulting in 8 features. Using features from approach 1, the classification accuracy of SVM increased from 90.8% to 91.16% while it remained the same in the case of LMT. Also, features selected using approach 1 yielded better classification rates than features selected using approach 2 for both classifiers. The findings in this experiment concludes that a set of 7 features selected using approach 1 with a 6-bit(64 levels) quantization scheme along with a displacement of d=2 are best to analyze diffraction images using GLCM.

Keywords— Diffraction imaging; GLCM; Extensive Feature correlation study(EFCS); CFS(Correlation based feature selection algorithm); SVM(Support Vector Machine); Logistic Model Trees(LMT).

#### I. INTRODUCTION

In molecular cell biology, the study of cellular shape and structure is becoming a major subject for analysis. For example, observing the temporal sequence of morphological changes in cells undergoing apoptosis (programmed cell death) can provide critical information to study how some cancers originate and progress. Not only various cellular activities, but extraction of morphological features are very important for cell study, differentiation and clinical diagnosis. In most of the cases, morphological study of cells relies on conventional microscopy. This is usually labor intensive and relies on fluorescent signals from stained cells as the molecular labels for analysis and classification. Also, it reveals very limited morphological and produces qualitative results rather than quantitative. In [1, 2, 3, 4, 5], through modelling the light scattering by single cells, it was shown that the spatial distribution of elastically scattered light intensity correlates with the 3D morphology of biological cells in the form of intracellular distribution of refractive index. It is in this aspect that many investigators are interested in a flow cytometry method for rapid and label-free classification of biological cells.

However, in current flow cytometry, the technology is designed on the concept to detect angularly integrated signals of scattered light to extract molecular and limited morphological information for cell differentiation. Also, it requires cell staining with multiple fluorescent dyes, thereby increasing the complexity in sample preparation, measurement and data analysis. It is in this context, that we have recently developed a polarization diffraction imaging flow cytometry (p-DIFC) method and shown its potential for cell characterization and classification [6,7,8,9,12,13]. p-DIFC method captures the spatial distribution of coherent light scatters by simultaneously acquiring two cross polarized diffraction images or a polarization image pair from single cells excited by a laser beam. Also, this method doesn't require cell staining with

multiple fluorescent reagents. The diffraction pattern or the light scattering occurs due to the varying refractive indices and can be captured as a diffraction image using a camera. Diffraction imaging technique is not new. In fact, diffraction images captured using X-ray crystallography are used to study arrangement of crystalline atoms in three dimensions. Also, diffraction imaging is used in coherent diffraction imaging or lens-less imaging for 2D and 3D reconstruction of various samples ranging from nanoparticles, nanotubes, bio materials and whole cells using X-rays, electrons, and tabletop lasers. To quantitatively characterize the fringe patterns on the diffraction images, we have developed image processing software based on Grey Level Co-occurrence Matrix (GLCM) algorithm for automated classification of cells [7, 10, 11].

In [7], we have clearly demonstrated that p-DIFC method has the capacity for rapid and label-free cell classification using GLCM algorithm. In [10], we have investigated and presented a new label-free method for the measurement of apoptosis in single HL-60 cells and found that 4 GLCM parameters extracted from the diffraction images present strong correlation with the apoptosis rates. Also in [11], we have demonstrated a robust way to classify Jurkat T and Ramos B cells with high classification rates using GLCM and SVM.

Our primary aim is to find an optimal subset of GLCM features that are more related to the class in terms of differentiating them and less correlated among each other. Our secondary aim is to find the optimal displacement factor d and an efficient quantization scheme that can best capture the fringe patterns on the diffraction image with minimal information loss and at the same time is computationally fast. The quantitative evaluation of the set of experiments on GLCM computing parameters, GLCM features and two learning algorithms would help achieve the aforementioned aims.

The organization of the paper goes by briefly describing the GLCM algorithm and its application in section 2, then the data set, software tools used, and the method of experiment in section 3. The features selection approaches are discussed in section 4. The classification results and conclusions are discussed in section 5. Lastly, the paper concludes by discussing and concluding the whole study in section 6 and 7 respectively.

#### II. GLCM AND APPLICATIONS

#### A. GLCM Algorithm

One of the most commonly used technique to study texture analysis is GLCM. The Grey level co-occurrence matrix was proposed by Haralick et al in 1973[26], describing 14 computable textural features based on grey-tone spatial dependencies. GLCM calculates second order statistics which depend on the co-occurrence of the pixel pairs for a given image.

The GLCM defines how often different combinations of gray level pixels occur in an image for a given distance d in a particular angle  $\theta$ . The distance d here refers to the distance between the pixel under observation and its neighbor. For a given Image I with g number of gray levels, GLCM matrix P will have g\*g number of rows and columns. The element P(i,j) of the GLCM specifies the number of times a pixel with intensity i occurs next to a pixel with intensity j in a specified angular direction  $\theta$  and an offset distance d between the pixels. The angular direction  $\theta$  is usually calculated using  $[0^{\circ}, 45^{\circ}, 90^{\circ}, 135^{\circ}]$ . Fig. 1 shows the possible orientation.

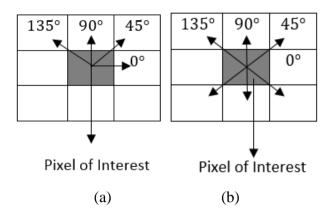
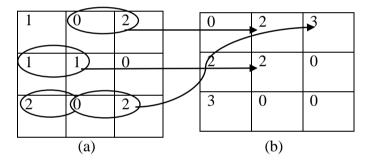


Fig. 1. (a) Asymmetric computation, (b) Symmetric computation.

GLCM matrices are symmetric i.e.  $P(i,j;d,0^{\circ}) = P(j,i;d,0^{\circ})$ . Fig. 1. (b) explains the symmetric computation of GLCM.

For example consider an image having 9 pixels with following gray level intensities. Fig. 2. (a)



| 0    | 0.16 | 0.25 |
|------|------|------|
| 0.16 | 0.16 | 0    |
| 0.25 | 0    | 0    |
|      | (c)  |      |

Fig. 2. (a) 3\*3 Image, (b) GLCM, (c) Normalized GLCM

Then the GLCM matrix (symmetric) for d=1 and  $\theta=0^{\circ}$  would be Fig. 2(b). Once the occurrences of all possible gray level pairs are computed, then the GLCM matrix is normalized by the following equation. See Fig. 2. (C)

$$P_{i,j=\frac{V_{i,j}}{\sum_{i,j=0}^{N-1}V_{i,j}}}$$

where, i is the row number (actual gray level of the reference cell) and j is the column number (actual gray level value of the neighboring cell).

#### B. Applications

Texture analysis techniques can be broadly classified into four categories, namely - statistical methods (GLCM, Gray Level run length matrix –GLRLM, Statistical feature Matrix-SFM), Geometrical methods (Voronoi tessellation features, structural models), Model based methods (Markov random fields, Fractals), and Signal processing methods (Spatial domain filtering, Fourier domain filtering, Gabor & Wavelet models) [37].

Among the statistical methods, GLCM is the most commonly used approach for texture analysis. The GLCM has been widely used in medical image analysis for automatic diagnosis of abdominal tumors [28], automatic detection of tumor subtypes in mammograms [29], and prediction of Cirrhosis in ultrasound images [30]. It has also been extensively used in the field of Remote Sensing to differentiate land categories [26] and analyze texture of SAR (Synthetic

aperture radar) images [31] [32]. It has also been used in auto classification of insects [34], automatic classification of woven fabrics [33], and many other areas.

The reason behind the popularity of GLCM is that the algorithm is very simple and at the same time provides good results for many kinds of images.

#### III. EXPERIMENT METHOD

For this experiment, 6 types of cultured cells (100 diffraction images per each cell) were used. The method used for capturing these images can be found in [6] [7] [9] [10] [11]. The 6 cells used are:

- a) Jurkat cells (pronounced yur'kat) are an immortalized line of human T lymphocyte cells
- b) Ramos is cell line of human B lymphocyte cells.
- c) HL-60 is a promyelocytic cell line of human promyeloblast cells.
- d) PC3 (PC-3) is a human prostate cancer cell lines.
- e) PCS- Primary Dermal Fibroblasts cells derived from normal human skin.
- f) WBC –Human white blood cells.

A set of 20 GLCM features (listed below) were computed for a total of 600 images using Matlab (R2013b). The fringe patterns on diffraction images do not have a specific orientation. Instead, the texture is distributed randomly across the image. Hence, for every image four GLCM's were calculated using angles [0°, 45°, 90°, 135°] respectively. Then the mean of the features calculated from these 4 matrices was used as an input to the classifiers. This process was repeated for different combinations of displacement (d=1, 2, 4, 8, 16, and 32) and gray levels (g=8, 16, 32, 64, 128, and 256) yielding 36 combinations in total.

All the feature values computed for 36 different combinations were stored in Excel and then converted to .csv (comma separated value) format.

The Correlation based feature selection (CFS, Approach 2) and the classification analysis using SVM (Support Vector Machine) and Logistic Model trees (LMT) were done in Weka (Version 3.6.12). SVM classification in Weka was done using an open source library for SVM, named LIBSVM (Version 3.20). However, LMT and CFS are in-built in Weka and do not require any external libraries or sources to run.

The classification analysis using SVM and LMT was done in three different scenarios. In the first scenario, all the 20 GLCM features were used. In the second scenario, only features selected using Extensive Feature Correlation Study (EFCS, Approach 1) were used. In the third scenario, only features selected using correlation based feature selection algorithm were used. In all of the scenarios, the classification process was repeated for 36 different combinations with stratified 10 fold cross validation. The classification results were tabulated in excel.

#### IV. FEATURE SELECTION

Feature selection is the process of selecting a subset of total features present that are highly correlated with the subject or class and yet uncorrelated with each other. For real time classification of biological cells, it is important to select the most relevant features that best capture various textures present on the diffraction images. However, the feature set calculated from GLCM often contains highly correlated features and creates difficulties like increase in computation time, lower learning speed of the machine learning algorithms, and in some cases decrease classification accuracy. Thus, it is important to remove redundant features from the feature set computed from GLCM.

Many researches use feature selection algorithms to select an optimal subset of features. Existing feature selection algorithms for machine learning can be broadly classified into two

categories, namely - wrappers and filters. The former are those which evaluate the features using feedback from a learning algorithm, and the latter are those which evaluate features using heuristic process based on the general characteristics of data [27].

Wrappers give better results than filters in terms of the accuracy of a learning algorithm because feature selection is based upon on the feedback received from that particular algorithm. Since the feature selection process is bound to a learning algorithm, wrappers are expensive to run and have to be re-executed each time when switching from one learning algorithm to another [27].

Filters are way faster than wrappers and do not require re-execution when working with different learning algorithms. Correlation based feature selector (CFS) was one such filter algorithm that was used to select an optimal set of features for this experiment.

However, in this experiment we selected two sets of features using two approaches. The first approach which we call it Extensive Feature Correlation Study (EFCS) aims to study 20 most commonly used GLCM features by many researches and select an optimal set based on previous research and numerical results on diffraction images.

In the second approach, we used correlation based feature selection algorithm (CFS) which is one of the most commonly used feature selection algorithm.

A. Extensive Feature Correlation Study (EFCS) of 20 Textural Features calculated from GLCM (Approach 1):

GLCM features broadly measure three kinds of texture concepts namely Contrast, Uniformity or Orderliness of pixels, and Correlation among the pixels. This method aims to study 20 most commonly used GLCM features, organize them into one of the texture group they belong to, and then select one or more features from each group that best represent them.

Notation:

Let p(i, j) be (i, j) th entry in a normalized GLCM,  $\mu_x$ ,  $\mu_y$  be the mean for the rows and columns of GLCM matrix,  $\sigma_x$ ,  $\sigma_y$  be the standard deviations for rows and columns of the GLCM matrix. Let  $\mu$  be the mean of the entire normalized GLCM.

The features are as follows.

1) Angular second moment or Energy or Uniformity: 
$$f_1 = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} p(i,j)^2$$

Energy measures the texture uniformity and randomness. Energy calculates the sum of squared elements in GLCM. If an image contains a homogenous texture, it will have very few gray -tone transitions, giving the GLCM only few entries but of very high values. Hence, the energy is high.

2) Contrast:

$$f_2 = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} (i-j)^2 p(i,j)$$

The diagonal elements of the GLCM represent pixel pairs with no grey level variation (0-0, 1-1, 2-2, 3-3 etc.). If there are large number of entries in the diagonal elements of the matrix, then it means that the image does not have many gray-tone transitions and hence, the contrast is very less. If the number of entries away from the diagonal are more (implying more gray-tone transitions, then the contrast is high due to many gray tone transitions in the image. Contrast increases exponentially as one moves away from the GLCM diagonal.

3) Correlation:

$$f_3 = \frac{\sum_i \sum_j (ij) p(i,j) - \mu_x \mu_y}{\sigma_x \sigma_y}$$

Correlation measures the linear dependence of neighboring gray tones. This features depends on the organization of texture in an image. Given a gray tone in any resolution cell, using a linear function, higher the probability of predicting gray tone in a neighboring resolution cell, higher the value of correlation [14]. This feature is uncorrelated with GLCM energy and entropy (which depend on pixel pair repetition) as it reaches maximum regardless of pixel pair occurrences. This feature is also uncorrelated with GLCM contrast, as the probability of predicting a gray level of one pixel from the second in a given pixel pair is completely independent from contrast [16].

4) Homogeneity or Inverse Difference Moment:

$$f_4 = \sum_{i=0}^{N_g - 1} \sum_{j=0}^{N_g - 1} \frac{1}{1 + (i - j)^2} p(i, j)$$

IDM measures image homogeneity. It takes large values for smaller gray tone differences in pair elements. It is more sensitive to entries present in or near the diagonal elements of GLCM. It is easy to guess that this feature is inversely correlated to contrast. But, in fact it depends on the combination of energy and contrast. IDM increases when contrast decreases and energy is kept constant. IDM increases when energy decreases and contrast is kept constant. IDM can be constant if there is an increase in contrast and decrease in energy [16]. So, this feature is dependent on their combination. Homogeneity decreases exponentially as one moves away from the GLCM diagonal.

5) Entropy:

$$f_5 = -\sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} p(i,j) \log(p(i,j))$$

Entropy measures the heterogeneity or the disorder of an image. It is inversely correlated to energy (or ASM). For an image which is not texturally uniform, there will be large number of entries of small values. Hence, entropy reaches maximum at this point. Entropy reaches maximum for an image having pixels of random gray level intensities (white noise).

6) Dissimilarity:

$$f_6 = \sum_{i} \sum_{j} |i - j| p(i, j)$$

Dissimilarity measures variation of gray level pairs in an image. This feature is very close to contrast as both of them calculate the same parameter with different weights. Dissimilarity always produces values lower than Contrast as it increases linearly rather than exponentially. This feature is highly correlated with contrast [17].

7) Sum of squares: Variance

$$f_7 = \sum_{i=0}^{N_g-1} \sum_{j=0}^{N_g-1} (i-\mu)^2 p(i,j)$$

Variance measures how homogenous areas are spread out on the image. It increases when gray level values differ from their mean. Low variance implies large areas of uniform homogeneity while high variance might indicate many small areas of homogenous regions [15, 16]. It is positively correlated to contrast in many practical cases but they measure different texture concepts. Variance is associated with the average gray level difference between pixels and their mean, unlike contrast where it is associated with the average gray level difference between neighboring pixels [16].

#### 8) Maximum Probability:

$$f_8 = MAX_{i,j}p(i,j)$$

This features measures texture uniformity solely on the basis of the highest probability. This feature was formulated in [18].

# Features calculated from Gray level sum histogram (GLSH) and Gray level difference histogram (GLDH)

The gray level sum histogram is a histogram of the sum of the pairs of pixels. It is computed from GLCM by summing the two-dimensional density p(i,j) over constant value of (i + j), i.e.

$$S_k = \sum_{\substack{i=0\\i+j=k}}^{N_g-1} \sum_{j=0}^{N_g-1} p(i,j), k = 0,...,2N_g - 2.$$

The gray level difference histogram is a histogram of the absolute differences of gray levels from pairs of pixels. It is computed from GLCM by summing the two-dimensional density p(i,j) over constant value of |i-j|.

$$D_k = \sum_{\substack{i=0\\|i-j|=k}}^{N_g-1} \sum_{j=0}^{N_g-1} p(i,j), k = 0, ..., N_g - 1.$$

It is obvious that features  $f_{10}$ ,  $f_{11}$  and  $f_{14}$ ,  $f_{15}$  are conceptually same as Entropy and Variance calculated from GLCM except that they are computed from GLSH and GLDH, respectively. In [21], Weszka compared the classification performance of texture measures computed from GLCM, GLDH, FPS (Fourier Power Spectrum), and GLRLM (Gray level run length matrix) on aerials and LANDSAT imagery. He found that GLCM and GLDH features were most useful and were equal in performance. In [22], Conners & Harlow made a theoretical comparison of four texture analyses to determine the amount of information captured in each of the algorithms. The algorithms that were examined are the spatial gray level dependence method (SGLDM) or GLCM, gray level run length method (GLRLM), gray level difference method (GLDM), and power spectral method (PSM). The results indicate that GLCM performed very well of the four considered.

The advantage of using features from the sum and difference histograms matrices is that, it has lower storage and lower computational requirements. But, deep investigation is necessary to check if there is any information loss when converting GLCM to GLSH and GLDH [23]. Also, a careful feature selection procedure may be required in many cases.

9) Sum Average or GLCM Mean:

$$f_9 = \sum_{k=0}^{2N_g - 2} kS_k = \mu_x + \mu_y$$

This feature weighs the pixel value by frequency of its occurrence in combination with a certain neighbor pixel value. This is one of the descriptive statistic on the GLCM.

10) Sum Entropy:

$$f_{10} = -\sum_{k=0}^{2N_g - 2} S_k \log S_k$$

11) Sum Variance:

$$f_{11} = \sum_{k=0}^{2N_g-2} (k-f_9)^2 S_k$$

12) Cluster Shade:

$$f_{12} = \sum_{k=0}^{2N_g - 2} (k - f_9)^3 S_k$$

13) Cluster Prominence:

$$f_{13} = \sum_{k=0}^{2N_g - 2} (k - f_9)^4 S_k$$

Cluster shade and Cluster Prominence are used to measure the skewness (measure of the asymmetry of the probability distribution of pixels) of the matrix. It is believed to emulate human perceptual behavior. The values of these features depend on the sums of rows and columns of the GLSH matrix. These features are close to features that measure the uniformity. When an image has little variations, then the value of these features are low. These features were formulated by Conners and Harlow in [24], in a search to be able to use GLCM not only to discriminate the patterns in texture but to be able to use them to characterize the structure in textures.

14) Difference Variance:

$$f_{14} = \sum_{k=0}^{N_g - 1} K^2 D_k$$

15) Difference Entropy:

$$f_{15} = -\sum_{k=0}^{N_g - 1} D_k \log D_k$$

### Other features:

16) Information Measure of Correlation 1:

$$f_{16} = \frac{HXY - HXY1}{\max\{HX, HY\}}$$

Where,

$$HXY = -\sum_{i} \sum_{j} p(i,j) \log(p(i,j)),$$

$$HXY1 = -\sum_{i} \sum_{j} p(i,j) \log\{p_x(i)p_y(j)\},\$$

HX and HY are entropies of  $p_x$  and  $p_y$ .

17) Information Measure of Correlation 2:

$$f_{17} = (1 - \exp[-2.0(HXY2 - HXY)])^{1/2}$$

Where,

$$HXY2 = -\sum_{i} \sum_{j} p_{x}(i) p_{y}(j) \log\{p_{x}(i) p_{y}(j)\}$$

Correlation measure  $f_3$  is the most popular measure of linear dependence between two random variables but it provides limited information about their dependence structure. Also, it cannot measure dependence when there exists a nonlinear structure between two random variables. In order to overcome these deficiencies,  $f_{16}$   $f_{17}$  were introduced by Linfoot in [25]. These features successfully preserve the properties of mutual information and can measure dependence between two random variables even when there exists a nonlinear structure between them. However, these two features are correlated and only usage of  $f_{16}$  is recommended [20].

18) Inverse Difference normalized (INN):

$$f_{18} = \sum_{i,j=1}^{N_g} \frac{p(i,j)}{1 + |i-j|/N_g^2}$$

This feature is inversely proportional to dissimilarity. This feature is modified by normalizing the gray level difference |i - j| by the number of gray levels  $N_g$ .

19) Inverse Difference moment normalized (IDN):

$$f_{19} = \sum_{i,j=1}^{N_g} \frac{p(i,j)}{1 + (i-j)^2 / N_g^2}$$

This feature is the normalized statistic of  $f_4$ . This is done by normalizing the gray level difference (i - j) by the number of gray levels  $N_g$ .

Without normalization, the above two features  $f_{18}f_{19}$  are based on the sum of p(i,j) weighted by a numerical series  $(\{1,\frac{1}{2},\frac{1}{3},\frac{1}{4}\}\ for\ f_{18}\ or\ \{1,\frac{1}{2},\frac{1}{5},\frac{1}{10}...\}\ for\ f_4$ . For smooth texture, the un-normalized features are likely to sum p(i,j) values that are close to one while coarse textures tend to sum p(i,j) values close to zero. This results in sparse cluster for a smooth texture and tight clusters for coarse texture. This is opposite to the expected behavior and hence normalization provides a series that is more linear in nature. Hence, preventing this drawback [23].

## 20) Auto Correlation:

$$f_{20} = \sum_{i=0}^{N_g - 1} \sum_{j=0}^{N_g - 1} (i, j). p(i, j)$$

This feature measures the amount of regularity as well as fineness/ coarseness of the texture present in the image. Like GLCM correlation it takes high values for image having repetitive or predictive pattern of texture elements. Auto correlation and GLCM correlation provide same information [19].

Table I. Classification of GLCM features into groups

|                         | Contrast Measures             |                   |
|-------------------------|-------------------------------|-------------------|
| Features                | Group 1                       | Recommended       |
|                         | _                             |                   |
|                         |                               |                   |
|                         |                               |                   |
| Contrast(CON)           | Measures the gray level       |                   |
|                         | local variations in an Image. |                   |
| Dissimilarity(DIS)      | Measures the same texture     |                   |
|                         | concept like Contrast and     |                   |
|                         | always produces values        |                   |
|                         | lower than Contrast. See Fig. |                   |
|                         | 3.                            |                   |
| Inverse Difference      | Inversely proportional to     |                   |
| Normalized(INN)         | Dissimilarity                 |                   |
| Inverse Difference      | Measure the extent to which   |                   |
| Moment(IDM)             | similar gray tones tend to be |                   |
|                         | neighbors. Dependent on the   | Contrast and IDM. |
|                         | combination of Contrast and   |                   |
|                         | Energy                        |                   |
| Inverse Difference      | Normalized statistic of IDM   |                   |
| Moment Normalized(IDN)  |                               |                   |
| Variance(VAR)           | Measures the average gray     |                   |
| G 71 (G77)              | level difference between      |                   |
| Sum Variance(SV)        | pixels and their mean. Close  |                   |
| Difference Verience(DE) | to Contrast in many cases,    |                   |
| Difference Variance(DF) | but both measure different    |                   |
|                         | texture concepts.             |                   |

| Uni   | formity Or Orderliness Group 2   |                                  |
|---|--|----------------------------------|
| Maximum probability(MAX)  | Measures texture uniformity solely on the basis of the highest probability of one pair of pixels that dominates other pairs.   |                                  |
| Energy(ENE)   | Measures image homogeneity. The more homogenous the larger the values.   |                                  |
| Entropy(ENT)  | Measures image Heterogeneity.  | Entropy and                      |
| Difference Entropy(DENT) Sum Entropy(SENT)  | The more homogenous the lower the values. Inversely proportional to Energy   | Entropy and Difference Entropy   |
| Cluster Shade(CS) Cluster Prominence(CP)  | Measures image uniformity and can characterize structure in textures   |                                  |
| Correlation   | and other descriptive statistics G   | roup 3                           |
| Correlation(COR)  | Measures the linear dependency between two pixels in an image. 0 is uncorrelated. 1 is perfectly correlated.   |                                  |
| Information Measure of correlation 1(IMC1) Information Measure of correlation 2(IMC2) | Can measures linear dependence<br>between two pixels even when<br>there exists a nonlinear structure<br>between them. Both these<br>features are correlated [20]. Using<br>one of them is recommended. | Correlation, IMC1 & Sum Average. |
| Auto Correlation(AC)  | Measure the same information provided by GLCM correlation.  For details see [19].  | a Sum Average.                   |
| Sum Average(SA)   | This feature weighs the pixel value by frequency of its occurrence in combination with a certain neighbor pixel value.   |                                  |

Group 1: From Fig. 3, it is evident that, when CON increases exponentially, DIS increases linearly. Choosing one among CON, DIS, and INN is recommended as all the three measure the same texture concept. VAR and CON measure different texture concepts but they hold similar results in many practical situations [16]. So, we ignore VAR. IDM is dependent on the combination of ENE and CON. IDN is a normalized feature of IDM. Hence, we choose CON and IDM to represent group 1 and ignore the rest.

Group 2: From Fig. 4, it is evident that the behavior of ENT, SENT, and DENT's feature curves for 50 images of HL\_60 diffraction images are very similar except for the difference in

feature weights. DENT seems to have a normalized range of values compared to the other two. MAX, ENE, and ENT are homogeneity statistics and choosing one of them is recommended.

On the other hand CS and CP are very close to features measuring uniformity but have some interesting properties compared to them. But both these features take high values and often reduce classification performance. In [32] the author reported that due to the high range of values and thus their influence on other features, exclusion of CS and CP increased classification accuracy. Hence, we chose ENT and DENT to represent group 2. Although ENT and DENT are same from a theoretical point of view, the reason for considering the latter is due to its normalized range of values.

Group 3: COR, AC, IMC1, and IMC2 measure the linear dependence between the pixels. But the latter two have some interesting properties compared to others and choosing one of them is recommended. On the other hand SA is uncorrelated with all features in this group and is one of the descriptive statistic of GLCM. Hence we chose COR, IMC1, and SA from group 3.

A total of 7 features were selected using this approach {Contrast, Inverse Difference Moment, Entropy, Difference Entropy, Correlation, Information Measure of Correlation 1 and Sum Average}.

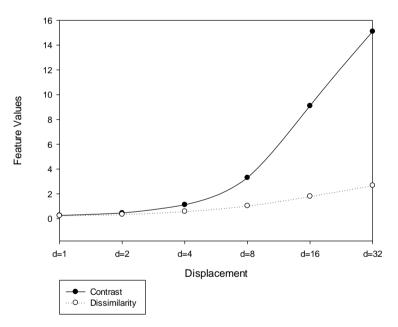


Fig. 3. Feature values for CON and DIS computed for HL\_60 cells (g=64, d=2). When CON increases exponentially, DIS increases linearly

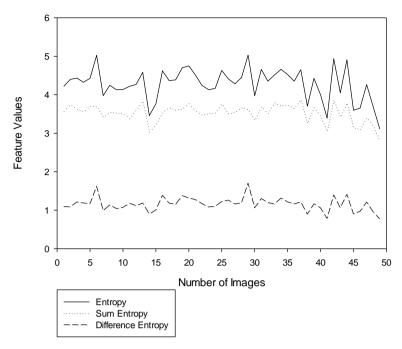


Fig. 4. Feature values of ENT, SENT, and DENT computed for 50 images of HL-60 cells (g=64, d=2).

#### B. Feature Selection using CFS(Approach 2)

CFS is a fully automatic algorithm that doesn't require the user to specify any thresholds or the number of features desired. The output of any learning algorithm that uses features selected using CFS can be represented in terms of original features, not in terms of a transformed space as CFS operates on original feature space.

CFS ranks feature subsets according to a correlation based heuristic evaluation function. The evaluation function produces subsets that contain highly correlated features with the class and uncorrelated with each other. Irrelevant features are removed as they have low correlation with the class. Redundant features that are highly correlated with one or more features are also removed. The feature is selected based upon the extent to which it predicts classes in areas of the instance space not already predicted by other features [27].

CFS's feature subset evaluation function is given by:

$$M_s = \frac{k\overline{r_{cf}}}{\sqrt{k + k(k-1)\overline{r_{ff}}}} \tag{1}$$

Where,  $M_s$  is the heuristic "merit" of a feature subset s containing k features.  $\overline{r_{cf}}$  is the average feature correlation  $(f \in S)$  and  $\overline{r_{ff}}$  is the average feature-feature inter correlation. The numerator of the CFS's feature subset evaluation function provides information on how predictive the set of features are in terms of the class, whereas the denominator provides information on how much redundancy there is among the features [27].

The implementation of CFS used in this experiment was done using best first heuristic search strategy. Best first strategy may start with the empty set of attributes and search forward, or start with the full set of attributes and search backward, or start at any point and search in both directions (by considering all possible single attribute additions and deletions at a given point).

A total of 8 features were selected using CFS algorithm {Autocorrelation, Correlation, Energy, Homogeneity, Maximum Probability, Sum Average, Information Measure of Correlation 1, and Information Measure of Correlation 2}.

#### **CLASSIFICATION RESULTS**

#### A. SVM

Support Vector Machines are one of the most successful tool for data classification. It was introduced by Vladimir Vapnik in 1995. A classification problem usually involves test data and training data. The goal of SVM is to build a model based on training data where each instance has a target value (or class labels) with a set of attributes ( or features) and predict the target values of the test data given only it's attributes [36]. SVM basically performs binary classification, however several SVM classifiers can be combined to do multiclass classification by comparing 'one against the rest' or 'one against one'. However in this experiment we have used LIBSVM which is an open source library for SVM. LIBSVM is an integrated software for SVM and has wide range of features like allowing the user to set different parameters, try different kernels, display useful statistics, cross validation for mode selection, efficient multiclass classification by comparing 'one against one' rather 'one against the rest' as the former has shorter training time.

The basic idea of SVM is to map the input data on to higher dimensional feature space nonlinearly related to the input space and determine a maximum margin hyper plane or decision boundary to separate the two classes of feature space, where margin is the distance between the hyper plane and the closest data point.

Let  $\{x_1, ..., x_n\}$  be our training set and let  $y_i \in \{1, -1\}$  be the class label of  $x_i$ . To find

optimal hyper plane 
$$w. x + b = 0$$
, the optimization problem in its basic form is given as
$$\min_{w,b} \frac{1}{2} |w|^2 + C \sum_{i=1}^m \xi_i$$
subject to  $y_i(wx_i + b) \ge 1 - \xi_i, \xi \ge 0$ 

The value of 'C' can be used to set the relative performance of maximizing the margin. In most of the real world problems, boundaries separating the two classes are highly nonlinear. To handle this kind of problems the input vector are mapped into a higher dimensional space where two classes can then be linearly separable [35]. The dot product in the feature space is given by function called kernel 'K'. Then the lagrangian dual of the nonlinear mapping can be given as

$$\min_{\alpha} \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} y_i y_j \alpha_i \alpha_j K(x_i, x_j) - \sum_{i=1}^{m} \alpha_i$$

$$(2)$$

subject to  $\sum_{i=1}^{m} y_i \alpha_i = 0$  and  $C_i \ge \alpha_i \ge 0$ , i = 1, ... m

where  $\alpha_1, \dots \alpha_m \ge 0$  are the lagrane multipliers and 'K' is the kernel function[35]. In this experiment polynomial kernel function was used. It is given as

$$K(x_i, x_j) = (\gamma x_i^t x_j + r)^d, \gamma > 0$$
(3)

Here, r,  $d \& \gamma$  are the kernel parameters.

Table II. Classification Results of SVM (no feature selection)

| Distanc | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|---------|-------|-------|-------|-------|-------|-------|
| e       |       |       |       |       |       |       |
| G=8     | 71.33 | 70.33 | 77.33 | 76.83 | 75.16 | 64.66 |
| G=16    | 82.16 | 83.66 | 85.83 | 82.5  | 79.83 | 68.16 |
| G=32    | 86.33 | 89    | 88    | 85    | 78.83 | 71.16 |
| G=64    | 88    | 89.66 | 89.83 | 85.33 | 80    | 72.33 |
| G=128   | 89    | 90.83 | 90.00 | 87.5  | 80.66 | 73.16 |
| G=256   | 90    | 90.16 | 90.66 | 88.66 | 82.33 | 76.66 |

Table III. Classification Results of SVM (features selected using EFCS- Approach 1)

| Distance | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|----------|-------|-------|-------|-------|-------|-------|
| G=8      | 69    | 71.83 | 75.16 | 76.33 | 73.33 | 64    |
| G=16     | 79.66 | 82    | 83    | 82.33 | 77.83 | 70    |
| G=32     | 86.16 | 89.33 | 89.33 | 83.83 | 80.16 | 70    |
| G=64     | 88.16 | 91.16 | 89.5  | 84    | 79.16 | 69.16 |
| G=128    | 89.5  | 91    | 89.16 | 84    | 79.33 | 71.5  |
| G=256    | 89.83 | 90.83 | 89.5  | 86.16 | 83.33 | 74.5  |

Table IV. Classification Accuracy of SVM (features selected using CFS- Approach 2)

| Distance | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|----------|-------|-------|-------|-------|-------|-------|
| G=8      | 68.83 | 69.16 | 75.66 | 75.83 | 72.66 | 64.66 |
| G=16     | 74.83 | 80.33 | 81.83 | 81.66 | 78.66 | 68.5  |
| G=32     | 80.83 | 86.16 | 86.66 | 84.5  | 80.33 | 72.5  |
| G=64     | 83.66 | 87.66 | 87.16 | 83.66 | 80.33 | 67.16 |

| G=128 | 85.16 | 85.83 | 86.16 | 84    | 79.83 | 68   |
|-------|-------|-------|-------|-------|-------|------|
| G=256 | 84.33 | 87.5  | 86.33 | 83.83 | 80.5  | 70.5 |

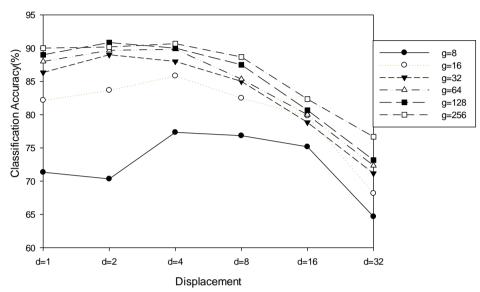


Fig. 5. Classification Accuracy of SVM (no feature selection) for all displacement values across all quantization levels

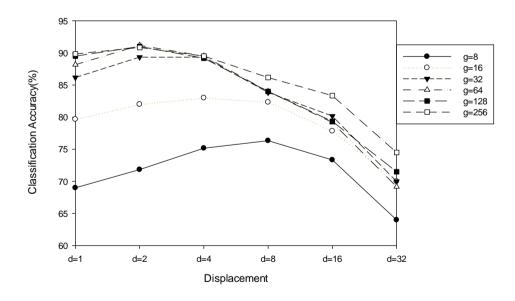


Fig. 6. Classification Accuracy of SVM (features selected using EFCS- Approach 1) for all displacement values across all quantization levels

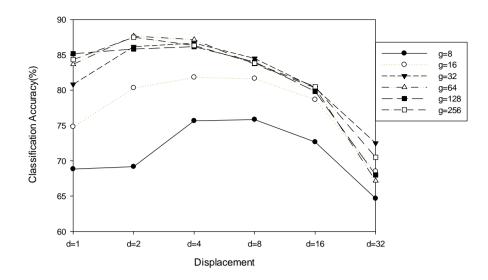


Fig. 7. Classification Accuracy of SVM (features selected using CFS- Approach 2) for all displacement values across all quantization levels

#### B. Logistic Model Trees

A logistic model tree is basically a standard decision tree with logistic regression function at leaves. As in the case of ordinary decision tree a test on one of the attribute is associated with every inner node of the tree. For numeric values, the node has two child nodes and the testing is done by comparing the attribute value with the threshold value. If the value of the instance is smaller than the threshold it is sorted down the left branch and sorted down to the right branch otherwise [38].

The tree structure of the logistic model tree consists of non-terminal (or inner nodes) N and a set of leaves or terminal nodes T. Let  $S = D_1 * .. * D_m$  denote the whole instance space, spanned by all attributes  $V = \{v_1, ..., v_m\}$  that are present in the dataset. Then every region is represented by a leaf in the tree[38]:

$$S = \bigcup_{t \in T} S_t, \quad S_t \cap S_{t'=\emptyset} \text{ for } t \neq t'$$

The leaves of the Logistic Model trees have logistic regression function  $f_t$  instead of having a class label. The logistic regression function models the class membership probabilities of all attributes present in the data and is given as

$$\Pr(G = j | X = x) = \frac{e^{F_j(x)}}{\sum_{k=1}^{J} e^{F_k(x)}}$$

where  $F_j(x) = \alpha_0^j + \sum_{v \in V_t} \alpha_v^j \cdot v$ 

if  $\alpha_{v_k}^j = 0$  for  $v_k \notin V_t$ , the model represented by the whole logistic model tree is then given by

$$f(x) = \sum_{t \in T} f_t(x).I(x \in S_t)$$
  
where  $I = (x \in S_t)$  is 1 if  $x \in S_t$  and 0 otherwise.

Table V. Classification Results of LMT (no feature selection)

| Distance | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|----------|-------|-------|-------|-------|-------|-------|
| G=8      | 66.33 | 66.83 | 74.66 | 74.16 | 72.66 | 64.66 |
| G=16     | 72.16 | 76.83 | 80.83 | 80.66 | 80    | 71.16 |
| G=32     | 80.83 | 85.16 | 85.16 | 81.83 | 79.16 | 69.83 |
| G=64     | 81.83 | 86.5  | 85.66 | 83.33 | 78.83 | 67.5  |
| G=128    | 82.33 | 85.66 | 86    | 83.16 | 79.66 | 69    |
| G=256    | 84.66 | 86    | 86.83 | 82.83 | 80    | 73.33 |

Table VI. Classification Results of LMT (features selected using EFCS- Approach 1)

| Distance | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|----------|-------|-------|-------|-------|-------|-------|
| G=8      | 64.5  | 69    | 74.66 | 75.16 | 75.5  | 66.33 |
| G=16     | 71    | 77.33 | 82    | 82.16 | 78.5  | 68.66 |
| G=32     | 80.16 | 85.16 | 86.33 | 81.66 | 77.66 | 67.5  |
| G=64     | 82.16 | 86.83 | 85.5  | 82.5  | 75.66 | 62.83 |
| G=128    | 83.33 | 86.16 | 85    | 81.66 | 76.83 | 65.33 |
| G=256    | 82.33 | 86.16 | 82.16 | 79.5  | 77.83 | 69.33 |

Table VII. Classification Results of LMT (features selected using CFS- Approach 2)

| Distance | d=1   | d=2   | d=4   | d=8   | d=16  | d=32  |
|----------|-------|-------|-------|-------|-------|-------|
| G=8      | 63.66 | 69.33 | 74    | 67.5  | 70.16 | 62.33 |
| G=16     | 70.5  | 76.16 | 80.5  | 78.5  | 77.5  | 69.16 |
| G=32     | 76.16 | 83    | 82.16 | 81.83 | 79.16 | 69.16 |
| G=64     | 77.5  | 84.33 | 83.16 | 80.33 | 77.5  | 67    |
| G=128    | 80.83 | 84    | 82.16 | 80.66 | 77.33 | 65    |
| G=256    | 80.33 | 83    | 81.33 | 80.83 | 78.33 | 68.66 |

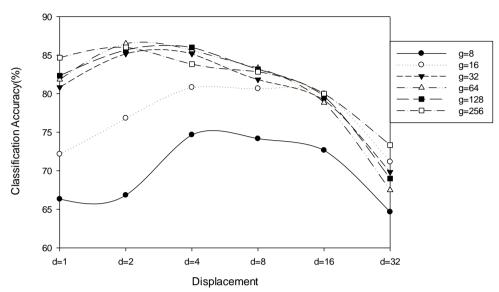


Fig. 8. Classification Accuracy of LMT (no feature selection) for all displacement values across all quantization levels

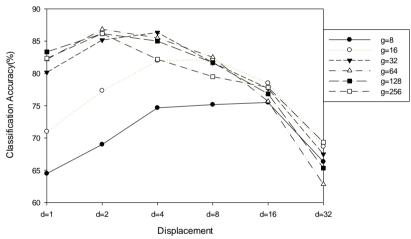


Fig. 9. Classification Accuracy of LMT (features selected using EFCS- Approach 1) for all displacement values across all quantization levels

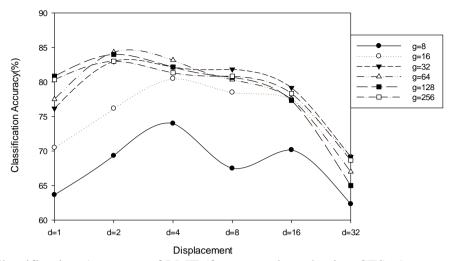


Fig. 10. Classification Accuracy of LMT (features selected using CFS- Approach 2) for all displacement values across all quantization levels

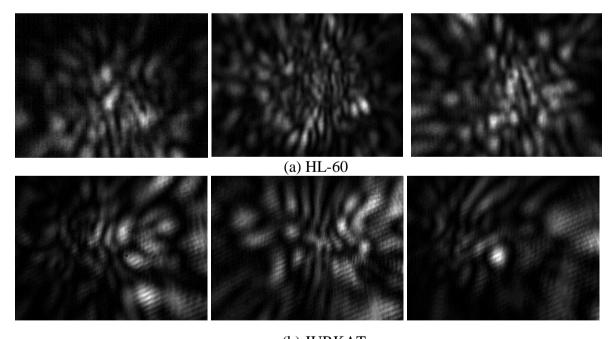
Several conclusion have been drawn from the classification results of SVM and LMT

- 1. Classification accuracy decreased when the gray level quantization was less than 32. This means that the low quantized versions of GLCM features are not sufficient enough to capture all the information from diffraction images.
- 2. Classification accuracy was maximum when the gray level quantization was 32 or more. Specifically, the accuracy was maximum when g=64. This hints us that 64-level scheme is sufficient to represent the diffraction images. Thus, we eliminate the need for 128-level and 256-level schemes which would computationally be very costly in a context of real time analysis.
- 3. Classification accuracy was maximum when displacement d=2 or 4 and decreased when d>4 or d<2. This hints us that d=2 or 4 is best to capture the fringe patterns on the diffraction images. Specifically, the maximum accuracy achieved was 91.16%, 86.83% using SVM and LMT respectively, when g=64 and d=2.
- 4. Using EFCS approach (7 features) the classification accuracy achieved was 91.16% using SVM, which is more than what was achieved using all the 20 features and features selected using CFS (8 features).
- 5. Using EFCS approach (7 features) the classification accuracy achieved was 86.83 % using LMT, which is same as what was achieved using all the 20 features and more than features selected using CFS (8 features).
- 6. The classification performance of SVM outperforms LMT in all cases.

#### VI. DISCUSSIONS

The study of morphological changes in biological cells is highly desired and can lead insights to many underlying activities. Second order GLCM statistics computed from diffraction images strongly provide the basis to distinguish different kinds of cells according to their diffraction patterns captured in flow cytometer settings. In [7], [10], and [11], although we have shown the potential of GLCM to classify diffraction images, much investigation was necessary to find the optimal feature set, effect of quantization level and displacement vector d. Since the dimension of GLCM is dependent on the number of gray levels, if the number is large, the computation of the GLCM would be very costly. On the other hand if the number of gray levels were too low it would fail to capture the texture elements in an image. Hence, through this extensive experimentation, it is clearly evident that a quantization level of 64-level with a displacement of d=2 best represents the diffraction images.

A close observation of the diffraction images of 6 type of cells in Fig. 11 discloses noticeable differences in their fringe patterns. We strongly argue that an optimal set of seven features selected using EFCS approach {Contrast, Correlation, Inverse Difference Moment, Entropy, Difference Entropy, Information Measure of Correlation 1 and Sum Average} are sufficient to quantify these differences. The validity of this argument can be verified by observing the classification results not just based on a single classifier, but both SVM and LMT, where the classification accuracy was better than the CFS approach and using all the 20 features.



(b) JURKAT

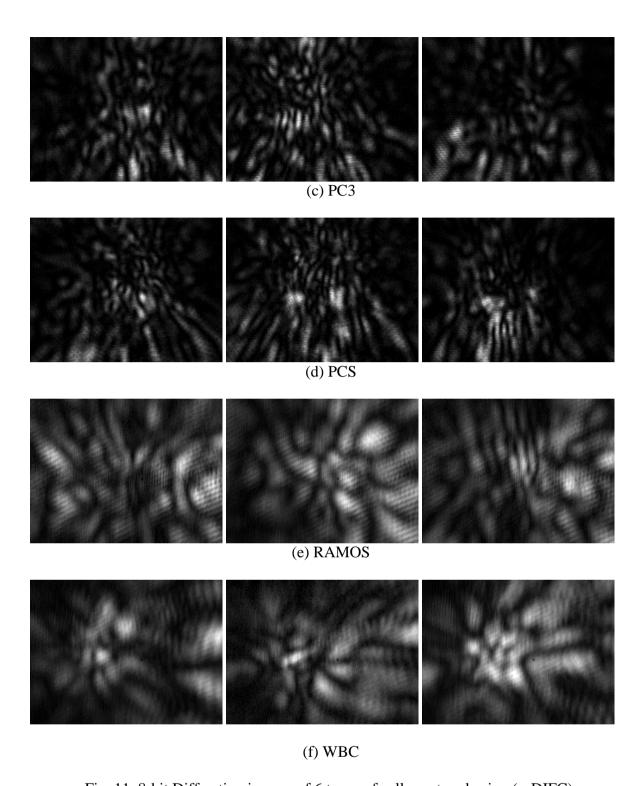
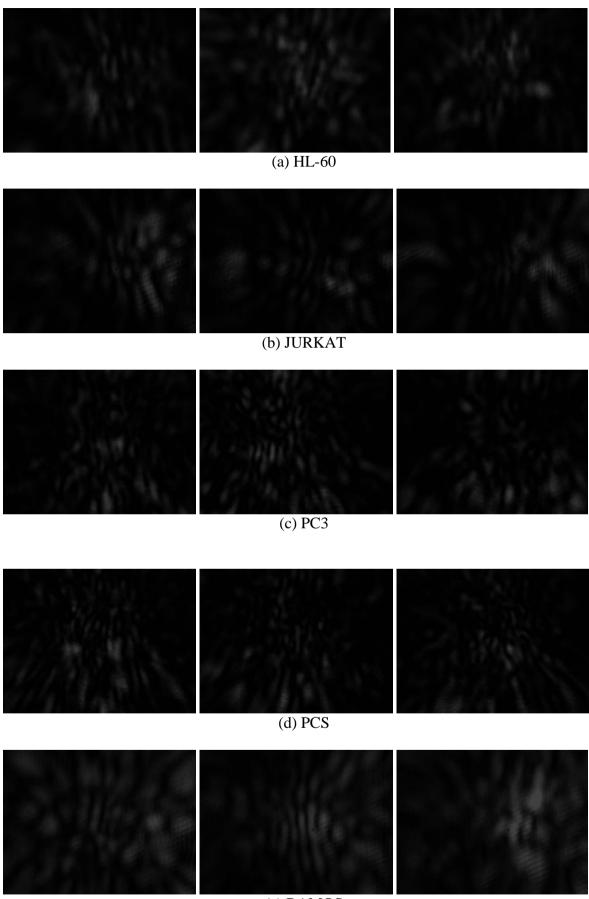


Fig. 11. 8-bit Diffraction images of 6 types of cells captured using (p-DIFC).

Note\* the original raw images were normalized from 12-bit to 8-bit to eliminate the images of over-exposure and under-exposure.



(e) RAMOS

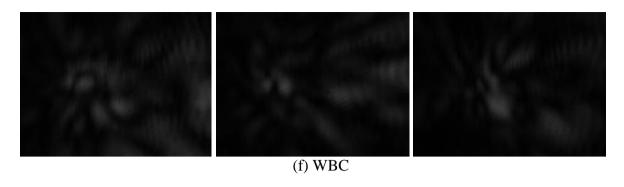


Fig. 12. 6-bit (64 levels) uniform quantized diffraction images in Matlab.

From Table 8, the CON values for PCS, PC3 and RAMOS are higher than the other cells. This is expected as one can observe from Fig. 12(c), (d), and (e) that the number of local variations are more compared to HL-60, JURKAT and WBC cells. COR and IMC1 values for HL-60 and WBC are somewhat higher than the other cells. This could be due to the predictive nature of the pattern or the linear dependence between the pixels. Also as the features values of COR and IMC1 are mean of four orientations, as opposed to a single orientation, hence it is difficult to understand the nature of values.

ENT values for RAMOS & WBC are higher than other cells implying the texture is less homogenous than other cells. On the other hand, SA values are similar for RAMOS &WBC as well as for PC3 & PCS and different for HL-60 & JURKAT.

Table VIII. Mean & Standard deviation values of 7 GLCM features selected using EFCS approach (g=64, d=2)

| С | CON      | COR             | IDM           | ENT        | DENT      | SA         | IMC1            |
|---|----------|-----------------|---------------|------------|-----------|------------|-----------------|
| # |          |                 |               |            |           |            |                 |
| 1 | 1.66±0.7 | 0.983±0.0       | 0.673±0.0     | 4.274±0.03 | 1.153±0.1 | 15.084±2.7 | -               |
|   | 51       | 06              | 74            | 93         | 6         | 21         | $0.52\pm0.061$  |
| 2 | 2.45±1.0 | $0.974\pm0.0$   | $0.619\pm0.0$ | 4.389±0.46 | 1.299±0.1 | 14.309±3.0 | -               |
|   | 12       | 07              | 74            |            | 7         | 55         | 0.453±0.0       |
|   |          |                 |               |            |           |            | 52              |
| 3 | 3.18±1.1 | 0.957±0.0       | $0.575\pm0.0$ | 4.282±0.41 | 1.412±0.1 | 11.576±2.0 | -               |
|   | 65       | 08              | 65            | 2          | 61        | 64         | 0.371±0.0       |
|   |          |                 |               |            |           |            | 38              |
| 4 | 3.01±1.0 | 0.957±0.0       | 0.6±0.051     | 4.181±0.35 | 1.385±0.1 | 11.132±1.8 | -               |
|   | 28       | 07              |               | 2          | 31        | 35         | $0.384\pm0.0$   |
|   |          |                 |               |            |           |            | 26              |
| 5 | 3.72±1.3 | 0.974±0.0       | 0.496±0.0     | 5.268±0.31 | 1.501±0.1 | 26.024±3.7 | -               |
|   | 92       | 08              | 63            | 1          | 51        | 97         | $0.409\pm0.0$   |
|   |          |                 |               |            |           |            | 45              |
| 6 | 2.486±1. | $0.985 \pm 0.0$ | $0.563\pm0.0$ | 5.109±0.32 | 1.33±0.15 | 26.736±4.3 | -               |
|   | 14       | 07              | 67            |            | 4         | 84         | $0.48 \pm 0.05$ |

Table IX. Confusion Matrix for SVM (g=64, d=2, accuracy=91.16%)

| a  | b  | С  | d  | e  | f  | ←classified as |
|----|----|----|----|----|----|----------------|
| 95 | 4  | 0  | 0  | 1  | 0  | a=HL-60        |
| 3  | 93 | 4  | 0  | 0  | 0  | b=JURKAT       |
| 0  | 1  | 84 | 15 | 0  | 0  | c=PC3          |
| 0  | 1  | 18 | 81 | 0  | 0  | d=PCS          |
| 0  | 0  | 0  | 0  | 99 | 1  | e=RAMOS        |
| 0  | 0  | 0  | 0  | 5  | 95 | f=WBC          |

Table X. Confusion Matrix for LMT (g=64, d=2, accuracy=86.83%)

| a  | b  | c  | d  | e  | f  | ←classified as |
|----|----|----|----|----|----|----------------|
| 90 | 7  | 2  | 0  | 1  | 0  | a=HL-60        |
| 9  | 87 | 4  | 0  | 0  | 0  | b=JURKAT       |
| 0  | 4  | 81 | 15 | 0  | 0  | c=PC3          |
| 0  | 1  | 19 | 80 | 0  | 0  | d=PCS          |
| 3  | 0  | 0  | 0  | 92 | 5  | e=RAMOS        |
| 0  | 0  | 0  | 0  | 9  | 91 | f=WBC          |

From Table 9 and 10, it is evident that most of the misclassification occurs for PC3 and PCS cells. On the other hand the average classification accuracy for other cells is around 95.5 %(SVM) and 90 %(LMT).

#### VII. CONCLUSION

In this paper, we have accomplished two tasks. First, we deeply investigated 20 commonly used GLCM parameters and proved that an optimal set of 7 features {Contrast, Correlation, Inverse Difference Moment, Entropy, Difference Entropy, Information measure of Correlation 1, and Sum Average} are sufficient to describe the diffraction images. Also, we have proved that these features perform better than those selected using CFS approach.

Second, we investigated that effect of quantization and displacement factors of GLCM on the performance of two classifiers, SVM and LMT. The findings conclude that a 6-bit (64 levels) quantization scheme along with a displacement of d=2 are best to analyze diffraction images using GLCM.

#### REFERENCES

- [1] A. Dunn, C. Smithpeter, A. J. Welch, and R. Richards-Kortum, "Finite-difference time-domain simulation of light scattering from single cells," *J. Biomed. Opt.* 2(3), 262–266, 1997.
- [2] R. S Brock, X. H. Hu, P. Yang, and J. Q Lu, "Evaluation of a parallel FDTD code and application to modeling of light scattering by deformed red blood cells," *Opt. Express* 13(14), 5279–5292, 2005.
- [3] J. Q. Lu, P. Yang, and X. H. Hu, "Simulations of light scattering from a biconcave red blood cell using the finite-difference time-domain method," *J. Biomed. Opt.* 10(2), 024022, 2005.
- [4] R. S. Brock, X. H. Hu, D. A. Weidner, J. R. Mourant, and J. Q. Lu, "Effect of detailed cell structure on light scattering distribution: FDTD study of a B-cell with 3D structure constructed from confocal images," *J. Quant. Spectrosc. Radiat. Transf.* 102(1), pp. 25–36, 2006.
- [5] H. Ding et al., "Angle-resolved Mueller matrix study of light scattering by B-cells at three wavelengths of 442, 633, and 850 nm," *J. Biomed. Opt. 12(3)*, 034032, 2007.
- [6] K. M. Jacobs, J. Q. Lu, and X. H. Hu, "Development of a diffraction imaging flow cytometer," *Opt. Lett.34 (19)*, pp. 2985–2987, 2009.
- [7] K. Dong et al., "Label-free classification of cultured cells through diffraction imaging," *Biomed. Opt. Express* 2(6), pp. 1717–1726, 2011.
- [8] S. Yu et al., "A novel method of diffraction imaging flow cytometry for sizing microspheres," *Opt. Express* 20(20), pp. 22245–22251, 2012.
- [9] J. Zhang et al., "Analysis of cellular objects through diffraction images acquired by flow cytometry," *Opt. Express* 21(21), pp. 24819–24828, 2013.
- [10] Xu Yang et al., "A quantitative method for measurement of HL-60 cell apoptosis based on diffraction imaging flow cytometry technique," *Biomed Opt Express*, 5(7): pp. 2172–2183, Jul. 2014.
- [11] Yuanming Feng et al., "Polarization Imaging and Classification of Jurkat T and Ramos B Cells Using a Flow Cytometer," *Cytometry Part A*, 85, pp. 817-826, June 2014.
- [12] Y. Sa et al., "Study of low speed flow cytometry for diffraction imaging with different chamber and nozzle designs." *Cytometry A 2013; 83A*,pp. 1027–1033, 2013.

- [13] Jacobs KM.et al., "Diffraction imaging of spheres and melanoma cells with a microscope objective," *J. Biophotonics* 2(8-9), pp. 521–527, 2009.
- [14] Robert Haralick, K. Shanmugam and I. Dinstein, "On Some Quickly Computable Features for Texture," in *Proceedings of the 1972 Symposium on Computer Image Processing and Recognition*, University of Missouri, Vol.2, pp. 12-2-1 to 12-2-10, August, 1972.
- [15] Robert Haralick, "On a Texture-Context Feature Extraction Algorithm for Remotely Sensed Imagery," *Proceedings of the IEEE Computer Society Conference on Decision and Control*, Gainesville, FL, pp. 650-657, Dec. 1971.
- [16] A. Baraldi and F. Parmiggiani, "An investigation of the textural characteristics associated with gray level co-occurrence matrix statistical parameters," *IEEE Trans. Geosci. Remote Sensing*, vol. 33, pp. 293–304, Mar. 1995.
- [17] A. Gebejes and R. Huertas, "Texture Characterization based on Grey-Level Co-occurrence Matrix," *Proceedings in Conference of Informatics and Management Sciences*, 2013.
- [18] Robert Haralick, "Statistical and Structural Approaches to Texture," *Proceedings of the IEEE*, Vol. 67, No. 5, May, 1979, pp. 786-804.
- [19] Van der Sanden, J. J. and D. H. Hoekman, "Review of relationships between grey-tone co-occurrence, semivariance and autocorrelation based image texture analysis approaches." *Canadian Journal of Remote Sensing*, vol. 38 no. 3, pp. 207-213, 2005.
- [20] J. M. Carstensen, "Description and simulation of visual texture," Ph.D. dissertation, Inst. Math. Modeling, Technical Univ. Denmark, Lyngby, Denmark, 1992.
- [21] J. S. Weszka, C. R. Dyer, and Azriel Rosenfeld, "A comparative study of texture measures for terrain classification," *IEEE Transactions on Systems, Man, and Cybernetics*, 6(4), pp. 269-285, 1976.
- [22] R.W Conners and C.A. Harlow, "A theoretical comparison of texture algorithms," *IEEE Transactions on Pattern Analysis and Machine Intelligence* 2, pp. 204-222, 1980.
- [23] David Anthony Clausi, "Texture Segmentation of SAR sea ice imagery," Phd thesis, University of Waterloo, 1996.
- [24] R. W. Conners, M. M. Trivedi, and C. A. Harlow, "Segmentation of a high-resolution urban scene using texture operators," *Comput. Vision, Graph., Image Processing*, vol. 25, pp.273, 1984.
- [25] E.H Linfoot, "An information measure of correlation," *Inform Contr*, Vol. 1, pp. 85-89, 1957.

- [26] R. M. Haralick, K. Shanmugan, and I. H. Dinstein, "Textural features for image classification", *IEEE Trans. Syst., Man, Cybern.*, vol. SMC-3, pp.610-621, 1973.
- [27] M. A Hall, "Correlation-based Feature Selection for Machine Learning," Unpublished doctoral dissertation, The University of Waikato, Hamilton, Newzealand, 1999.
- [28] D. Mitrea, M. Socaciu, R. Badea and A. Golea, "Texture based characterization and automatic diagnosis of the abdominal tumors from ultrasound images using third order GLCM features," in: *Proceedings of the Fourth International Congress on Image and Signal Processing*, pp. 1558-1562, 2011.
- [29] M. Mohamed Fathima, D. Manimegalai, and S. Thaiyalnayaki, "Automatic detection of tumor subtype in mammograms based On GLCM and DWT features using SVM," *Information Communication and Embedded Systems (ICICES)*, vol., no., pp.809,813, 21-22, Feb. 2013.
- [30] Jitendra Virmani, Vinod Kumar, Naveen Kalra, and Niranjan Khandelwal, "Prediction of Cirrhosis Based on Singular Value Decomposition of Gray Level Co-occurence Marix and a neural Network Classifier," *Developments in E-systems Engineering (DeSE)*, p.p 146 151, 2011.
- [31] Jia Longhao, Zhou Zhongfa, and Li Bo, "Study of SAR Image Texture Feature Extraction Based on GLCM in Guizhou Karst Mountainous Region," *Remote Sensing, Environment and Transportation Engineering (RSETE)*, 2012 2nd International Conference on, 2012.
- [32] L. Soh and C. Tsatsoulis, "Texture analysis of sar sea ice imagery using gray level co-occurances matrices," *IEEE Trans. on Geoscience and Remote Sensing*, 37(2):pp. 780-795, 1999.
- Yassine Ben Salem, and Salem Nasri, "Automatic Classification of Woven Fabrics using Multi-class Support Vector Machine," *J RJTA*, 13 (2), pp. 28–36, 2009.
- [34] L.Q. Zhu and Z. Zhang, "Auto-classification of Insect Images Based on Color Histogram and GLCM," *Seventh International Conference on Fuzzy Systems and Knowledge Discovery*, 2010.
- [35] Lawrence R. Rabiner, "A tutorial on HMMs and selected applications in speech recognition," *Proceedings of IEEE*, Vol77. N02, Feb. 1989.
- [36] Chih-Wei Hsu, Chih-Chung Chang, and Chih-Jen Lin, "A Practical Guide to Support Vector Classification," Technical Report, National Taiwan University, 2003.

- [37] M. Tuceryan and A. K. Jain, "Texture Analysis," In *Handbook of Pattern Recognition and Computer Vision*, Second Edition, C. H. Chen, L. F. Pau, and P. Wang (editors), World Scientific Publishing, Co., pp. 235 276,1998.
- [38] L. Niels, H. Mark, and F. Eibe, "Logistic model trees". Mach. Learn., pp. 161–205,2005.

#### **APPENDIX 1 CLASSIFICATION STATISTICS AND RESULTS**

0.837

0.859

0.964

0.951

0.857

PC3

PCS

RAMOS

WBC

0.914

0.726

0.759

0.922

0.933

0.857

```
64, d=2, SVM no feature selection
=== Stratified cross-validation ===
=== Summary ==
Correctly Classified Instances
                               538
                                           89.6667 %
Incorrectly Classified Instances
                                          10.3333 %
                                62
                          0.876
Kappa statistic
Mean absolute error
                             0.0344
Root mean squared error
                               0.1856
Relative absolute error
                             12.4 %
                              49.7996 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
                        0.941 0.95
         0.95
                0.012
                                      0.945 0.969 HL 60
         0.9
               0.012
                        0.938
                               0.9
                                      0.918
                                              0.944 JURKAT
         0.88
                0.044
                        0.8
                               0.88
                                      0.838
                                              0.918
                                                     PC3
         0.83
                0.02
                        0.892
                              0.83
                                      0.86
                                              0.905 PCS
         0.91
                0.02
                        0.901
                               0.91
                                      0.905
                                               0.945
                                                     RAMOS
         0.91
                       0.919
                                       0.915
                                               0.947
                0.016
                               0.91
                                                       WBC
Weighted Avg.
               0.897
                       0.021
                               0.898
                                       0.897
                                               0.897
                                                       0.938
=== Confusion Matrix ===
 a b c d e f <-- classified as
95 3 1 0 1 0 | a = HL_60
 5 90 4 1 0 0 b = JURKAT
 0 \ 3 \ 88 \ 9 \ 0 \ 0 \mid c = PC3
 0 0 17 83 0 0 d = PCS
 1 0 0 0 91 8 | e = RAMOS
 0\ 0\ 0\ 0\ 9\ 91\ |\ f = WBC
64,d=2, SVM CFS feature selection
=== Stratified cross-validation ===
=== Summary ===
                                          85.6667 %
Correctly Classified Instances
                               514
Incorrectly Classified Instances
                                86
                                          14.3333 %
Kappa statistic
                          0.828
                             0.0478
Mean absolute error
                               0.2186
Root mean squared error
Relative absolute error
                             17.2 %
                              58.6515 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.9
               0.014
                       0.928
                               0.9
                                      0.914
                                              0.943 HL_60
         0.88
                0.02
                        0.898
                               0.88
                                      0.889
                                               0.93
                                                     JURKAT
```

Weighted Avg. === Confusion Matrix ===

0.73

0.77

0.95

0.91

0.056

0.052

0.022

0.008

0.857

0.723

0.748

0.896

0.958

0.029

0.73

0.77

0.95

0.91

0.858

a b c d e f <-- classified as 90 7 1 0 2 0 | a = HL\_60 6 88 5 1 0 0 | b = JURKAT  $0\ 2\ 73\ 25\ 0\ 0\ |\ c = PC3$  $0 \ 1 \ 22 \ 77 \ 0 \ 0 \mid d = PCS$  $1 \ 0 \ 0 \ 0 \ 95 \ 4 \mid \ e = RAMOS$ 0 0 0 0 9 91 | f = WBC

#### 64,d=2, SVM EFCS feature selection

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                547
                                            91.1667 %
Incorrectly Classified Instances
                                            8.8333 %
                                53
                           0.894
Kappa statistic
                              0.0294
Mean absolute error
Root mean squared error
                                0.1716
Relative absolute error
                              10.6 %
                               46.0435 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.95
                0.006
                         0.969
                                 0.95
                                        0.96
                                                0.972 HL_60
         0.93
                0.012
                         0.939
                                 0.93
                                        0.935
                                                0.959
                                                       JURKAT
         0.84
                0.044
                         0.792
                                 0.84
                                        0.816
                                                0.898 PC3
         0.81
                0.03
                        0.844
                                        0.827
                                                0.89 PCS
                                0.81
         0.99
                0.012
                         0.943
                                0.99
                                        0.966
                                                0.989 RAMOS
         0.95
                0.002
                         0.99
                                0.95
                                       0.969
                                                0.974
                                                       WBC
Weighted Avg.
               0.912
                       0.018
                                0.913
                                        0.912
                                                0.912
                                                        0.947
=== Confusion Matrix ===
 a b c d e f <-- classified as
95 4 0 0 1 0 | a = HL_60
 3 93 4 0 0 0 | b = JURKAT
 0 \ 1 \ 84 \ 15 \ 0 \ 0 \mid c = PC3
 0 1 18 81 0 0 | d = PCS
 0\ 0\ 0\ 99\ 1\mid e = RAMOS
 0\ 0\ 0\ 0\ 5\ 95\ |\ f = WBC
64,d=2, LMT no feature selection
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                519
                                            86.5 %
Incorrectly Classified Instances
                                81
                                           13.5
                                                 %
Kappa statistic
                           0.838
Mean absolute error
                              0.0664
Root mean squared error
                                0.1866
Relative absolute error
                              23.9145 %
                               50.07 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.88
                0.018
                         0.907
                                 0.88
                                        0.893
                                                0.967 HL_60
         0.87
                0.028
                                 0.87
                                        0.866
                                                0.974
                                                       JURKAT
                         0.861
         0.8
                0.046
                                               0.961 PC3
                        0.777
                                0.8
                                       0.788
                0.034
                         0.827
                                        0.818
                                                0.964 PCS
         0.81
                                 0.81
         0.93
                0.024
                         0.886
                                 0.93
                                        0.907
                                                0.978
                                                       RAMOS
                                               0.986 WBC
         0.9
                0.012
                        0.938
                                0.9
                                       0.918
Weighted Avg.
               0.865
                       0.027
                                0.866
                                       0.865
                                               0.865
                                                        0.972
=== Confusion Matrix ===
 a b c d e f <-- classified as
88 9 1 0 2 0 | a = HL_60
 8 87 4 1 0 0 | b = JURKAT
 0 \ 4 \ 80 \ 16 \ 0 \ 0 \ | \ c = PC3
```

0 1 18 81 0 0 | d = PCS 1 0 0 0 93 6 | e = RAMOS 0 0 0 0 10 90 | f = WBC

#### 64,d=2, LMT CFS feature selection

```
=== Stratified cross-validation ===
=== Summary ===
```

Correctly Classified Instances 506 84.3333 % Incorrectly Classified Instances 94 15.6667 % Kappa statistic 0.812

Mean absolute error 0.0752
Root mean squared error 0.1996
Relative absolute error 27.0629 %
Root relative squared error 53.5662 %
Total Number of Instances 600

=== Detailed Accuracy By Class ===

```
TP Rate FP Rate Precision Recall F-Measure ROC Area Class
              0.022
                      0.891
                             0.9
                                    0.896
                                           0.962 HL_60
        0.81
               0.016
                       0.91
                              0.81
                                    0.857
                                            0.966 JURKAT
                                            0.949 PC3
        0.77
               0.054
                       0.74
                              0.77
                                    0.755
        0.85
               0.042
                       0.802
                              0.85
                                     0.825
                                            0.968 PCS
        0.9
               0.034
                      0.841
                              0.9
                                    0.87
                                           0.987 RAMOS
        0.83
               0.02
                      0.892
                             0.83
                                    0.86
                                            0.987
                                                   WBC
Weighted Avg.
              0.843
                                    0.843
                                            0.844
                      0.031
                             0.846
                                                   0.97
```

=== Confusion Matrix ===

a b c d e f <-- classified as 90 5 2 0 1 2 | a = HL\_60 7 81 11 1 0 0 | b = JURKAT 1 2 77 20 0 0 | c = PC3 0 1 14 85 0 0 | d = PCS 2 0 0 0 90 8 | e = RAMOS 1 0 0 0 16 83 | f = WBC

#### 64,d=2, LMT EFCS feature selection

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 521 86.8333 % Incorrectly Classified Instances 79 13.1667 %

Kappa statistic

Mean absolute error

Root mean squared error

Root relative squared error

Total Number of Instances

0.842

0.0606

0.1813

21.811 %

48.6593 %

#### === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.9 0.024 0.882 0.9 0.891 0.972 HL 60 0.87 0.024 0.879 0.874 0.969 JURKAT 0.87 0.81 0.05 0.764 0.81 0.786 0.959 PC3 0.8 0.03 0.842 0.821 0.975 PCS 0.8 0.92 0.979 0.02 0.902 0.92 0.911 RAMOS 0.948 0.91 0.01 0.91 0.929 0.99 **WBC** Weighted Avg. 0.868 0.026 0.87 0.868 0.869 0.974

=== Confusion Matrix ===

a b c d e f <-- classified as 90 7 2 0 1 0 | a = HL\_60 9 87 4 0 0 0 | b = JURKAT 0 4 81 15 0 0 | c = PC3 0 1 19 80 0 0 | d = PCS 3 0 0 0 92 5 | e = RAMOS 0 0 0 0 991 | f = WBC

#### 64,d=4, SVM no feature selection

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 539 89.8333 % Incorrectly Classified Instances 61 10.1667 %

#### === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.94 0.016 0.922 0.94 0.931 0.962 HL 60 0.9 0.01 0.947 0.9 0.923 0.945 JURKAT 0.85 0.034 0.833 0.85 0.842 0.908 PC3 0.915 PCS 0.86 0.856 0.86 0.030.851 0.91 0.018 0.91 0.91 0.91 0.946 RAMOS 0.93 0.014 0.93 0.93 0.93 0.958 WBC Weighted Avg. 0.898 0.02 0.899 0.898 0.899 0.939

## === Confusion Matrix ===

a b c d e f <-- classified as 94 5 0 0 1 0 | a = HL\_60 6 90 3 0 1 0 | b = JURKAT 0 0 85 15 0 0 | c = PC3 0 0 14 86 0 0 | d = PCS 2 0 0 0 91 7 | e = RAMOS 0 0 0 0 7 93 | f = WBC

## 64,d=4, SVM CFS feature selection

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 523 87.1667 % Incorrectly Classified Instances 77 12.8333 %

Kappa statistic

Mean absolute error

Root mean squared error

Root relative squared error

Total Number of Instances

0.846

0.0428

0.2068

15.4 %

55.4977 %

#### === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.91 0.018 0.91 0.91 0.91 0.946 HL\_60 0.88 0.014 0.926 0.88 0.903 0.933 JURKAT 0.794 0.85 0.044 0.85 0.821 0.903 PC3 0.82 0.03 0.8450.82 0.832 0.895 PCS 0.9 0.026 0.874 0.9 0.887 0.937 RAMOS 0.87 0.022 0.888 0.87 0.879 0.924 WBC Weighted Avg. 0.872 0.026 0.873 0.872 0.872 0.923

#### === Confusion Matrix ===

## 64,d=4, SVM EFCS feature selection

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 537 89.5 % Incorrectly Classified Instances 63 10.5 %

#### === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.93 0.02 0.903 0.93 0.916 0.955 HL 60 0.9 0.012 0.938 0.9 0.918 0.944 JURKAT 0.87 0.044 0.798 0.87 0.833 0.913 PC3 0.829 0.8 0.026 0.86 0.8 0.887 PCS 0.962 RAMOS 0.94 0.016 0.922 0.94 0.931 0.93 0.008 0.959 0.93 0.944 0.961 WBC Weighted Avg. 0.895 0.021 0.897 0.895 0.895 0.937

## === Confusion Matrix ===

#### 64,d=4, LMT no feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 514 85.6667 % Incorrectly Classified Instances 86 14.3333 %

Kappa statistic

Mean absolute error

Root mean squared error

Relative absolute error

Root relative squared error

Total Number of Instances

0.828

0.0726

0.186

26.1242 %

49.9016 %

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.88 0.028 0.863 0.88 0.871 0.975 HL\_60 0.978 JURKAT 0.84 0.020.894 0.84 0.866 0.82 0.044 0.788 0.82 0.804 0.974 PC3 0.82 0.034 0.828 0.82 0.824 0.983 PCS 0.9 0.026 0.874 0.9 0.887 0.99 RAMOS WBC 0.88 0.02 0.898 0.88 0.889 0.99 Weighted Avg. 0.8570.029 0.857 0.857 0.857 0.982

# === Confusion Matrix ===

a b c d e f <-- classified as 88 8 1 0 2 1 | a = HL\_60 12 84 3 1 0 0 | b = JURKAT 0 2 82 16 0 0 | c = PC3 0 0 18 82 0 0 | d = PCS 1 0 0 0 90 9 | e = RAMOS 1 0 0 0 11 88 | f = WBC

# 64,d=4, LMT CFS feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                499
                                            83.1667 %
                                            16.8333 %
Incorrectly Classified Instances
                                101
                           0.798
Kappa statistic
Mean absolute error
                              0.0784
Root mean squared error
                                0.2057
                              28.2391 %
Relative absolute error
Root relative squared error
                               55.193 %
Total Number of Instances
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.88
                0.03
                        0.854
                                0.88
                                       0.867
                                                0.964 HL 60
                                                0.966 JURKAT
         0.84
                0.026
                         0.866
                                0.84
                                        0.853
                0.052
                        0.755
                                       0.777
                                               0.971 PC3
         0.8
                                0.8
         0.76
                0.036
                         0.809
                                0.76
                                        0.784
                                                0.979 PCS
         0.89
                0.04
                        0.817
                                       0.852
                                                0.977 RAMOS
                                0.89
         0.82
                0.018
                         0.901
                                0.82
                                        0.859
                                                0.983
                                                       WBC
                                       0.832
Weighted Avg.
               0.832
                       0.034
                                0.834
                                               0.832
                                                        0.973
=== Confusion Matrix ===
 a b c d e f <-- classified as
88 9 1 0 2 0 | a = HL_60
12 84 2 1 1 0 | b = JURKAT
 0 \ 3 \ 80 \ 17 \ 0 \ 0 \ | \ c = PC3
 0 1 23 76 0 0 d = PCS
 2 0 0 0 89 9 | e = RAMOS
 1 0 0 0 17 82 | f = WBC
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                513
                                           85.5 %
Incorrectly Classified Instances
                                87
                                           14.5
                                                 %
Kappa statistic
                           0.826
Mean absolute error
                              0.0676
                                0.1911
Root mean squared error
Relative absolute error
                              24.3445 %
Root relative squared error
                               51.2728 %
Total Number of Instances
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.87
                0.03
                        0.853
                                0.87
                                       0.861
                                               0.963 HL 60
         0.86
                0.028
                         0.86
                                0.86
                                       0.86
                                               0.974
                                                      JURKAT
         0.78
                0.038
                         0.804
                                0.78
                                        0.792
                                                0.966 PC3
                        0.848
                                                0.981 PCS
         0.84
                0.03
                                0.84
                                       0.844
         0.88
                0.026
                         0.871
                                0.88
                                        0.876
                                                0.974
                                                       RAMOS
         0.9
                0.022
                        0.891
                                0.9
                                       0.896
                                               0.986
                                                       WBC
                       0.029
Weighted Avg.
               0.855
                                0.855
                                       0.855
                                               0.855
                                                        0.974
=== Confusion Matrix ===
 a b c d e f <-- classified as
87 8 1 0 3 1 | a = HL_60
12 86 2 0 0 0 | b = JURKAT
 2 5 78 15 0 0 | c = PC3
 0\ 0\ 16\ 84\ 0\ 0\mid\ d=PCS
 1 1 0 0 88 10 | e = RAMOS
```

0 0 0 0 10 90 | f = WBC

#### 128 ,d=2, SVM no feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 545 90.8333 % Incorrectly Classified Instances 55 9.1667 % Kappa statistic 0.89

Mean absolute error 0.0306
Root mean squared error 0.1748
Relative absolute error 11 %
Root relative squared error 46.9042 %
Total Number of Instances 600

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.95 0.006 0.969 0.95 0.972 HL 60 0.96 0.91 0.012 0.938 0.91 0.924 0.949 JURKAT 0.87 0.036 0.829 0.87 0.849 0.917 PC3 0.022 0.884 0.929 0.88 0.889 0.88 PCS RAMOS 0.92 0.018 0.911 0.92 0.915 0.951 0.92 0.016 0.92 0.92 0.92 0.952 WBC Weighted Avg. 0.908 0.018 0.909 0.908 0.909 0.945

=== Confusion Matrix ===

a b c d e f <-- classified as 95 3 1 0 1 0 | a = HL\_60 3 91 5 1 0 0 | b = JURKAT 0 3 87 10 0 0 | c = PC3 0 0 12 88 0 0 | d = PCS 0 0 0 0 92 8 | e = RAMOS 0 0 0 0 8 92 | f = WBC

# 128 ,d=2, SVM CFS feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 526 87.6667 % Incorrectly Classified Instances 74 12.3333 %

Kappa statistic

Mean absolute error

Root mean squared error
Relative absolute error
Root relative squared error
Total Number of Instances

0.852

0.0411

0.2028

14.8 %

54.4059 %

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.93 0.01 0.949 0.93 0.939 0.96 HL\_60 0.948 JURKAT 0.91 0.014 0.929 0.910.919 0.82 0.048 0.774 0.82 0.796 0.886 PC3 0.8 0.034 0.825 0.812 0.883 PCS 0.8 0.93 0.024 0.886 0.93 0.907 0.953 RAMOS 0.018 0.906 0.888 0.926 WBC 0.87 0.87 Weighted Avg. 0.877 0.025 0.878 0.877 0.877 0.926

=== Confusion Matrix ===

## 128 ,d=2, SVM EFCS feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 546 91 % Incorrectly Classified Instances 54 9 % Kappa statistic 0.892 0.03 Mean absolute error 0.1732 Root mean squared error 10.8 % Relative absolute error 46.4758 % Root relative squared error Total Number of Instances 600

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.95 0.008 0.96 0.95 0.955 0.971 HL 60 0.93 0.012 0.939 0.93 0.935 0.959 JURKAT 0.87 0.044 0.798 0.87 0.833 0.913 PC3 0.024 0.81 0.893 0.81 0.871 0.839 PCS RAMOS 0.98 0.016 0.925 0.98 0.951 0.982 0.92 0.004 0.979 0.92 0.948 0.958 WBC Weighted Avg. 0.91 0.018 0.912 0.91 0.91 0.946

=== Confusion Matrix ===

a b c d e f <-- classified as 95 3 1 0 1 0 | a = HL\_60 3 93 3 1 0 0 | b = JURKAT 0 2 87 11 0 0 | c = PC3 0 118 81 0 0 | d = PCS 0 0 0 0 98 2 | e = RAMOS 1 0 0 0 7 92 | f = WBC

#### 128, d=2, LMT no feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 514 85.6667 % Incorrectly Classified Instances 86 14.3333 % Kappa statistic 0.828 Mean absolute error 0.0646 Root mean squared error 0.1924 Relative absolute error 23.2393 % Root relative squared error 51.6345 %

=== Detailed Accuracy By Class ===

Total Number of Instances

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.87 0.018 0.906 0.87 0.888 0.957 HL\_60 0.86 0.028 0.86 0.86 0.86 0.955 JURKAT 0.959 PC3 0.83 0.052 0.761 0.83 0.794 0.8 0.03 0.842 0.8 0.821 0.971 PCS 0.93 0.036 0.838 0.93 0.882 0.977 RAMOS 0.85 0.008 0.955 0.85 0.899 0.982 WBC Weighted Avg. 0.857 0.029 0.86 0.857 0.8570.967

600

=== Confusion Matrix ===

## 128 ,d=2, LMT CFS feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 504 84 % Incorrectly Classified Instances 96 16 % Kappa statistic 0.808 Mean absolute error 0.0722 Root mean squared error 0.2007

Mean absolute error 0.0722

Root mean squared error 0.2007

Relative absolute error 25.9897 %

Root relative squared error 53.8599 %

Total Number of Instances 600

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.957 HL\_60 0.88 0.014 0.926 0.88 0.903 0.83 0.03 0.847 0.83 0.838 0.942 JURKAT 0.79 0.056 0.738 0.79 0.763 0.954 PC3 0.973 PCS 0.034 0.81 0.827 0.81 0.818 0.9 0.036 0.833 0.9 0.865 0.979 RAMOS 0.83 0.022 0.883 0.83 0.856 0.978 WBC Weighted Avg. 0.84 0.032 0.842 0.84 0.841 0.964

=== Confusion Matrix ===

## 128 ,d=2, LMT EFCS feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 522 86.16 % Incorrectly Classified Instances 78 13 %

Kappa statistic 0.844
Mean absolute error 0.0613
Root mean squared error 0.183
Relative absolute error 22.0849 %
Root relative squared error 49.0908 %
Total Number of Instances 600

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.89 0.018 0.908 0.89 0.899 0.982 HL\_60 0.978 JURKAT 0.88 0.018 0.907 0.88 0.893 0.84 0.042 0.8 0.84 0.82 0.967 PC3 0.85 0.03 0.85 0.85 0.85 0.975 PCS 0.9 0.032 0.849 0.9 0.874 0.986 RAMOS 0.016 0.915 0.86 0.887 0.978 WBC 0.86 Weighted Avg. 0.87 0.026 0.872 0.87 0.87 0.978

=== Confusion Matrix ===

## 128 ,d=4, SVM no feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                 540
                                              90
                                                    %
Incorrectly Classified Instances
                                              10
                                                    %
Kappa statistic
Mean absolute error
                                0.0333
Root mean squared error
                                  0.1826
Relative absolute error
Root relative squared error
                                 48.9898 %
Total Number of Instances
                                 600
```

=== Detailed Accuracy By Class ===

```
TP Rate FP Rate Precision Recall F-Measure ROC Area Class
        0.92
               0.012
                      0.939
                              0.92
                                    0.929
                                            0.954 HL_60
        0.91
               0.014
                      0.929
                              0.91
                                    0.919
                                            0.948 JURKAT
                                            0.908 PC3
               0.034
        0.85
                      0.833
                              0.85
                                    0.842
        0.88
               0.028
                      0.863
                              0.88
                                    0.871
                                            0.926 PCS
        0.92
               0.018
                      0.911
                              0.92
                                    0.915
                                            0.951 RAMOS
        0.92
               0.014
                      0.929
                              0.92
                                    0.925
                                            0.953 WBC
Weighted Avg.
              0.9
                          0.901 0.9
                                        0.9
                   0.02
                                               0.94
```

=== Confusion Matrix ===

## 128 ,d=4, SVM CFS feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 529 88.1667 % Incorrectly Classified Instances 71 11.8333 % 0.858 Kappa statistic 0.0394 Mean absolute error Root mean squared error 0.1986 Relative absolute error 14.2 % Root relative squared error 53.2917 % Total Number of Instances 600

=== Detailed Accuracy By Class ===

```
TP Rate FP Rate Precision Recall F-Measure ROC Area Class
        0.89
               0.012
                       0.937
                              0.89
                                     0.913
                                             0.939 HL_60
        0.91
                                             0.943 JURKAT
               0.024
                       0.883
                              0.91
                                     0.897
        0.84
               0.036
                       0.824
                              0.84
                                     0.832
                                             0.902 PC3
        0.84
               0.032
                       0.84
                              0.84
                                     0.84
                                            0.904 PCS
        0.93
               0.022
                       0.894
                              0.93
                                     0.912
                                             0.954 RAMOS
                                             0.932
        0.88
               0.016
                       0.917
                                     0.898
                                                    WBC
                              0.88
Weighted Avg.
              0.882
                      0.024
                              0.882
                                     0.882
                                            0.882
                                                    0.929
```

=== Confusion Matrix ===

## 128 ,d=4, SVM EFCS feature selection.

```
=== Stratified cross-validation ==
```

=== Summary ===

Correctly Classified Instances 535 89.1667 % 10.8333 % Incorrectly Classified Instances 65

Kappa statistic 0.87

0.0361 Mean absolute error Root mean squared error 0.19 13 % Relative absolute error Root relative squared error 50.9902 % Total Number of Instances 600

#### === Detailed Accuracy By Class ===

```
TP Rate FP Rate Precision Recall F-Measure ROC Area Class
        0.93
               0.018
                       0.912
                              0.93
                                     0.921
                                             0.956 HL_60
        0.91
               0.012
                       0.938
                              0.91
                                     0.924
                                             0.949 JURKAT
        0.87
               0.044
                       0.798
                              0.87
                                     0.833
                                             0.913 PC3
                                   0.829
        0.8
               0.026
                      0.86
                             0.8
                                           0.887 PCS
                                             0.951 RAMOS
        0.92
               0.018
                       0.911
                              0.92
                                     0.915
        0.92
               0.012
                       0.939
                              0.92
                                     0.929
                                             0.954
                                                    WBC
Weighted Avg.
              0.892
                      0.022
                             0.893
                                     0.892
                                            0.892
                                                    0.935
```

## === Confusion Matrix ===

a b c d e f <-- classified as 93 6 0 0 1 0 | a = HL\_60 7 91 2 0 0 0 | b = JURKAT  $0\ 0.87\ 13\ 0\ 0\ |\ c = PC3$ 0 0 20 80 0 0 | d = PCS  $2\ 0\ 0\ 92\ 6\mid\ e=RAMOS$ 0 0 0 0 8 92 | f = WBC

## 128, d=4, LMT no feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 86 % Incorrectly Classified Instances 84 14 % 0.832 Kappa statistic Mean absolute error 0.0731

Root mean squared error 0.1876 Relative absolute error 26.3064 % Root relative squared error 50.3264 % Total Number of Instances 600

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.87 0.02 0.897 0.87 0.883 0.964 HL\_60 0.989 JURKAT 0.88 0.026 0.871 0.876 0.88 0.84 0.046 0.785 0.84 0.812 0.968 PC3 0.8 0.03 0.842 0.8 0.821 0.981 PCS 0.89 0.026 0.873 0.89 0.881 0.97 RAMOS 0.02 0.898 0.88 0.889 0.984 WBC 0.88 Weighted Avg. 0.860.028 0.861 0.86 0.86 0.976

# === Confusion Matrix ===

a b c d e f <-- classified as 87 9 1 0 2 1 | a = HL\_60 8 88 2 2 0 0 | b = JURKAT  $0 \ 3 \ 84 \ 13 \ 0 \ 0 \mid c = PC3$ 0 0 20 80 0 0 d = PCS 2 0 0 0 89 9 | e = RAMOS  $0\ 1\ 0\ 0\ 11\ 88\mid\ f=WBC$ 

# 128, d=4, LMT CFS feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                493
                                            82 1667 %
Incorrectly Classified Instances
                                107
                                            17.8333 %
Kappa statistic
                           0.786
Mean absolute error
                              0.0911
Root mean squared error
                                0.2075
Relative absolute error
                              32.7936 %
                               55.6901 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.85
                0.016
                         0.914
                                0.85
                                        0.881
                                                0.977 HL_60
         0.89
                0.034
                         0.84
                                0.89
                                       0.864
                                                0.978
                                                      JURKAT
         0.73
                0.054
                         0.73
                                0.73
                                       0.73
                                               0.957
                                                      PC3
         0.76
                0.048
                                               0.968 PCS
                         0.76
                                0.76
                                       0.76
         0.85
                0.032
                         0.842
                                0.85
                                        0.846
                                                0.985 RAMOS
                0.03
                                       0.85
                                              0.98 WBC
         0.85
                        0.85
                               0.85
                                                       0.974
Weighted Avg.
               0.822
                       0.036
                                0.823
                                       0.822
                                               0.822
=== Confusion Matrix ===
 a b c d e f <-- classified as
85 10 2 0 2 1 | a = HL_60
 7 89 3 1 0 0 | b = JURKAT
 0 4 73 23 0 0 | c = PC3
 0 \ 2 \ 22 \ 76 \ 0 \ 0 \mid d = PCS
 1 0 0 0 85 14 | e = RAMOS
0 1 0 0 14 85 | f = WBC
128 ,d=4, LMT EFCS feature selection.
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                523
                                           87.1667 %
Incorrectly Classified Instances
                                77
                                           12.8333 %
Kappa statistic
                           0.846
Mean absolute error
                              0.0635
Root mean squared error
                                0.189
                              22.8697 %
Relative absolute error
                               50.7029 %
Root relative squared error
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
                0.034
                                0.87
                                                0.963 HL 60
         0.87
                         0.837
                                        0.853
                0.022
                                        0.879
                                                0.969
                                                       JURKAT
         0.87
                         0.888
                                0.87
         0.86
                0.03
                        0.851
                                0.86
                                       0.856
                                                0.971
                                                       PC3
                                               0.977
         0.87
                0.026
                         0.87
                                0.87
                                       0.87
                                                       PCS
                                               0.976 RAMOS
                0.024
         0.88
                         0.88
                                       0.88
                                0.88
         0.88
                0.018
                         0.907
                                0.88
                                        0.893
                                                0.962
                                                       WBC
               0.872
                                       0.872
Weighted Avg.
                       0.026
                                0.872
                                               0.872
                                                        0.97
=== Confusion Matrix ===
a b c d e f <-- classified as
87 7 2 0 3 1 | a = HL_60
12\ 87\ 0\ 1\ 0\ 0\mid b=JURKAT
 0\ 2\ 86\ 12\ 0\ 0\ |\ c = PC3
 0 0 13 87 0 0 d = PCS
```

#### 256 ,d=2, SVM no feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 541 90.1667 % Incorrectly Classified Instances 59 9.8333 % Kappa statistic 0.882

Kappa statistic

Mean absolute error

Root mean squared error

Root relative squared error

Total Number of Instances

0.882

0.0328

0.181

11.8 %

48.5798 %

#### === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.967 HL\_60 0.94 0.006 0.969 0.94 0.954 0.92 0.016 0.92 0.92 0.92 0.952 JURKAT 0.82 0.04 0.804 0.82 0.812 0.89 PC3 0.026 0.87 0.87 0.87 0.87 0.922 PCS RAMOS 0.93 0.016 0.921 0.93 0.925 0.957 0.93 0.014 0.93 0.93 0.93 0.958 WBC Weighted Avg. 0.902 0.02 0.902 0.902 0.902 0.941

## === Confusion Matrix ===

# 256 ,d=2, SVM CFS feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 525 87.5 % Incorrectly Classified Instances 75 12.5 % Kappa statistic 0.85

Kappa statistic
Mean absolute error
Root mean squared error
Relative absolute error
Root relative squared error
Total Number of Instances

0.85
0.0417
0.2041
15 %
54.7723 %

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.91 0.012 0.938 0.91 0.924 0.949 HL\_60 0.952 JURKAT 0.93 0.026 0.877 0.93 0.903 0.79 0.042 0.79 0.79 0.79 0.874 PC3 0.84 0.03 0.848 0.844 0.905 PCS 0.84 0.92 0.024 0.885 0.92 0.902 0.948 RAMOS 0.86 0.016 0.915 0.887 0.922 WBC 0.86 Weighted Avg. 0.875 0.025 0.876 0.875 0.875 0.925

# === Confusion Matrix ===

```
256 ,d=2, SVM EFCS feature selection.
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                           90.8333 %
                               545
Incorrectly Classified Instances
                                           9.1667 %
Kappa statistic
Mean absolute error
                             0.0306
                               0.1748
Root mean squared error
Relative absolute error
Root relative squared error
                              46.9042 %
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.97
                0.008
                        0.96
                               0.97
                                      0.965
                                               0.981 HL_60
         0.91
                0.004
                        0.978
                                0.91
                                       0.943
                                               0.953 JURKAT
                0.052
         0.88
                        0.772
                                0.88
                                       0.822
                                               0.914
         0.81
                0.024
                        0.871
                                0.81
                                       0.839
                                               0.893
         0.95
                0.012
                        0.941
                                0.95
                                       0.945
                                               0.969 RAMOS
         0.93
                0.01
                        0.949
                               0.93
                                      0.939
                                               0.96
Weighted Avg.
               0.908
                       0.018
                                      0.908
                                              0.909
```

0.912

PC3

PCS

WBC

0.945

=== Confusion Matrix ===

a b c d e f <-- classified as 97 1 2 0 0 0 | a = HL\_60 3 91 5 1 0 0 | b = JURKAT  $0\ 1\ 88\ 11\ 0\ 0\mid\ c=PC3$  $0 \ 0 \ 19 \ 81 \ 0 \ 0 \mid \ d = PCS$ 0 0 0 0 95 5 | e = RAMOS 1 0 0 0 6 93 | f = WBC

# 256, d=2, LMT no feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
```

Correctly Classified Instances % 516 86 Incorrectly Classified Instances 84 14 % Kappa statistic 0.832 Mean absolute error 0.0618 Root mean squared error 0.1929 Relative absolute error 22.2558 % 51.7713 % Root relative squared error Total Number of Instances 600

# === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.87 0.018 0.906 0.87 0.8880.962 HL\_60 0.86 0.032 0.843 0.86 0.851 0.956 JURKAT 0.78 0.05 0.757 0.78 0.768 0.955 PC3 0.844 0.967 0.81 0.827 PCS 0.03 0.81 0.94 0.026 0.879 0.94 0.908 0.985 RAMOS WBC 0.9 0.012 0.938 0.9 0.918 0.983 Weighted Avg. 0.86 0.028 0.861 0.86 0.86 0.968

#### === Confusion Matrix ===

a b c d e f <-- classified as 87 7 2 0 3 1 | a = HL\_60 8 86 5 1 0 0 | b = JURKAT 0 8781400 | c = PC3 $0\ 1\ 18\ 81\ 0\ 0\mid\ d=PCS$ 1 0 0 0 94 5 | e = RAMOS 0 0 0 0 10 90 | f = WBC

## 256 ,d=2, LMT CFS feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                498
                                            83
                                                 %
Incorrectly Classified Instances
                                102
                                            17
                                                 %
                           0.796
Kappa statistic
Mean absolute error
                              0.0753
                                0.2092
Root mean squared error
Relative absolute error
                              27.1218 %
Root relative squared error
                               56.1249 %
Total Number of Instances
                                600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.89
                0.024
                         0.881
                                 0.89
                                        0.886
                                                0.957 HL_60
         0.84
                0.034
                         0.832
                                 0.84
                                        0.836
                                                0.948 JURKAT
                                                0.952 PC3
                0.054
         0.74
                         0.733
                                 0.74
                                        0.736
```

0.811

0.841

0.884

0.034 0.83

0.77

0.9

0.84

0.79

0.87

0.83

0.962 PCS

0.862 0.977 WBC

0.83

0.977 RAMOS

0.962

=== Confusion Matrix ===

0.77

0.9

0.84

Weighted Avg.

0.036

0.034

0.022

0.83

a b c d e f <-- classified as 89 7 1 0 1 2 | a = HL\_60 10 84 5 1 0 0 | b = JURKAT 1 8 74 17 0 0 | c = PC3 0 2 21 77 0 0 | d = PCS 1 0 0 0 90 9 | e = RAMOS 0 0 0 0 16 84 | f = WBC

# 256,d=2, LMT EFCS feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 517 86.1667 % Incorrectly Classified Instances 83 13.8333 % Kappa statistic 0.834 Mean absolute error Root mean squared error 0.1906 Relative absolute error 22.1285 % Root relative squared error 51.1313 % Total Number of Instances

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.91 0.910.022 0.892 0.901 0.969 HL 60 0.86 0.03 0.851 0.86 0.856 0.962 JURKAT 0.82 0.052 0.759 0.82 0.788 0.956 PC3 0.81 0.026 0.862 0.81 0.835 0.971 PCS 0.908 0.018 0.899 0.988 RAMOS 0.89 0.89 0.88 0.018 0.907 0.88 0.893 0.978 WBC Weighted Avg. 0.862 0.028 0.863 0.862 0.862 0.971

=== Confusion Matrix ===

## 256, d=4, SVM no feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
```

Correctly Classified Instances 544 90.6667 % Incorrectly Classified Instances 56 9.3333 % Kappa statistic 0.888

Mean absolute error 0.0311
Root mean squared error 0.1764
Relative absolute error 11.2 %
Root relative squared error 47.3286 %
Total Number of Instances 600

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.93 0.008 0.959 0.93 0.944 0.961 HL\_60 0.93 0.012 0.939 0.93 0.935 0.959 JURKAT 0.897 0.83 0.036 0.822 0.83 0.826 PC3 0.87 0.032 0.845 0.87 0.857 0.919 PCS 0.95 0.016 0.922 0.95 0.936 0.967 RAMOS 0.93 0.008 0.959 0.93 0.944 0.961 WBC Weighted Avg. 0.907 0.019 0.908 0.907 0.907 0.944

=== Confusion Matrix ===

# 256, d=4, SVM CFS feature selection.

=== Stratified cross-validation ===

=== Summary ===

Correctly Classified Instances 518 86.3333 % Incorrectly Classified Instances 82 13.6667 %

Kappa statistic

Mean absolute error

Root mean squared error

Root relative squared error

Total Number of Instances

0.836

0.0456

0.2134

16.4 %

57.2713 %

=== Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.86 0.028 0.86 0.86 0.86 0.916 HL\_60 0.86 0.028 0.86 0.86 0.916 JURKAT 0.86 0.84 0.036 0.824 0.84 0.832 0.902 PC3 0.032 0.84 0.84 0.84 0.904 PCS 0.84 0.91 0.024 0.883 0.91 0.897 0.943 RAMOS 0.892 0.927 0.87 0.016 0.916 0.87 WBC Weighted Avg. 0.027 0.863 0.864 0.863 0.863 0.918

=== Confusion Matrix ===

## 256, d=4, SVM EFCS feature selection.

```
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                                537
                                            89 5 %
Incorrectly Classified Instances
                                            10.5
                                                  %
                            0.874
Kappa statistic
Mean absolute error
                              0.035
                                0.1871
Root mean squared error
Relative absolute error
                              12.6 %
Root relative squared error
                                50.1996 %
Total Number of Instances
                                600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.93
                 0.02
                         0.903
                                0.93
                                        0.916
         0.91
                 0.008
                         0.958
                                 0.91
                                        0.933
```

0.955 HL\_60 0.951 JURKAT 0.88 0.0440.8 0.88 0.838 0.918 PC3 0.82 0.024 0.872 0.82 0.845 0.898 PCS 0.9 0.016 0.918 0.9 0.909 0.942 RAMOS 0.93 0.014 0.93 0.93 0.93 0.958 WBC Weighted Avg. 0.895 0.021 0.897 0.895 0.895 0.937

=== Confusion Matrix ===

## 256, d=4, LMT no feature selection.

```
=== Stratified cross-validation ===
```

=== Summary ===

Correctly Classified Instances 521 86.8333 % Incorrectly Classified Instances 79 13.1667 % Kappa statistic 0.842 Mean absolute error 0.064 Root mean squared error 0.1814 Relative absolute error 23.0395 % Root relative squared error 48.6868 % Total Number of Instances

## === Detailed Accuracy By Class ===

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.87 0.016 0.916 0.87 0.892 0.972 HL 60 0.93 0.0220.894 0.93 0.912 0.992 JURKAT 0.82 0.044 0.788 0.82 0.804 0.975 PC3 0.8 0.032 0.8 0.98 PCS 0.833 0.816 0.868 0.92 0.977 RAMOS 0.92 0.028 0.893 0.87 0.016 0.916 0.87 0.892 0.986 WBC Weighted Avg. 0.868 0.026 0.869 0.868 0.868 0.98

## === Confusion Matrix ===

```
256, d=4, LMT CFS feature selection
=== Stratified cross-validation ===
=== Summary ===
Correctly Classified Instances
                               488
                                          81.3333 %
Incorrectly Classified Instances
                               112
                                           18.6667 %
                          0.776
Kappa statistic
Mean absolute error
                             0.0923
Root mean squared error
                               0.2181
Relative absolute error
                             33.239 %
Root relative squared error
                              58.5143 %
Total Number of Instances
                               600
=== Detailed Accuracy By Class ===
        TP Rate FP Rate Precision Recall F-Measure ROC Area Class
         0.82
                0.02
                       0.891
                               0.82
                                      0.854
                                              0.975 HL_60
         0.85
                0.038
                        0.817
                                0.85
                                       0.833
                                               0.964 JURKAT
                0.052
         0.75
                        0.743
                                0.75
                                       0.746
                                               0.95
         0.77
                0.044
                        0.778
                                0.77
                                       0.774
                                               0.953 PCS
         0.88
                0.044
                        0.8
                              0.88
                                      0.838
                                              0.978 RAMOS
         0.81
                0.026
                        0.862 0.81
                                       0.835
                                               0.963
Weighted Avg.
                      0.037
                               0.815
                                              0.813
               0.813
                                      0.813
```

PC3

WBC

0.964

=== Confusion Matrix ===

 $a\ b\ c\ d\ e\ f\ <\!--$  classified as 82 14 1 0 2 1 | a = HL\_60 9 85 3 1 2 0 | b = JURKAT  $0\ 4\ 75\ 21\ 0\ 0\mid\ c=PC3$  $0 \ 1 \ 22 \ 77 \ 0 \ 0 \mid d = PCS$ 0 0 0 0 88 12 | e = RAMOS 1 0 0 0 18 81 | f = WBC

=== Stratified cross-validation ===

# 256, d=4, LMT EFCS feature selection

```
=== Summary ===
Correctly Classified Instances
                                              82.5
                                                    %
Incorrectly Classified Instances
                                 105
                                              17.5
                                                     %
Kappa statistic
                             0.79
Mean absolute error
Root mean squared error
                                  0.2141
Relative absolute error
                               27.7895 %
Root relative squared error
                                 57.4525 %
```

=== Detailed Accuracy By Class ===

Total Number of Instances

TP Rate FP Rate Precision Recall F-Measure ROC Area Class 0.87 0.034 0.837 0.87 0.853 0.964 HL 60 0.84 0.0280.857 0.84 0.848 0.964 JURKAT 0.73 0.06 0.709 0.73 0.719 0.944 PC3 0.74 0.044 0.771 0.74 0.755 0.965 PCS 0.91 0.026 0.875 0.91 0.892 0.981 RAMOS 0.86 0.018 0.905 0.86 0.882 0.969 WBC Weighted Avg. 0.825 0.035 0.826 0.825 0.825 0.965

=== Confusion Matrix ===

a b c d e f <-- classified as 87 8 1 0 2 2 | a = HL\_60 12 84 3 0 1 0 | b = JURKAT 0 4 73 22 0 1 | c = PC3 0 1 25 74 0 0 d = PCS  $3\ 0\ 0\ 91\ 6\mid\ e=RAMOS$ 2 1 1 0 10 86 | f = WBC