

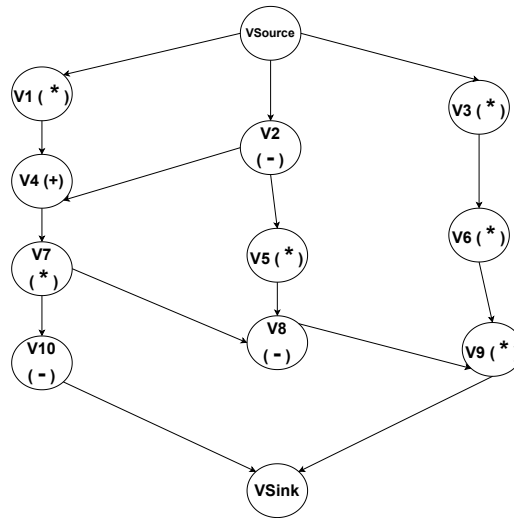
C-Based VLSI (CS 577) Mid Sem Examination (Part B)

Total Marks: 30

Name:

Roll No:

- Given 2 resources of type Mult (*) and 2 resources of type ALU (+, -, <) and each operation of the unit cycle, answer the following questions on ILP formulation of the following sequence graph. Write your answers based on the Boolean variable x_{il} , where i represents the node v_i and l is the time step. Consider the ASAP and ALAP bound for x_{il} . To compute ALAP, consider the latency obtained by ASAP scheduling. (2+2+4+3+4 =15)



- Write the objective function of ML-RC scheduling.
 - Write the objective fn. of MR-LC scheduling assuming the cost of MULT and ALU as 10 and 2, respectively.
 - Determine the correct inequality representing the data dependency constraint (i) between operations V3 and V6 and (ii) between operations V5 and V8.
 - Write down the inequality representing the unique start time of operations V3 and V9.
 - Determine the resource constraints in the time step 3.
- Consider the following code snippet: $a = b + c$; $d = d + b$; $x = a - d$; The questions are interdependent. Use the solution of the previous question to answer the next: (2 + 3 + 3 + 4 + 3 == 15)
 - Schedule the behavior considering only one ALU (+, -) and each operation is a single cycle.
 - Identify the lifetime of the variables (draw only a diagram to show lifetime).
 - Find the variable to register mapping where at most two variables can be mapped to one register.
 - Draw the datapath of the design. The datapath must use minimum-size multiplexers (some code modification may need to achieve that).
 - Find the control signal value in each state and draw the final controller FSM.

Variable	a	b	c	d	x
Register					

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(Supplementary Answer Sheet)

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Q 1. Subjective

ASAP

1	V ₁	V ₃	V ₂
2	V ₆	V ₅	V ₄
3	V ₇		
4		V ₁₀	V ₈
5	V ₉		

ALAP

1	V ₂	V ₂
2		V ₄
3	V ₇	V ₅ V ₃
4	V ₆	V ₆
5	V ₉	V ₁₀

a) MRC obj. fun = $C^T \cdot t$ $C = [0 \ 0 \ 0 \ \dots \ 2]$

b) Obj. fun. MRC = $C^T a$

$$= [10 \ 20] \begin{bmatrix} a_{MUL} \\ a_{ALU} \end{bmatrix}$$

$$= 10 \cdot a_{MUL} + 2 \cdot a_{ALU}$$

c) Data dependency

i) $(V_2 \rightarrow V_6)$

$$2x_{6,2} + 3x_{6,3} + 4x_{6,4} \geq x_{2,2} + 2x_{2,3} + 3x_{2,4} + 1$$

ii) $(V_5 \rightarrow V_6)$

$$4x_{6,4} \geq 2x_{5,2} + 3x_{5,3} + 1$$

d) Unique start time

$$V_3 = x_{3,1} + x_{3,2} + x_{3,3} = 1$$

$$V_9 = x_{9,5} = 1$$

e) Resource constraint at t.s 3

$$MUL = x_{3,3} + x_{7,3} + x_{5,3} + x_{6,3} \leq 2$$

OR $x_{3,3} + x_{5,3} + x_{6,3} \leq 1$

ALU = No op.

$[1 \ 0 \ 0 \ 0] \Rightarrow J^T D$ - multi. p.d.o

$A^T D = 0.5 AM$ multi. p.d.o

$\begin{bmatrix} 0.5 & 0 \\ 0.5 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 \end{bmatrix} =$

$0.5 \cdot 1 + 0.5 \cdot 0 = 0.5$

prob. opt. at $(V_2 = 0, V_6 = 1)$

$2x_{6,2} + 3x_{6,3} + 4x_{6,4} \leq 1x_{2,2} + 2x_{2,3} + 3x_{2,4} + 1$

$(2x_{6,2} + 3x_{6,3} + 4x_{6,4} - 1x_{2,2} - 2x_{2,3} - 3x_{2,4}) \leq 0$

$2x_{6,2} + 3x_{6,3} + 4x_{6,4} - 1x_{2,2} - 2x_{2,3} - 3x_{2,4} \leq 0$

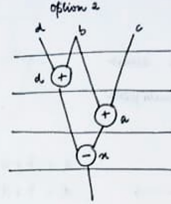
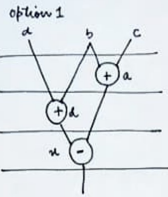
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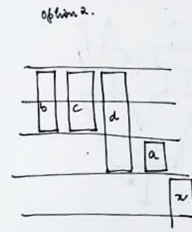
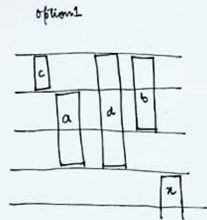
Q8. Rewrite

$$\begin{aligned} a &= b + c; \\ d &= d + b; \\ x &= a - d; \end{aligned}$$

(a) Considering only one ALU Schedule: (both options will be considered correct).



(b) lifetime of the variables



(c) Variable to register mapping

option 1-1

$$\begin{aligned} R1 &= a, c \\ R2 &= d \\ R3 &= b, x \end{aligned}$$

option 1-2

$$\begin{aligned} R1 &= a, x \\ R2 &= d, x \\ R3 &= b \end{aligned}$$

option 2-1

$$\begin{aligned} R1 &= d \\ R2 &= b, a \\ R3 &= c, x \end{aligned}$$

option 2-2

$$\begin{aligned} R1 &= d \\ R2 &= b, x \\ R3 &= a, c \end{aligned}$$

$$\begin{aligned} R1 &= b, x \\ R2 &= d \\ R3 &= b, x \end{aligned}$$

(d) Optimization of the design
for minimum-gate multiplier
code modification:

$$\begin{aligned} a &= b + c \\ d &= d + b \\ x &= a - d \end{aligned}$$

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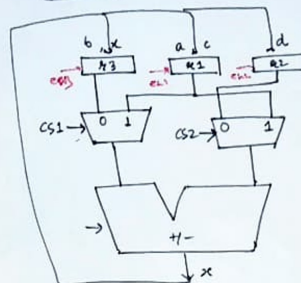
$$\begin{aligned} a &= b + c \\ d &= b + d \\ x &= a - d \end{aligned}$$

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(d)

option 1.1



(a)

	CS1	en	en1	en2	e3
e31	0	1	1	0	0
en	0	0	0	1	0
e32	1	0	0	0	1